

Tidy data analysis for demography using R

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Outline

- 1 Vital objects
- 2 Using the Human Mortality and Fertility Databases
- 3 Plots
- 4 Life tables and life expectancy
- 5 Mortality models
- 6 Future plans

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Australian Deaths 1901–2020

```
tibble::as_tibble(aus) |>  
  arrange(desc(State), Year, Age, Sex)
```

A tibble: 145,440 x 7

| | Year | Age | Sex | State | Mortality | Exposure | Deaths |
|----|-------|-------|--------|-------|-----------|----------|--------|
| | <int> | <int> | <chr> | <chr> | <dbl> | <dbl> | <dbl> |
| 1 | 1901 | 0 | female | WA | 0.129 | 2511 | 325 |
| 2 | 1901 | 0 | male | WA | 0.158 | 2634 | 416 |
| 3 | 1901 | 1 | female | WA | 0.0275 | 2219 | 61 |
| 4 | 1901 | 1 | male | WA | 0.0391 | 2175 | 85 |
| 5 | 1901 | 2 | female | WA | 0.00688 | 2180 | 15 |
| 6 | 1901 | 2 | male | WA | 0.0131 | 2208 | 29 |
| 7 | 1901 | 3 | female | WA | 0.00584 | 1884 | 11 |
| 8 | 1901 | 3 | male | WA | 0.00503 | 1988 | 10 |
| 9 | 1901 | 4 | female | WA | 0.00290 | 1722 | 5 |
| 10 | 1901 | 4 | male | WA | 0.00287 | 1743 | 5 |



Australian Deaths 1901–2020

```
tsibble::as_tsibble(aus) |>  
  arrange(desc(State), Year, Age, Sex)
```

```
# A tsibble: 145,440 x 7 [1Y]
```

```
# Key:      Age, Sex, State [1,212]
```

| | Year | Age | Sex | State | Mortality | Exposure | Deaths |
|---|-------|-------|--------|-------|-----------|----------|--------|
| | <int> | <int> | <chr> | <chr> | <dbl> | <dbl> | <dbl> |
| 1 | 1901 | 0 | female | WA | 0.129 | 2511 | 325 |
| 2 | 1901 | 0 | male | WA | 0.158 | 2634 | 416 |
| 3 | 1901 | 1 | female | WA | 0.0275 | 2219 | 61 |
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| 5 | 1901 | 2 | female | WA | 0.00688 | 2180 | 15 |
| 6 | 1901 | 2 | male | WA | 0.0131 | 2208 | 29 |
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Australian Deaths 1901–2020

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```
# Key:      Age, Sex, State [1,212]
```

| | Year | Age | Sex | State | Mortality | Exposure | Deaths |
|---|-------|-------|--------|-------|-----------|----------|--------|
| | <int> | <int> | <chr> | <chr> | <dbl> | <dbl> | <dbl> |
| 1 | 1901 | 0 | female | WA | 0.129 | 2511 | 325 |
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| 8 | 1901 | 3 | male | WA | 0.00503 | 1988 | 10 |
| 9 | 1901 | 4 | female | WA | 0.00290 | 1722 | 5 |

Variables

Index:

■ Year

Keys:

■ Age

■ Sex

■ State



Australian Deaths 1901–2020

```
tsibble::as_tsibble(aus) |>  
  arrange(desc(State), Year, Age, Sex)
```

```
# A tsibble: 145,440 x 7 [1Y]
```

```
# Key:      Age, Sex, State [1,212]
```

| | Year | Age | Sex | State | Mortality | Exposure | Deaths |
|---|-------|-------|--------|-------|-----------|----------|--------|
| | <int> | <int> | <chr> | <chr> | <dbl> | <dbl> | <dbl> |
| 1 | 1901 | 0 | female | WA | 0.129 | 2511 | 325 |
| 2 | 1901 | 0 | male | WA | 0.158 | 2634 | 416 |
| 3 | 1901 | 1 | female | WA | 0.0275 | 2219 | 61 |
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| 5 | 1901 | 2 | female | WA | 0.00688 | 2180 | 15 |
| 6 | 1901 | 2 | male | WA | 0.0131 | 2208 | 29 |
| 7 | 1901 | 3 | female | WA | 0.00584 | 1884 | 11 |
| 8 | 1901 | 3 | male | WA | 0.00503 | 1988 | 10 |
| 9 | 1901 | 4 | female | WA | 0.00290 | 1722 | 5 |

Variables

Index:

■ Year

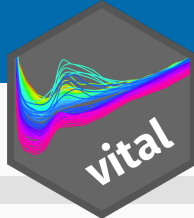
Keys:

■ Age

■ Sex

■ State

Every row must have a unique combination of Index and Keys



Australian Deaths 1901–2020

aus

```
# A vital: 145,440 x 7 [1Y]
```

```
# Key:      Age, Sex, State [1,212]
```

| | Year | Age | Sex | State | Mortality | Exposure | Deaths |
|----|-------|-------|--------|-------|-----------|----------|--------|
| | <int> | <int> | <chr> | <chr> | <dbl> | <dbl> | <dbl> |
| 1 | 1901 | 0 | female | WA | 0.129 | 2511 | 325 |
| 2 | 1901 | 0 | male | WA | 0.158 | 2634 | 416 |
| 3 | 1901 | 1 | female | WA | 0.0275 | 2219 | 61 |
| 4 | 1901 | 1 | male | WA | 0.0391 | 2175 | 85 |
| 5 | 1901 | 2 | female | WA | 0.00688 | 2180 | 15 |
| 6 | 1901 | 2 | male | WA | 0.0131 | 2208 | 29 |
| 7 | 1901 | 3 | female | WA | 0.00584 | 1884 | 11 |
| 8 | 1901 | 3 | male | WA | 0.00503 | 1988 | 10 |
| 9 | 1901 | 4 | female | WA | 0.00290 | 1722 | 5 |
| 10 | 1901 | 4 | male | WA | 0.00287 | 1743 | 5 |

Variables

Index:

■ Year

Keys:

■ Age

■ Sex

■ State

Variables denoting age, sex, deaths, births and population can also be specified.

Every row must have a unique combination of Index and Keys

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Human Mortality Database

Reliability and Accuracy Matter

The Human Mortality Database (HMD) is the world's leading scientific data resource on mortality in developed countries. The HMD provides detailed high-quality harmonized mortality and population estimates to researchers, students, journalists, policy analysts, and others interested in human longevity. The HMD follows open data principles.

- > [Short-Term Mortality Fluctuations](#)
- > [Cause-of-Death Data Series](#)
- > [Subnational Mortality Databases](#)
- > [Citing HMD](#)

Data by country or area

[Australia](#)[Denmark](#)[Ireland](#)[Norway](#)[Switzerland](#)[Austria](#)[Estonia](#)[Israel](#)[Poland](#)[Taiwan](#)[Belarus](#)[Finland](#)[Italy](#)[Portugal](#)[U.K.](#)[Belgium](#)[France](#)[Japan](#)[Republic of Korea](#)[U.S.A.](#)

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Human Fertility Database

The Human Fertility Database (HFD) is the leading scientific data resource on fertility in the developed countries. This open access database provides detailed and high-quality historical and recent data on period and cohort fertility by age of mother and birth order. The HFD is entirely based on official vital statistics and places a great emphasis on rigorous data checking and documentation. The HFD adopts uniform methodology to warrant data comparability across time and between countries. The database follows open data principles.

[> Short-Term Fertility Fluctuations](#)[> Human Fertility Collection](#)[> Citing HFD](#)[> What's new](#)

For users who seek fast access to the most commonly used summary indicators of period and cohort fertility, we provide excel tables comprising the following indicators for all the HFD countries:

HFD summary indicators

[Total fertility rate](#)[Tempo-adjusted TFR](#)[Mean age at birth](#)[Mean age at first birth](#)[Completed cohort fertility](#)[Cohort parity](#)

HMD imports

```
norway <- read_hmd(  
  country = "NOR",  
  username = "Nora.Weigh@mymail.com",  
  password = "FF!5xeEFa6"  
)  
norway_births <- read_hmd(  
  country = "NOR",  
  username = "Nora.Weigh@mymail.com",  
  password = "FF!5xeEFa6",  
  variables = "Births"  
)
```

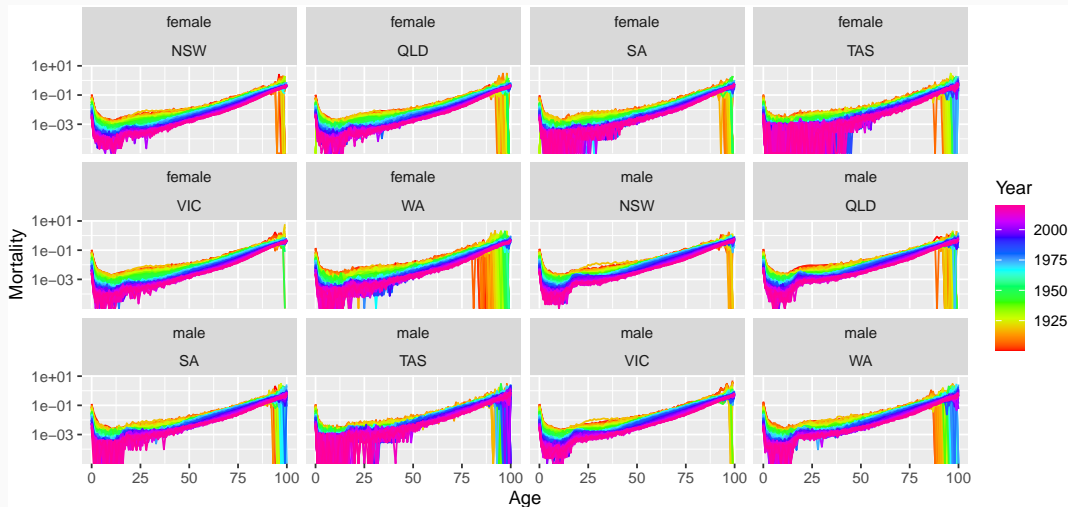
- Uses HMDHFDplus package to handle the downloads.
- Default variables: Deaths, Exposures, Population, Mx
- Only 1x1 data supported.
- read_hmd_files() and read_hfd_files() allow reading of downloaded files.

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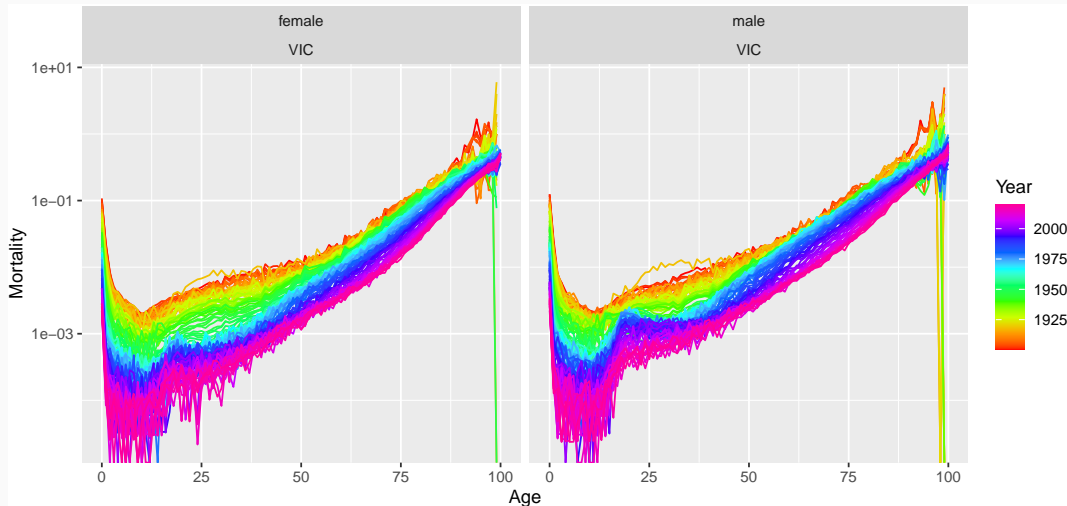
Rainbow plots

```
aus |> autoplot(Mortality) + scale_y_log10()
```



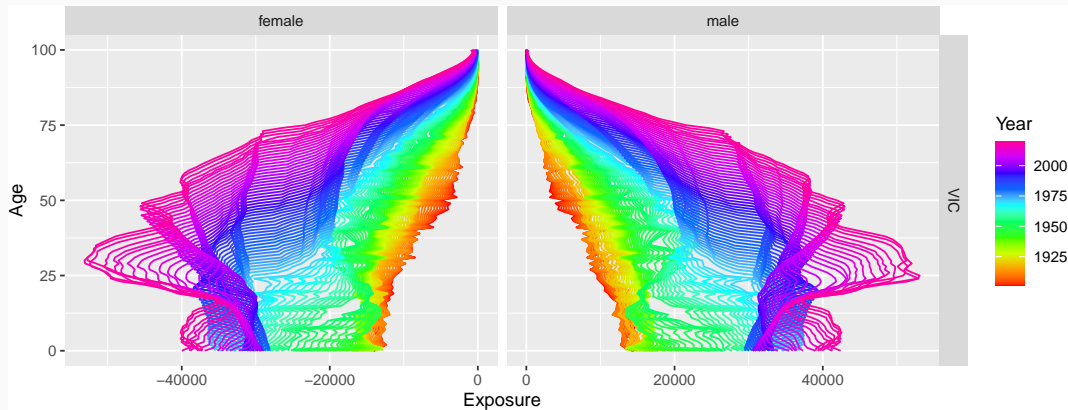
Rainbow plots

```
aus |> filter(State == "VIC") |> autoplot(Mortality) + scale_y_log10()
```



Rainbow plots

```
aus |> filter(State == "VIC") |>  
  mutate(Exposure = if_else(Sex == "female", -Exposure, Exposure)) |>  
  autoplot(Exposure) +  
  facet_grid(State ~ Sex, scales = "free_x") + coord_flip()
```



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Life tables

```
life_table(aus)
```

```
# A vital: 145,440 x 14 [1Y]
```

```
# Key:      Age, Sex, State [1,212]
```

| | Year | Age | Sex | State | mx | qx | lx | dx | Lx | Tx | ex | rx |
|----|-------|-------|-------|-------|---------|---------|-------|---------|-------|-------|-------|-------|
| | <int> | <int> | <chr> | <chr> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> | <dbl> |
| 1 | 1901 | 0 | fema~ | NSW | 0.107 | 0.100 | 1 | 1.00e-1 | 0.935 | 56.2 | 56.2 | 0.935 |
| 2 | 1901 | 1 | fema~ | NSW | 0.0247 | 0.0244 | 0.900 | 2.20e-2 | 0.889 | 55.3 | 61.5 | 0.951 |
| 3 | 1901 | 2 | fema~ | NSW | 0.00686 | 0.00683 | 0.878 | 6.00e-3 | 0.875 | 54.4 | 62.0 | 0.984 |
| 4 | 1901 | 3 | fema~ | NSW | 0.00441 | 0.00441 | 0.872 | 3.84e-3 | 0.870 | 53.5 | 61.4 | 0.994 |
| 5 | 1901 | 4 | fema~ | NSW | 0.00374 | 0.00374 | 0.868 | 3.24e-3 | 0.867 | 52.7 | 60.7 | 0.996 |
| 6 | 1901 | 5 | fema~ | NSW | 0.00274 | 0.00274 | 0.865 | 2.37e-3 | 0.864 | 51.8 | 59.9 | 0.997 |
| 7 | 1901 | 6 | fema~ | NSW | 0.00252 | 0.00251 | 0.863 | 2.17e-3 | 0.861 | 50.9 | 59.1 | 0.997 |
| 8 | 1901 | 7 | fema~ | NSW | 0.00216 | 0.00216 | 0.860 | 1.86e-3 | 0.859 | 50.1 | 58.2 | 0.998 |
| 9 | 1901 | 8 | fema~ | NSW | 0.00169 | 0.00169 | 0.859 | 1.45e-3 | 0.858 | 49.2 | 57.3 | 0.998 |
| 10 | 1901 | 9 | fema~ | NSW | 0.00109 | 0.00109 | 0.857 | 9.36e-4 | 0.857 | 48.4 | 56.4 | 0.999 |

```
# i 145,430 more rows
```

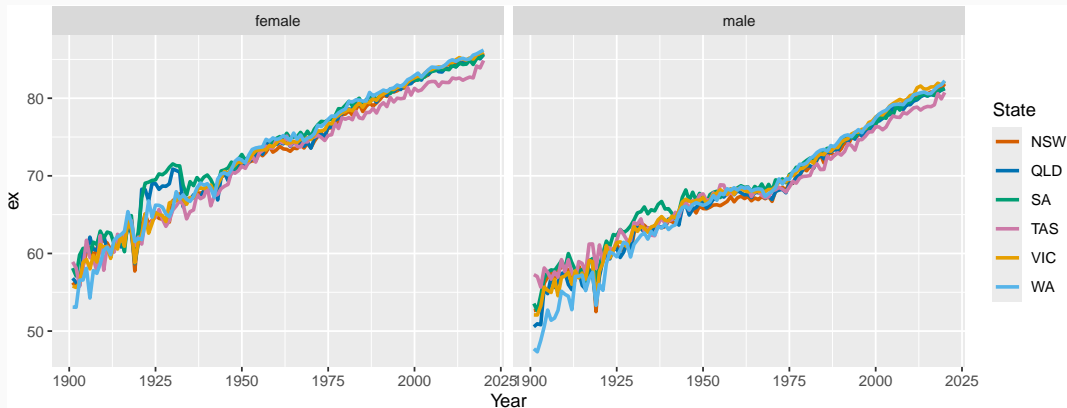
Life expectancy

```
life_expectancy(aus)
```

```
# A vital: 1,440 x 8 [1Y]
# Key:      Age, Sex, State [12]
  Year  Age Sex  State  ex    rx    nx    ax
  <int> <int> <chr> <chr> <dbl> <dbl> <dbl> <dbl>
1  1901     0 female NSW    56.2 0.935     1 0.352
2  1901     0 female QLD    56.8 0.937     1 0.338
3  1901     0 female SA     58.1 0.939     1 0.324
4  1901     0 female TAS    58.9 0.946     1 0.275
5  1901     0 female VIC    55.8 0.937     1 0.334
6  1901     0 female WA     53.1 0.922     1 0.35
7  1901     0 male  NSW    52.6 0.925     1 0.33
8  1901     0 male  QLD    50.6 0.924     1 0.33
9  1901     0 male  SA     53.5 0.922     1 0.33
10 1901     0 male  TAS    57.3 0.930     1 0.33
# i 1,430 more rows
```

Life expectancy

```
life_expectancy(aus) |>  
  ggplot(aes(x = Year, y = ex, colour = State)) +  
  geom_line(linewidth = 1) +  
  facet_grid(. ~ Sex)
```



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Benchmark models

```
fit <- aus |>
  model(
    naive = FNAIVE(Mortality),
    mean = FMEAN(Mortality)
  )
fit
```

```
# A mable: 12 x 4
```

```
# Key:      Sex, State [12]
```

| | Sex | State | naive | mean |
|---|--------|-------|----------|---------|
| | <chr> | <chr> | <model> | <model> |
| 1 | female | NSW | <FNAIVE> | <FMEAN> |
| 2 | female | QLD | <FNAIVE> | <FMEAN> |
| 3 | female | SA | <FNAIVE> | <FMEAN> |
| 4 | female | TAS | <FNAIVE> | <FMEAN> |
| 5 | female | VIC | <FNAIVE> | <FMEAN> |
| 6 | female | WA | <FNAIVE> | <FMEAN> |

Benchmark models

```
fit |>  
  filter(Sex == "female", State == "NSW") |>  
  select(mean) |>  
  report()
```

Series: Mortality

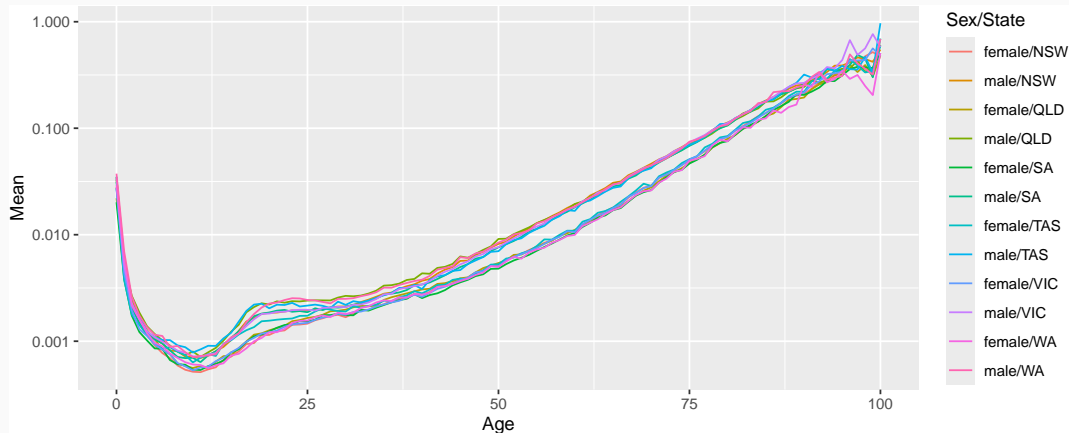
Model: FMEAN

A tibble: 101 x 3

| | Age | mean | sigma |
|---|-------|----------|----------|
| | <int> | <dbl> | <dbl> |
| 1 | 0 | 0.0279 | 0.0256 |
| 2 | 1 | 0.00528 | 0.00648 |
| 3 | 2 | 0.00223 | 0.00245 |
| 4 | 3 | 0.00145 | 0.00151 |
| 5 | 4 | 0.00115 | 0.00116 |
| 6 | 5 | 0.000915 | 0.000913 |

Benchmark models

```
fit |>  
  select(mean) |>  
  autoplot() + scale_y_log10()
```



Lee-Carter models

```
fit <- aus |>
  model(
    naive = FNAIVE(Mortality),
    mean = FMEAN(Mortality),
    lc = LC(log(Mortality))
  )
fit
```

A mable: 12 x 5

Key: Sex, State [12]

| | Sex | State | naive | mean | lc |
|---|--------|-------|----------|---------|---------|
| | <chr> | <chr> | <model> | <model> | <model> |
| 1 | female | NSW | <FNAIVE> | <FMEAN> | <LC> |
| 2 | female | QLD | <FNAIVE> | <FMEAN> | <LC> |
| 3 | female | SA | <FNAIVE> | <FMEAN> | <LC> |
| 4 | female | TAS | <FNAIVE> | <FMEAN> | <LC> |
| 5 | female | VIC | <FNAIVE> | <FMEAN> | <LC> |

Lee-Carter models

```
fit |>  
  filter(Sex == "female", State == "NSW") |>  
  select(lc) |>  
  report()
```

Series: Mortality

Model: LC

Transformation: log(Mortality)

Options:

Adjust method: dt

Jump choice: fit

Age functions

A tibble: 101 x 3

| | Age | ax | bx |
|---|-------|-------|--------|
| | <int> | <dbl> | <dbl> |
| 1 | 0 | -4.07 | 0.0155 |
| 2 | 1 | -6.20 | 0.0221 |

Lee-Carter models

Age functions

```
# A tibble: 101 × 3
  Age    ax    bx
<int> <dbl> <dbl>
1     0 -4.07 0.0155
2     1 -6.20 0.0221
3     2 -6.89 0.0199
# i 98 more rows
```

Time coefficients

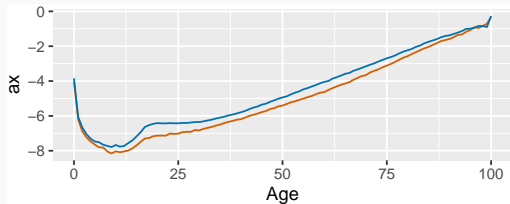
```
# A tsibble: 120 x 2 [1Y]
  Year    kt
<int> <dbl>
1  1901 109.
2  1902 111.
3  1903 108.
# i 117 more rows
```

Time series model: RW w/ drift

Variance explained: 86.61%

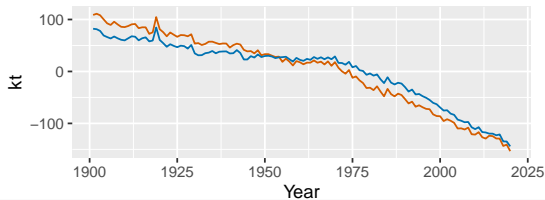
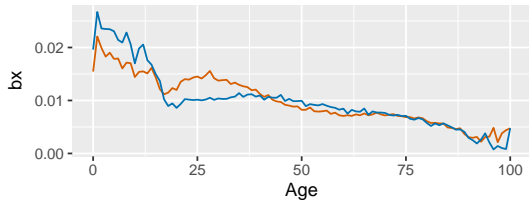
Lee-Carter models

```
fit |>  
  filter(State == "NSW") |>  
  select(lc) |>  
  autoplot()
```



Sex/State

- female/NSW
- male/NSW



Lee-Carter models

```
fit |> select(lc) |> age_components()
```

```
# A tibble: 1,212 x 5
```

| | Sex | State | Age | ax | bx |
|----|--------|-------|-------|-------|--------|
| | <chr> | <chr> | <int> | <dbl> | <dbl> |
| 1 | female | NSW | 0 | -4.07 | 0.0155 |
| 2 | female | NSW | 1 | -6.20 | 0.0221 |
| 3 | female | NSW | 2 | -6.89 | 0.0199 |
| 4 | female | NSW | 3 | -7.24 | 0.0183 |
| 5 | female | NSW | 4 | -7.47 | 0.0190 |
| 6 | female | NSW | 5 | -7.65 | 0.0178 |
| 7 | female | NSW | 6 | -7.80 | 0.0179 |
| 8 | female | NSW | 7 | -7.81 | 0.0160 |
| 9 | female | NSW | 8 | -8.05 | 0.0171 |
| 10 | female | NSW | 9 | -8.15 | 0.0170 |

```
# i 1,202 more rows
```

Lee-Carter models

```
fit |> select(lc) |> time_components()
```

```
# A tsibble: 1,440 x 4 [1Y]
# Key:      Sex, State [12]
   Sex      State Year    kt
   <chr>   <chr> <int> <dbl>
1 female NSW    1901 109.
2 female NSW    1902 111.
3 female NSW    1903 108.
4 female NSW    1904 100.
5 female NSW    1905  92.7
6 female NSW    1906  89.5
7 female NSW    1907  95.7
8 female NSW    1908  90.5
9 female NSW    1909  85.9
10 female NSW   1910  85.4
# i 1,430 more rows
```

Functional data models

Coherent FDM (generalizing Lee-Li)

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Future plans

- Stochastic population forecasting (as per Booth-Hyndman 2008)
- StMoMo
- other tools in the demography package
- demography package to be maintained but not developed