

QUIZ 4 - SOLUTIONS  
INSTRUCTOR: FORAKER

1. A special operations unit is looking to buy new weapons for use in upcoming deployments. There are four weapons available that can effectively engage targets at different ranges. The different weapons, their costs, and capabilities are summarized in the table below. A YES in the column for a weapon means that it can effectively engage targets at that range.

Target Range	Weapon 1	Weapon 2	Weapon 3	Weapon 4
Short	YES	YES	YES	YES
Medium	NO	YES	YES	NO
Long	NO	NO	YES	YES
Cost	\$ 6300	\$ 5400	\$ 4600	\$ 3100

Use the variable  $X_j$  defined below, to answer the following questions. Remember to define **ANY** other terms you use in your answers to the questions below.

$$X_j = \begin{cases} 1 & \text{if Weapon } j \text{ is selected} \\ 0 & \text{otherwise.} \end{cases}$$

- (a) (5 Points) Write an objective function that finds a minimum cost collection of weapons.

$$\min 6300X_1 + 5400X_2 + 4600X_3 + 3100X_4$$

or

$$\min \sum_{j \in J} cost_j X_j, \quad J = \{1, 2, 3, 4\} \text{ and } cost_j \text{ is given in the table above}$$

- (b) (5 Points) Write the set covering constraints which ensure the unit will have **AT LEAST ONE** weapon that can effectively engage targets at each range.

$$\begin{aligned} X_1 + X_2 + X_3 + X_4 &\geq 1 \\ X_2 + X_3 &\geq 1 \\ X_3 + X_4 &\geq 1 \end{aligned}$$

- (c) (5 Points) Write the set partitioning constraints which ensure the unit will have **EXACTLY ONE** weapon that can effectively engage targets at each range.

$$\begin{aligned} X_1 + X_2 + X_3 + X_4 &= 1 \\ X_2 + X_3 &= 1 \\ X_3 + X_4 &= 1 \end{aligned}$$