

# Forecast reconciliation

## 4. Probabilistic forecast reconciliation

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# Outline



# Notation reminder

- Data:  $\mathbf{y}_t = \mathbf{S}\mathbf{b}_t$  where  $\mathbf{S}$  is a summing matrix and  $\mathbf{b}_t$  is a vector of disaggregated time series
- Base forecasts:  $\hat{\mathbf{y}}_{T+h|T}$
- Reconciled forecasts:  $\tilde{\mathbf{y}}_{T+h|T} = \mathbf{S}\mathbf{G}\hat{\mathbf{y}}_{T+h|T}$
- MinT:  $\mathbf{G} = (\mathbf{S}'\mathbf{W}_h^{-1}\mathbf{S})^{-1}\mathbf{S}'\mathbf{W}_h^{-1}$  where  $\mathbf{W}_h$  is covariance matrix of base forecast errors.

# Probabilistic forecasts

- Gaussian
- Non-parametric
- Count

# References

-  Ben Taieb, S, JW Taylor, and RJ Hyndman (2021). Hierarchical Probabilistic Forecasting of Electricity Demand with Smart Meter Data. *J American Statistical Association* **116**(533), 27–43.
-  Panagiotelis, A, P Gamakumara, G Athanasopoulos, and RJ Hyndman (2023). Probabilistic forecast reconciliation: properties, evaluation and score optimisation. *European J Operational Research* **306**(2), 693–706.