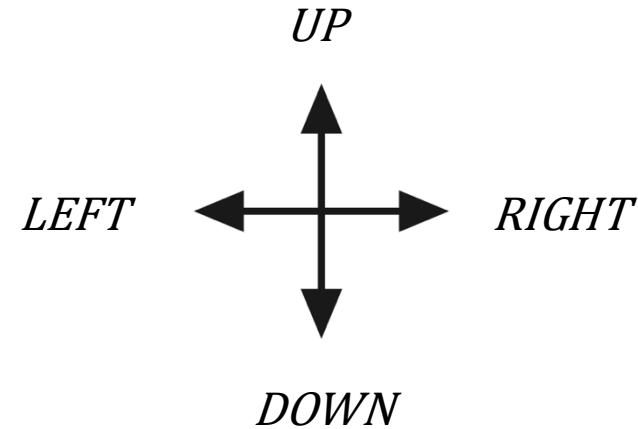
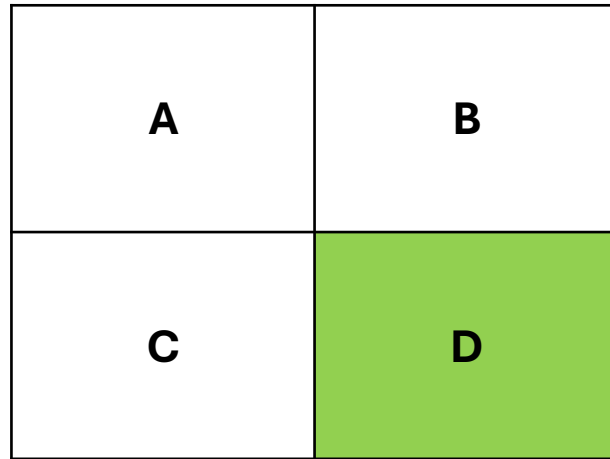
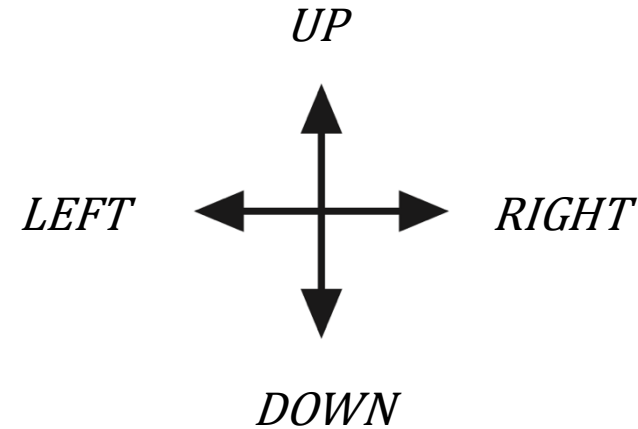
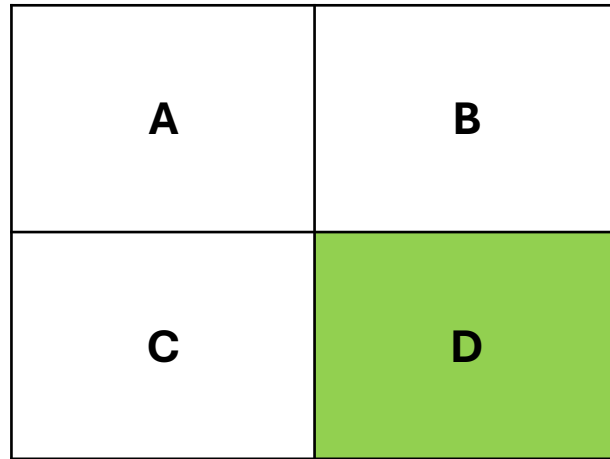


Example: 2x2 Gridworld



- **States** $\mathcal{S} = (A, B, C, D)$
- **Actions** $\mathcal{A} = (UP, DOWN, LEFT, RIGHT)$
- **Policy** \mathcal{P} = From every state, choose each action with probability 0.25
- **Reward** ($\mathcal{R} = -1$) *per step*
- Discount Factor ($\gamma = 1$)

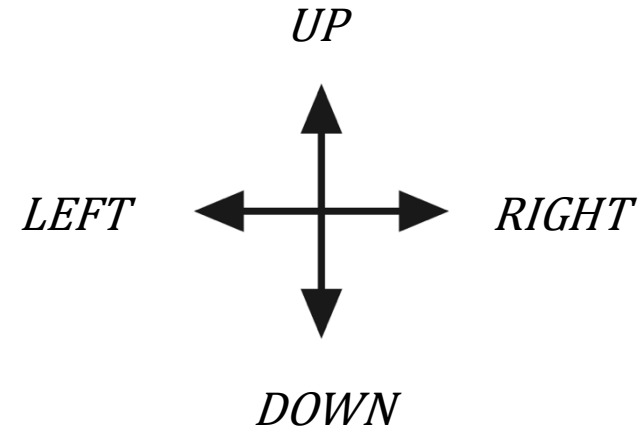
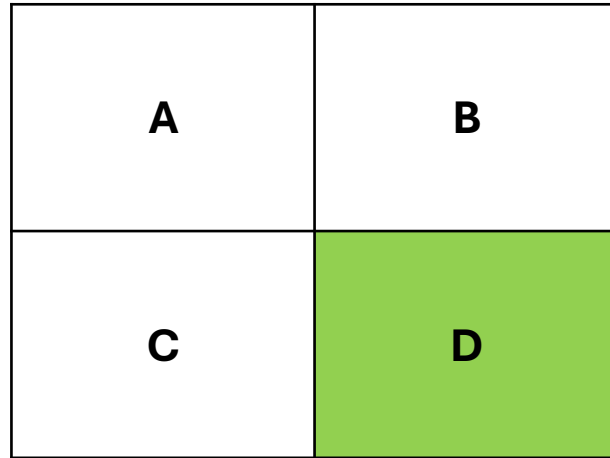
Example: 2x2 Gridworld



- Undiscounted MDP ($\gamma = 1$)
- Non-terminal states (A,B,C)
- Terminal State (D)
- Agent follows a uniform random policy

$$\pi(\text{up} \mid \cdot) = \pi(\text{left} \mid \cdot) = \pi(\text{down} \mid \cdot) = \pi(\text{right} \mid \cdot) = 0.25$$

Example: 2x2 Gridworld



Rules:

- From each state, actions move you in that direction if possible, otherwise you stay in the same square.
- Reward is -1 until the terminal state is reached.
- The goal is to reach state D which gives **0 reward** and ends the episode.

	$v_k(s)$	$v_{k+1}(s)$	$v_{k+2}(s)$
A	0		
B	0		
C	0		

0	0
0	

$$k = 0$$

Initially, we set the value functions $v_k(s)$ of all states to **zero**

	$v_k(s)$	$v_{k+1}(s)$	$v_{k+2}(s)$
A	0		
B	0		
C	0		

0	0
0	

$$k = 0$$

We then use the **Bellman equation** to update the value function $v_k(s)$ of all states at each k iteration.

	$v_k(s)$	$v_{k+1}(s)$	$v_{k+2}(s)$
A	0		
B	0		
C	0		

0	0
0	

$k = 0$

$$v_{k+1}(s) = \sum_a \pi(a | s) [r(s, a) + \gamma v_k(s')]$$

$$v_{k+1}(A) = \frac{1}{4} [(-1 + v(A)) + (-1 + v(B)) + (-1 + v(C)) + (-1 + v(A))]$$

Using the Bellman equation, we get this

	$v_k(s)$	$v_{k+1}(s)$	$v_{k+2}(s)$
A	0		
B	0		
C	0		

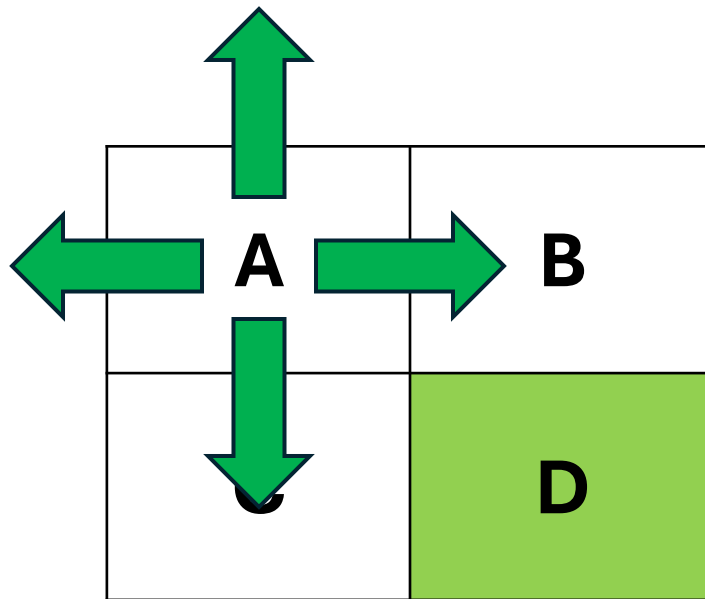
0	0
0	

$k = 0$

$$v_{k+1}(s) = \sum_a \pi(a | s) [r(s, a) + \gamma v_k(s')]$$

$$v_{k+1}(A) = \frac{1}{4} [(-1 + v(A)) + (-1 + v(B)) + (-1 + v(C)) + (-1 + v(A))]$$

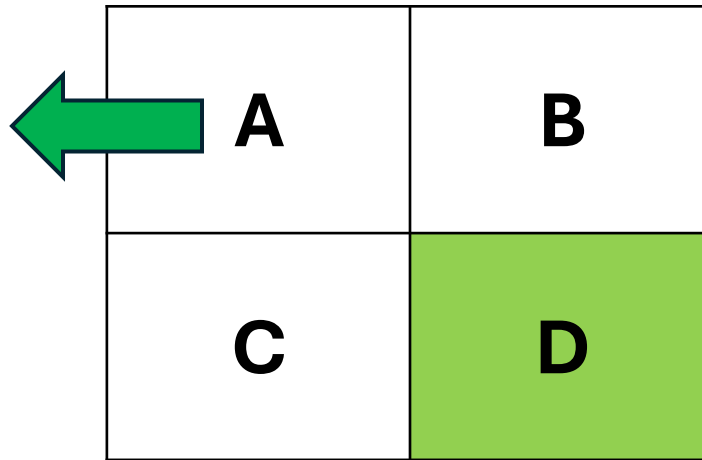
Let us this break down. To update the value function of **state A**, we get the sum of the immediate reward plus the value function of the next state for all possible actions from state A.



0	0
0	

$$v_{k+1}(A) = \frac{1}{4} [(-1 + v(A)) + (-1 + v(B)) + (-1 + v(C)) + (-1 + v(A))]$$

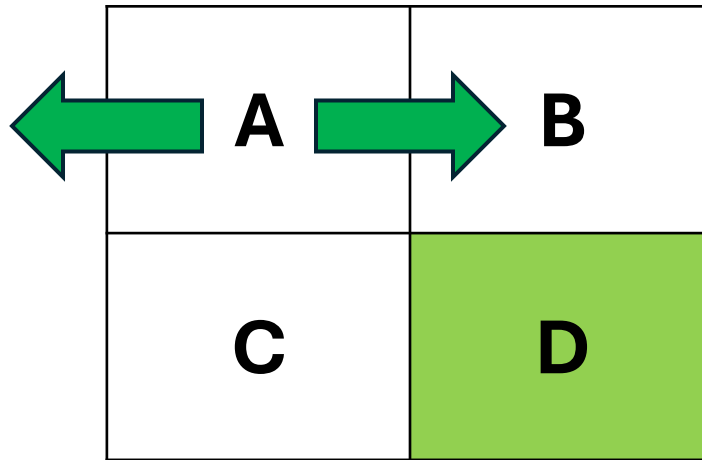
Let us this break down. To update the value function of **state A**, we get the sum of the immediate reward plus the value function of the next state for all possible actions from **state A**.



0	0
0	

$$v_{k+1}(A) = \frac{1}{4} [\underbrace{(-1 + v(A))}_{\text{LEFT}} + (-1 + v(B)) + (-1 + v(C)) + (-1 + v(A))]$$

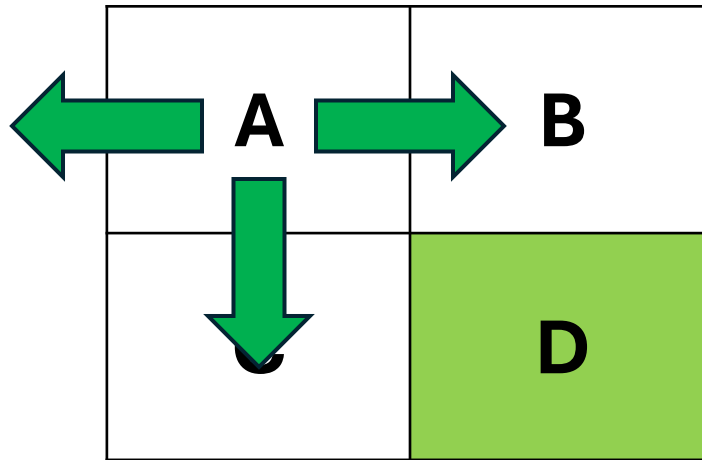
First term: When we go **LEFT**, we stay in **state A** and we will get a reward of -1 plus the value function of **state A**.



0	0
0	

$$v_{k+1}(A) = \frac{1}{4} [(-1 + v(A)) + \underbrace{(-1 + v(\mathbf{B}))}_{\text{Second term}} + (-1 + v(C)) + (-1 + v(A))]$$

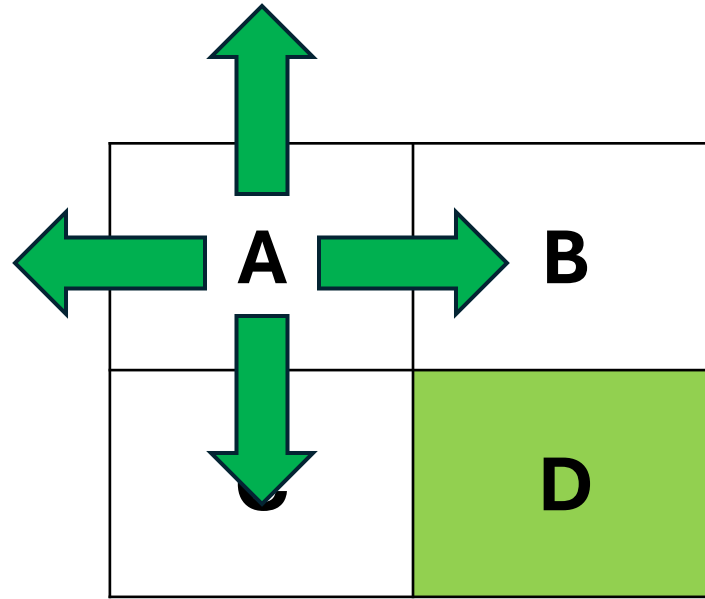
Second term: When we go **RIGHT**, we go to **state B** and we will get a reward of -1 plus the value function of **state B**.



0	0
0	

$$v_{k+1}(A) = \frac{1}{4} [(-1 + v(A)) + (-1 + v(B)) + \underbrace{(-1 + v(C))}_{\text{Third term}} + (-1 + v(A))]$$

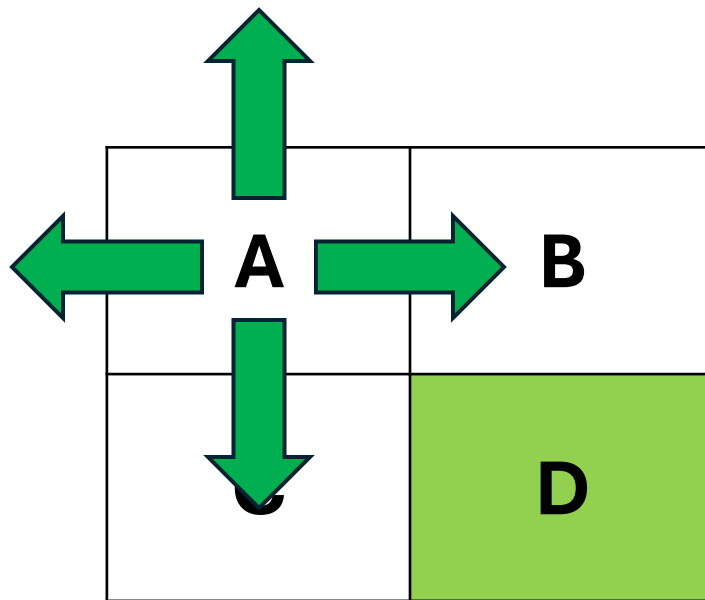
Third term: When we go **DOWN**, we go to **state C** and we will get a reward of -1 plus the value function of **state A**.



0	0
0	

$$v_{k+1}(A) = \frac{1}{4} [(-1 + v(A)) + (-1 + v(B)) + (-1 + v(C)) + \underbrace{(-1 + v(A))}_{\text{UP}}]$$

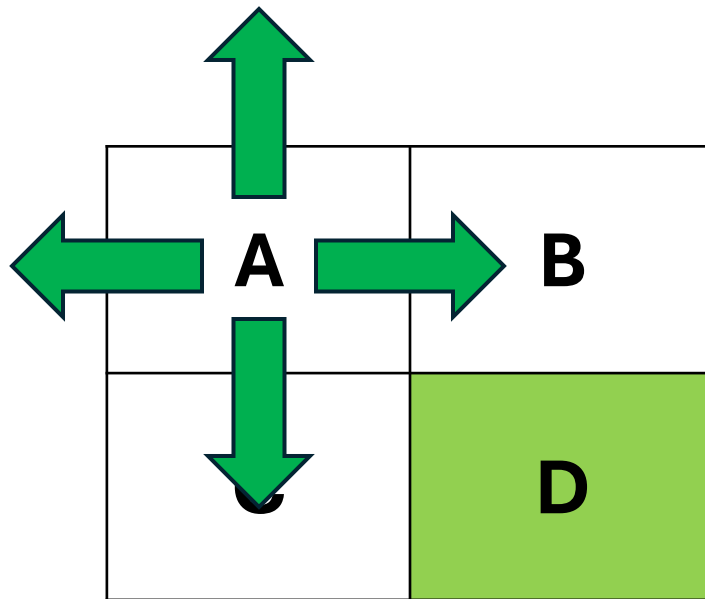
Fourth term: When we go **UP**, we stay in **state A** and we will get a reward of -1 plus the value function of **state A**.



0	0
0	

$$v_{k+1}(A) = \underbrace{\frac{1}{4}}_{\text{uniform random policy}} [(-1 + v(A)) + (-1 + v(B)) + (-1 + v(C)) + (-1 + v(A))]$$

One fourth is the uniform random **policy** for all actions. The agent follows this policy of having a 25% probability of choosing **action \mathcal{A}** .



0	0
0	

$$v_{k+1}(A) = \frac{1}{4} [(-1 + v(A)) + (-1 + v(B)) + (-1 + v(C)) + (-1 + v(A))]$$

The discount factor γ is omitted because we set it to 1. If we have a different value for the discount factor, we would multiply it to each value function of the next state.

	$v_k(s)$	$v_{k+1}(s)$	$v_{k+2}(s)$
A	0		
B	0		
C	0		

0	0
0	

$$k = 1$$

$$v_{k+1}(s) = \sum_a \pi(a | s) [r(s, a) + \gamma v_k(s')]$$

$$v_{k+1}(A) = \frac{1}{4} [(-1 + v(A)) + (-1 + v(B)) + (-1 + v(C)) + (-1 + v(A))]$$

$$v_{k+1}(A) = \frac{1}{4} [(-1 + 0) + (-1 + 0) + (-1 + 0) + (-1 + 0)]$$

$$v_{k+1}(A) = -1$$

	$v_k(s)$	$v_{k+1}(s)$	$v_{k+2}(s)$
A	0	-1	
B	0		
C	0		

-1	0
0	

$$k = 1$$

$$v_{k+1}(A) = \frac{1}{4} [(-1 + v(A)) + (-1 + v(B)) + (-1 + v(C)) + (-1 + v(A))]$$

$$v_{k+1}(A) = \frac{1}{4} [(-1 + 0) + (-1 + 0) + (-1 + 0) + (-1 + 0)]$$

$$v_{k+1}(A) = -1$$

We now store the new value function of **state A**

	$v_k(s)$	$v_{k+1}(s)$	$v_{k+2}(s)$
A	0	-1	
B	0		
C	0		

-1	0
0	

$$k = 1$$

$$v_{k+1}(B) = \frac{1}{4}[(-1 + v(A)) + (-1 + v(B)) + (-1 + v(D)) + (-1 + v(B))]$$

$$v_{k+1}(B) = \frac{1}{4}[(-1 + 0) + (-1 + 0) + (-1 + 0) + (-1 + 0)]$$

$$v_{k+1}(B) = -1$$

We do the same process for **state B**

	$v_k(s)$	$v_{k+1}(s)$	$v_{k+2}(s)$
A	0	-1	
B	0	-1	
C	0		

-1	-1
0	

$$k = 1$$

$$v_{k+1}(C) = \frac{1}{4} [(-1 + v(C)) + (-1 + v(D)) + (-1 + v(C)) + (-1 + v(A))]$$

$$v_{k+1}(C) = \frac{1}{4} [(-1 + 0) + (-1 + 0) + (-1 + 0) + (-1 + 0)]$$

$$v_{k+1}(C) = -1$$

And **state C**

	$v_k(s)$	$v_{k+1}(s)$	$v_{k+2}(s)$
A	0	-1	
B	0	-1	
C	0	-1	

-1	-1
-1	

$$k = 1$$

$$v_{k+1}(C) = \frac{1}{4} [(-1 + v(C)) + (-1 + v(D)) + (-1 + v(C)) + (-1 + v(A))]$$

$$v_{k+1}(C) = \frac{1}{4} [(-1 + 0) + (-1 + 0) + (-1 + 0) + (-1 + 0)]$$

$$v_{k+1}(C) = -1$$

And **state C**

0	0
0	0

$k = 0$

-1	-1
-1	0

$k = 1$

After one iteration, the value functions for **states A, B** and **C** were changed from -1 to 0.

-1	-1
-1	0

$k = 1$

$$q(s, a) = \sum_{s', r} P(s', r \mid s, a) [r + v(s')]$$

We now use the Bellman equation to compute the action-value functions for each state to improve our existing **policy**.

-1	-1
-1	0

$k = 1$

$$q(s, a) = \sum_{s', r} P(s', r \mid s, a) [r + v(s')]$$

Let us start computing the action-value functions of **state A**

-1	-1
-1	0

$k = 1$

$$q(s, a) = \sum_{s', r} P(s', r \mid s, a) [r + v(s')]$$

$$q(A, LEFT) = -1 + v(A)$$

$$q(A, LEFT) = -1 + (-1)$$

$$q(A, LEFT) = -2$$

-1	-1
-1	0

$k = 1$

$$q(s, a) = \sum_{s', r} P(s', r \mid s, a) [r + v(s')]$$

$$q(A, RIGHT) = -1 + v(B)$$

$$q(A, RIGHT) = -1 + (-1)$$

$$q(A, RIGHT) = -2$$

-1	-1
-1	0

$k = 1$

$$q(s, a) = \sum_{s', r} P(s', r \mid s, a) [r + v(s')]$$

$$q(A, DOWN) = -1 + v(C)$$

$$q(A, DOWN) = -1 + (-1)$$

$$q(A, DOWN) = -2$$

-1	-1
-1	0

$k = 1$

$$q(s, a) = \sum_{s', r} P(s', r \mid s, a) [r + v(s')]$$

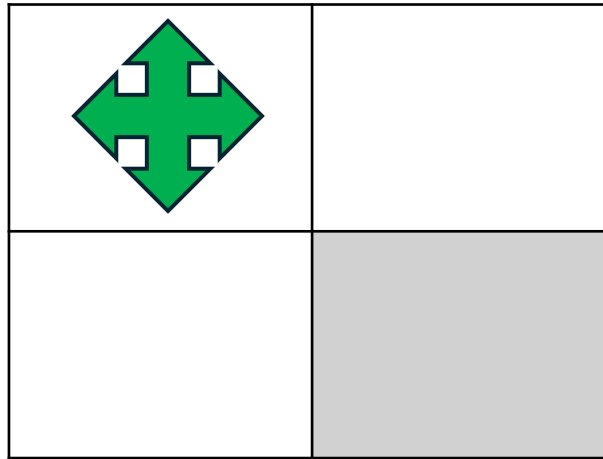
$$q(A, UP) = -1 + v(A)$$

$$q(A, UP) = -1 + (-1)$$

$$q(A, UP) = -2$$

$$q(A, UP) = -2$$

$$q(A, LEFT) = -2$$



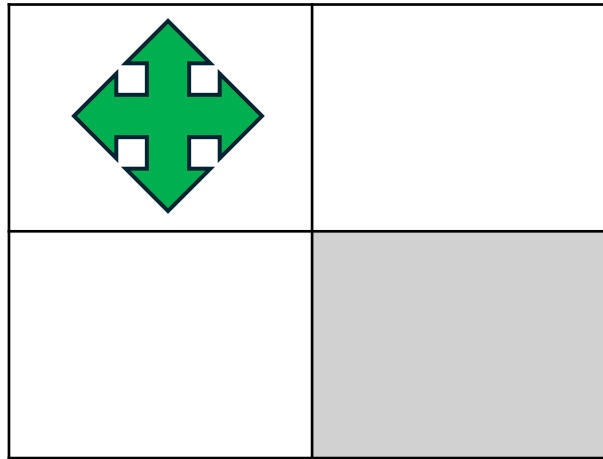
$$q(A, RIGHT) = -2$$

$$q(A, DOWN) = -2$$

We can now map the value for each **action** from **state A**

$$q(A, UP) = -2$$

$$q(A, LEFT) = -2$$



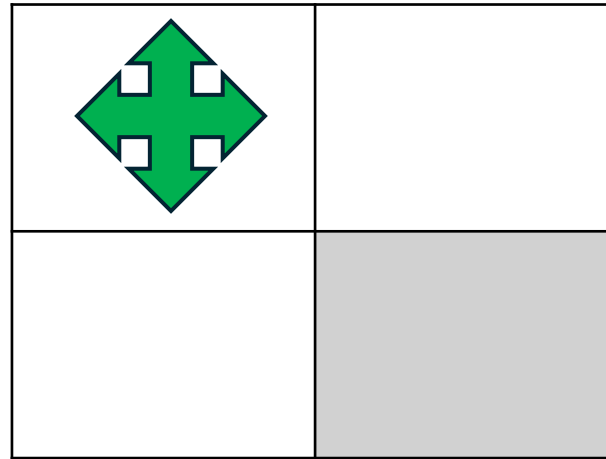
$$q(A, RIGHT) = -2$$

$$q(A, DOWN) = -2$$

This simply tells us that from **state A**, there is no best action to take because all of their values are the same.

$$q(A, UP) = -2$$

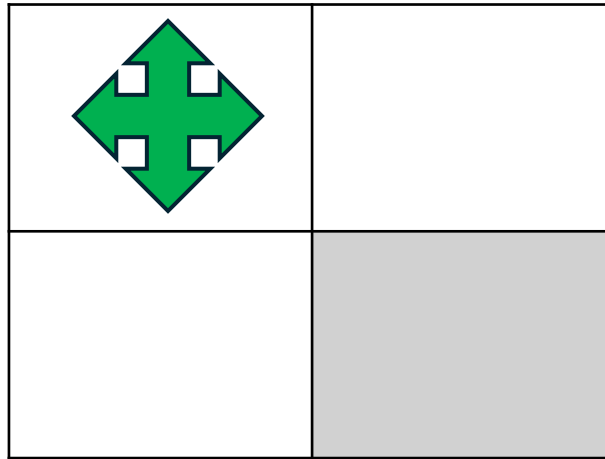
$$q(A, LEFT) = -2$$



$$q(A, RIGHT) = -2$$

$$q(A, DOWN) = -2$$


Because all of the values are the same, the **policy** will also be the same for **state A**



Let us now calculate the action-value functions for **state B**

-1	-1
-1	0

$k = 1$


	

$$q(s, a) = \sum_{s', r} P(s', r \mid s, a) [r + v(s')]$$

Similar to **state A**, we use the Bellman equation to compute the action-value functions for **state B**.

-1	-1
-1	0

$k = 1$

$$q(s, a) = \sum_{s', r} P(s', r \mid s, a) [r + v(s')]$$


$$q(B, LEFT) = -1 + v(A)$$

$$q(B, LEFT) = -1 + (-1)$$

$$q(B, LEFT) = -2$$

-1	-1
-1	0

$k = 1$

$$q(s, a) = \sum_{s', r} P(s', r \mid s, a) [r + v(s')]$$


$$q(B, RIGHT) = -1 + v(B)$$

$$q(B, RIGHT) = -1 + (-1)$$

$$q(B, RIGHT) = -2$$

-1	-1
-1	0

$k = 1$

$$q(s, a) = \sum_{s', r} P(s', r \mid s, a) [r + v(s')]$$


$$q(B, DOWN) = -1 + v(D)$$

$$q(B, DOWN) = -1 + (0)$$

$$q(B, DOWN) = -1$$

-1	-1
-1	0

$k = 1$

$$q(s, a) = \sum_{s', r} P(s', r \mid s, a) [r + v(s')]$$

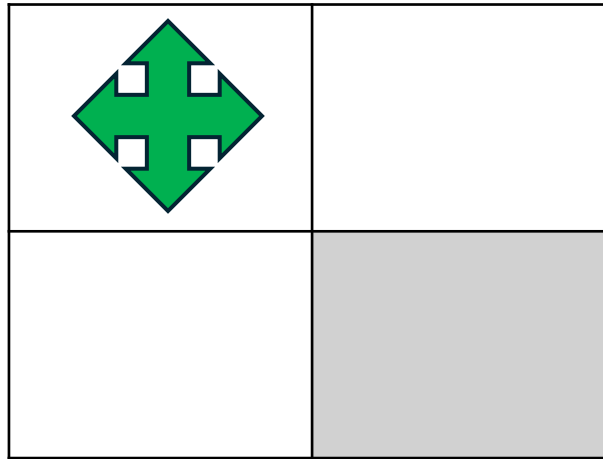
$$q(B, UP) = -1 + v(B)$$

$$q(B, UP) = -1 + (-1)$$

$$q(B, UP) = -2$$

$$q(B, UP) = -2$$

$$q(B, LEFT) = -2$$



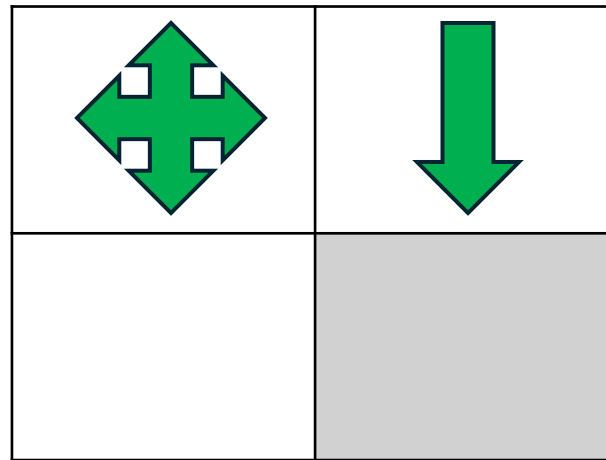
$$q(B, RIGHT) = -2$$

$$q(B, DOWN) = -1$$

We can now map the value for each **action** from **state B**

$$q(B, UP) = -2$$

$$q(B, LEFT) = -2$$



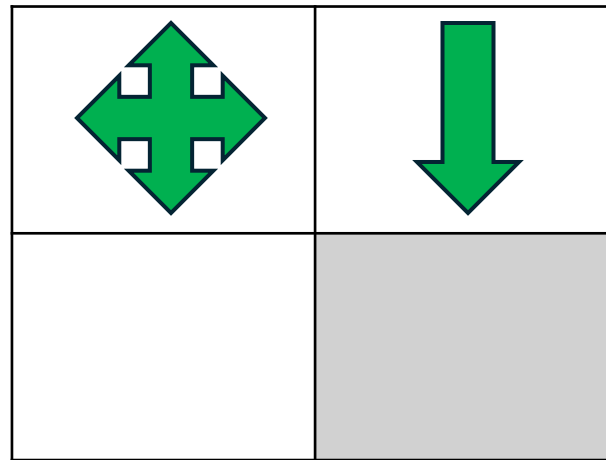
$$q(B, RIGHT) = -2$$

$$q(B, DOWN) = -1$$

This simply tells us that from **state B**, the best action to take is to go **DOWN** because going down has the highest value of all actions.

$$q(B, UP) = -2$$

$$q(B, LEFT) = -2$$



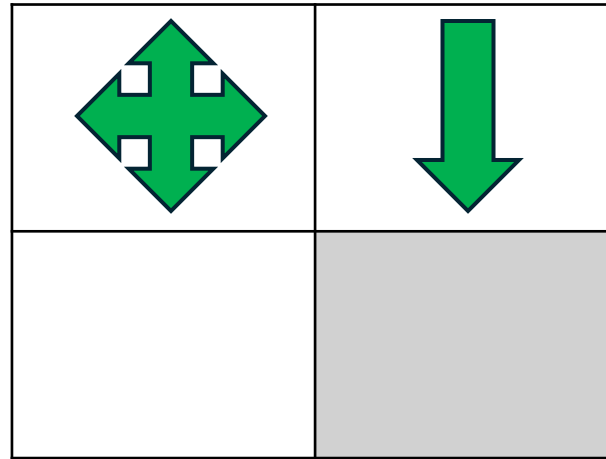
$$q(B, RIGHT) = -2$$

$$q(B, DOWN) = -1$$

Which makes sense because going **DOWN** will go to our goal which is **state D**.

$$q(B, UP) = -2$$

$$q(B, LEFT) = -2$$

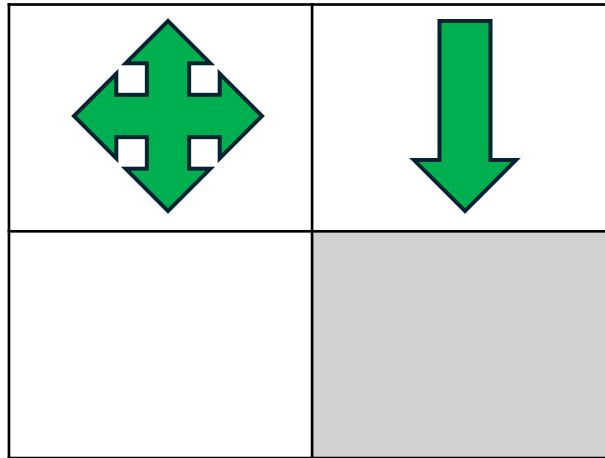


$$q(B, RIGHT) = -2$$

$$q(B, DOWN) = -1$$

Because of this, we can now update the policy for **state B**.



$$\pi(B) = \{DOWN\}$$



Let us now calculate the action-value functions for **state C**

-1	-1
-1	0

$k = 1$



	

$$q(s, a) = \sum_{s', r} P(s', r \mid s, a) [r + v(s')]$$

Similar to **state A** and **B**, we use the Bellman equation to compute the action-value functions for **state C**.

-1	-1
-1	0

$k = 1$

$$q(s, a) = \sum_{s', r} P(s', r \mid s, a) [r + v(s')]$$



$$q(C, LEFT) = -1 + v(C)$$

$$q(C, LEFT) = -1 + (-1)$$

$$q(C, LEFT) = -2$$

-1	-1
-1	0

$k = 1$

$$q(s, a) = \sum_{s', r} P(s', r \mid s, a) [r + v(s')]$$



$$q(C, RIGHT) = -1 + v(D)$$

$$q(C, RIGHT) = -1 + (0)$$

$$q(C, RIGHT) = -1$$

-1	-1
-1	0

$k = 1$

$$q(s, a) = \sum_{s', r} P(s', r \mid s, a) [r + v(s')]$$



$$q(C, DOWN) = -1 + v(C)$$

$$q(C, DOWN) = -1 + (-1)$$

$$q(C, DOWN) = -2$$

-1	-1
-1	0

$k = 1$

$$q(s, a) = \sum_{s', r} P(s', r \mid s, a) [r + v(s')]$$

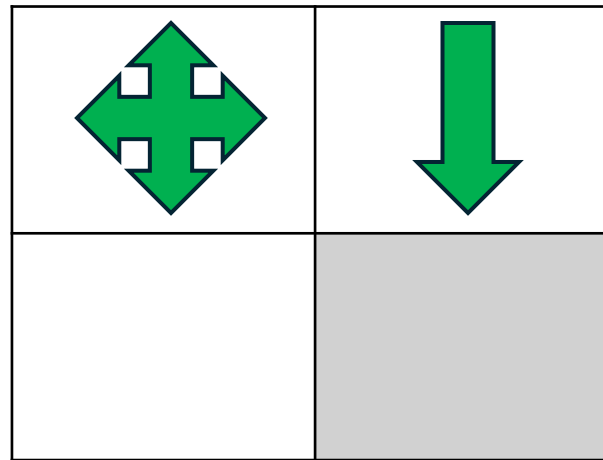
$$q(C, UP) = -1 + v(A)$$

$$q(C, UP) = -1 + (-1)$$

$$q(C, UP) = -2$$

$$q(C, UP) = -2$$

$$q(C, LEFT) = -2$$



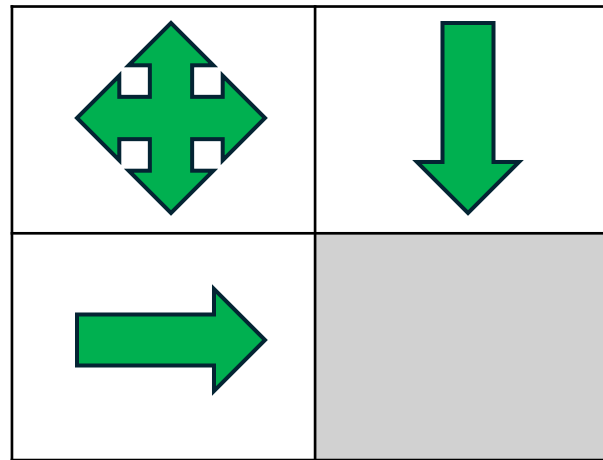
$$q(C, RIGHT) = -1$$

$$q(C, DOWN) = -2$$

We can now map the value for each **action** from **state C**

$$q(C, UP) = -2$$

$$q(C, LEFT) = -2$$



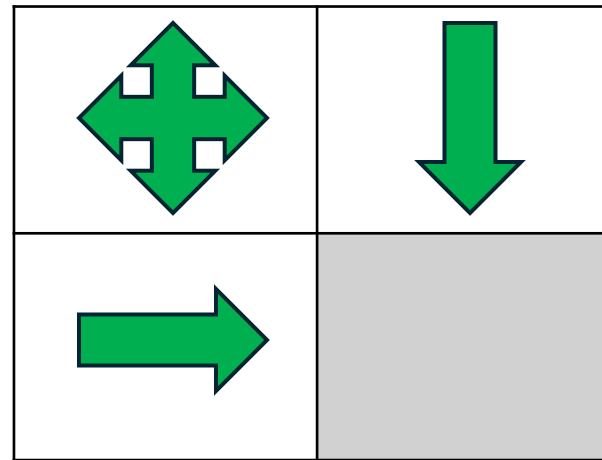
$$q(C, RIGHT) = -1$$

$$q(C, DOWN) = -2$$

This simply tells us that from **state C**, the best action to take is to go **RIGHT** because going right has the highest value of all actions.

$$q(C, UP) = -2$$

$$q(C, LEFT) = -2$$



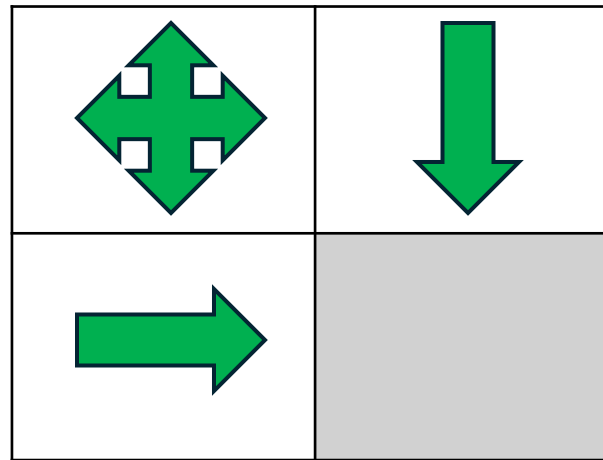
$$q(C, RIGHT) = -1$$

$$q(C, DOWN) = -2$$

Which makes sense because going **RIGHT** will go to our goal which is **state D**.

$$q(C, UP) = -2$$

$$q(C, LEFT) = -2$$



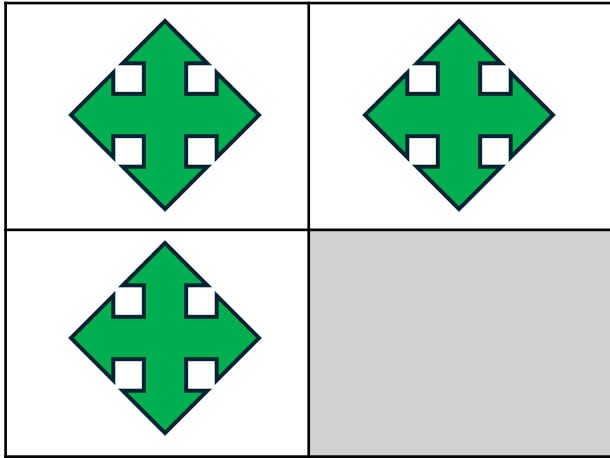
$$q(C, RIGHT) = -2$$

$$q(C, DOWN) = -1$$

Just like before, we can now update our policy for **state C**.

$$\pi(C) = \{RIGHT\}$$

$$k = 0$$



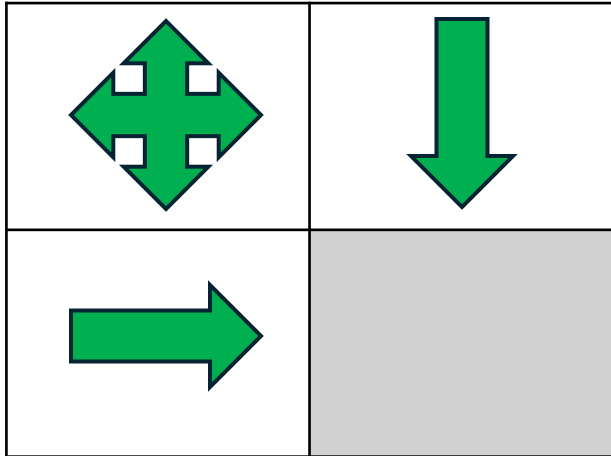
$$\pi(A) = \{LEFT, RIGHT, UP, DOWN\}$$

$$\pi(B) = \{LEFT, RIGHT, UP, DOWN\}$$

$$\pi(C) = \{LEFT, RIGHT, UP, DOWN\}$$

Initially, we started with this **uniform random policy**

$$k = 1$$



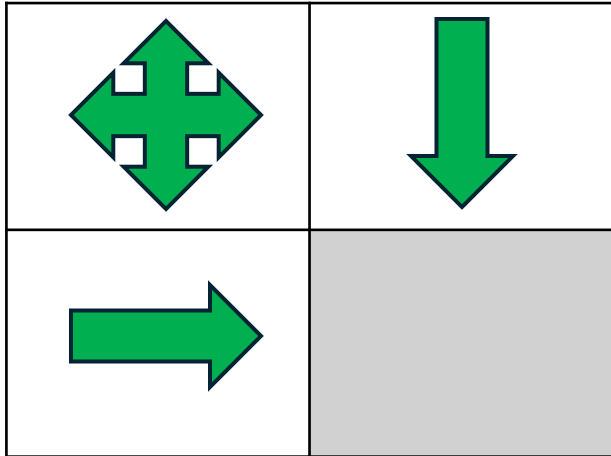
$$\pi(A) = \{LEFT, RIGHT, UP, DOWN\}$$

$$\pi(B) = \{DOWN\}$$

$$\pi(C) = \{RIGHT\}$$

After 1 iteration, we improved our **previous policy**.

$$k = 1$$



$$\pi(A) = \{LEFT, RIGHT, UP, DOWN\}$$

$$\pi(B) = \{DOWN\}$$

$$\pi(C) = \{RIGHT\}$$

Let us do one last iteration if we can reach convergence,
or in RL terms, find the **optimal policy** π_*

	$v_k(s)$	$v_{k+1}(s)$	$v_{k+2}(s)$
A	0	-1	-2
B	0	-1	
C	0	-1	

-2	-1
-1	

$k = 1$

$$v_{k+2}(s) = \sum_a \pi(a | s) [r(s, a) + \gamma v_{k+1}(s')]$$

$$v_{k+2}(A) = \frac{1}{4} [(-1 + v_{k+1}(A)) + (-1 + v_{k+1}(B)) + (-1 + v_{k+1}(C)) + (-1 + v_{k+1}(A))]$$

$$v_{k+2}(A) = \frac{1}{4} [(-1 - 1) + (-1 - 1) + (-1 - 1) + (-1 - 1)]$$

$$v_{k+2}(A) = -2$$

	$v_k(s)$	$v_{k+1}(s)$	$v_{k+2}(s)$
A	0	-1	-2
B	0	-1	-1.75
C	0	-1	

-2	-1.75
-1	

$k = 1$

$$v_{k+2}(s) = \sum_a \pi(a | s) [r(s, a) + \gamma v_{k+1}(s')]$$

$$v_{k+2}(B) = \frac{1}{4} [(-1 + v_{k+1}(A)) + (-1 + v_{k+1}(B)) + (-1 + v_{k+1}(D)) + (-1 + v_{k+1}(B))]$$

$$v_{k+2}(B) = \frac{1}{4} [(-1 - 1) + (-1 - 1) + (-1 + 0) + (-1 - 1)]$$

$$v_{k+2}(B) = -1.75$$

	$v_k(s)$	$v_{k+1}(s)$	$v_{k+2}(s)$
A	0	-1	-2
B	0	-1	-1.75
C	0	-1	-1.75

-2	-1.75
-1.75	

$k = 1$

$$v_{k+2}(s) = \sum_a \pi(a | s) [r(s, a) + \gamma v_{k+1}(s')]$$

$$v_{k+2}(C) = \frac{1}{4} [(-1 + v_{k+1}(C)) + (-1 + v_{k+1}(D)) + (-1 + v_{k+1}(C)) + (-1 + v_{k+1}(A))]$$

$$v_{k+2}(C) = \frac{1}{4} [(-1 - 1) + (-1 + 0) + (-1) + (-1 - 1)]$$

$$v_{k+2}(C) = -1.75$$

-2	-1.75
-1.75	0

$k = 2$

$$q(s, a) = \sum_{s', r} P(s', r \mid s, a) [r + v(s')]$$

$$q(A, LEFT) = -1 + v(A)$$

$$q(A, LEFT) = -1 + (-2)$$

$$q(A, LEFT) = -3$$

-2	-1.75
-1.75	0

$k = 2$

$$q(s, a) = \sum_{s', r} P(s', r \mid s, a) [r + v(s')]$$

$$q(A, RIGHT) = -1 + v(B)$$

$$q(A, RIGHT) = -1 + (-1.75)$$

$$q(A, RIGHT) = -2.75$$

-2	-1.75
-1.75	0

$k = 2$

$$q(s, a) = \sum_{s', r} P(s', r \mid s, a) [r + v(s')]$$

$$q(A, DOWN) = -1 + v(C)$$

$$q(A, DOWN) = -1 + (-1.75)$$

$$q(A, DOWN) = -2.75$$

-2	-1.75
-1.75	0

$k = 2$

$$q(s, a) = \sum_{s', r} P(s', r \mid s, a) [r + v(s')]$$

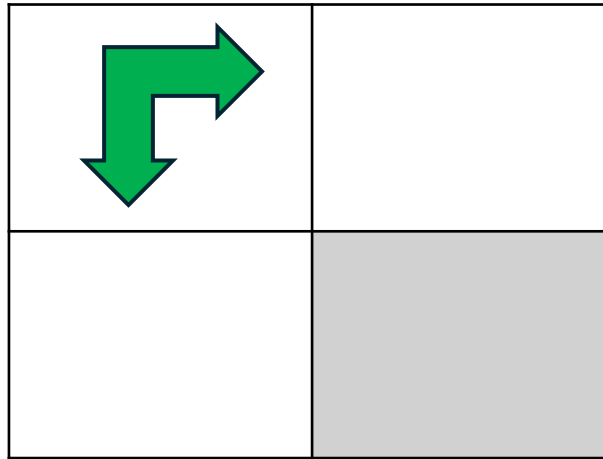
$$q(A, UP) = -1 + v(A)$$

$$q(A, UP) = -1 + (-2)$$

$$q(A, UP) = -3$$

$$q(A, UP) = -3$$

$$q(A, LEFT) = -3$$



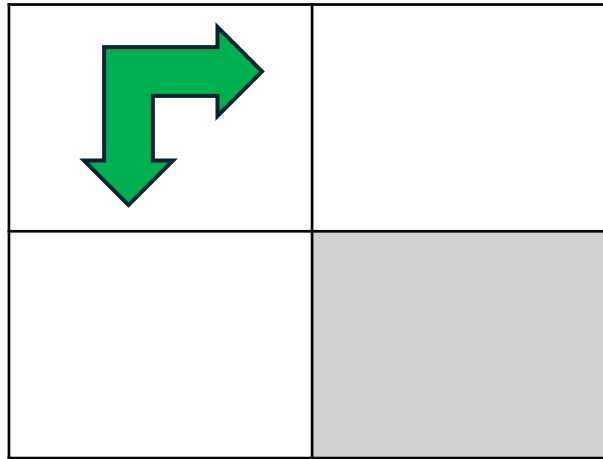
$$q(A, RIGHT) = -2.75$$

$$q(A, DOWN) = -2.75$$

We can now map the value for each **action** from **state A**

$$q(A, UP) = -3$$

$$q(A, LEFT) = -3$$



$$q(A, RIGHT) = -2.75$$

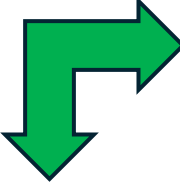
$$q(A, DOWN) = -2.75$$

And update the existing policy for **state A**

$$\pi(A) = \{RIGHT, DOWN\}$$

-2	-1.75
-1.75	0

$k = 2$

$$q(s, a) = \sum_{s', r} P(s', r \mid s, a) [r + v(s')]$$

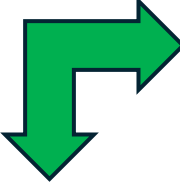
$$q(B, LEFT) = -1 + v(A)$$

$$q(B, LEFT) = -1 + (-2)$$

$$q(B, LEFT) = -3$$

-2	-1.75
-1.75	0

$k = 2$

$$q(s, a) = \sum_{s', r} P(s', r \mid s, a) [r + v(s')]$$

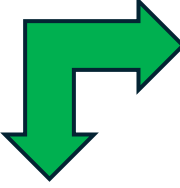
$$q(B, RIGHT) = -1 + v(B)$$

$$q(B, RIGHT) = -1 + (-1.75)$$

$$q(B, RIGHT) = -2.75$$

-2	-1.75
-1.75	0

$k = 2$

$$q(s, a) = \sum_{s', r} P(s', r \mid s, a) [r + v(s')]$$

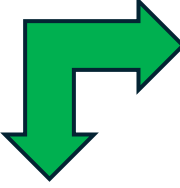
$$q(B, DOWN) = -1 + v(D)$$

$$q(B, DOWN) = -1 + (0)$$

$$q(B, DOWN) = -1$$

-2	-1.75
-1.75	0

$k = 2$

$$q(s, a) = \sum_{s', r} P(s', r \mid s, a) [r + v(s')]$$

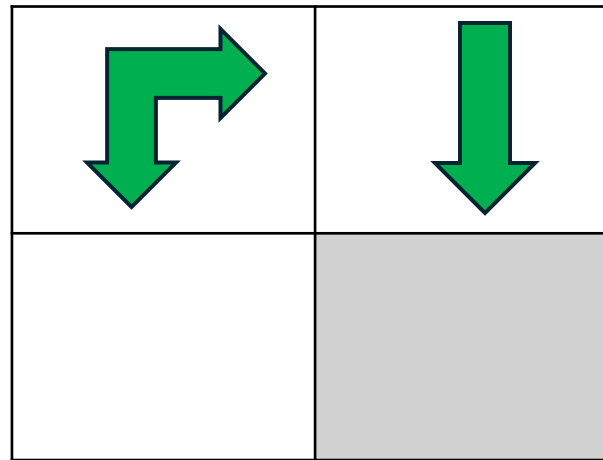
$$q(B, UP) = -1 + v(B)$$

$$q(B, UP) = -1 + (-1.75)$$

$$q(B, UP) = -2.75$$

$$q(B, UP) = -2.75$$

$$q(B, LEFT) = -3$$



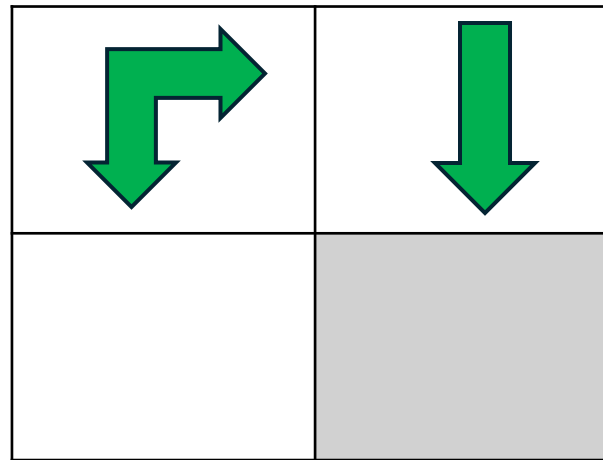
$$q(B, RIGHT) = -2.75$$

$$q(B, DOWN) = -1$$

We can now map the value for each **action** from **state B**

$$q(B, UP) = -2.75$$

$$q(B, LEFT) = -3$$



$$q(B, RIGHT) = -2.75$$

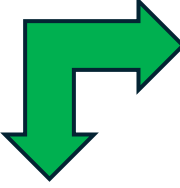

$$q(B, DOWN) = -1$$

Because **DOWN** has the highest action-value function The policy of **state B** will **not change**

$$\pi(B) = \{DOWN\}$$

-2	-1.75
-1.75	0

$k = 2$

$$q(s, a) = \sum_{s', r} P(s', r \mid s, a) [r + v(s')]$$

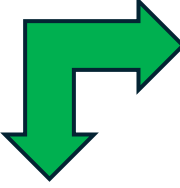

$$q(C, LEFT) = -1 + v(C)$$

$$q(C, LEFT) = -1 + (-1.75)$$

$$q(C, LEFT) = -2.75$$

-2	-1.75
-1.75	0

$k = 2$

$$q(s, a) = \sum_{s', r} P(s', r \mid s, a) [r + v(s')]$$

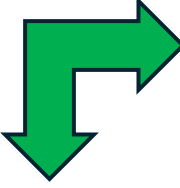

$$q(C, RIGHT) = -1 + v(D)$$

$$q(C, RIGHT) = -1 + (0)$$

$$q(C, RIGHT) = -1$$

-2	-1.75
-1.75	0

$k = 2$

$$q(s, a) = \sum_{s', r} P(s', r \mid s, a) [r + v(s')]$$

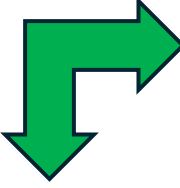

$$q(C, DOWN) = -1 + v(C)$$

$$q(C, DOWN) = -1 + (-1.75)$$

$$q(C, DOWN) = -2.75$$

-2	-1.75
-1.75	0

$k = 2$

$$q(s, a) = \sum_{s', r} P(s', r \mid s, a) [r + v(s')]$$

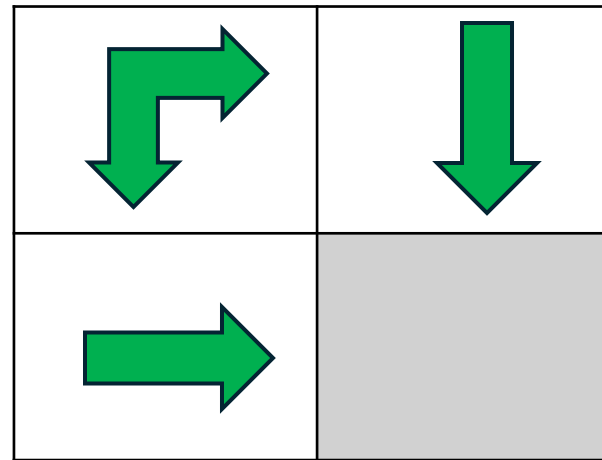
$$q(C, UP) = -1 + v(A)$$

$$q(C, UP) = -1 + (-2)$$

$$q(C, UP) = -3$$

$$q(C, UP) = -3$$

$$q(C, LEFT) = -2.75$$



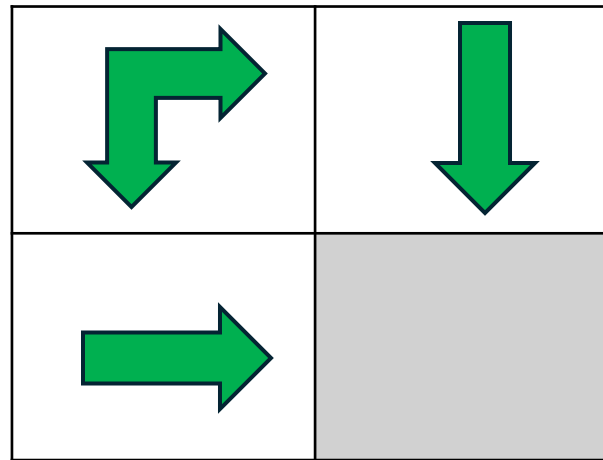
$$q(C, RIGHT) = -1$$

$$q(C, DOWN) = -2.75$$

We can now map the value for each **action** from **state C** and update our **policy**

$$q(C, UP) = -3$$

$$q(C, LEFT) = -2.75$$



$$q(C, RIGHT) = -1$$

$$q(C, DOWN) = -2.75$$

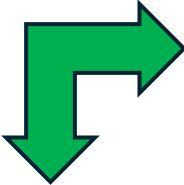

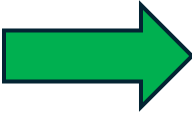
Similar to **state B**, the **policy** for **state C** will stay the same because going right has the highest action value

$$\pi(C) = \{RIGHT\}$$

$k = 2$

-2	-1.75
-1.75	0

Value function v_k
at time step k




Greedy Policy with
respect to v_k

After the second iteration, we can see that we achieved the optimal policy π_*

Value function v_k at time step k for the random policy

-1	-1
-1	0

Greedy Policy with respect to v_k

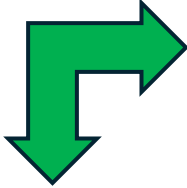


	
	

$$k = 1$$

Value function v_k at time step k for the random policy

-2	-1.75
-1.75	0

Greedy Policy with respect to v_k

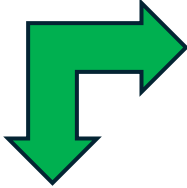


	
	

$$k = 2$$

Value function v_k at time step k for the random policy

-2.875	-2.375
-2.375	0

Greedy Policy with respect to v_k

$k = 3 \text{ onwards}$

Value function for all states at each k iteration

$k = 0$

0	0
0	0

$k = 1$

-1	-1
-1	0

$k = 2$

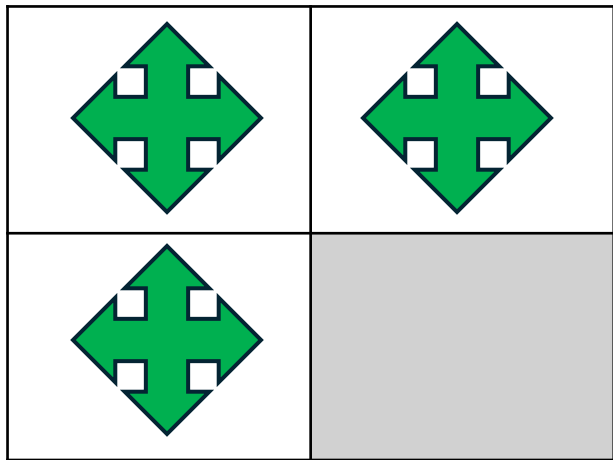
-2	-1.75
-1.75	0

$k = 3$

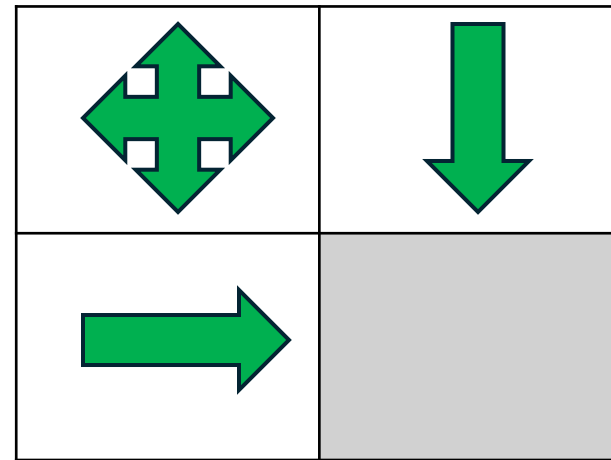
-2.875	-2.375
-2.375	0

Policy improvement each k iteration

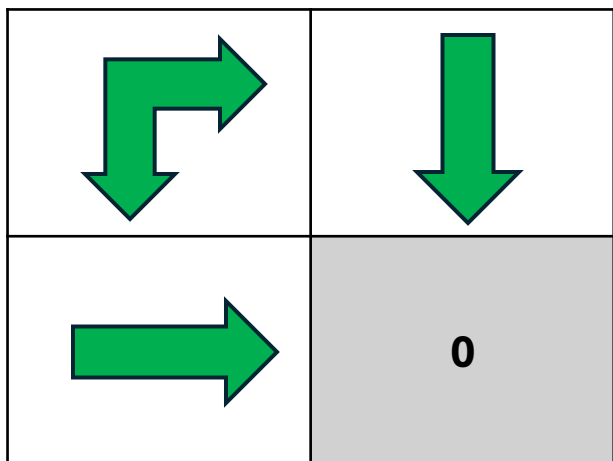
$k = 0$



$k = 1$



$k = 2$



$k = 3$

