



# GRATIS: GeneRAting Time Series with diverse and controllable characteristics

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#### Time series features

- seasonal period(s)
- length
- ACF and PACF based features - calculated on raw, differenced, and remainder series.
- strength of seasonality
- strength of trend
- peaks, troughs
- spectral entropy
- linearity

- curvature
- spikiness
- stability
- lumpiness
- Hurst exponent
- nonlinearity
- unit root test statistics
- crossing points, flat spots
- ARCH/GARCH statistics and ACF of squared series and residuals.

## Mixture autoregressive (MAR) models

### AR(p) model

$$\mathbf{x}_t = \phi_0 + \phi_1 \mathbf{x}_{t-1} + \dots + \phi_p \mathbf{x}_{t-p} + \varepsilon_t, \quad \varepsilon_t \sim \mathsf{N}(0, \sigma^2)$$

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#### $MAR(K; p_1, p_2, \dots, p_K)$ model

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#### **MAR** models

- can contain multiple stationary or non-stationary autoregressive components.
- can handle nonlinearity, non-Gaussianity, cycles and heteroskedasticity

## **GRATIS** package

GeneRAting TIme Series with diverse and controllable characteristics





- https://github.com/ykang/gratis
- https://cran.r-project.org/package=gratis