



# Forecasting the age structure of the scientific workforce in Australia

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30 June 2025





#### **Labour force model**

$$P_{x+1,t+1} = P_{x,t}(1 - m_{x,t} - r_{x,t}) + G_{x,t} + N_{x,t}$$

x = Aget = Year

 $P_{x,t}$  = number of equivalent full-time workers

 $m_{x,t}$  = probability of death

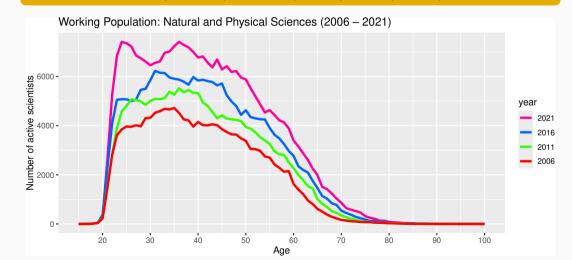
 $r_{x,t}$  = probability of retirement

 $G_{x,t}$  = number of graduates

 $N_{x,t}$  = net number of migrants

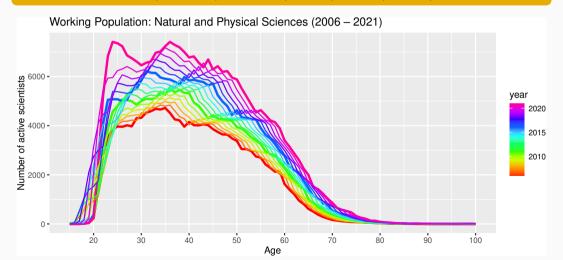
## Working population: $P_{x,t}$

$$P_{x+1,t+1} = P_{x,t}(1 - m_{x,t} - r_{x,t}) + G_{x,t} + N_{x,t}$$



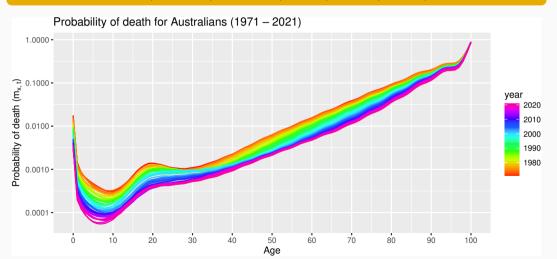
### Working population: $P_{x,t}$

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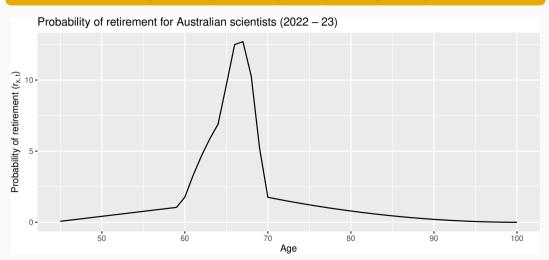
#### Death rates: $m_{x,t}$

$$P_{x+1,t+1} = P_{x,t}(1 - m_{x,t} - r_{x,t}) + G_{x,t} + N_{x,t}$$

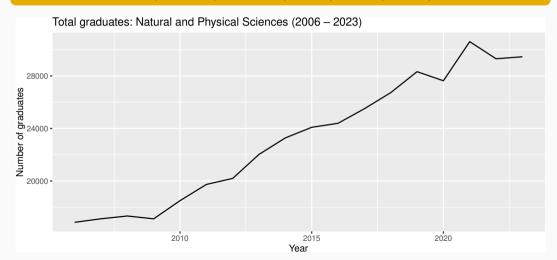


#### Retirement rates: $r_{x,t}$

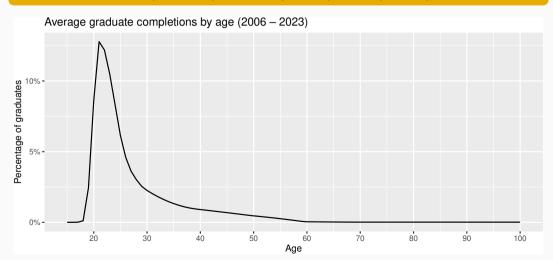
$$P_{x+1,t+1} = P_{x,t}(1 - m_{x,t} - r_{x,t}) + G_{x,t} + N_{x,t}$$



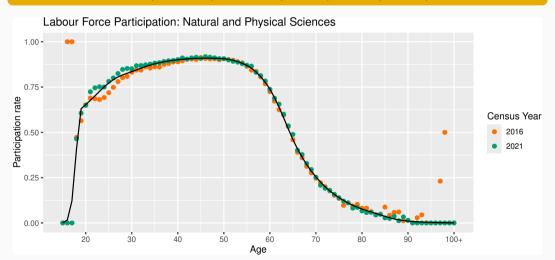
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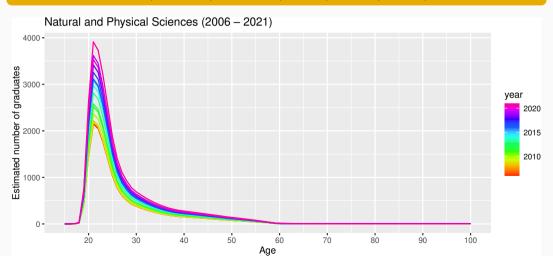
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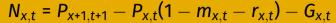
### **Net migration:** $N_{x,t}$

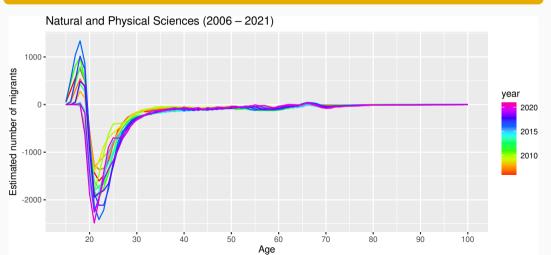
$$P_{x+1,t+1} = P_{x,t}(1 - m_{x,t} - r_{x,t}) + G_{x,t} + N_{x,t}$$

### **Net migration:** $N_{x,t}$

$$N_{x,t} = P_{x+1,t+1} - P_{x,t}(1 - m_{x,t} - r_{x,t}) - G_{x,t}$$

#### Net migration: $N_{x,t}$





#### Forecasting models

$$P_{x+1,t+1} = P_{x,t}(1 - m_{x,t} - r_{x,t}) + G_{x,t} + N_{x,t}$$

 $m_{x,t}$ : a functional time series model

 $r_{x,t}$ : assumed constant over time

 $G_{x,t}$ : ARIMA model of total graduates by year, disaggregated by age using constant functions of age (for graduate age distribution and labour force participation distribution)

 $N_{x,t}$ : a functional time series model