#### Math 23C Term Project

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#### Question

Can the price changes in certain commodities reveal the kind of recession the U.S. is in? How do qualitatively different recessions affect commodities' prices? We are specifically interested in the dotcom crash of the early 2000s, the Great Recession, and the COVID-19 pandemic.

#### Motivation

"The stock market is not the economy." This refrain frequently sounds. We have decided to assess whether commodity prices that could signal the health of the general public correlated with unemployment rates across two decades. The three significant recessions in this time period affected different populations differently. Could the differences in commodity prices signal which populations were significantly affected, and how affected they were? Are there differences in how each type of recession affects them?

In general, the risk-adjusted long-run expected returns to all publicly traded assets are the same throughout the economy. If one commodity had a higher expected return than another, traders would sell the less profitable asset and buy the more profitable one, until the costs of each are proportionate to their future returns. The best null hypothesis for changes in asset prices is that all of them (specifically all the ones that are equally risky) will rise or fall by the same amount, all other factors equal.

However, different goods change in value differently in relation to different world events, and some commodities are correlated with other ones. We have selected a list of commodities that we hypothesize will behave differently during qualitatively different recessions. Did some of the selected commodities respond differently to these qualitatively different recessions?

Auxiliary questions we'll be considering are 1. What the price signals about the good and its consumers 2. Whether there were supply and demand shocks that affected the prices

#### Hypothesis

Pre-register our hypotheses here!

#### Analysis

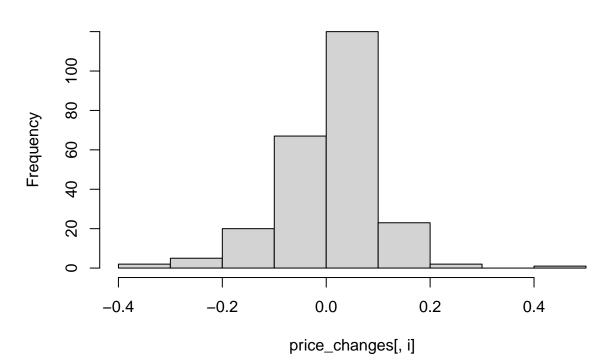
```
commodity_prices <- read.csv("source_data/commodities data.csv")
recession_dates <- read.csv("source_data/monthly recession indicator.csv")

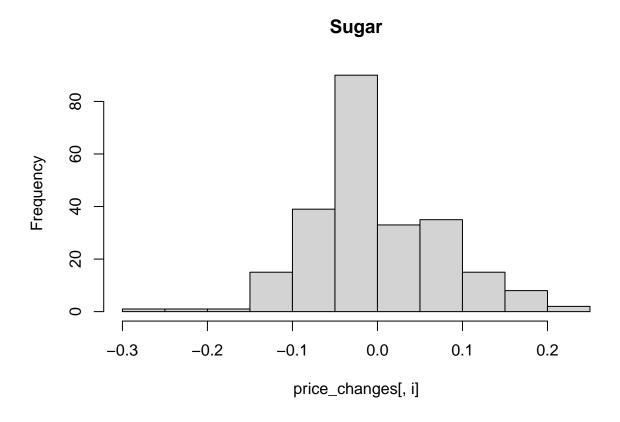
recession_dates <- recession_dates[c(-242),] # Removed the entry for March 2021 so that the datasets ha commodity_prices[,9] <- decomma(commodity_prices[,9]) # Remove commas from the price of gold column.

goods <- c("Month","Crude_oil", "Sugar", "Soybeans", "Wheat", "Beef", "Rubber", "Cocoa_beans", "Gold", names(commodity_prices) <- goods
```

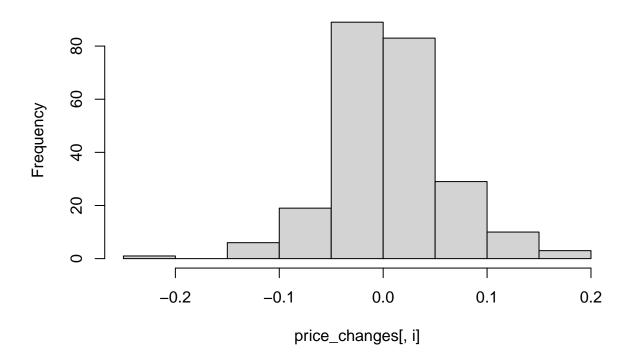
```
# Adding a column to distinguish the three different recessions in our date range.
recession_dates$which_recession <- recession_dates$USREC</pre>
recession_dates[84:101,3] <- 2*recession_dates[84:101,3]</pre>
recession_dates[230:241,3] <- 3*recession_dates[230:241,3]</pre>
# Find month-over-month price changes for each commodity
price_changes <- commodity_prices</pre>
for (c in 2:11) {
  for (r in 2:241) {
    price_changes[r,c] <- commodity_prices[r,c] / commodity_prices[r-1,c] - 1</pre>
}
price_changes$recession_bool <- recession_dates$USREC</pre>
price_changes$which_recession <- recession_dates$which_recession</pre>
price_changes <- price_changes[c(-1),]</pre>
# Display a histogram of the price changes
for (i in 2:11) {
  name <- goods[i]</pre>
  hist(price_changes[,i], main=name)
}
```

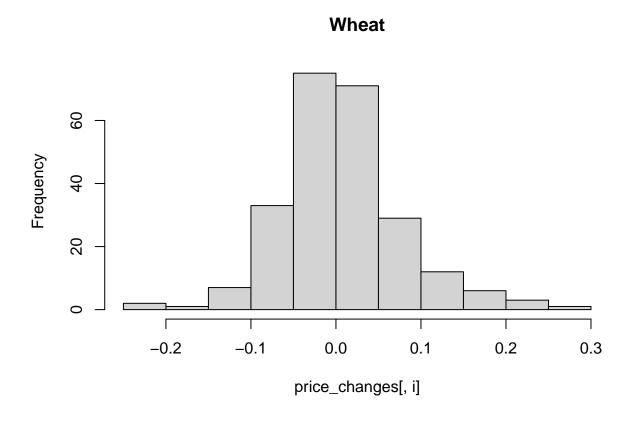
#### Crude\_oil

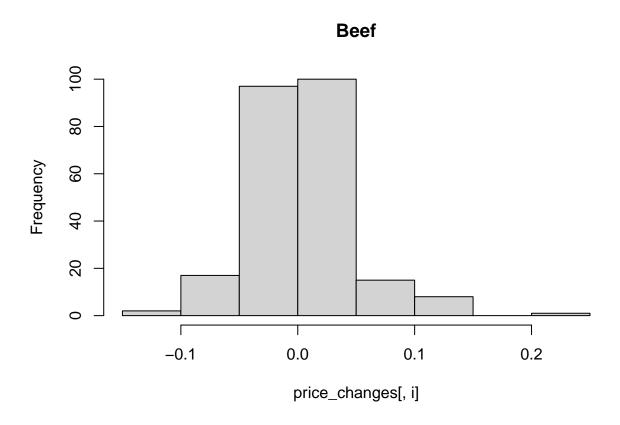




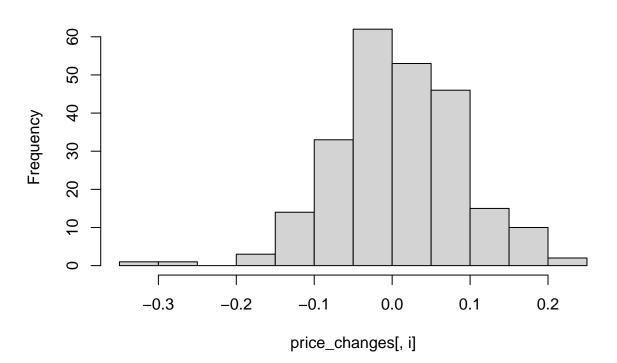
# Soybeans



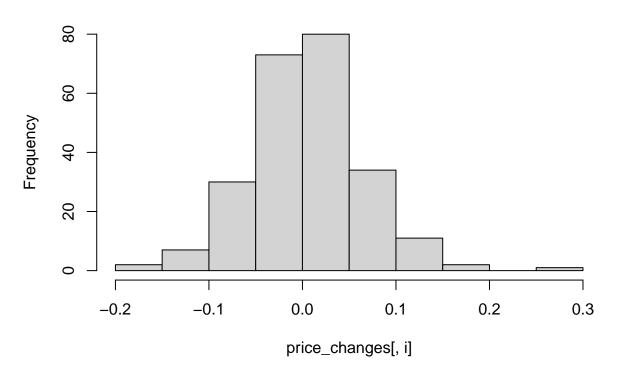


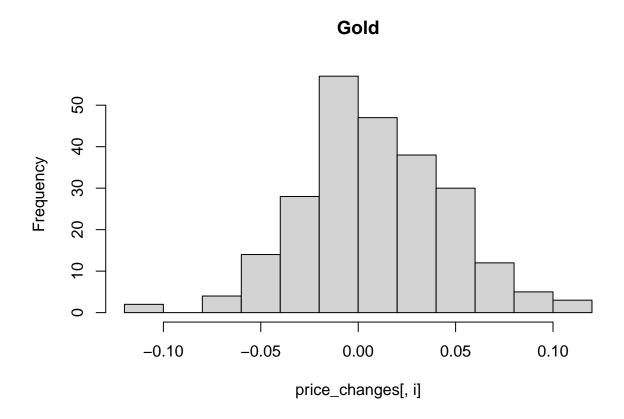


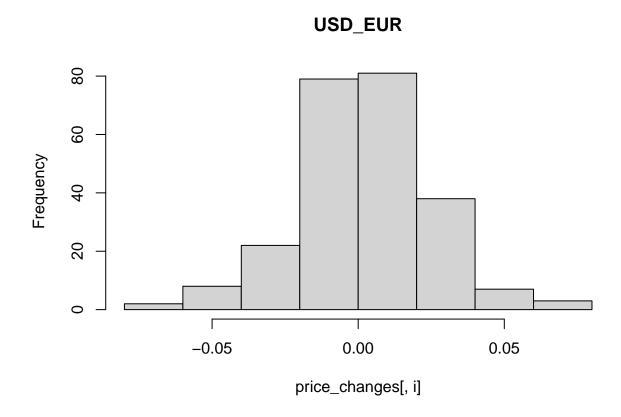
# Rubber



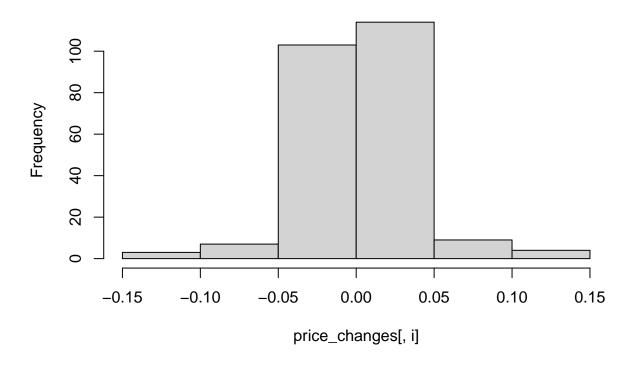
#### Cocoa\_beans





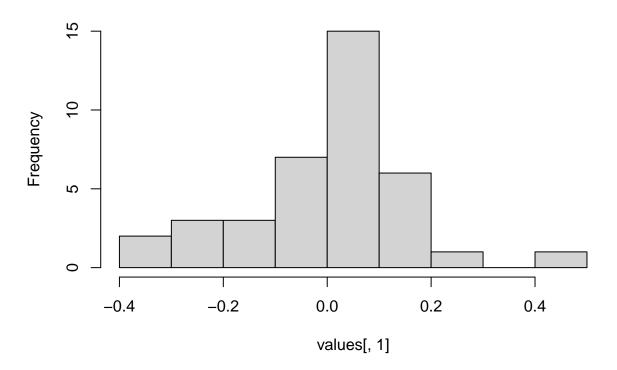


#### Ice\_cream

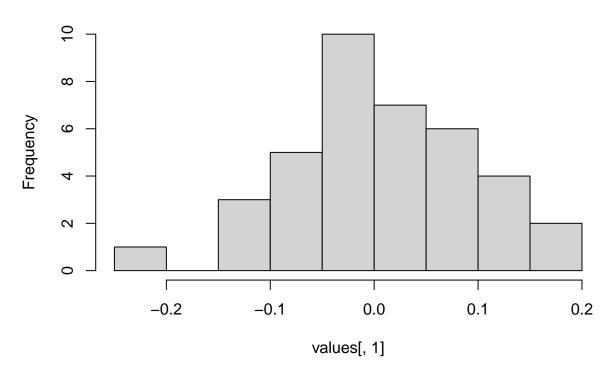


```
# Repeating that, but during recessions only
for (i in 2:11) {
  name <- paste(goods[i],"(recession)")
  values <- price_changes[,c(i,13)]
  values <- values[values[,2] == 1,]
  hist(values[,1], main=name)
}</pre>
```

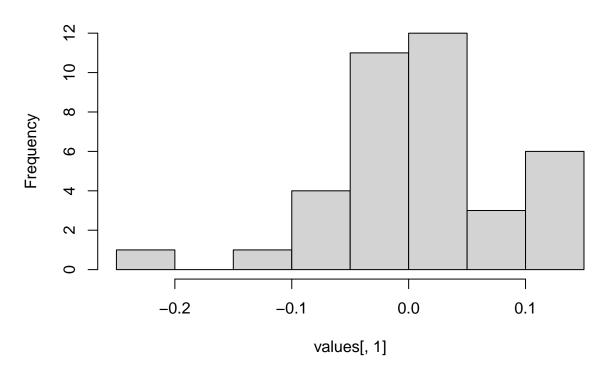
# Crude\_oil (recession)



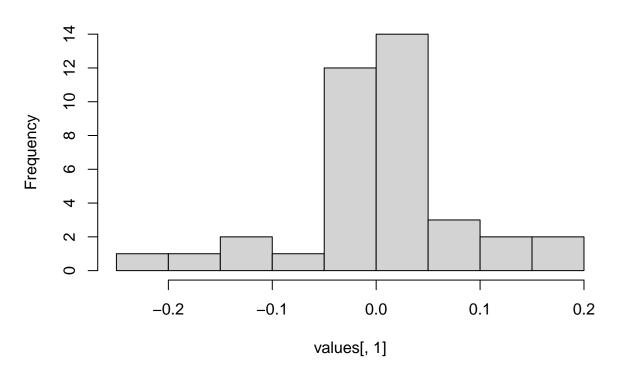
# Sugar (recession)



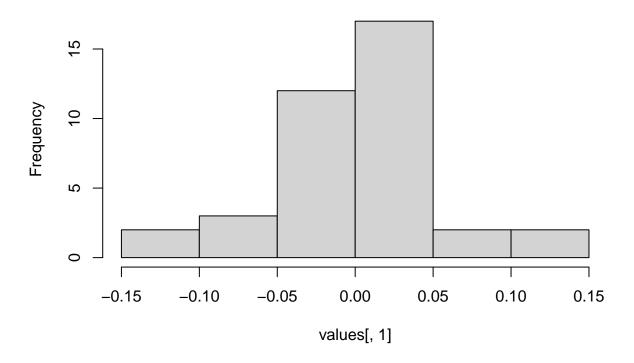
# Soybeans (recession)



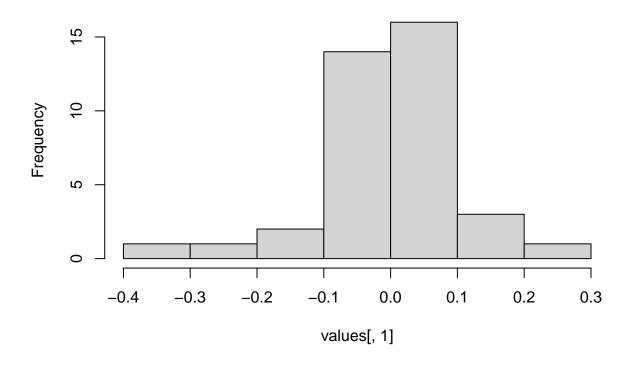
# Wheat (recession)



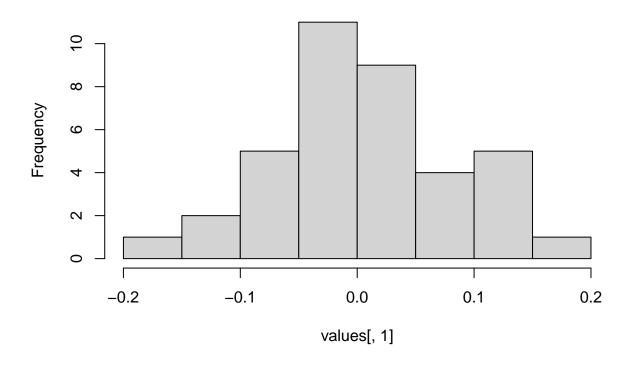
# Beef (recession)



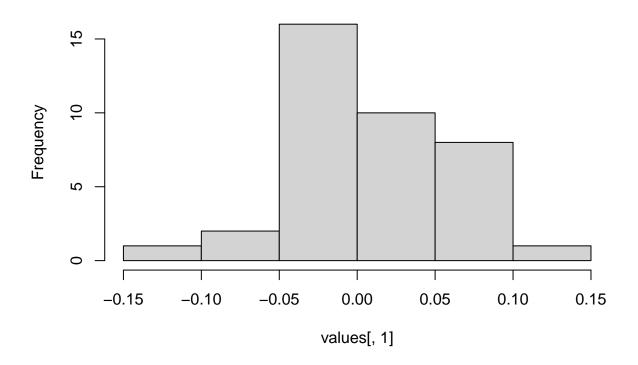
#### **Rubber (recession)**



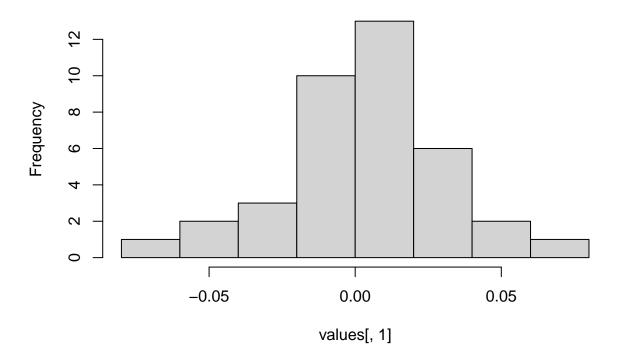
# Cocoa\_beans (recession)



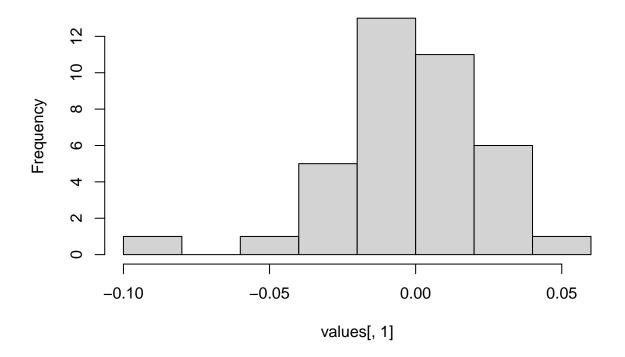
# Gold (recession)



# **USD\_EUR** (recession)

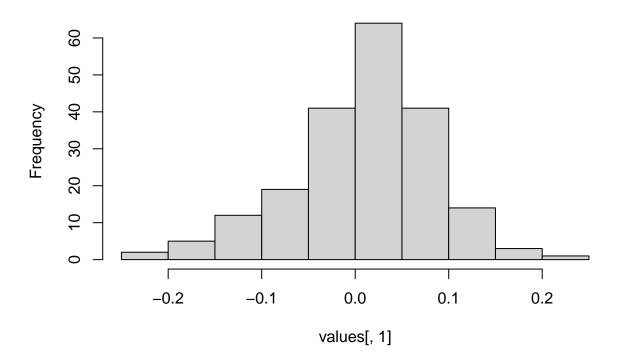


#### lce\_cream (recession)

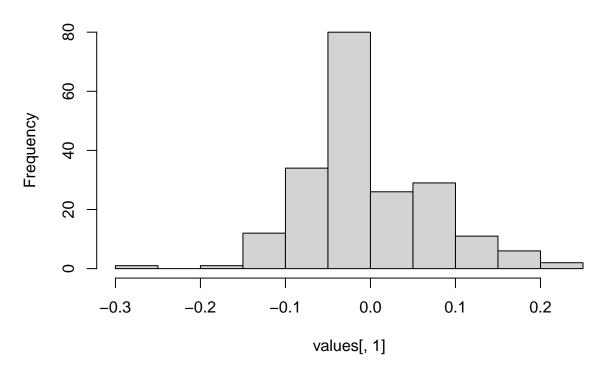


```
# Repeat for months not in recession
for (i in 2:11) {
  name <- paste(goods[i],"(non-recession)")
  values <- price_changes[,c(i,13)]
  values <- values[values[,2] == 0,]
  hist(values[,1], main=name)
}</pre>
```

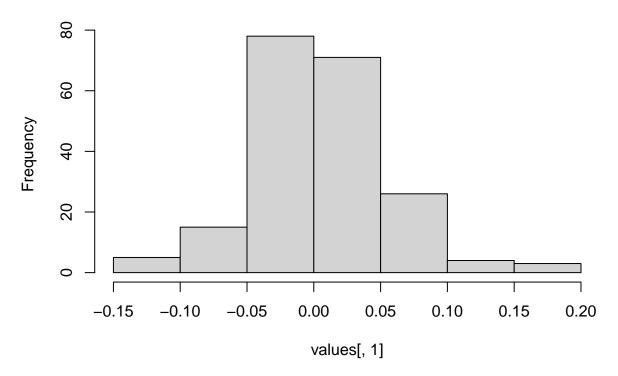
# Crude\_oil (non-recession)



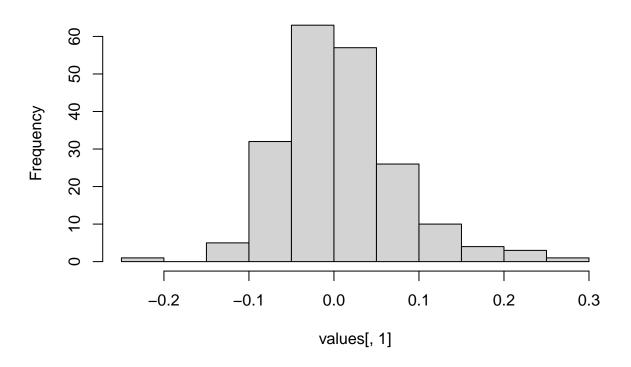
# Sugar (non-recession)



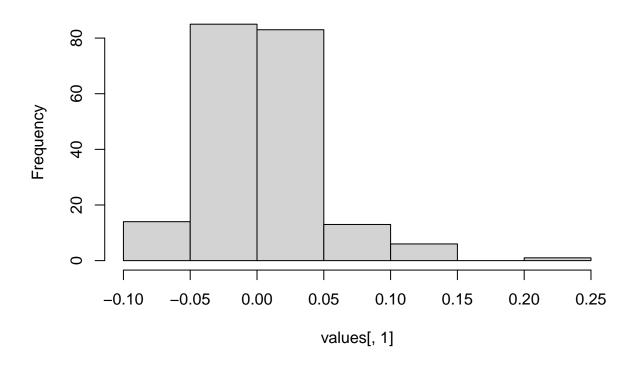
#### Soybeans (non-recession)



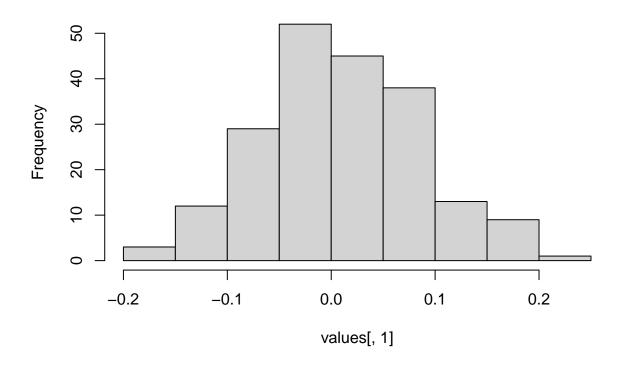
#### Wheat (non-recession)



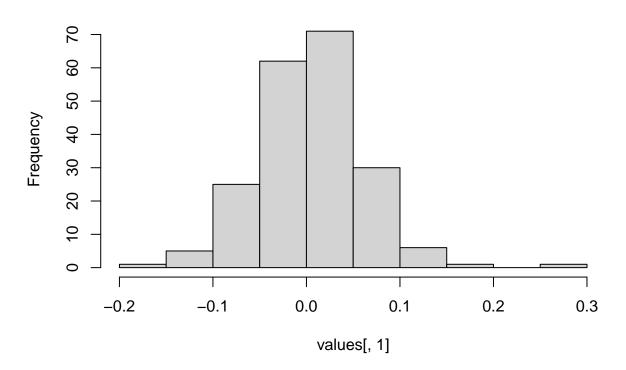
#### Beef (non-recession)



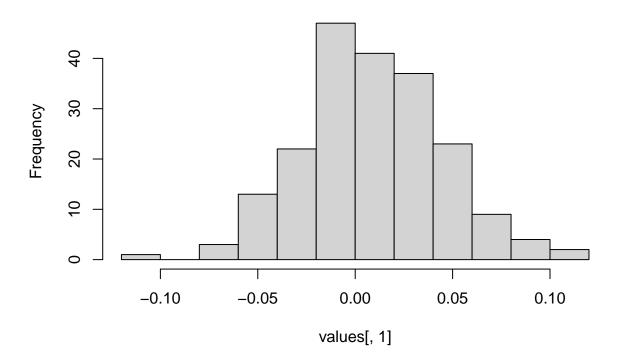
# Rubber (non-recession)



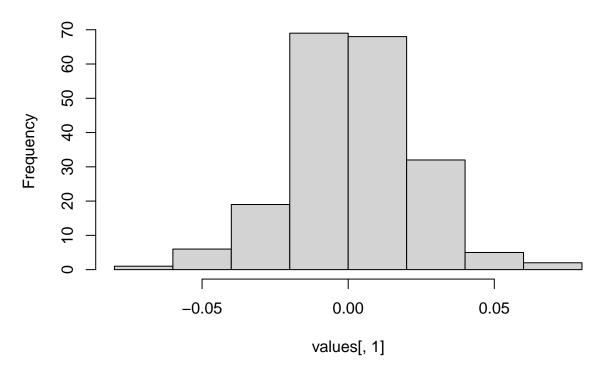
# Cocoa\_beans (non-recession)



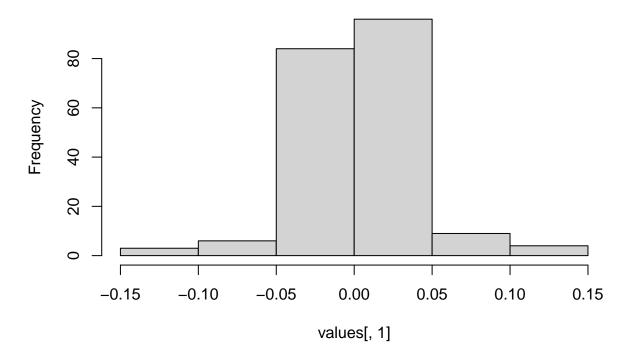
# Gold (non-recession)



# USD\_EUR (non-recession)

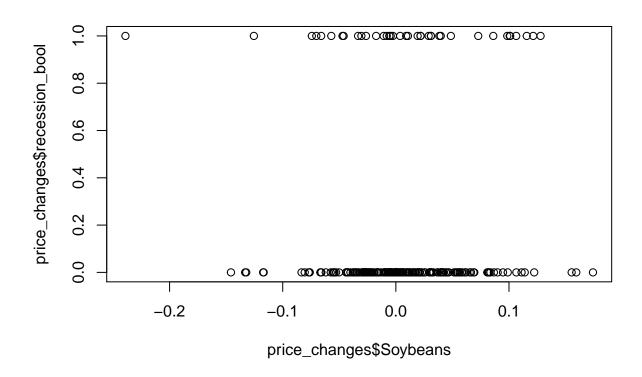


#### Ice\_cream (non-recession)



```
soybeans_regression <- glm(recession_bool ~ Soybeans, data = price_changes, family = 'binomial')
summary(soybeans_regression)</pre>
```

```
##
## Call:
## glm(formula = recession_bool ~ Soybeans, family = "binomial",
       data = price_changes)
##
##
## Deviance Residuals:
      Min
                 1Q
                     Median
                                   3Q
                                           Max
   -0.6622
           -0.5949 -0.5817
                                        2.0888
##
                              -0.5656
##
## Coefficients:
##
               Estimate Std. Error z value Pr(>|z|)
## (Intercept) -1.6825
                            0.1794 - 9.379
                                             <2e-16 ***
## Soybeans
                 1.5869
                            3.2948
                                     0.482
                                               0.63
##
  ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
  (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 209.71 on 239
                                     degrees of freedom
## Residual deviance: 209.48 on 238 degrees of freedom
## AIC: 213.48
## Number of Fisher Scoring iterations: 4
```



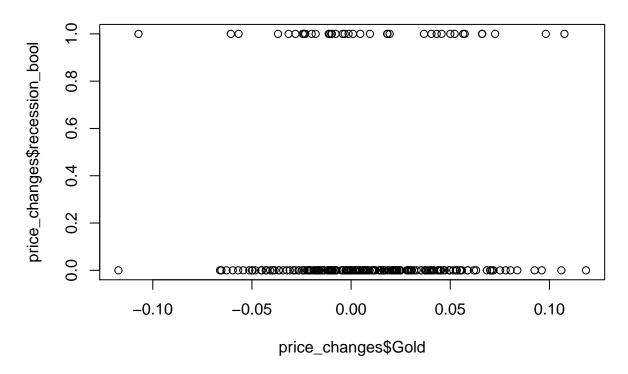
```
summary(gold_regression)
##
## Call:
  glm(formula = recession_bool ~ Gold, family = "binomial", data = price_changes)
##
## Deviance Residuals:
##
      Min
                     Median
                                   3Q
                                           Max
                1Q
## -0.6153 -0.5911 -0.5845 -0.5761
                                        1.9676
##
## Coefficients:
##
              Estimate Std. Error z value Pr(>|z|)
## (Intercept) -1.6793
                            0.1827
                                   -9.194
                                             <2e-16 ***
                0.9375
                            4.7325
                                     0.198
                                              0.843
## Gold
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
  (Dispersion parameter for binomial family taken to be 1)
##
      Null deviance: 209.71 on 239
                                     degrees of freedom
## Residual deviance: 209.67 on 238 degrees of freedom
```

gold\_regression <- glm(recession\_bool ~ Gold, data = price\_changes, family = 'binomial')</pre>

## AIC: 213.67

##

```
## Number of Fisher Scoring iterations: 3
plot(price_changes$Gold, price_changes$recession_bool)
```

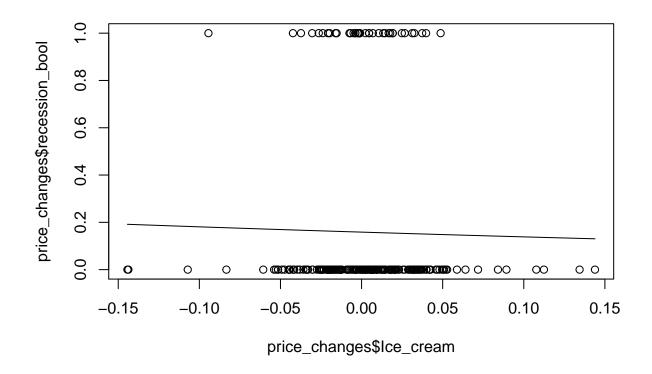


```
goods_vs_recession_logistic_model <- glm(</pre>
  recession_bool ~ Crude_oil + Sugar + Soybeans + Wheat + Beef + Rubber + Cocoa_beans + Gold + USD_EUR
  data = price_changes, family = 'binomial')
summary(goods_vs_recession_logistic_model)
##
## Call:
  glm(formula = recession_bool ~ Crude_oil + Sugar + Soybeans +
##
       Wheat + Beef + Rubber + Cocoa_beans + Gold + USD_EUR + Ice_cream,
##
       family = "binomial", data = price_changes)
##
## Deviance Residuals:
##
       Min
                 1Q
                      Median
                                    3Q
                                            Max
            -0.6123
                     -0.5662
                                          2.0971
##
   -0.8139
                              -0.4928
##
## Coefficients:
##
               Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                -1.7006
                             0.1882
                                     -9.036
                                               <2e-16 ***
## Crude_oil
                                     -0.561
                                                0.575
                -1.2750
                             2.2732
## Sugar
                 2.3158
                             2.6110
                                      0.887
                                                0.375
## Soybeans
                 3.3223
                             3.9135
                                      0.849
                                                0.396
## Wheat
                -2.3030
                             2.8125
                                     -0.819
                                                0.413
## Beef
                             4.4501
                 1.2275
                                      0.276
                                                0.783
```

```
## Rubber
               -1.6263
                           2.5382 -0.641
                                             0.522
## Cocoa_beans 0.6074
                                             0.849
                           3.1873
                                  0.191
                           5.3050
## Gold
              0.6411
                                   0.121
                                             0.904
                0.5395
## USD_EUR
                           9.3769
                                  0.058
                                             0.954
## Ice cream
               -1.0465
                           5.1222 -0.204
                                             0.838
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
      Null deviance: 209.71 on 239 degrees of freedom
## Residual deviance: 207.41 on 229 degrees of freedom
## AIC: 229.41
##
## Number of Fisher Scoring iterations: 4
negative_goods_regression <- glm(recession_bool ~ Crude_oil + Wheat + Rubber + Ice_cream, data = price_</pre>
summary(negative_goods_regression)
##
## Call:
## glm(formula = recession_bool ~ Crude_oil + Wheat + Rubber + Ice_cream,
      family = "binomial", data = price_changes)
##
## Deviance Residuals:
##
      Min
           1Q
                    Median
                                  3Q
                                          Max
## -0.6870 -0.6013 -0.5820 -0.5460
                                       2.0757
##
## Coefficients:
              Estimate Std. Error z value Pr(>|z|)
##
                         0.1774 -9.349 <2e-16 ***
## (Intercept) -1.6582
## Crude_oil
               -0.2640
                           2.0091 -0.131
                                             0.895
               -0.7643
                           2.5456 -0.300
## Wheat
                                             0.764
## Rubber
               -0.8586
                           2.4213 -0.355
                                             0.723
## Ice_cream
              -1.5616
                           5.0401 -0.310
                                             0.757
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
      Null deviance: 209.71 on 239 degrees of freedom
## Residual deviance: 209.22 on 235 degrees of freedom
## AIC: 219.22
##
## Number of Fisher Scoring iterations: 4
# Probability of a recession if all of these goods lost 100% of their value this month:
inv.logit(-1.6582+0.2640+0.7643+0.8586+1.5616)
## [1] 0.8569641
# Probability of a recession if all of these goods doubled in price last month:
inv.logit(-1.6582-0.2640-0.7643-0.8586-1.5616)
```

## [1] 0.00601958

```
icecream_regression <- glm(recession_bool ~ Ice_cream, data = price_changes, family = 'binomial')</pre>
summary(icecream_regression)
##
## Call:
## glm(formula = recession_bool ~ Ice_cream, family = "binomial",
##
       data = price_changes)
##
## Deviance Residuals:
##
       Min
                1Q Median
                                   3Q
                                           Max
## -0.6524 -0.5946 -0.5845 -0.5708
                                        1.9529
## Coefficients:
              Estimate Std. Error z value Pr(>|z|)
##
## (Intercept) -1.6687
                           0.1769 -9.434
                                             <2e-16 ***
## Ice_cream
             -1.5900
                            4.9778 -0.319
                                              0.749
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 209.71 on 239 degrees of freedom
## Residual deviance: 209.61 on 238 degrees of freedom
## AIC: 213.61
##
## Number of Fisher Scoring iterations: 3
plot(price_changes$Ice_cream, price_changes$recession_bool)
curve(inv.logit(-1.5900*x-1.6687), add=TRUE)
```



```
icecream_predictions <- as.factor(predict(icecream_regression, newdata=price_changes, type='response')
confusionMatrix(icecream_predictions, reference = as.factor(price_changes$recession_bool==1))</pre>
```

```
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction FALSE TRUE
##
        FALSE
                109
        TRUE
                 93
                       20
##
##
##
                  Accuracy : 0.5375
                    95% CI : (0.4722, 0.6019)
##
       No Information Rate: 0.8417
##
##
       P-Value [Acc > NIR] : 1
##
##
                     Kappa: 0.0366
##
##
    Mcnemar's Test P-Value : 2.16e-12
##
               Sensitivity: 0.5396
##
##
               Specificity: 0.5263
            Pos Pred Value: 0.8583
##
            Neg Pred Value: 0.1770
##
                Prevalence: 0.8417
##
##
            Detection Rate: 0.4542
      Detection Prevalence: 0.5292
##
```

```
##
         Balanced Accuracy: 0.5330
##
##
          'Positive' Class : FALSE
##
recession_predictions <- as.factor(predict(goods_vs_recession_logistic_model, newdata=price_changes, ty
confusionMatrix(recession_predictions, reference = as.factor(price_changes$recession_bool==1))
## Confusion Matrix and Statistics
##
             Reference
##
## Prediction FALSE TRUE
##
       FALSE
               104
##
        TRUE
                 98
                      19
##
##
                  Accuracy : 0.5125
                    95% CI : (0.4474, 0.5773)
##
##
       No Information Rate: 0.8417
##
       P-Value [Acc > NIR] : 1
##
##
                     Kappa: 0.0081
##
##
   Mcnemar's Test P-Value : 5.55e-13
##
##
               Sensitivity: 0.5149
##
               Specificity: 0.5000
            Pos Pred Value: 0.8455
##
##
            Neg Pred Value: 0.1624
##
                Prevalence: 0.8417
##
            Detection Rate: 0.4333
##
      Detection Prevalence : 0.5125
```

Balanced Accuracy: 0.5074

'Positive' Class : FALSE

## ## ##

##