



# **vital: Tidy data analysis for demography**

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# Demographic data structures in R packages

Package	Data class
demography	demogdata
StMoMo	StMoMoData (created by converting a demogdata object)
StanMoMo	Lists of matrices
lifecontingencies	data.frame
BayesMortalityPlus	tibble (that needs to be converted to a matrix for fitting)
MortalityLaws	individual vectors
HMDHFDplus	data.frame



## Australian Deaths 1901–2020

```
# A tibble: 145,440 x 7
```

	Year	Age	Sex	State	Mortality	Exposure	Deaths
	<int>	<int>	<chr>	<chr>	<dbl>	<dbl>	<dbl>
1	1901	0	female	WA	0.129	2511	325
2	1901	0	male	WA	0.158	2634	416
3	1901	1	female	WA	0.0275	2219	61
4	1901	1	male	WA	0.0391	2175	85
5	1901	2	female	WA	0.00688	2180	15
6	1901	2	male	WA	0.0131	2208	29
7	1901	3	female	WA	0.00584	1884	11
8	1901	3	male	WA	0.00503	1988	10
9	1901	4	female	WA	0.00290	1722	5
10	1901	4	male	WA	0.00287	1743	5

```
# i 145,430 more rows
```



## Australian Deaths 1901–2020

```
# A tsibble: 145,440 x 7 [1Y]
```

```
# Key:      Age, Sex, State [1,212]
```

	Year	Age	Sex	State	Mortality	Exposure	Deaths
	<int>	<int>	<chr>	<chr>	<dbl>	<dbl>	<dbl>
1	1901	0	female	WA	0.129	2511	325
2	1901	0	male	WA	0.158	2634	416
3	1901	1	female	WA	0.0275	2219	61
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9	1901	4	female	WA	0.00290	1722	5
10	1901	4	male	WA	0.00287	1743	5

```
# i 145,430 more rows
```

## Variables

Index:

■ Year

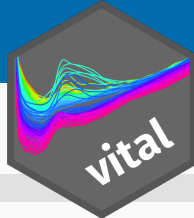
Keys:

■ Age

■ Sex

■ State

Every row must have a unique combination of Index and Keys



## Australian Deaths 1901–2020

aus

```
# A vital: 145,440 x 7 [1Y]
# Key:      Age x (Sex, State) [101 x 12]
  Year  Age Sex  State Mortality Exposure Deaths
  <int> <int> <chr> <chr>      <dbl>      <dbl>      <dbl>
1  1901     0 female WA         0.129        2511        325
2  1901     0 male  WA         0.158        2634        416
3  1901     1 female WA         0.0275       2219         61
4  1901     1 male  WA         0.0391       2175         85
5  1901     2 female WA         0.00688      2180         15
6  1901     2 male  WA         0.0131      2208         29
7  1901     3 female WA         0.00584      1884         11
8  1901     3 male  WA         0.00503      1988         10
9  1901     4 female WA         0.00290       1722          5
10 1901     4 male  WA         0.00287      1743          5
# i 145,430 more rows
```

### Variables

Index:

■ Year

Keys:

■ Age

■ Sex

■ State

Every row must have a unique combination of Index and Keys

Variables denoting age, sex, deaths, births and population can also be specified as attributes.

# vital objects

```
index_var(aus)
```

```
[1] "Year"
```

```
key_vars(aus)
```

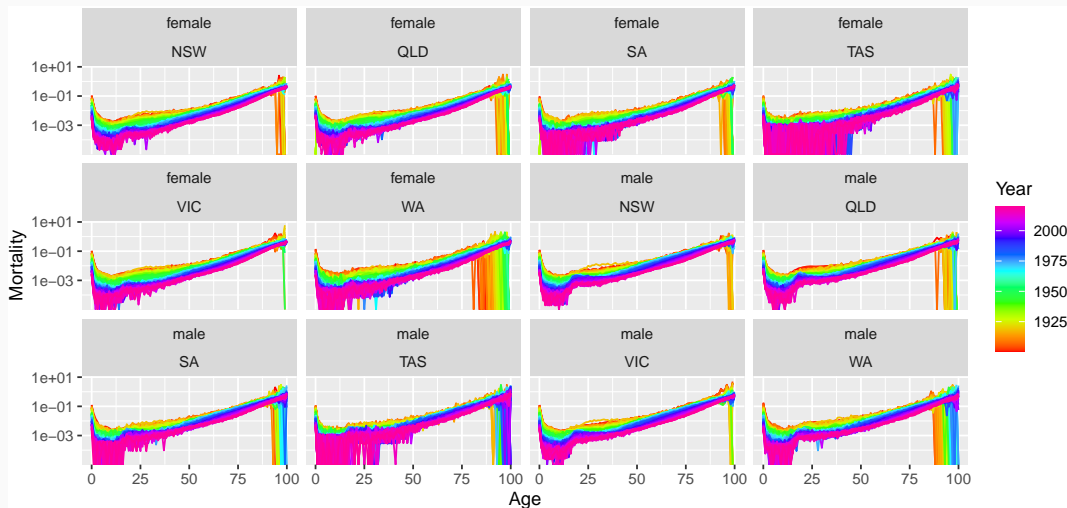
```
[1] "Age"    "Sex"    "State"
```

```
vital_vars(aus)
```

age	sex	deaths	population
"Age"	"Sex"	"Deaths"	"Exposure"

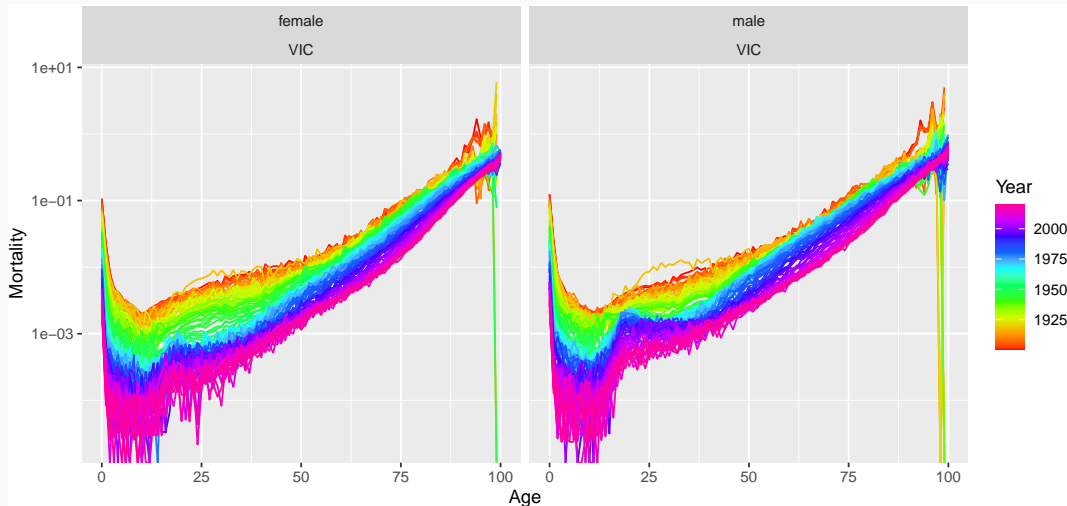
# Rainbow plots

```
aus |> autoplot(Mortality) + scale_y_log10()
```



# Rainbow plots

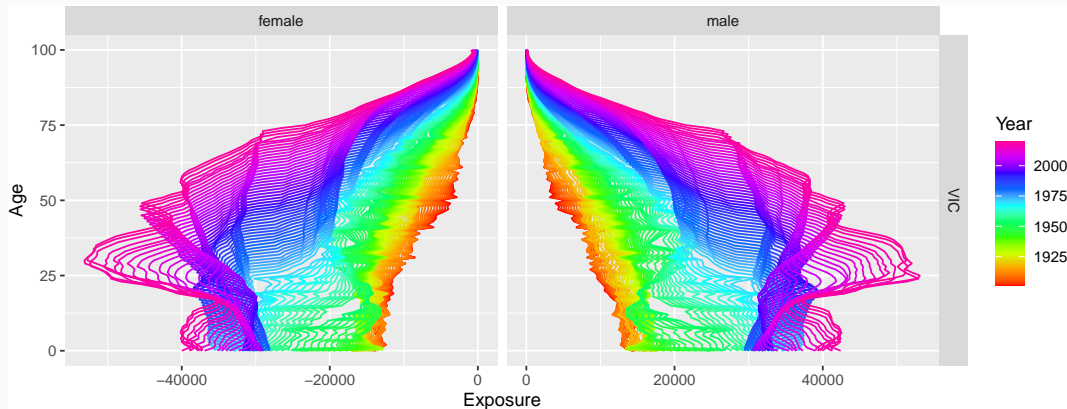
```
aus |> filter(State == "VIC") |> autoplot(Mortality) + scale_y_log10()
```





# Rainbow plots

```
aus |> filter(State == "VIC") |>  
  mutate(Exposure = if_else(Sex == "female", -Exposure, Exposure)) |>  
  autoplot(Exposure) +  
  facet_grid(State ~ Sex, scales = "free_x") + coord_flip()
```



# Smoothing

```
sm_aus <- aus |> smooth_mortality(Mortality)
sm_aus
```

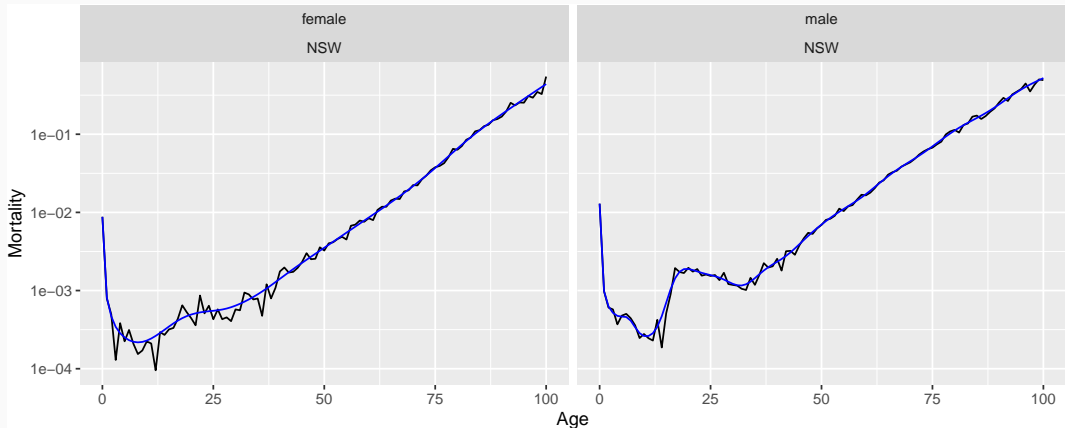
```
# A vital: 145,440 x 9 [1Y]
```

```
# Key:      Age x (Sex, State) [101 x 12]
```

	Year	Age	Sex	State	Mortality	Exposure	Deaths	.smooth	.smooth_se
	<int>	<dbl>	<chr>	<chr>	<dbl>	<dbl>	<dbl>	<dbl[1d]>	<dbl[1d]>
1	1901	0	female	NSW	0.107	17143	1833	0.107	0.00295
2	1901	1	female	NSW	0.0247	15071	373	0.0237	0.00141
3	1901	2	female	NSW	0.00686	15461	106	0.00804	0.000670
4	1901	3	female	NSW	0.00441	15629	69	0.00461	0.000405
5	1901	4	female	NSW	0.00374	15762	59	0.00341	0.000305
6	1901	5	female	NSW	0.00274	16030	44	0.00275	0.000251
7	1901	6	female	NSW	0.00252	16289	41	0.00230	0.000215
8	1901	7	female	NSW	0.00216	16639	36	0.00197	0.000189
9	1901	8	female	NSW	0.00169	16554	28	0.00175	0.000173
10	1901	9	female	NSW	0.00109	16468	18	0.00162	0.000163

# Smoothing

```
sm_aus <- aus |> smooth_mortality(Mortality)
sm_aus |> filter(State == "NSW", Year == 1980) |> autoplot(Mortality) +
  geom_line(aes(y = .smooth), col = "blue") + scale_y_log10()
```



# Life tables

```
life_table(aus)
```

```
# A vital: 145,440 x 14 [1Y]
```

```
# Key:      Age x (Sex, State) [101 x 12]
```

	Year	Age	Sex	State	mx	qx	lx	dx	Lx	Tx	ex	rx
	<int>	<int>	<chr>	<chr>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>
1	1901	0	fema~	NSW	0.107	0.100	1	1.00e-1	0.935	56.2	56.2	0.935
2	1901	1	fema~	NSW	0.0247	0.0244	0.900	2.20e-2	0.889	55.3	61.5	0.951
3	1901	2	fema~	NSW	0.00686	0.00683	0.878	6.00e-3	0.875	54.4	62.0	0.984
4	1901	3	fema~	NSW	0.00441	0.00441	0.872	3.84e-3	0.870	53.5	61.4	0.994
5	1901	4	fema~	NSW	0.00374	0.00374	0.868	3.24e-3	0.867	52.7	60.7	0.996
6	1901	5	fema~	NSW	0.00274	0.00274	0.865	2.37e-3	0.864	51.8	59.9	0.997
7	1901	6	fema~	NSW	0.00252	0.00251	0.863	2.17e-3	0.861	50.9	59.1	0.997
8	1901	7	fema~	NSW	0.00216	0.00216	0.860	1.86e-3	0.859	50.1	58.2	0.998
9	1901	8	fema~	NSW	0.00169	0.00169	0.859	1.45e-3	0.858	49.2	57.3	0.998
10	1901	9	fema~	NSW	0.00109	0.00109	0.857	9.36e-4	0.857	48.4	56.4	0.999

```
# i 145,430 more rows
```

# Life expectancy

```
life_expectancy(aus)
```

```
# A vital: 1,440 x 8 [1Y]
```

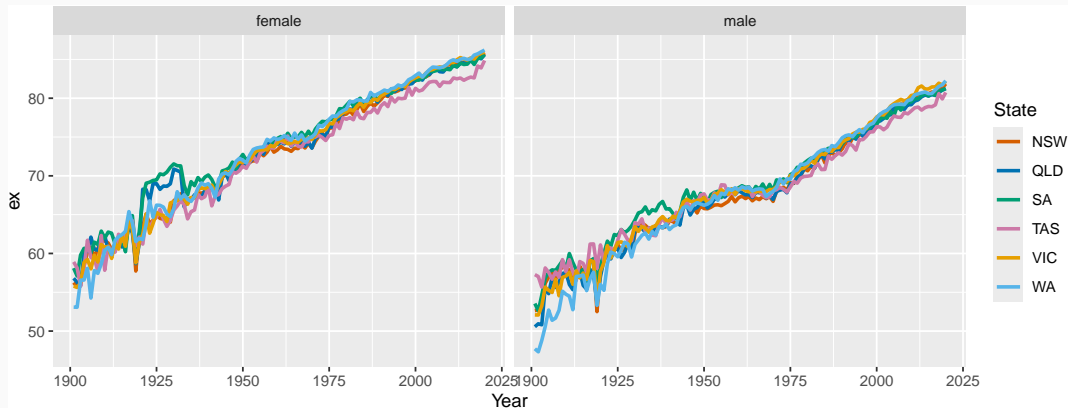
```
# Key:      Age x (Sex, State) [1 x 12]
```

	Year	Age	Sex	State	ex	rx	nx	ax
	<int>	<int>	<chr>	<chr>	<dbl>	<dbl>	<dbl>	<dbl>
1	1901	0	female	NSW	56.2	0.935	1	0.352
2	1901	0	female	QLD	56.8	0.937	1	0.338
3	1901	0	female	SA	58.1	0.939	1	0.324
4	1901	0	female	TAS	58.9	0.946	1	0.275
5	1901	0	female	VIC	55.8	0.937	1	0.334
6	1901	0	female	WA	53.1	0.922	1	0.35
7	1901	0	male	NSW	52.6	0.925	1	0.33
8	1901	0	male	QLD	50.6	0.924	1	0.33
9	1901	0	male	SA	53.5	0.922	1	0.33
10	1901	0	male	TAS	57.3	0.930	1	0.33

```
# i 1,430 more rows
```

# Life expectancy

```
life_expectancy(aus) |>  
  ggplot(aes(x = Year, y = ex, colour = State)) +  
  geom_line(linewidth = 1) +  
  facet_grid(. ~ Sex)
```



# Mortality models

$m_{x,t}$  = mortality rate at age  $x$  in year  $t$ .

Naive:  $m_{x,t} = m_{x,t-1} + \varepsilon_{x,t}$

Lee-Carter:  $\log(m_{x,t}) = a_x + k_t b_x + \varepsilon_{x,t}$

$\varepsilon_{x,t}$  = noise term with variance  $\sigma_x^2$ .

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```
fit <- aus |>
  model(
    naive = FNAIVE(Mortality),
    lc = LC(log(Mortality))
  )
```



# Mortality models

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```
fit <- aus |>
  model(
    naive = FNAIVE(Mortality),
    lc = LC(log(Mortality))
  )
```

fit

```
# A mable: 12 x 4
# Key:      Sex, State [12]
   Sex      State      naive      lc
   <chr>   <chr>   <model> <model>
1 female NSW      <FNAIVE> <LC>
2 female QLD      <FNAIVE> <LC>
3 female SA       <FNAIVE> <LC>
4 female TAS      <FNAIVE> <LC>
5 female VIC      <FNAIVE> <LC>
6 female WA       <FNAIVE> <LC>
7 male  NSW      <FNAIVE> <LC>
8 male  QLD      <FNAIVE> <LC>
9 male  SA       <FNAIVE> <LC>
10 male TAS      <FNAIVE> <LC>
11 male VIC      <FNAIVE> <LC>
12 male WA       <FNAIVE> <LC>
```

```
fit |>
  filter(Sex == "female",
         State == "NSW") |>
  select(lc) |>
  report()
```

Series: Mortality

Model: LC

Transformation: log(Mortality)

Options:

Adjust method: dt

Jump choice: fit

Age functions

```
# A tibble: 101 × 3
  Age    ax    bx
<int> <dbl> <dbl>
1     0 -4.07 0.0155
2     1 -6.20 0.0221
3     2 -6.89 0.0199
# i 98 more rows
```

Time coefficients

```
# A tsibble: 120 × 2 [1Y]
  Year    kt
<int> <dbl>
1  1901 109.
2  1902 111.
3  1903 108.
# i 117 more rows
```

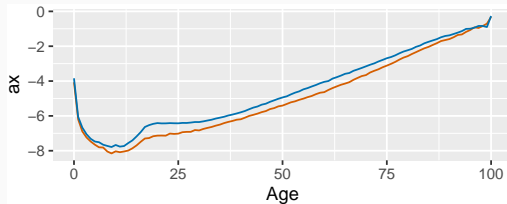
Time series model: RW w/ drift

Variance explained: 86.61%

# Lee-Carter models

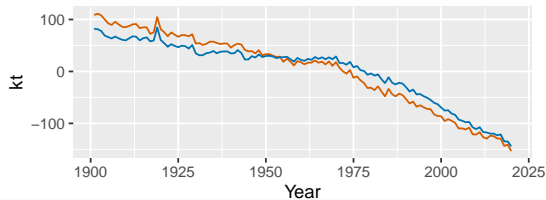
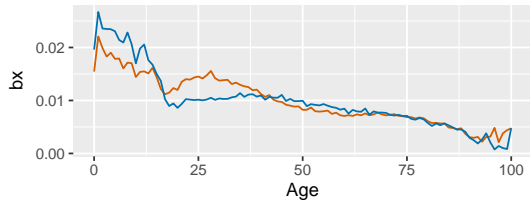
$$\log(m_{x,t}) = a_x + k_t b_x + \varepsilon_{x,t}$$

```
fit |>  
  filter(State == "NSW") |>  
  select(lc) |>  
  autoplot()
```



Sex/State

— female/NSW  
— male/NSW



# Lee-Carter models

$$\log(m_{x,t}) = a_x + k_t b_x + \varepsilon_{x,t}$$

```
fit |> select(lc) |> age_components()
```

```
# A tibble: 1,212 x 5
```

	Sex	State	Age	ax	bx
	<chr>	<chr>	<int>	<dbl>	<dbl>
1	female	NSW	0	-4.07	0.0155
2	female	NSW	1	-6.20	0.0221
3	female	NSW	2	-6.89	0.0199
4	female	NSW	3	-7.24	0.0183
5	female	NSW	4	-7.47	0.0190
6	female	NSW	5	-7.65	0.0178
7	female	NSW	6	-7.80	0.0179
8	female	NSW	7	-7.81	0.0160
9	female	NSW	8	-8.05	0.0171
10	female	NSW	9	-8.15	0.0170

```
# i 1,202 more rows
```

```
fit |> select(lc) |> time_components()
```

```
# A tsibble: 1,440 x 4 [1Y]
```

# Key:	Sex	State	Year	kt
	<chr>	<chr>	<int>	<dbl>
1	female	NSW	1901	109.
2	female	NSW	1902	111.
3	female	NSW	1903	108.
4	female	NSW	1904	100.
5	female	NSW	1905	92.7
6	female	NSW	1906	89.5
7	female	NSW	1907	95.7
8	female	NSW	1908	90.5
9	female	NSW	1909	85.9
10	female	NSW	1910	85.4

```
# i 1,430 more rows
```

# Forecasts

```
fc <- fit |> forecast(h = 20)
fc
```

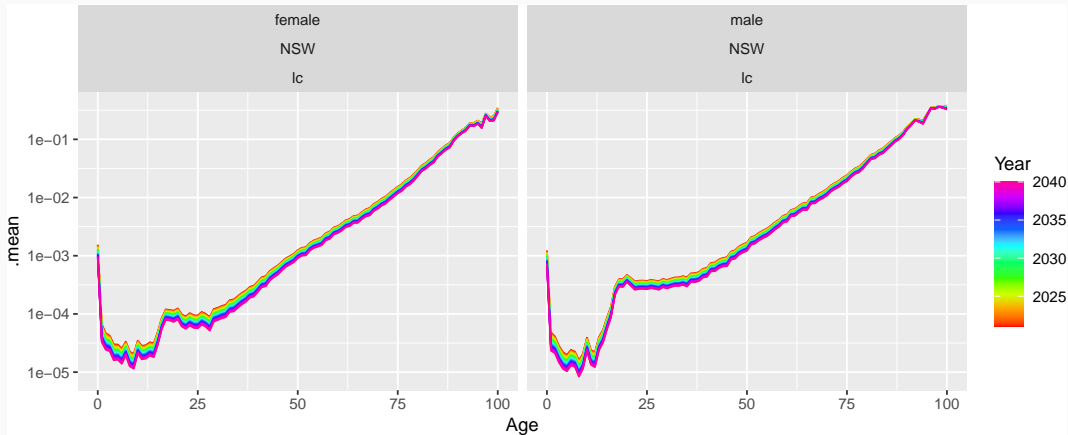
```
# A vital fable: 48,480 x 7 [1Y]
```

```
# Key:           Age x (Sex, State, .model) [101 x 24]
```

	Sex	State	.model	Year	Age	Mortality	.mean
	<chr>	<chr>	<chr>	<dbl>	<int>	<dist>	<dbl>
1	female	NSW	naive	2021	0	N(0.0027, 1.8e-05)	0.00270
2	female	NSW	naive	2022	0	N(0.0027, 3.6e-05)	0.00270
3	female	NSW	naive	2023	0	N(0.0027, 5.4e-05)	0.00270
4	female	NSW	naive	2024	0	N(0.0027, 7.2e-05)	0.00270
5	female	NSW	naive	2025	0	N(0.0027, 9e-05)	0.00270
6	female	NSW	naive	2026	0	N(0.0027, 0.00011)	0.00270
7	female	NSW	naive	2027	0	N(0.0027, 0.00013)	0.00270
8	female	NSW	naive	2028	0	N(0.0027, 0.00014)	0.00270
9	female	NSW	naive	2029	0	N(0.0027, 0.00016)	0.00270
10	female	NSW	naive	2030	0	N(0.0027, 0.00018)	0.00270

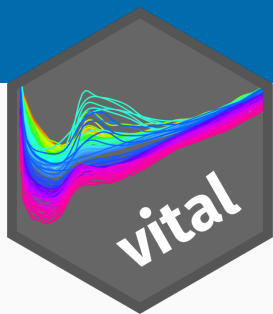
# NSW forecasts using Lee-Carter method

```
fc |> filter(State == "NSW", .model == "lc") |>  
  autoplot() + scale_y_log10()
```



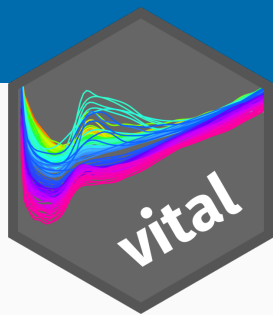
# Other functionality

- Import data from Human Mortality Database and Human Fertility Database
- Convert demogdata, tsibble & data.frame objects to vital.
- Compute net migration from population, births and deaths.
- Compute total fertility rates from age-specific fertility rates.
- Various smoothing functions
- Other mortality models including functional data models, and coherent functional data models.



# Future plans

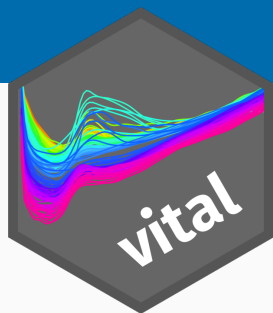
- Remaining tools from the demography package
- Stochastic population forecasting (as per Hyndman-Booth, IJF, 2008)
- All models handled by StMoMo package
- All methods from MortalityLaws package
- Suggestions from users





# Future plans

- Remaining tools from the demography package
- Stochastic population forecasting (as per Hyndman-Booth, IJF, 2008)
- All models handled by StMoMo package
- All methods from MortalityLaws package
- Suggestions from users



- **Slides:** [robjhyndman.com/user2024](http://robjhyndman.com/user2024)
- **Package:** [pkg.robjhyndman.com/vital/](http://pkg.robjhyndman.com/vital/)