



# Tidy data analysis for demography using R

Rob J Hyndman

26 June 2024

# Outline

- 1 Vital objects
- 2 Using the Human Mortality and Fertility Databases
- 3 Plots
- 4 Life tables and life expectancy
- 5 Mortality models
- 6 Other features and future plans

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# Demographic data structures in R packages

Package	Data class
demography	demogdata
StMoMo	StMoMoData (created by converting a demogdata object)
StanMoMo	Lists of matrices
lifecontingencies	data.frame
BayesMortalityPlus	tibble (that needs to be converted to a matrix for fitting)
MortalityLaws	individual vectors
HMDHFDplus	data.frame



## Australian Deaths 1901–2020

# A tibble: 145,440 x 7

	Year	Age	Sex	State	Mortality	Exposure	Deaths
	<int>	<int>	<chr>	<chr>	<dbl>	<dbl>	<dbl>
1	1901	0	female	WA	0.129	2511	325
2	1901	0	male	WA	0.158	2634	416
3	1901	1	female	WA	0.0275	2219	61
4	1901	1	male	WA	0.0391	2175	85
5	1901	2	female	WA	0.00688	2180	15
6	1901	2	male	WA	0.0131	2208	29
7	1901	3	female	WA	0.00584	1884	11
8	1901	3	male	WA	0.00503	1988	10
9	1901	4	female	WA	0.00290	1722	5
10	1901	4	male	WA	0.00287	1743	5

# i 145,430 more rows



## Australian Deaths 1901–2020

```
# A tsibble: 145,440 x 7 [1Y]
```

```
# Key:      Age, Sex, State [1,212]
```

	Year	Age	Sex	State	Mortality	Exposure	Deaths
	<int>	<int>	<chr>	<chr>	<dbl>	<dbl>	<dbl>
1	1901	0	female	WA	0.129	2511	325
2	1901	0	male	WA	0.158	2634	416
3	1901	1	female	WA	0.0275	2219	61
4	1901	1	male	WA	0.0391	2175	85
5	1901	2	female	WA	0.00688	2180	15
6	1901	2	male	WA	0.0131	2208	29
7	1901	3	female	WA	0.00584	1884	11
8	1901	3	male	WA	0.00503	1988	10
9	1901	4	female	WA	0.00290	1722	5
10	1901	4	male	WA	0.00287	1743	5

```
# i 145,430 more rows
```

## Variables

Index:

■ Year

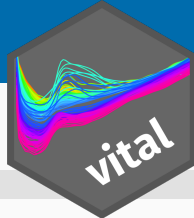
Keys:

■ Age

■ Sex

■ State

Every row must have a unique combination of Index and Keys



## Australian Deaths 1901–2020

aus

```
# A vital: 145,440 x 7 [1Y]
```

```
# Key:      Age x (Sex, State) [101 x 12]
```

	Year	Age	Sex	State	Mortality	Exposure	Deaths
	<int>	<int>	<chr>	<chr>	<dbl>	<dbl>	<dbl>
1	1901	0	female	WA	0.129	2511	325
2	1901	0	male	WA	0.158	2634	416
3	1901	1	female	WA	0.0275	2219	61
4	1901	1	male	WA	0.0391	2175	85
5	1901	2	female	WA	0.00688	2180	15
6	1901	2	male	WA	0.0131	2208	29
7	1901	3	female	WA	0.00584	1884	11
8	1901	3	male	WA	0.00503	1988	10
9	1901	4	female	WA	0.00290	1722	5
10	1901	4	male	WA	0.00287	1743	5

```
# i 145,430 more rows
```

## Variables

Index:

■ Year

Keys:

■ Age

■ Sex

■ State

Every row must have a unique combination of Index and Keys

Variables denoting age, sex, deaths, births and population can also be specified as attributes.

# vital objects

```
index_var(aus)
```

```
[1] "Year"
```

```
key_vars(aus)
```

```
[1] "Age"    "Sex"    "State"
```

```
vital_vars(aus)
```

age	sex	deaths	population
"Age"	"Sex"	"Deaths"	"Exposure"



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## Human Mortality Database

### Reliability and Accuracy Matter

The Human Mortality Database (HMD) is the world's leading scientific data resource on mortality in developed countries. The HMD provides detailed high-quality harmonized mortality and population estimates to researchers, students, journalists, policy analysts, and others interested in human longevity. The HMD follows open data principles.

- > [Short-Term Mortality Fluctuations](#)
- > [Cause-of-Death Data Series](#)
- > [Subnational Mortality Databases](#)
- > [Citing HMD](#)

#### Data by country or area

[Australia](#)[Denmark](#)[Ireland](#)[Norway](#)[Switzerland](#)[Austria](#)[Estonia](#)[Israel](#)[Poland](#)[Taiwan](#)[Belarus](#)[Finland](#)[Italy](#)[Portugal](#)[U.K.](#)[Belgium](#)[France](#)[Japan](#)[Republic of Korea](#)[U.S.A.](#)



## Human Fertility Database

The Human Fertility Database (HFD) is the leading scientific data resource on fertility in the developed countries. This open access database provides detailed and high-quality historical and recent data on period and cohort fertility by age of mother and birth order. The HFD is entirely based on official vital statistics and places a great emphasis on rigorous data checking and documentation. The HFD adopts uniform methodology to warrant data comparability across time and between countries. The database follows open data principles.

[> Short-Term Fertility Fluctuations](#)[> Human Fertility Collection](#)[> Citing HFD](#)[> What's new](#)

For users who seek fast access to the most commonly used summary indicators of period and cohort fertility, we provide excel tables comprising the following indicators for all the HFD countries:

### HFD summary indicators

[Total fertility rate](#)[Tempo-adjusted TFR](#)[Mean age at birth](#)[Mean age at first birth](#)[Completed cohort fertility](#)[Cohort parity](#)

# HMD imports

```
norway ← read_hmd(  
  country = "NOR",  
  username = "Nora.Weigh@mymail.com",  
  password = "FF!5xeEFa6"  
)  
norway_births ← read_hmd(  
  country = "NOR",  
  username = "Nora.Weigh@mymail.com",  
  password = "FF!5xeEFa6",  
  variables = "Births"  
)
```

- Uses HMDHFDplus package to handle the downloads.
- Default variables: Deaths, Exposures, Population, Mx
- Only 1 × 1 data supported.
- read\_hmd\_files() and read\_hfd\_files() allow reading of downloaded files.

# HMD imports

```
norway_births
```

```
# A vital: 531 x 3 [1Y]
# Key:      Sex [3]
  Year Sex   Births
  <int> <chr>  <int>
1  1846 Female 20156
2  1846 Male  21372
3  1846 Total 41528
4  1847 Female 20199
5  1847 Male  21411
6  1847 Total 41610
7  1848 Female 19686
8  1848 Male  20868
9  1848 Total 40554
10 1849 Female 21424
# i 521 more rows
```

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# Recall: Australian mortality data

```
aus
```

```
# A vital: 145,440 x 7 [1Y]
```

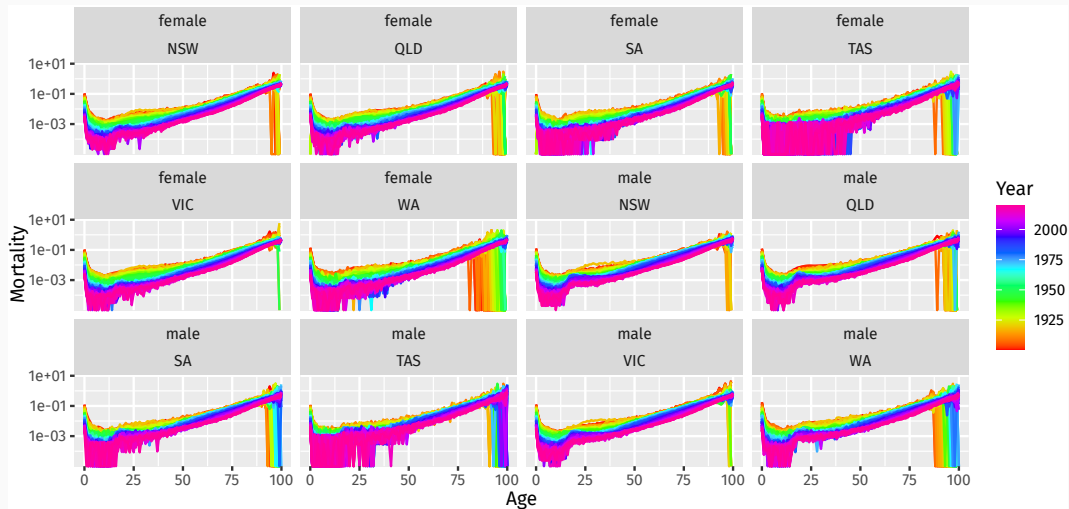
```
# Key:      Age x (Sex, State) [101 x 12]
```

	Year	Age	Sex	State	Mortality	Exposure	Deaths
	<int>	<int>	<chr>	<chr>	<dbl>	<dbl>	<dbl>
1	1901	0	female	WA	0.129	2511	325
2	1901	0	male	WA	0.158	2634	416
3	1901	1	female	WA	0.0275	2219	61
4	1901	1	male	WA	0.0391	2175	85
5	1901	2	female	WA	0.00688	2180	15
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7	1901	3	female	WA	0.00584	1884	11
8	1901	3	male	WA	0.00503	1988	10
9	1901	4	female	WA	0.00290	1722	5
10	1901	4	male	WA	0.00287	1743	5

```
# i 145,430 more rows
```

# Rainbow plots

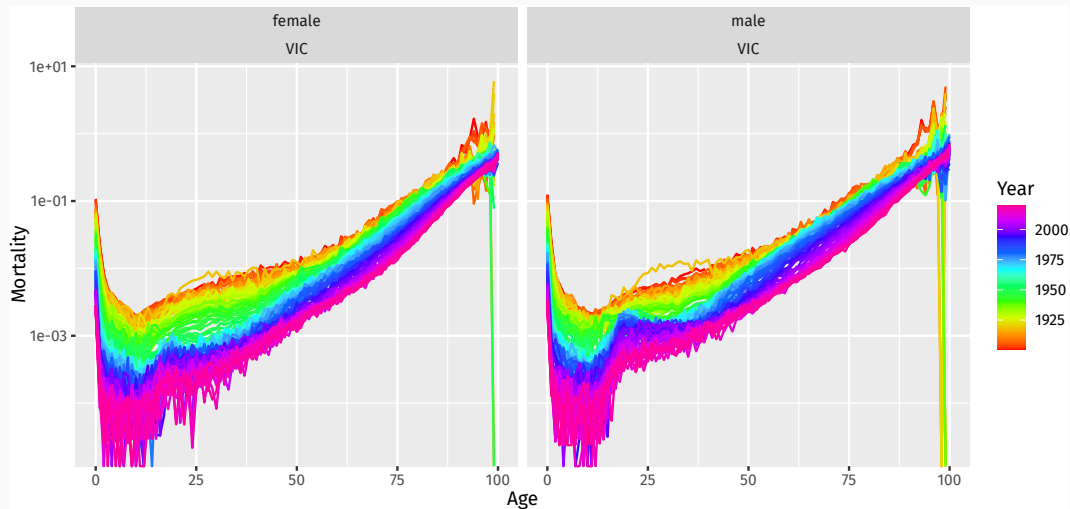
```
aus > autoplot(Mortality) + scale_y_log10()
```





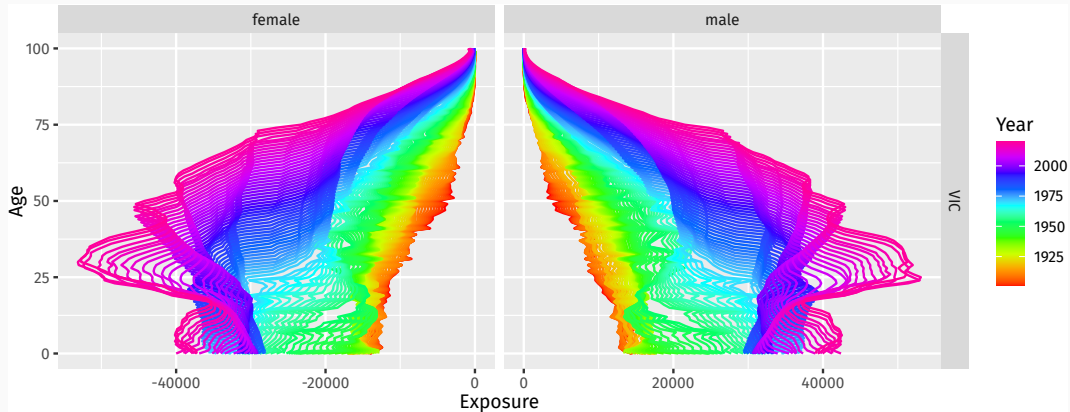
# Rainbow plots

```
aus > filter(State == "VIC") > autoplot(Mortality) + scale_y_log10()
```



# Rainbow plots

```
aus > filter(State == "VIC") >  
  mutate(Exposure = if_else(Sex == "female", -Exposure, Exposure)) >  
  autoplot(Exposure) +  
  facet_grid(State ~ Sex, scales = "free_x") + coord_flip()
```



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# Life tables

```
life_table(aus)
```

```
# A vital: 145,440 x 14 [1Y]
```

```
# Key:      Age x (Sex, State) [101 x 12]
```

	Year	Age	Sex	State	mx	qx	lx	dx	Lx	Tx	ex	rx
	<int>	<int>	<chr>	<chr>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>
1	1901	0	fema~	NSW	0.107	0.100	1	1.00e-1	0.935	56.2	56.2	0.935
2	1901	1	fema~	NSW	0.0247	0.0244	0.900	2.20e-2	0.889	55.3	61.5	0.951
3	1901	2	fema~	NSW	0.00686	0.00683	0.878	6.00e-3	0.875	54.4	62.0	0.984
4	1901	3	fema~	NSW	0.00441	0.00441	0.872	3.84e-3	0.870	53.5	61.4	0.994
5	1901	4	fema~	NSW	0.00374	0.00374	0.868	3.24e-3	0.867	52.7	60.7	0.996
6	1901	5	fema~	NSW	0.00274	0.00274	0.865	2.37e-3	0.864	51.8	59.9	0.997
7	1901	6	fema~	NSW	0.00252	0.00251	0.863	2.17e-3	0.861	50.9	59.1	0.997
8	1901	7	fema~	NSW	0.00216	0.00216	0.860	1.86e-3	0.859	50.1	58.2	0.998
9	1901	8	fema~	NSW	0.00169	0.00169	0.859	1.45e-3	0.858	49.2	57.3	0.998
10	1901	9	fema~	NSW	0.00109	0.00109	0.857	9.36e-4	0.857	48.4	56.4	0.999

```
# i 145,430 more rows
```

```
# i 2 more variables: nx <dbl>, ax <dbl>
```

# Life expectancy

```
life_expectancy(aus)
```

```
# A vital: 1,440 x 8 [1Y]
```

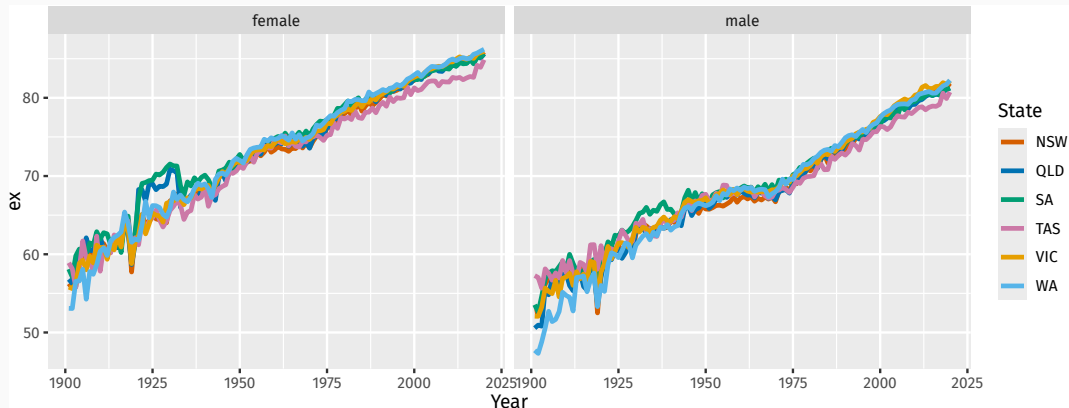
```
# Key:      Age x (Sex, State) [1 x 12]
```

	Year	Age	Sex	State	ex	rx	nx	ax
	<int>	<int>	<chr>	<chr>	<dbl>	<dbl>	<dbl>	<dbl>
1	1901	0	female	NSW	56.2	0.935	1	0.352
2	1901	0	female	QLD	56.8	0.937	1	0.338
3	1901	0	female	SA	58.1	0.939	1	0.324
4	1901	0	female	TAS	58.9	0.946	1	0.275
5	1901	0	female	VIC	55.8	0.937	1	0.334
6	1901	0	female	WA	53.1	0.922	1	0.35
7	1901	0	male	NSW	52.6	0.925	1	0.33
8	1901	0	male	QLD	50.6	0.924	1	0.33
9	1901	0	male	SA	53.5	0.922	1	0.33
10	1901	0	male	TAS	57.3	0.930	1	0.33

```
# i 1,430 more rows
```

# Life expectancy

```
life_expectancy(aus) ▷  
  ggplot(aes(x = Year, y = ex, colour = State)) +  
  geom_line(linewidth = 1) +  
  facet_grid(. ~ Sex)
```



# Life table calculations

- All available years and ages are included in the tables.
- $q_x = m_x / (1 + [(1 - a_x)m_x])$  as per Chiang (1984).
- The code has only been tested for data based on single-year age groups.
- Same code base as for the demography package.
- Life expectancy with `life_expectancy()` computes  $e_x$  with  $x = 0$  by default, but other values are possible.

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# Mortality models

$m_{x,t}$  = mortality rate at age  $x$  in year  $t$ .

Naive:  $m_{x,t} = m_{x,t-1} + \varepsilon_{x,t}$

Lee-Carter:  $\log(m_{x,t}) = a_x + k_t b_x + \varepsilon_{x,t}$

$\varepsilon_{x,t}$  = noise term with variance  $\sigma_x^2$ .

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Lee-Carter:  $\log(m_{x,t}) = a_x + k_t b_x + \varepsilon_{x,t}$

$\varepsilon_{x,t}$  = noise term with variance  $\sigma_x^2$ .

## Lee-Carter variations

- Lee & Carter (*JASA* 1992)
- Lee & Miller (*Demography* 2001)
- Booth, Maindonald & Smith (*Population Studies* 2002)

# Mortality models

$m_{x,t}$  = mortality rate at age  $x$  in year  $t$ .

Naive:  $m_{x,t} = m_{x,t-1} + \varepsilon_{x,t}$

Lee-Carter:  $\log(m_{x,t}) = a_x + k_t b_x + \varepsilon_{x,t}$

$\varepsilon_{x,t}$  = noise term with variance  $\sigma_x^2$ .

```
fit ← aus ▷  
  model(  
    naive = FNAIVE(Mortality),  
    lc = LC(log(Mortality))  
  )
```

# Mortality models

$m_{x,t}$  = mortality rate at age  $x$  in year  $t$ .

Naive:  $m_{x,t} = m_{x,t-1} + \varepsilon_{x,t}$

Lee-Carter:  $\log(m_{x,t}) = a_x + k_t b_x + \varepsilon_{x,t}$

$\varepsilon_{x,t}$  = noise term with variance  $\sigma_x^2$ .

```
fit ← aus ▷  
  model(  
    naive = FNAIVE(Mortality),  
    lc = LC(log(Mortality))  
  )
```

fit

# A mable: 12 x 4

# Key: Sex, State [12]

	Sex	State	naive	lc
	<chr>	<chr>	<model>	<model>
1	female	NSW	<FNAIVE>	<LC>
2	female	QLD	<FNAIVE>	<LC>
3	female	SA	<FNAIVE>	<LC>
4	female	TAS	<FNAIVE>	<LC>
5	female	VIC	<FNAIVE>	<LC>
6	female	WA	<FNAIVE>	<LC>
7	male	NSW	<FNAIVE>	<LC>
8	male	QLD	<FNAIVE>	<LC>
9	male	SA	<FNAIVE>	<LC>
10	male	TAS	<FNAIVE>	<LC>
11	male	VIC	<FNAIVE>	<LC>
12	male	WA	<FNAIVE>	<LC>

```
fit ▷  
  filter(Sex == "female",  
         State == "NSW") ▷  
  select(lc) ▷  
  report()
```

Series: Mortality

Model: LC

Transformation: log(Mortality)

Options:

Adjust method: dt

Jump choice: fit

Age functions

# A tibble: 101 × 3

	Age	ax	bx
	<int>	<dbl>	<dbl>
1	0	-4.07	0.0155
2	1	-6.20	0.0221
3	2	-6.89	0.0199

# i 98 more rows

Time coefficients

# A tsibble: 120 × 2 [1Y]

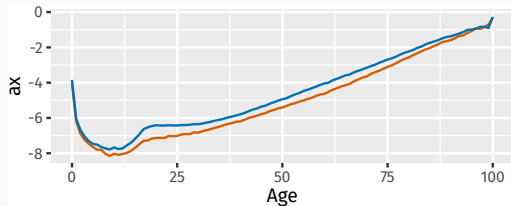
	Year	kt
	<int>	<dbl>
1	1901	109.
2	1902	111.
3	1903	108.

# i 117 more rows

# Lee-Carter models

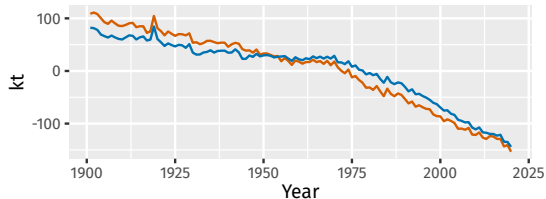
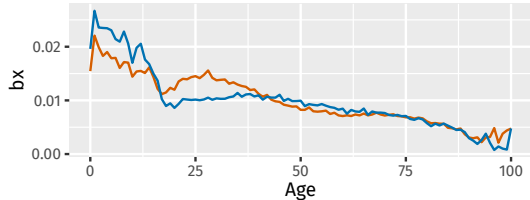
$$\log(m_{x,t}) = a_x + k_t b_x + \varepsilon_{x,t}$$

```
fit ▷  
  filter(State == "NSW") ▷  
  select(lc) ▷  
  autoplot()
```



Sex/State

- female/NSW
- male/NSW



# Lee-Carter models

$$\log(m_{x,t}) = a_x + k_t b_x + \varepsilon_{x,t}$$

```
fit ▷ select(lc) ▷ age_components()
```

```
# A tibble: 1,212 x 5
```

	Sex	State	Age	ax	bx
	<chr>	<chr>	<int>	<dbl>	<dbl>
1	female	NSW	0	-4.07	0.0155
2	female	NSW	1	-6.20	0.0221
3	female	NSW	2	-6.89	0.0199
4	female	NSW	3	-7.24	0.0183
5	female	NSW	4	-7.47	0.0190
6	female	NSW	5	-7.65	0.0178
7	female	NSW	6	-7.80	0.0179
8	female	NSW	7	-7.81	0.0160
9	female	NSW	8	-8.05	0.0171
10	female	NSW	9	-8.15	0.0170

```
# i 1,202 more rows
```

```
fit ▷ select(lc) ▷ time_components()
```

```
# A tsibble: 1,440 x 4 [1Y]
```

```
# Key:           Sex, State [12]
```

	Sex	State	Year	kt
	<chr>	<chr>	<int>	<dbl>
1	female	NSW	1901	109.
2	female	NSW	1902	111.
3	female	NSW	1903	108.
4	female	NSW	1904	100.
5	female	NSW	1905	92.7
6	female	NSW	1906	89.5
7	female	NSW	1907	95.7
8	female	NSW	1908	90.5
9	female	NSW	1909	85.9
10	female	NSW	1910	85.4

```
# i 1,430 more rows
```

# Forecasts

```
fc ← fit ▷ forecast(h = 20)
fc
```

```
# A vital fable: 48,480 x 7 [1Y]
```

```
# Key:           Age x (Sex, State, .model) [101 x 24]
```

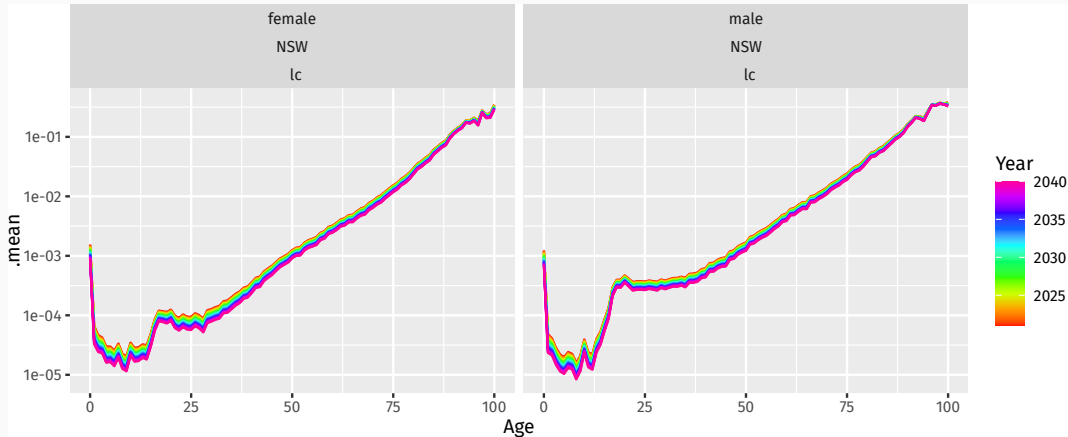
	Sex	State	.model	Year	Age	Mortality	.mean
	<chr>	<chr>	<chr>	<dbl>	<int>	<dist>	<dbl>
1	female	NSW	naive	2021	0	N(0.0027, 1.8e-05)	0.00270
2	female	NSW	naive	2022	0	N(0.0027, 3.6e-05)	0.00270
3	female	NSW	naive	2023	0	N(0.0027, 5.4e-05)	0.00270
4	female	NSW	naive	2024	0	N(0.0027, 7.2e-05)	0.00270
5	female	NSW	naive	2025	0	N(0.0027, 9e-05)	0.00270
6	female	NSW	naive	2026	0	N(0.0027, 0.00011)	0.00270
7	female	NSW	naive	2027	0	N(0.0027, 0.00013)	0.00270
8	female	NSW	naive	2028	0	N(0.0027, 0.00014)	0.00270
9	female	NSW	naive	2029	0	N(0.0027, 0.00016)	0.00270
10	female	NSW	naive	2030	0	N(0.0027, 0.00018)	0.00270

```
# i 48,470 more rows
```



# NSW forecasts using Lee-Carter method

```
fc > filter(State == "NSW", .model == "lc") >  
  autoplot() + scale_y_log10()
```



Let  $m_{x,t}$  be the mortality rate at age  $x$  in year  $t$ .

$$\log(m_{t,x}) = s_t(x) + \sigma_t(x)\varepsilon_{t,x}$$

$$s_t(x) = \mu(x) + \sum_{j=1}^J \beta_{tj} \phi_j(x) + e_t(x)$$

- $s_t(x)$  = smoothed version of  $y_t(x)$
- $\mu(x)$  = mean  $s_t(x)$  across years.
- $\phi_j(x)$  and  $\beta_{tj}$  estimated using principal component analysis.
- $\beta_{1j}, \dots, \beta_{Tj}$  modelled with ARIMA or ARFIMA processes.

# Functional data models

```
sm_aus ← aus ▷ smooth_mortality(Mortality)
sm_aus
```

```
# A vital: 145,440 x 9 [1Y]
```

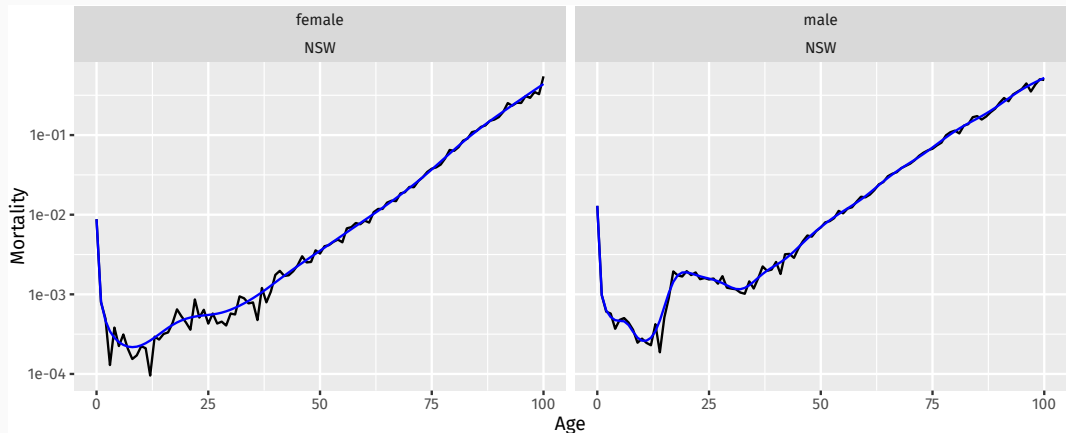
```
# Key:      Age x (Sex, State) [101 x 12]
```

	Year	Age	Sex	State	Mortality	Exposure	Deaths	.smooth	.smooth_se
	<int>	<dbl>	<chr>	<chr>	<dbl>	<dbl>	<dbl>	<dbl[1d]>	<dbl[1d]>
1	1901	0	female	NSW	0.107	17143	1833	0.107	0.00295
2	1901	1	female	NSW	0.0247	15071	373	0.0237	0.00141
3	1901	2	female	NSW	0.00686	15461	106	0.00804	0.000670
4	1901	3	female	NSW	0.00441	15629	69	0.00461	0.000405
5	1901	4	female	NSW	0.00374	15762	59	0.00341	0.000305
6	1901	5	female	NSW	0.00274	16030	44	0.00275	0.000251
7	1901	6	female	NSW	0.00252	16289	41	0.00230	0.000215
8	1901	7	female	NSW	0.00216	16639	36	0.00197	0.000189
9	1901	8	female	NSW	0.00169	16554	28	0.00175	0.000173
10	1901	9	female	NSW	0.00109	16468	18	0.00162	0.000163

```
# i 145,430 more rows
```

# Functional data models

```
sm_au ← aus ▷ smooth_mortality(Mortality)
sm_au ▷ filter(State == "NSW", Year == 1980) ▷ autoplot(Mortality) +
  geom_line(aes(y = .smooth), col = "blue") + scale_y_log10()
```



# Functional data models

```
fit ← sm_aus ▷ model(hu = FDM(log(.smooth)))  
fit
```

```
# A mable: 12 x 3
```

```
# Key:      Sex, State [12]
```

	Sex	State	hu
	<chr>	<chr>	<model>
1	female	NSW	<FDM>
2	female	QLD	<FDM>
3	female	SA	<FDM>
4	female	TAS	<FDM>
5	female	VIC	<FDM>
6	female	WA	<FDM>
7	male	NSW	<FDM>
8	male	QLD	<FDM>
9	male	SA	<FDM>
10	male	TAS	<FDM>
11	male	VIC	<FDM>
12	male	WA	<FDM>

# Functional data models

$$s_t(x) = \mu(x) + \sum_{j=1}^J \beta_{tj} \phi_j(x) + e_t(x)$$

```
fit ▷  
  filter(Sex == "female", State == "NSW") ▷  
  report()
```

Series: .smooth

Model: FDM

Transformation: log(.smooth)

Basis functions

# A tibble: 101 x 8

	Age	mean	phi1	phi2	phi3	phi4	phi5	phi6
	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>
1	0	-4.07	0.147	0.0625	-0.0270	0.0986	0.0112	-0.0624
2	1	-6.16	0.200	-0.0609	-0.194	0.116	0.0383	-0.238
3	2	-6.82	0.182	-0.0483	-0.157	0.0924	0.0443	-0.264
4	3	-7.17	0.170	-0.0368	-0.130	0.0362	0.000338	-0.321
5	4	-7.40	0.164	-0.0165	-0.114	-0.0154	-0.0303	-0.374

# i 96 more rows

# Functional data models

$$s_t(x) = \mu(x) + \sum_{j=1}^J \beta_{tj} \phi_j(x) + e_t(x)$$

Coefficients

```
# A tsibble: 120 x 8 [1Y]
```

	Year	mean	beta1	beta2	beta3	beta4	beta5	beta6
	<int>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>
1	1901	1	11.1	-0.522	-0.0553	0.207	0.358	0.0305
2	1902	1	11.8	-0.649	0.399	0.856	0.0319	0.422
3	1903	1	11.5	-0.930	-0.485	0.398	0.399	-0.376
4	1904	1	11.1	-0.827	-0.214	-0.000305	0.00125	-0.0783
5	1905	1	10.2	-0.563	-0.105	0.324	0.122	0.0478

```
# i 115 more rows
```

```
# i Use 'print(n = ...)' to see more rows
```

Time series models

```
beta1 : ARIMA(0,1,1) w/ drift
```

```
beta2 : ARIMA(0,2,2)
```

```
beta3 : ARIMA(1,0,1)
```

```
beta4 : ARIMA(0,0,2)
```

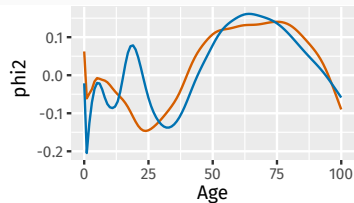
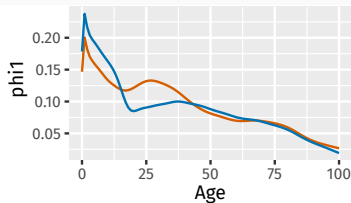
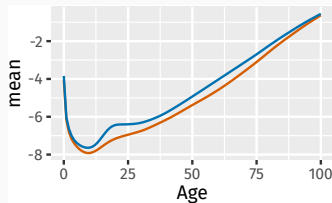
```
beta5 : ARIMA(0,0,0)
```

```
beta6 : ARIMA(2,0,2)
```

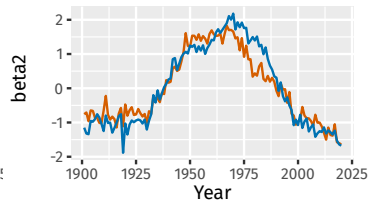
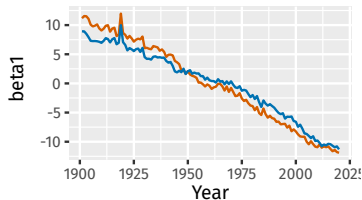
# Functional data models

$$s_t(x) = \mu(x) + \sum_{j=1}^J \beta_{tj} \phi_j(x) + e_t(x)$$

```
fit ▷  
  filter(State == "NSW") ▷  
  autoplot()
```



Sex/State  
— female/NSW  
— male/NSW





# Functional data models

$$s_t(x) = \mu(x) + \sum_{j=1}^J \beta_{tj} \phi_j(x) + e_t(x)$$

```
fit > age_components()
```

```
# A tibble: 1,212 x 10
```

	Sex	State	Age	mean	phi1	phi2	phi3	phi4	phi5	phi6
	<chr>	<chr>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>
1	female	NSW	0	-4.07	0.147	0.0625	-0.0270	0.0986	0.0112	-0.0624
2	female	NSW	1	-6.16	0.200	-0.0609	-0.194	0.116	0.0383	-0.238
3	female	NSW	2	-6.82	0.182	-0.0483	-0.157	0.0924	0.0443	-0.264
4	female	NSW	3	-7.17	0.170	-0.0368	-0.130	0.0362	0.000338	-0.321
5	female	NSW	4	-7.40	0.164	-0.0165	-0.114	-0.0154	-0.0303	-0.374
6	female	NSW	5	-7.57	0.158	-0.00759	-0.121	-0.0564	0.0247	-0.315
7	female	NSW	6	-7.71	0.153	-0.00942	-0.133	-0.0976	0.112	-0.197
8	female	NSW	7	-7.81	0.149	-0.0121	-0.143	-0.143	0.175	-0.0863
9	female	NSW	8	-7.88	0.143	-0.0141	-0.148	-0.181	0.211	0.0131
10	female	NSW	9	-7.92	0.138	-0.0185	-0.142	-0.196	0.236	0.101

```
# i 1,202 more rows
```

# Functional data models

$$s_t(x) = \mu(x) + \sum_{j=1}^J \beta_{tj} \phi_j(x) + e_t(x)$$

```
fit > time_components()
```

```
# A tsibble: 1,440 x 10 [1Y]
```

```
# Key:           Sex, State [12]
```

	Sex	State	Year	mean	beta1	beta2	beta3	beta4	beta5	beta6
	<chr>	<chr>	<int>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>
1	female	NSW	1901	1	11.2	-0.756	-0.0301	0.269	-0.155	0.409
2	female	NSW	1902	1	11.6	-0.708	0.0899	0.207	0.0282	0.507
3	female	NSW	1903	1	11.5	-0.962	0.169	-0.103	0.366	0.323
4	female	NSW	1904	1	11.1	-0.648	0.0985	-0.433	0.131	0.270
5	female	NSW	1905	1	10.1	-0.660	0.342	-0.0910	0.0862	0.612
6	female	NSW	1906	1	9.78	-0.865	0.496	-0.147	-0.101	0.306
7	female	NSW	1907	1	9.90	-0.861	0.0530	1.33	0.278	0.181
8	female	NSW	1908	1	10.1	-1.01	0.554	-0.0198	-0.00428	0.578
9	female	NSW	1909	1	9.42	-1.02	0.293	-0.365	-0.149	0.353
10	female	NSW	1910	1	9.08	-0.650	0.172	-0.559	-0.253	0.0110

```
# i 1,430 more rows
```

$$y_t(x) = s_t(x) + \sigma_t(x)\varepsilon_{t,x}$$

$$s_t(x) = \mu(x) + \sum_{j=1}^J \beta_{tj} \phi_j(x) + e_t(x)$$

- $y_t(x) = \log(m_{x,t}^M m_{x,t}^F)$  and  $\log(m_{x,t}^M / m_{x,t}^F)$
- $s_t(x)$  = smoothed version of  $y_t(x)$
- $\mu(x)$  = mean  $s_t(x)$  across years.
- $\phi_j(x)$  and  $\beta_{tj}$  estimated using principal component analysis.
- $\beta_{1j}, \dots, \beta_{Tj}$  modelled with ARIMA for products and ARMA for ratios (to ensure stationary sex-ratios)

# Coherent functional models

```
pr <- sm_aus > make_pr(.smooth)
pr
```

```
# A vital: 218,160 x 9 [1Y]
```

```
# Key:      Age x (Sex, State) [101 x 18]
```

	Year	Age	Sex	State	Mortality	Exposure	Deaths	.smooth	.smooth_se
	<int>	<dbl>	<chr>	<chr>	<dbl>	<dbl>	<dbl>	<dbl[1d]>	<dbl[1d]>
1	1901	0	female	NSW	0.107	17143	1833	0.939	0.00295
2	1901	1	female	NSW	0.0247	15071	373	1.03	0.00141
3	1901	2	female	NSW	0.00686	15461	106	0.965	0.000670
4	1901	3	female	NSW	0.00441	15629	69	0.982	0.000405
5	1901	4	female	NSW	0.00374	15762	59	1.02	0.000305
6	1901	5	female	NSW	0.00274	16030	44	1.04	0.000251
7	1901	6	female	NSW	0.00252	16289	41	1.04	0.000215
8	1901	7	female	NSW	0.00216	16639	36	1.01	0.000189
9	1901	8	female	NSW	0.00169	16554	28	0.972	0.000173
10	1901	9	female	NSW	0.00109	16468	18	0.938	0.000163

```
# i 218,150 more rows
```

# Coherent functional models

```
pr <- sm_aus > make_pr(.smooth)
fit <- pr > model(hby = FDM(log(.smooth), coherent = TRUE))
fit
```

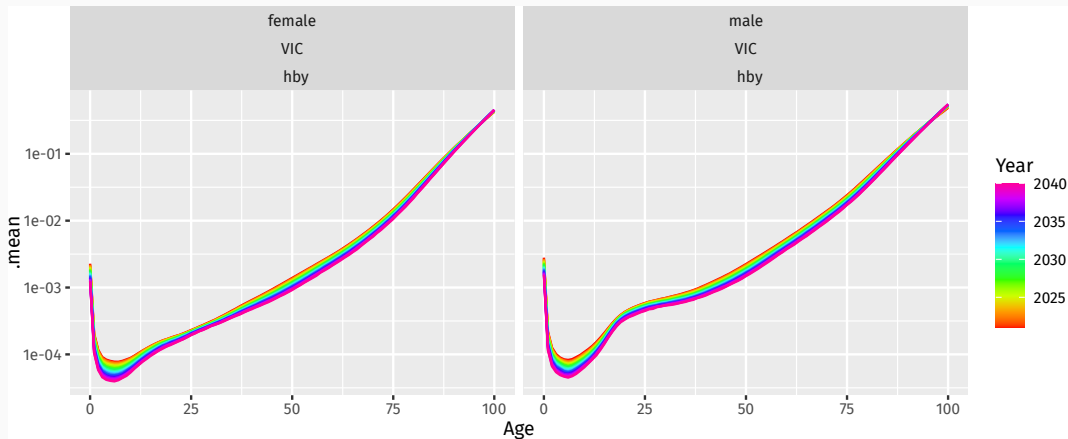
```
# A mable: 18 x 3
```

```
# Key:      Sex, State [18]
```

	Sex	State	hby
	<chr>	<chr>	<model>
1	female	NSW	<FDM>
2	female	QLD	<FDM>
3	female	SA	<FDM>
4	female	TAS	<FDM>
5	female	VIC	<FDM>
6	female	WA	<FDM>
7	geometric_mean	NSW	<FDM>
8	geometric_mean	QLD	<FDM>
9	geometric_mean	SA	<FDM>
10	geometric_mean	TAS	<FDM>
11	geometric_mean	VIC	<FDM>

# Coherent functional models

```
fc <- fit ▷ forecast(h = 20) ▷ undo_pr(.smooth)  
fc ▷ filter(State == "VIC") ▷ autoplot() + scale_y_log10()
```

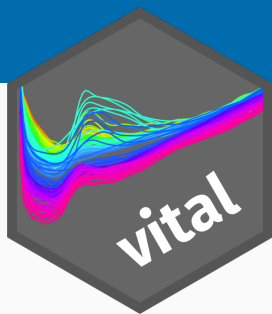


# Outline

- 1 Vital objects
- 2 Using the Human Mortality and Fertility Databases
- 3 Plots
- 4 Life tables and life expectancy
- 5 Mortality models
- 6 Other features and future plans

## Other functionality

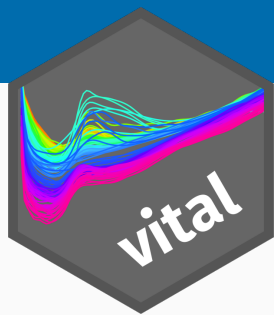
- Convert demogdata, tsibble & data.frame objects to vital.
- Compute net migration from population, births and deaths.
- Compute total fertility rates from age-specific fertility rates.
- Various smoothing functions





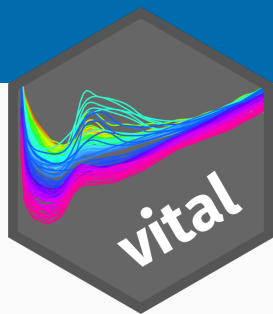
# Future plans

- Remaining tools from the demography package
- Stochastic population forecasting (as per Hyndman & Booth, *IJF*, 2008)
- All models handled by StMoMo package
- All methods from MortalityLaws package
- Suggestions from users



# Future plans

- Remaining tools from the demography package
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- **Slides:** [robjhyndman.com/mpidr2024](http://robjhyndman.com/mpidr2024)
- **Package:** [pkg.robjhyndman.com/vital/](http://pkg.robjhyndman.com/vital/)