

Consider the function $f: R \rightarrow S$ given by

$$f(x) = x \cdot x_i^{-1}.$$

We claim that this function is:

- one to one
- onto
- a homomorphism

and therefore is a ring homomorphism.