

# Exercise 5

## Instructions

1. Play Blackjack in small groups. One student acts as the **dealer**, the others are **players**.
2. Use a **fixed policy**:
  - *Hit if your total < 20, otherwise Stand.*
3. For each episode (a full hand until win/loss/draw):
  - a. Record the **sequence of states, actions, and rewards**.
  - b. Compute **MC updates** (after the episode).
  - c. Compute **TD(0) updates** (during the episode).
4. Compare how the two methods update the value table.

# Part A: Record an Episode

Step	State (Player Sum, Dealer Showing, Usable Ace?)	Action (Hit=1, Stand=0)	Reward $G$	Next State
1				
2				
...				
END				

# Part B: Monte Carlo Update (First-Visit)

- At the end of the episode, compute the **return**

$$G_t = R_{t+1} + R_{t+2} + \dots + R_T$$

- For each state visited **first time** in the episode:

$$\underline{V(S_t)} \leftarrow \underline{V(S_t)} + \alpha [G_t - \underline{V(S_t)}]$$

New value of state t	Former estimation of value of state t (= Expected return starting at that state)	Learning Rate	Return at timestep t	Former estimation of value of state t (= Expected return starting at that state)
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# Part B: Monte Carlo Update (First-Visit)

- Record the **sequence of states, actions, and rewards**.

State $S$	Return $G$	Visit Count $N(s)$	Old $V(s)$	New $V(s)$

- Use  $\alpha = \frac{1}{n}$  for manual calculations.

# Part C: TD(0) update

- Update **during the episode** for each transition:

$$V(S_t) \leftarrow V(S_t) + \alpha [R_{t+1} + \gamma V(S_{t+1}) - V(S_t)]$$

The diagram illustrates the TD(0) update equation with color-coded components and labels:

- $V(S_t)$  (green underline): New value of state t
- $V(S_t)$  (blue underline): Former estimation of value of state t
- $\alpha$  (red underline): Learning Rate
- $R_{t+1}$  (orange underline): Reward
- $\gamma V(S_{t+1})$  (purple underline): Discounted value of next state
- $V(S_t)$  (blue underline): TD Target

- Take  $\gamma = 1.0$ , choose  $\alpha = 0.5$  for manual calculations.

# Part C: TD(0) update

Step	State $s$	Reward $r$	Next State $s'$	Old $V(s)$	New $V(s)$
1					
2					