

# From Candy Auction to Maximum Revenue

Finding the Sweet Spot: Price Optimization Through Data

## Part 1: Reviewing Our Auction Data

Yesterday, we conducted a candy auction where each group could buy as many candies as they wanted at each price point. Let's organize what we discovered about **demand** – how many candies people wanted to buy at different prices.

### Step 1: Record Your Auction Results

Fill in the table below with the data from our 5 auction rounds:

Round	Price (\$)	Total Quantity Demanded
		<i>(candies bought by all groups)</i>
1	_____	_____
2	_____	_____
3	_____	_____
4	_____	_____
5	_____	_____

### Step 2: Quick Check on Demand

**Question:** Look at your Price vs. Quantity Demanded data. What pattern do you notice?

\_\_\_\_\_

\_\_\_\_\_

This pattern is called the **Law of Demand** in economics!

## Part 2: From Demand to Revenue

Now comes the business insight: It's not just about how many we sell – it's about how much money we make!

### Step 3: Calculate Revenue

For each round, calculate the **revenue** (total money collected):

$$\text{Revenue} = \text{Price} \times \text{Quantity Demanded}$$

Round	Price (\$)	Quantity Demanded	Revenue (\$)
	<i>(copy from above)</i>	<i>(copy from above)</i>	<i>(calculate: Price <math>\times</math> Quantity)</i>
1	_____	_____	_____
2	_____	_____	_____
3	_____	_____	_____
4	_____	_____	_____
5	_____	_____	_____

### Step 4: The Million Dollar Question

Looking at your revenue column, which price gave you the **highest revenue**?

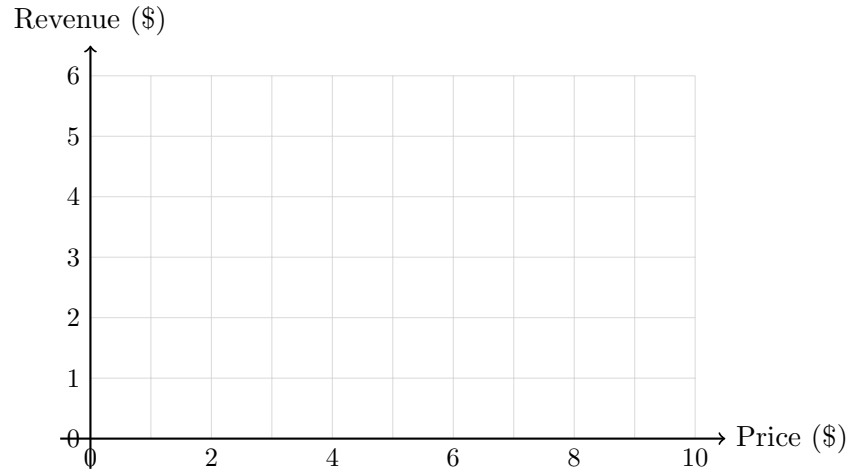
Price: \$ \_\_\_\_\_ Revenue at that price: \$ \_\_\_\_\_

## Part 3: Creating the Revenue Graph in Desmos

### Step 5: Plot Price vs. Revenue

- Open Desmos graphing calculator
- Create a new table with two columns:
  - Column 1: Label it  $x_1$  (this is Price)
  - Column 2: Label it  $y_1$  (this is Revenue)
- Enter your 5 data points from the Price and Revenue columns above
- You should see dots forming a curve!

**Sketch what you see:**



## Part 4: Finding the Perfect Price with Regression

### Step 6: Fit a Quadratic (Parabola) to Your Data

In Desmos, type this in a new line:

$$y_1 \sim ax_1^2 + bx_1 + c$$

Desmos will automatically find the best-fitting parabola! Write the equation it gives you:

$$R(p) = \underline{\hspace{2cm}} p^2 + \underline{\hspace{2cm}} p + \underline{\hspace{2cm}}$$

Record the values Desmos calculated:

- $a = \underline{\hspace{2cm}}$  (this should be negative because our parabola opens down and has a maximum)
- $b = \underline{\hspace{2cm}}$
- $c = \underline{\hspace{2cm}}$

## Part 5: The Vertex – Your Optimal Price!

The highest point on your revenue parabola is called the **vertex**. This tells you the best price to charge!

### Step 7: Find the Vertex Graphically

- a) Click on the highest point of your parabola in Desmos
- b) Desmos will show you the coordinates: (Price, Revenue)

**Vertex from Graph:** Price = \$\_\_\_\_\_ Maximum Revenue = \$\_\_\_\_\_

### Step 8: Find the Vertex Using Algebra

For any parabola  $y = ax^2 + bx + c$ , the x-coordinate of the vertex is:

$$x = -\frac{b}{2a}$$

Using your values of  $a$  and  $b$  from Step 6:

$$\begin{aligned} \text{Optimal Price} &= -\frac{b}{2a} \\ &= -\frac{\underline{\hspace{2cm}}}{2 \times (\underline{\hspace{2cm}})} \\ &= -\frac{\underline{\hspace{2cm}}}{\underline{\hspace{2cm}}} \\ &= \$\underline{\hspace{2cm}} \end{aligned}$$

**Check:** Does this match what you found graphically?    Yes    No

## Part 6: Making Business Sense

### Step 9: Interpret Your Results

Complete these sentences based on your analysis:

- If we price the candy too low (like \$\_\_\_\_\_), we sell a lot but don't make much per candy, so our total revenue is \_\_\_\_\_.
- If we price the candy too high (like \$\_\_\_\_\_), we make a lot per candy but \_\_\_\_\_, so our total revenue is also low.
- The "sweet spot" price that maximizes our revenue is \$\_\_\_\_\_, which would give us a revenue of \$\_\_\_\_\_.

### Step 10: Business Recommendation

Write a 2-3 sentence recommendation to a candy store owner based on your analysis:

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Name: \_\_\_\_\_ Period: \_\_\_\_\_ Date: \_\_\_\_\_

### Extension Question (if time allows)

**Think About It:** We found the price that maximizes *revenue*, but businesses care about *profit*. What additional information would we need to find the price that maximizes profit instead?

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*Next Class: We'll apply these same techniques to help real local businesses (Golden Monkey, Mande'e's, and Yas Chicken) find their optimal prices!*