



Tidy data analysis for demography using R

Rob J Hyndman

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Outline

- 1 Vital objects
- 2 Using the Human Mortality and Fertility Databases
- 3 Plots
- 4 Life tables and life expectancy
- 5 Mortality models
- 6 Future plans

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Demographic data structures in R packages

Package	Data class
demography	demogdata
StMoMo	StMoMoData (created by converting a demogdata object)
StanMoMo	Lists of matrices
lifecontingencies	data.frame
BayesMortalityPlus	tibble (that needs to be converted to a matrix for fitting)
MortalityLaws	individual vectors
HMDHFDplus	data.frame



Australian Deaths 1901–2020

A tibble: 145,440 x 7

	Year	Age	Sex	State	Mortality	Exposure	Deaths
	<int>	<int>	<chr>	<chr>	<dbl>	<dbl>	<dbl>
1	1901	0	female	WA	0.129	2511	325
2	1901	0	male	WA	0.158	2634	416
3	1901	1	female	WA	0.0275	2219	61
4	1901	1	male	WA	0.0391	2175	85
5	1901	2	female	WA	0.00688	2180	15
6	1901	2	male	WA	0.0131	2208	29
7	1901	3	female	WA	0.00584	1884	11
8	1901	3	male	WA	0.00503	1988	10
9	1901	4	female	WA	0.00290	1722	5
10	1901	4	male	WA	0.00287	1743	5

i 145,430 more rows



Australian Deaths 1901–2020

```
# A tsibble: 145,440 x 7 [1Y]
```

```
# Key:      Age, Sex, State [1,212]
```

	Year	Age	Sex	State	Mortality	Exposure	Deaths
	<int>	<int>	<chr>	<chr>	<dbl>	<dbl>	<dbl>
1	1901	0	female	WA	0.129	2511	325
2	1901	0	male	WA	0.158	2634	416
3	1901	1	female	WA	0.0275	2219	61
4	1901	1	male	WA	0.0391	2175	85
5	1901	2	female	WA	0.00688	2180	15
6	1901	2	male	WA	0.0131	2208	29
7	1901	3	female	WA	0.00584	1884	11
8	1901	3	male	WA	0.00503	1988	10
9	1901	4	female	WA	0.00290	1722	5
10	1901	4	male	WA	0.00287	1743	5

```
# i 145,430 more rows
```

Variables

Index:

■ Year

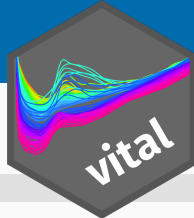
Keys:

■ Age

■ Sex

■ State

Every row must have a unique combination of Index and Keys



Australian Deaths 1901–2020

aus

```
# A vital: 145,440 x 7 [1Y]
# Key:      Age x (Sex, State) [101 x 12]
  Year  Age Sex  State Mortality Exposure Deaths
  <int> <int> <chr> <chr>      <dbl>      <dbl>    <dbl>
1  1901     0 female WA        0.129        2511        325
2  1901     0 male  WA        0.158        2634        416
3  1901     1 female WA        0.0275        2219         61
4  1901     1 male  WA        0.0391        2175         85
5  1901     2 female WA        0.00688        2180         15
6  1901     2 male  WA        0.0131        2208         29
7  1901     3 female WA        0.00584        1884         11
8  1901     3 male  WA        0.00503        1988         10
9  1901     4 female WA        0.00290        1722          5
10 1901     4 male  WA        0.00287        1743          5
# i 145,430 more rows
```

Variables

Index:

■ Year

Keys:

■ Age

■ Sex

■ State

Every row must have a unique combination of Index and Keys

Variables denoting age, sex, deaths, births and population can also be specified.

vital objects

```
index_var(aus)
```

```
[1] "Year"
```

```
key_vars(aus)
```

```
[1] "Age"    "Sex"    "State"
```

```
vital_vars(aus)
```

age	sex	deaths	population
"Age"	"Sex"	"Deaths"	"Exposure"

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Human Mortality Database

Reliability and Accuracy Matter

The Human Mortality Database (HMD) is the world's leading scientific data resource on mortality in developed countries. The HMD provides detailed high-quality harmonized mortality and population estimates to researchers, students, journalists, policy analysts, and others interested in human longevity. The HMD follows open data principles.

- > Short-Term Mortality Fluctuations
- > Cause-of-Death Data Series
- > Subnational Mortality Databases
- > Citing HMD

Data by country or area

Australia	Denmark	Ireland	Norway	Switzerland
Austria	Estonia	Israel	Poland	Taiwan
Belarus	Finland	Italy	Portugal	U.K.
Belgium	France	Japan	Republic of Korea	U.S.A.



Human Fertility Database

The Human Fertility Database (HFD) is the leading scientific data resource on fertility in the developed countries. This open access database provides detailed and high-quality historical and recent data on period and cohort fertility by age of mother and birth order. The HFD is entirely based on official vital statistics and places a great emphasis on rigorous data checking and documentation. The HFD adopts uniform methodology to warrant data comparability across time and between countries. The database follows open data principles.

- > [Short-Term Fertility Fluctuations](#)
- > [Human Fertility Collection](#)
- > [Citing HFD](#)
- > [What's new](#)

For users who seek fast access to the most commonly used summary indicators of period and cohort fertility, we provide excel tables comprising the following indicators for all the HFD countries:

HFD summary indicators

[Total fertility rate](#)[Tempo-adjusted TFR](#)[Mean age at birth](#)[Mean age at first birth](#)[Completed cohort fertility](#)[Cohort parity](#)

HMD imports

```
norway <- read_hmd(  
  country = "NOR",  
  username = "Nora.Weigh@mymail.com",  
  password = "FF!5xeEFa6"  
)  
norway_births <- read_hmd(  
  country = "NOR",  
  username = "Nora.Weigh@mymail.com",  
  password = "FF!5xeEFa6",  
  variables = "Births"  
)
```

- Uses HMDHFDplus package to handle the downloads.
- Default variables: Deaths, Exposures, Population, Mx
- Only 1×1 data supported.
- `read_hmd_files()` and `read_hfd_files()` allow reading of downloaded files.

HMD imports

```
norway_births
```

```
# A tibble: 531 x 3 [1Y]
# Key:   Sex [3]
   Year Sex    Births
   <int> <chr>   <int>
1  1846 Female  20156
2  1846 Male   21372
3  1846 Total  41528
4  1847 Female  20199
5  1847 Male   21411
6  1847 Total  41610
7  1848 Female  19686
8  1848 Male   20868
9  1848 Total  40554
10 1849 Female  21424
# i 521 more rows
```

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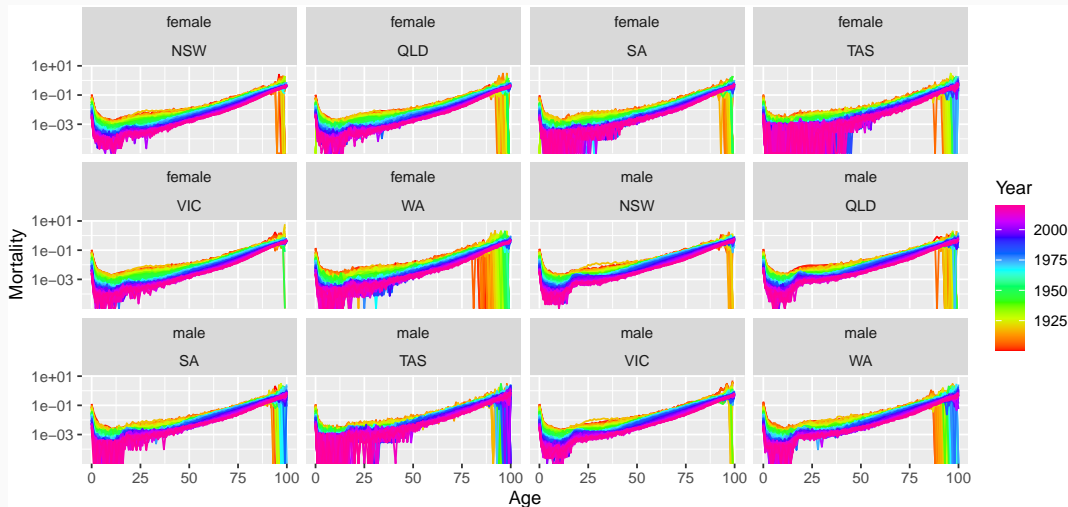
Recall: Australian mortality data

```
aus
```

```
# A vital: 145,440 x 7 [1Y]
# Key:      Age x (Sex, State) [101 x 12]
  Year  Age Sex   State Mortality Exposure Deaths
  <int> <int> <chr> <chr>    <dbl>    <dbl>    <dbl>
1  1901     0 female WA      0.129     2511     325
2  1901     0 male  WA      0.158     2634     416
3  1901     1 female WA      0.0275    2219      61
4  1901     1 male  WA      0.0391    2175      85
5  1901     2 female WA      0.00688   2180      15
6  1901     2 male  WA      0.0131    2208      29
7  1901     3 female WA      0.00584   1884      11
8  1901     3 male  WA      0.00503   1988      10
9  1901     4 female WA      0.00290   1722       5
10 1901     4 male  WA      0.00287   1743       5
# i 145,430 more rows
```

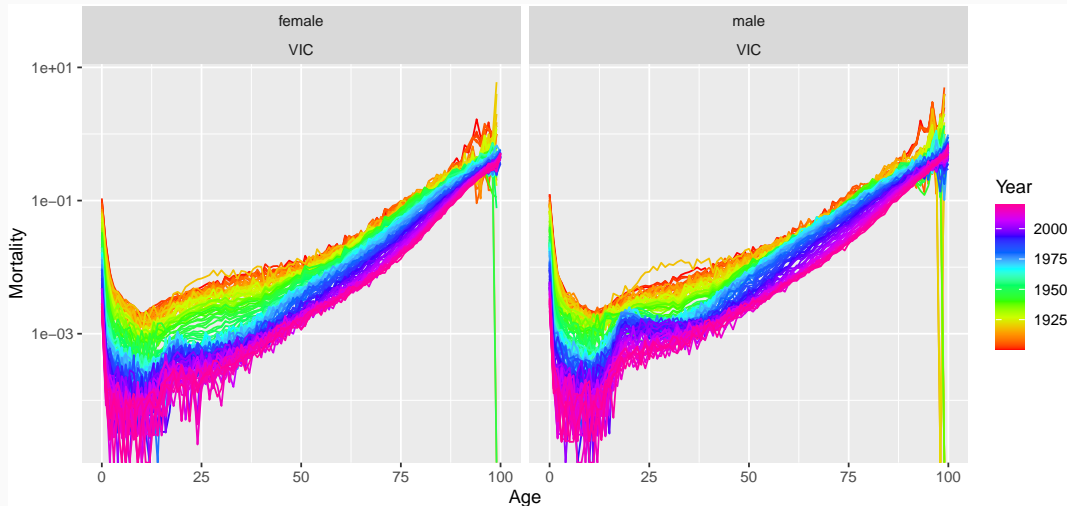
Rainbow plots

```
aus |> autoplot(Mortality) + scale_y_log10()
```



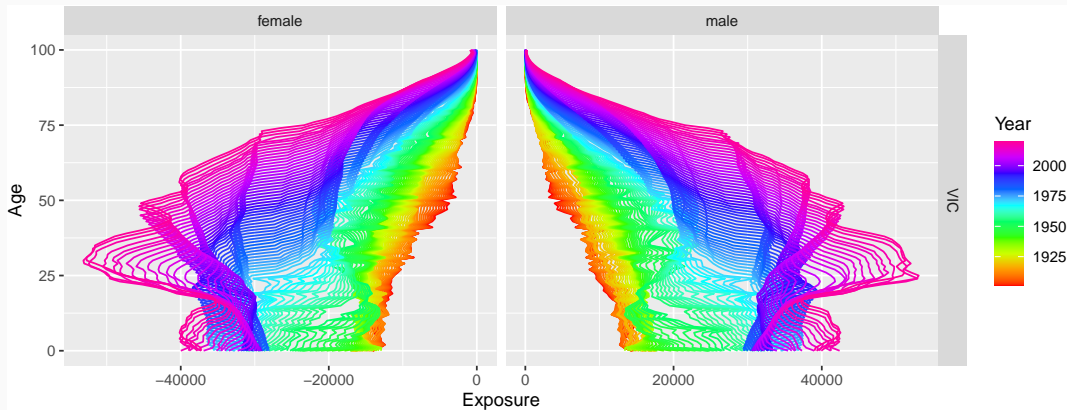
Rainbow plots

```
aus |> filter(State == "VIC") |> autoplot(Mortality) + scale_y_log10()
```



Rainbow plots

```
aus |> filter(State == "VIC") |>  
  mutate(Exposure = if_else(Sex == "female", -Exposure, Exposure)) |>  
  autoplot(Exposure) +  
  facet_grid(State ~ Sex, scales = "free_x") + coord_flip()
```



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Life tables

```
life_table(aus)
```

```
# A vital: 145,440 x 14 [1Y]
```

```
# Key:      Age x (Sex, State) [101 x 12]
```

	Year	Age	Sex	State	mx	qx	lx	dx	Lx	Tx	ex	rx
	<int>	<int>	<chr>	<chr>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>
1	1901	0	fema~	NSW	0.107	0.100	1	1.00e-1	0.935	56.2	56.2	0.935
2	1901	1	fema~	NSW	0.0247	0.0244	0.900	2.20e-2	0.889	55.3	61.5	0.951
3	1901	2	fema~	NSW	0.00686	0.00683	0.878	6.00e-3	0.875	54.4	62.0	0.984
4	1901	3	fema~	NSW	0.00441	0.00441	0.872	3.84e-3	0.870	53.5	61.4	0.994
5	1901	4	fema~	NSW	0.00374	0.00374	0.868	3.24e-3	0.867	52.7	60.7	0.996
6	1901	5	fema~	NSW	0.00274	0.00274	0.865	2.37e-3	0.864	51.8	59.9	0.997
7	1901	6	fema~	NSW	0.00252	0.00251	0.863	2.17e-3	0.861	50.9	59.1	0.997
8	1901	7	fema~	NSW	0.00216	0.00216	0.860	1.86e-3	0.859	50.1	58.2	0.998
9	1901	8	fema~	NSW	0.00169	0.00169	0.859	1.45e-3	0.858	49.2	57.3	0.998
10	1901	9	fema~	NSW	0.00109	0.00109	0.857	9.36e-4	0.857	48.4	56.4	0.999

```
# i 145,430 more rows
```

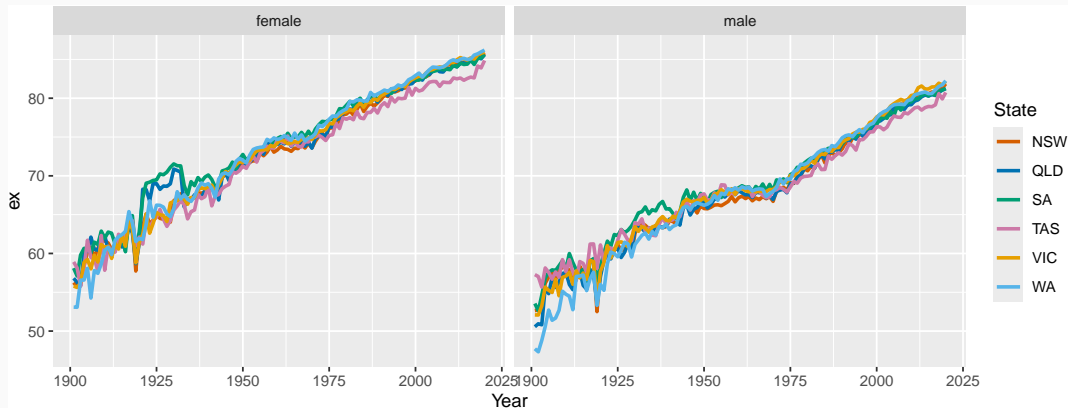
Life expectancy

```
life_expectancy(aus)
```

```
# A vital: 1,440 x 8 [1Y]
# Key:      Age x (Sex, State) [1 x 12]
   Year  Age Sex   State   ex    rx    nx    ax
   <int> <int> <chr> <chr> <dbl> <dbl> <dbl> <dbl>
1  1901     0 female NSW    56.2 0.935     1 0.352
2  1901     0 female QLD    56.8 0.937     1 0.338
3  1901     0 female SA     58.1 0.939     1 0.324
4  1901     0 female TAS    58.9 0.946     1 0.275
5  1901     0 female VIC    55.8 0.937     1 0.334
6  1901     0 female WA     53.1 0.922     1 0.35
7  1901     0 male   NSW    52.6 0.925     1 0.33
8  1901     0 male   QLD    50.6 0.924     1 0.33
9  1901     0 male   SA     53.5 0.922     1 0.33
10 1901     0 male   TAS    57.3 0.930     1 0.33
# i 1,430 more rows
```

Life expectancy

```
life_expectancy(aus) |>  
  ggplot(aes(x = Year, y = ex, colour = State)) +  
  geom_line(linewidth = 1) +  
  facet_grid(. ~ Sex)
```



Life table calculations

- All available years and ages are included in the tables.
- $q_x = m_x / (1 + [(1 - a_x)m_x])$ as per Chiang (1984).
- The code has only been tested for data based on single-year age groups.
- Same code base as for the demography package.
- Life expectancy with `life_expectancy()` computes e_x with $x = 0$ by default, but other values are possible.

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Mortality models

Let $m_{x,t}$ be the mortality rate at age x in year t .

Naive model:

$$m_{x,t} = m_{x,t-1} + \varepsilon_{x,t}$$

Mean model:

$$m_{x,t} = \mu_x + \varepsilon_{x,t}$$

Lee-Carter model:

$$\log(m_{x,t}) = a_x + k_t b_x + \varepsilon_{x,t}$$

where $\varepsilon_{x,t} \sim$ is noise term with variance σ_x^2 .

Mortality models

```
fit <- aus |>
  model(
    naive = FNAIVE(Mortality),
    mean = FMEAN(Mortality),
    lc = LC(log(Mortality))
  )
fit
```

A mable: 12 x 5

Key: Sex, State [12]

	Sex	State	naive	mean	lc
	<chr>	<chr>	<model>	<model>	<model>
1	female	NSW	<FNAIVE>	<FMEAN>	<LC>
2	female	QLD	<FNAIVE>	<FMEAN>	<LC>
3	female	SA	<FNAIVE>	<FMEAN>	<LC>
4	female	TAS	<FNAIVE>	<FMEAN>	<LC>
5	female	VIC	<FNAIVE>	<FMEAN>	<LC>

Naive model

```
fit |>
  filter(Sex == "female", State == "NSW") |>
  select(naive) |>
  report()
```

Series: Mortality

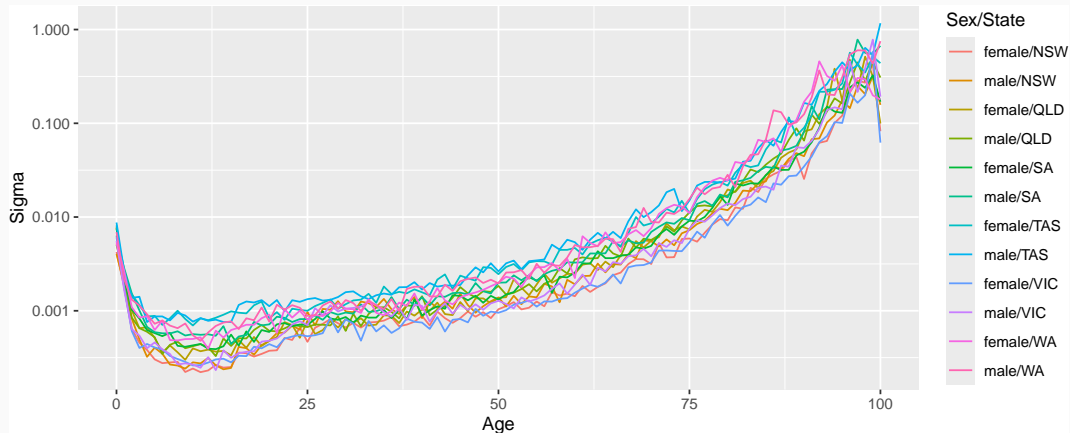
Model: FNAIVE

A tibble: 101 x 2

	Age	sigma
	<int>	<dbl>
1	0	0.00424
2	1	0.00180
3	2	0.000642
4	3	0.000455
5	4	0.000382
6	5	0.000303

Naive models

```
fit |>  
  select(naive) |>  
  autoplot() + scale_y_log10()
```



Lee-Carter models

Let $m_{x,t}$ be the mortality rate at age x in year t .

$$\log(m_{x,t}) = a_x + k_t b_x + \varepsilon_{x,t}$$

- a_x is the mean log mortality rate at age x .
- k_t tracks mortality changes over time.
- b_x allows changes in mortality rates to vary by age.
- $\varepsilon_{x,t}$ is the error term.
- Estimation of k_t and b_x via principal component analysis.
- k_t forecast using a random walk with drift = ARIMA(0,1,0)

Lee-Carter models

```
fit |>  
  filter(Sex == "female", State == "NSW") |>  
  select(lc) |>  
  report()
```

Series: Mortality

Model: LC

Transformation: $\log(\text{Mortality})$

Options:

Adjust method: dt

Jump choice: fit

Age functions

A tibble: 101 x 3

	Age	ax	bx
	<int>	<dbl>	<dbl>
1	0	-4.07	0.0155
2	1	-6.20	0.0221

Lee-Carter models

Age functions

```
# A tibble: 101 × 3
  Age    ax    bx
<int> <dbl> <dbl>
1     0 -4.07 0.0155
2     1 -6.20 0.0221
3     2 -6.89 0.0199
# i 98 more rows
```

Time coefficients

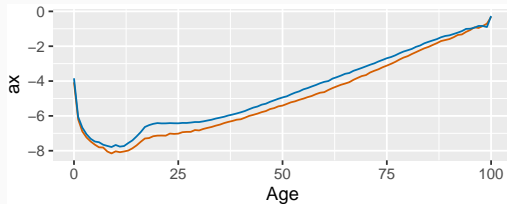
```
# A tsibble: 120 x 2 [1Y]
  Year    kt
<int> <dbl>
1  1901 109.
2  1902 111.
3  1903 108.
# i 117 more rows
```

Time series model: RW w/ drift

Variance explained: 86.61%

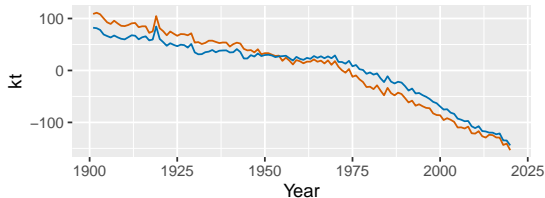
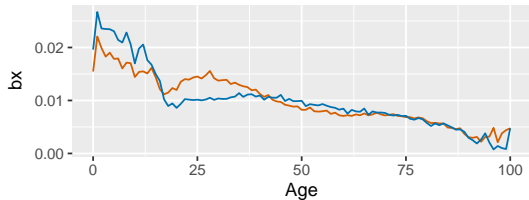
Lee-Carter models

```
fit |>  
  filter(State == "NSW") |>  
  select(lc) |>  
  autoplot()
```



Sex/State

- female/NSW
- male/NSW



Lee-Carter models

```
fit |> select(lc) |> age_components()
```

```
# A tibble: 1,212 x 5
```

	Sex	State	Age	ax	bx
	<chr>	<chr>	<int>	<dbl>	<dbl>
1	female	NSW	0	-4.07	0.0155
2	female	NSW	1	-6.20	0.0221
3	female	NSW	2	-6.89	0.0199
4	female	NSW	3	-7.24	0.0183
5	female	NSW	4	-7.47	0.0190
6	female	NSW	5	-7.65	0.0178
7	female	NSW	6	-7.80	0.0179
8	female	NSW	7	-7.81	0.0160
9	female	NSW	8	-8.05	0.0171
10	female	NSW	9	-8.15	0.0170

```
# i 1,202 more rows
```

Lee-Carter models

```
fit |> select(lc) |> time_components()
```

```
# A tsibble: 1,440 x 4 [1Y]
# Key:      Sex, State [12]
   Sex      State Year    kt
   <chr>   <chr> <int> <dbl>
1 female NSW    1901 109.
2 female NSW    1902 111.
3 female NSW    1903 108.
4 female NSW    1904 100.
5 female NSW    1905  92.7
6 female NSW    1906  89.5
7 female NSW    1907  95.7
8 female NSW    1908  90.5
9 female NSW    1909  85.9
10 female NSW   1910  85.4
# i 1,430 more rows
```

Lee-Carter forecasts

```
fc <- fit |> forecast(h = 20)
fc
```

```
# A vital fable: 72,720 x 7 [1Y]
```

```
# Key:           Age x (Sex, State, .model) [101 x 36]
```

	Sex	State	.model	Year	Age	Mortality	.mean
	<chr>	<chr>	<chr>	<dbl>	<int>	<dist>	<dbl>
1	female	NSW	naive	2021	0	N(0.0027, 1.8e-05)	0.00270
2	female	NSW	naive	2022	0	N(0.0027, 3.6e-05)	0.00270
3	female	NSW	naive	2023	0	N(0.0027, 5.4e-05)	0.00270
4	female	NSW	naive	2024	0	N(0.0027, 7.2e-05)	0.00270
5	female	NSW	naive	2025	0	N(0.0027, 9e-05)	0.00270
6	female	NSW	naive	2026	0	N(0.0027, 0.00011)	0.00270
7	female	NSW	naive	2027	0	N(0.0027, 0.00013)	0.00270
8	female	NSW	naive	2028	0	N(0.0027, 0.00014)	0.00270
9	female	NSW	naive	2029	0	N(0.0027, 0.00016)	0.00270
10	female	NSW	naive	2030	0	N(0.0027, 0.00018)	0.00270

Lee-Carter forecasts

```
fc |> filter(.model == "lc")
```

```
# A vital fable: 24,240 x 7 [1Y]
```

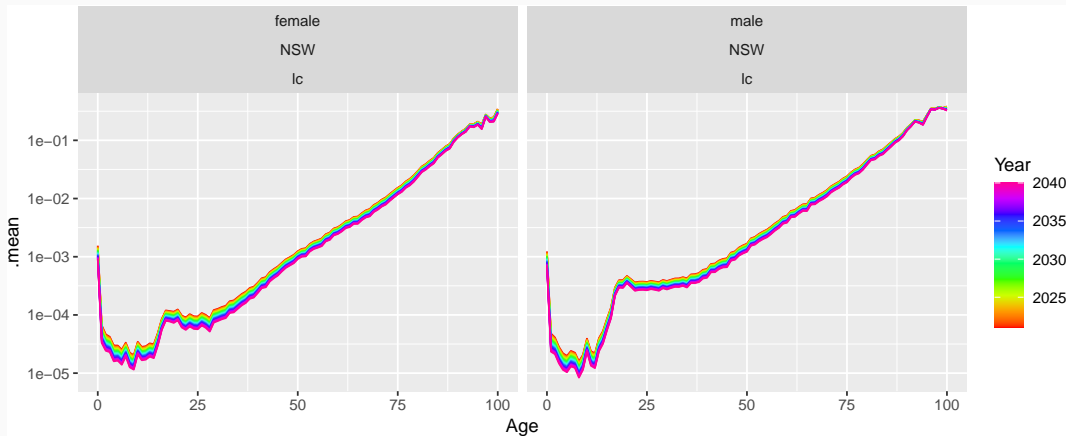
```
# Key:           Age x (Sex, State, .model) [101 x 12]
```

	Sex	State	.model	Year	Age	Mortality	.mean
	<chr>	<chr>	<chr>	<dbl>	<int>	<dist>	<dbl>
1	female	NSW	lc	2021	0	t(N(-6.5, 0.011))	0.00155
2	female	NSW	lc	2022	0	t(N(-6.5, 0.022))	0.00151
3	female	NSW	lc	2023	0	t(N(-6.5, 0.034))	0.00146
4	female	NSW	lc	2024	0	t(N(-6.6, 0.046))	0.00142
5	female	NSW	lc	2025	0	t(N(-6.6, 0.058))	0.00138
6	female	NSW	lc	2026	0	t(N(-6.6, 0.07))	0.00135
7	female	NSW	lc	2027	0	t(N(-6.7, 0.082))	0.00131
8	female	NSW	lc	2028	0	t(N(-6.7, 0.094))	0.00127
9	female	NSW	lc	2029	0	t(N(-6.7, 0.11))	0.00124
10	female	NSW	lc	2030	0	t(N(-6.8, 0.12))	0.00120

```
# i 24,230 more rows
```

Lee-Carter forecasts

```
fc |> filter(State == "NSW", .model == "lc") |>  
  autoplot() + scale_y_log10()
```



Functional data models

Let $m_{x,t}$ be the mortality rate at age x in year t .

$$\log(m_{t,x}) = s_t(x) + \sigma_t(x)\varepsilon_{t,x}$$

$$s_t(x) = \mu(x) + \sum_{j=1}^J \beta_{t,j} \phi_j(x) + e_t(x)$$

- $s_t(x)$ = smoothed version of $y_t(x)$
- $\mu(x)$ = mean $s_t(x)$ across years.
- $\phi_j(x)$ and $\beta_{t,j}$ estimated using principal component analysis.
- $\beta_{1,j}, \dots, \beta_{T,j}$ modelled with ARIMA or ARFIMA processes.

Functional data models

```
sm_aus <- aus |> smooth_mortality(Mortality)
sm_aus
```

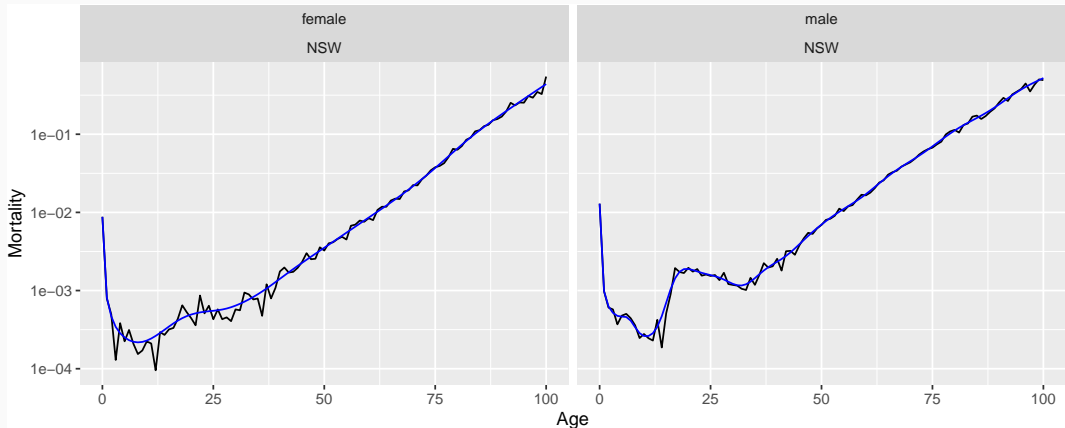
```
# A vital: 145,440 x 9 [1Y]
```

```
# Key:      Age x (Sex, State) [101 x 12]
```

	Year	Age	Sex	State	Mortality	Exposure	Deaths	.smooth	.smooth_se
	<int>	<dbl>	<chr>	<chr>	<dbl>	<dbl>	<dbl>	<dbl[1d]>	<dbl[1d]>
1	1901	0	female	NSW	0.107	17143	1833	0.107	0.00295
2	1901	1	female	NSW	0.0247	15071	373	0.0237	0.00141
3	1901	2	female	NSW	0.00686	15461	106	0.00804	0.000670
4	1901	3	female	NSW	0.00441	15629	69	0.00461	0.000405
5	1901	4	female	NSW	0.00374	15762	59	0.00341	0.000305
6	1901	5	female	NSW	0.00274	16030	44	0.00275	0.000251
7	1901	6	female	NSW	0.00252	16289	41	0.00230	0.000215
8	1901	7	female	NSW	0.00216	16639	36	0.00197	0.000189
9	1901	8	female	NSW	0.00169	16554	28	0.00175	0.000173
10	1901	9	female	NSW	0.00109	16468	18	0.00162	0.000163

Functional data models

```
sm_aus <- aus |> smooth_mortality(Mortality)
sm_aus |> filter(State == "NSW", Year == 1980) |> autoplot(Mortality) +
  geom_line(aes(y = .smooth), col = "blue") + scale_y_log10()
```



Functional data models

```
fit <- sm_aus |> model(hu = FDM(log(.smooth)))  
fit
```

```
# A mable: 12 x 3
```

```
# Key:      Sex, State [12]
```

	Sex	State	hu
	<chr>	<chr>	<model>
1	female	NSW	<FDM>
2	female	QLD	<FDM>
3	female	SA	<FDM>
4	female	TAS	<FDM>
5	female	VIC	<FDM>
6	female	WA	<FDM>
7	male	NSW	<FDM>
8	male	QLD	<FDM>
9	male	SA	<FDM>
10	male	TAS	<FDM>

Functional data models

```
fit |>  
  filter(Sex == "female", State == "NSW") |>  
  select(hu) |>  
  report()
```

Series: .smooth

Model: FDM

Transformation: log(.smooth)

Basis functions

A tibble: 101 x 8

	Age	mean	phi1	phi2	phi3	phi4	phi5	phi6
	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>
1	0	-4.07	0.147	0.0625	-0.0270	0.0986	0.0112	-0.0624
2	1	-6.16	0.200	-0.0609	-0.194	0.116	0.0383	-0.238
3	2	-6.82	0.182	-0.0483	-0.157	0.0924	0.0443	-0.264
4	3	-7.17	0.170	-0.0368	-0.130	0.0362	0.000338	-0.321
5	4	-7.40	0.164	-0.0165	-0.114	-0.0154	-0.0303	-0.374

i 96 more rows

Functional data models

Coefficients

```
# A tsibble: 120 x 8 [1Y]
  Year mean beta1 beta2 beta3 beta4 beta5 beta6
  <int> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl>
1  1901     1  11.1 -0.522 -0.0553  0.207  0.358  0.0305
2  1902     1  11.8 -0.649  0.399  0.856  0.0319  0.422
3  1903     1  11.5 -0.930 -0.485  0.398  0.399 -0.376
4  1904     1  11.1 -0.827 -0.214 -0.000305 0.00125 -0.0783
5  1905     1  10.2 -0.563 -0.105  0.324  0.122  0.0478
# i 115 more rows
# i Use `print(n = ...)` to see more rows
```

Time series models

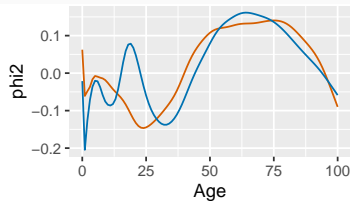
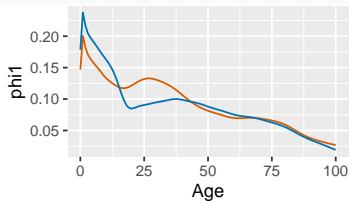
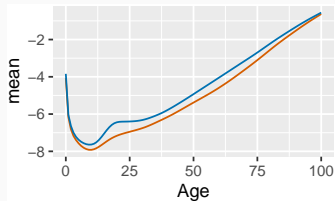
```
beta1 : ARIMA(0,1,1) w/ drift
beta2 : ARIMA(0,2,2)
beta3 : ARIMA(1,0,1)
beta4 : ARIMA(0,0,2)
beta5 : ARIMA(0,0,0)
beta6 : ARIMA(2,0,2)
```

Variance explained

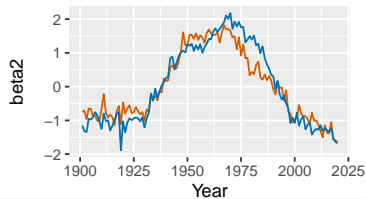
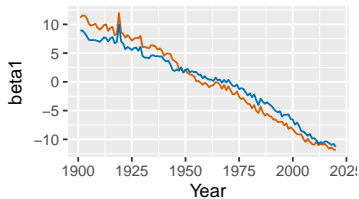
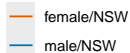
91.38 + 1.81 + 0.58 + 0.49 + 0.42 + 0.39 = 95.06%

Functional data models

```
fit |>  
  filter(State == "NSW") |>  
  select(hu) |>  
  autoplot()
```



Sex/State



Functional data models

```
fit |> select(hu) |> age_components()
```

```
# A tibble: 1,212 x 10
```

	Sex	State	Age	mean	phi1	phi2	phi3	phi4	phi5	phi6
	<chr>	<chr>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>
1	female	NSW	0	-4.07	0.147	0.0625	-0.0270	0.0986	0.0112	-0.0624
2	female	NSW	1	-6.16	0.200	-0.0609	-0.194	0.116	0.0383	-0.238
3	female	NSW	2	-6.82	0.182	-0.0483	-0.157	0.0924	0.0443	-0.264
4	female	NSW	3	-7.17	0.170	-0.0368	-0.130	0.0362	0.000338	-0.321
5	female	NSW	4	-7.40	0.164	-0.0165	-0.114	-0.0154	-0.0303	-0.374
6	female	NSW	5	-7.57	0.158	-0.00759	-0.121	-0.0564	0.0247	-0.315
7	female	NSW	6	-7.71	0.153	-0.00942	-0.133	-0.0976	0.112	-0.197
8	female	NSW	7	-7.81	0.149	-0.0121	-0.143	-0.143	0.175	-0.0863
9	female	NSW	8	-7.88	0.143	-0.0141	-0.148	-0.181	0.211	0.0131
10	female	NSW	9	-7.92	0.138	-0.0185	-0.142	-0.196	0.236	0.101

```
# i 1,202 more rows
```

Functional data models

```
fit |> select(hu) |> time_components()
```

```
# A tsibble: 1,440 x 10 [1Y]
```

```
# Key:           Sex, State [12]
```

	Sex	State	Year	mean	beta1	beta2	beta3	beta4	beta5	beta6
	<chr>	<chr>	<int>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>
1	female	NSW	1901	1	11.2	-0.756	-0.0301	0.269	-0.155	0.409
2	female	NSW	1902	1	11.6	-0.708	0.0899	0.207	0.0282	0.507
3	female	NSW	1903	1	11.5	-0.962	0.169	-0.103	0.366	0.323
4	female	NSW	1904	1	11.1	-0.648	0.0985	-0.433	0.131	0.270
5	female	NSW	1905	1	10.1	-0.660	0.342	-0.0910	0.0862	0.612
6	female	NSW	1906	1	9.78	-0.865	0.496	-0.147	-0.101	0.306
7	female	NSW	1907	1	9.90	-0.861	0.0530	1.33	0.278	0.181
8	female	NSW	1908	1	10.1	-1.01	0.554	-0.0198	-0.00428	0.578
9	female	NSW	1909	1	9.42	-1.02	0.293	-0.365	-0.149	0.353
10	female	NSW	1910	1	9.08	-0.650	0.172	-0.559	-0.253	0.0110

```
# i 1,430 more rows
```

Coherent functional models

$$y_t(x) = s_t(x) + \sigma_t(x)\varepsilon_{t,x}$$

$$s_t(x) = \mu(x) + \sum_{j=1}^J \beta_{t,j} \phi_j(x) + e_t(x)$$

- $y_t(x) = \log(m_{x,t}^M m_{x,t}^F)$ and $\log(m_{x,t}^M / m_{x,t}^F)$
- $s_t(x)$ = smoothed version of $y_t(x)$
- $\mu(x)$ = mean $s_t(x)$ across years.
- $\phi_j(x)$ and $\beta_{t,j}$ estimated using principal component analysis.
- $\beta_{1,j}, \dots, \beta_{T,j}$ modelled with ARIMA for products and ARMA for ratios (to ensure stationary sex-ratios)

Coherent functional models

```
pr <- sm_aus |> make_pr(.smooth)
pr
```

```
# A vital: 218,160 x 9 [1Y]
```

```
# Key:      Age x (Sex, State) [101 x 18]
```

	Year	Age	Sex	State	Mortality	Exposure	Deaths	.smooth	.smooth_se
	<int>	<dbl>	<chr>	<chr>	<dbl>	<dbl>	<dbl>	<dbl[1d]>	<dbl[1d]>
1	1901	0	female	NSW	0.107	17143	1833	0.939	0.00295
2	1901	1	female	NSW	0.0247	15071	373	1.03	0.00141
3	1901	2	female	NSW	0.00686	15461	106	0.965	0.000670
4	1901	3	female	NSW	0.00441	15629	69	0.982	0.000405
5	1901	4	female	NSW	0.00374	15762	59	1.02	0.000305
6	1901	5	female	NSW	0.00274	16030	44	1.04	0.000251
7	1901	6	female	NSW	0.00252	16289	41	1.04	0.000215
8	1901	7	female	NSW	0.00216	16639	36	1.01	0.000189
9	1901	8	female	NSW	0.00169	16554	28	0.972	0.000173
10	1901	9	female	NSW	0.00109	16468	18	0.938	0.000163

Coherent functional models

```
pr <- sm_aus |> make_pr(.smooth)
fit <- pr |> model(hby = FDM(log(.smooth), coherent = TRUE))
fit
```

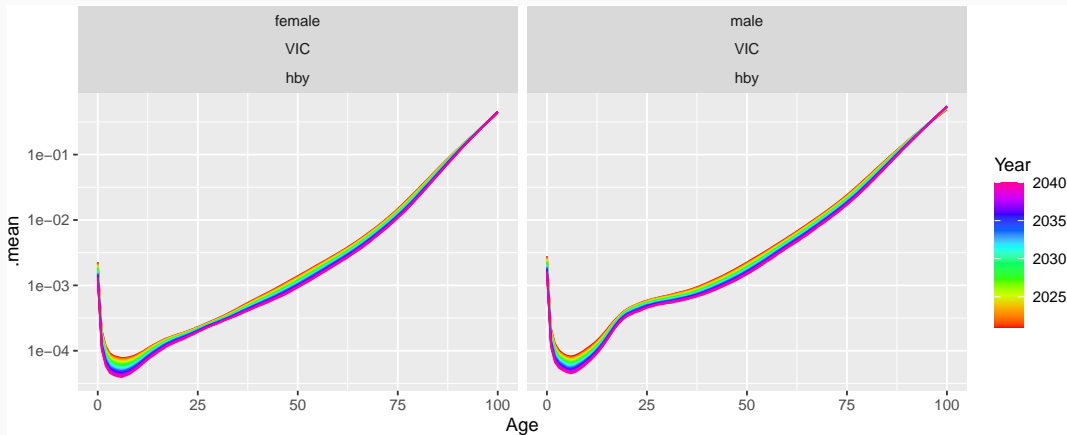
```
# A mable: 18 x 3
```

```
# Key:      Sex, State [18]
```

	Sex	State	hby
	<chr>	<chr>	<model>
1	female	NSW	<FDM>
2	female	QLD	<FDM>
3	female	SA	<FDM>
4	female	TAS	<FDM>
5	female	VIC	<FDM>
6	female	WA	<FDM>
7	geometric_mean	NSW	<FDM>
8	geometric_mean	QLD	<FDM>
9	geometric_mean	SA	<FDM>

Coherent functional models

```
fc <- fit |> forecast(h = 20) |> undo_pr(.smooth)  
fc |> filter(State == "VIC") |> autoplot() + scale_y_log10()
```



Outline

- 1 Vital objects
- 2 Using the Human Mortality and Fertility Databases
- 3 Plots
- 4 Life tables and life expectancy
- 5 Mortality models
- 6 Future plans

Future plans

- Remaining tools from the demography package
- Stochastic population forecasting (as per Hyndman-Booth, IJF, 2008)
- All models handled by stMoMo package
- All methods from MortalityLaws package
- demography package to be maintained but not developed
- Suggestions from users

<https://pkg.robjhyndman.com/vital/>