On Adding Pattern Matching to Haskell-based Deeply Embedded Domain Specific Languages

Not For Distribution

Anonymous Author(s)

Abstract

Capturing control flow is the Achilles heel of Haskell-based deeply embedded domain specific languages. Rather than use the builtin control flow mechanisms, artificial control flow combinators are used instead.

However, capturing traditional control flow in an deeply embedded domain specific language would support the writing of programs in a natural style by allowing the programmer to use the constructs that are already builtin to the base language, such as pattern matching and recursion.

In this paper, we expand the capabilities of traditional, Haskell-based, deep embeddings with a compiler extension for reifying conditionals and pattern matching. With this new support, the Haskell that we capture for expressing deeply embedded domain specific languages can be cleaner, Haskell-idiomatic, and more declarative in nature.

CCS Concepts • Software and its engineering → Translator writing systems and compiler generators; Source code generation; Domain specific languages;

ACM Reference Format:

Anonymous Author(s). 2020. On Adding Pattern Matching to Haskell-based Deeply Embedded Domain Specific Languages Not For Distribution. In *Proceedings of the 19th ACM SIGPLAN International Conference on Generative Programming: Concepts and Experiences (GPCE '20) November 15 – 20, 2020, Chicago, Illinois, United States.* ACM, New York, NY, USA, 13 pages. https://doi.org/1

1 Introduction

Embedded domain specific languages (EDSLs) have long been an effective technique for constructing reusable tools for working in a variety of different problem domains. Haskell is a language which is particularly well-suited to EDSLs due

Permission to make digital or hard copies of all or part of this work for personal or classroom use is granted without fee provided that copies are not made or distributed for profit or commercial advantage and that copies bear this notice and the full citation on the first page. Copyrights for components of this work owned by others than ACM must be honored. Abstracting with credit is permitted. To copy otherwise, or republish, to post on servers or to redistribute to lists, requires prior specific permission and/or a fee. Request permissions from permissions@acm.org.

GPCE~'20,~November~15-20,~2020,~Chicago,~Illinois,~United~States

© 2020 Association for Computing Machinery.

ACM ISBN 978-1-4503-XXXX-X/18/06...\$15.00

https://doi.org/1

to its lazy evaluation, first-class functions and lexical closures. Despite these advantages Haskell provides for creating EDSLs, there are a few constructs for which representations have proven illusive. One prominent example is that of a case expression. Pattern matching is a convenient way to implement control flow structures and to inspect data structures, so it is frequently a desirable feature for many EDSLs.

Additionally, lambdas can also be difficult to implement in EDSLs. A major reason for this is that control flow constructs which are typically *outside* the EDSL, such as pattern matching and tail recursion, can make it challenging to "look inside" the lambda. When these control structures are reified within the EDSL, it is easier to also reify lambdas, as you can simply apply them to a dummy argument to access their body (with the dummy value substituted for the argument).

TODO: Maybe add brief summary of relationship to lambdas?

The following contributions are made by this paper:

- A representation of pattern matching in a Haskell EDSL (Section 3)
- A representation of lambdas (Section 5) in the EDSL, taking advantage of the fact that both pattern matching and tail recursion are already captured in the EDSL.
- A GHC Core plugin which transforms a subset of standard Haskell code into this EDSL for pattern matching, extended with tail recursion, lambdas and primitive operations (Section 8)
- An implementation of a interpreter for the "standard" semantics of the EDSL (Section 6).
- An outline of a C backend for this EDSL (Section 7).

Readers who are primarily interested only in the encoding of pattern matching itself can direct most of their attention to Sections 2, 3 and 6. Most of the technical aspects of the transformation performed by the Core plugin are described in Section 8.

1.1 Motivation

TODO: Expand?

A major benefit of the Haskell language is that it is frequently possible derive a Haskell implementation from a

specification, either partially or fully. Examples of this technique include the work in [Elliott 2018] as well as the work in [Elliott 2019]. When it is not possible to fully derive an implementation from a specification, it is often easier to check a Haskell implementation against a specification than it is in many imperative languages due, in part, to the management of side effects in Haskell. This is more difficult to do using an imperative language such as C, as they provide no restrictions on where side effects can occur.

Haskell EDSLs that support powerful language features like pattern matching allow these advantages to be brought to problem domains where it is currently either difficult or impossible to use a language that has these benefits.

TODO: Cite examples where Haskell implementations have been derived specifications. Conal Elliott's latest two papers (as of May 2020), [Elliott 2018] and [Elliott 2019], would be good examples of this. (This is now cited)

A paper which describes a Haskell implementation derived from an operational semantics would also be a good example.

1.2 Overview

 In this EDSL, the type representing values in the expression language is E t and there are two basic functions which translate values to and from this expression language with the following type signatures (omitting type class constraints for the moment):

```
rep :: a -> E a abs :: E a -> a
```

Additionally, the following functions mark the parts of the code which the Core plugin will target:

```
internalize :: E a -> a
externalize :: a -> E a
```

The E type is the type of expressions in the EDSL. In this paper, the data constructors of this type will be described incrementally as they are needed.

1.3 Translation Example

TODO: Does it make sense for this to be a subsection of the intro?

In the example below, the Core plugin transforms example into example:

```
import Data.Char (ord)

x :: Either Char Int
x = Left 'a'
```

```
example :: Int
example =
  internalize (externalize
    (case x of
      Left c -> ord c
      Right i -> i))
example' :: Int
example' =
  abs (CaseExp
        (LeftExp 'a')
        (SumMatchExp (OneProdMatch
                        (Lam 1
                          (Ord (Var 1))))
                      (OneSumMatch
                        (OneProdMatch
                          (Lam 2
                            (Var 2)))))
```

2 Representing Algebraic Datatypes

TODO: Look into generic-sop and compare then cite corresponding paper.

Briefly, a algebraic type T with an automatically generated ERep instance is given a representation in terms of Either, (,), () and Void. This "standardized" type representation is given by ERepTy T. ERepTy is an type family associated to the type class ERep. This type will be called the *canonical type* of T.

Only the "outermost" type will be deconstructed into these fundamental building blocks, and further deconstruction can take place on these pieces later on. For example, consider this type:

```
instance ERep ComplexPair
```

Note that the instance definition is automatically generated from the Generic instance.

Given this code, ERepTy ComplexPair ~ (Complex Double, Complex Double). Here is an example that demonstrates why this is more useful than if it *fully* deconstructed each type into Either, (,) and ():

```
sumComplexPair ::
   ComplexPair -> Complex Double
sumComplexPair p =
```

```
internalize (externalize
  (case p of
    ComplexPair a b -> a + b))
```

If ERepTy ComplexPair were fully deconstructed into ((Double, Double), (Double, Double)), we would need a Num instance for (Double, Double). What we really want is to use the fact that a Num instance already exists for Complex Double. This is exactly what preserving this type information allows us to do. We can later use this preserved type information in backends, through the corresponding Typeable instances (for instance, to provide special support for arithmetic on complex numbers).

It is important to note that we are still able to further deconstruct this type with further pattern matches, since ERepTy (Complex Double) ~ (Double, Double):

```
realSum :: ComplexPair -> Double
realSum p =
  internalize (externalize
  (case p of
        ComplexPair a b ->
        case a of
        a_real :+ _ ->
        case b of
        b_real :+ _ ->
        a_real + b_real))
```

Note that the above pattern matches can be written as a single nested pattern match. Both forms compile down to the same Core representation.

An additional benefit of this is that recursive types require no special handling. For example, consider:

```
data IntList = Nil | Cons Int IntList
  deriving (Generic, Show)
```

```
instance ERep IntList
```

Note that ERepTy IntList ~ Either () (Int, IntList). If ERepTy attempted to "fully deconstruct" IntList, it would send the compiler into an infinite loop.

This allows us to implement functions on such recursive types:

```
isEmpty :: IntList -> Bool
isEmpty t =
  internalize (externalize
    (case t of
      Nil -> True
      Cons x xs -> False))

intListSum :: (Int, IntList) -> Int
intListSum p =
  internalize (externalize)
```

```
(case p of
  (acc, t) ->
    case t of
    Nil -> acc
    Cons x xs ->
        intListSum
        (x+acc, xs)))
```

2.1 E, ERep, ERepTy

There are three interconnected foundational parts: E, ERep and ERepTy. E is the deep embedding of the EDSL (a GADT that encodes expressions in the DSL language). ERep is a type class which represents all Haskell types which can be represented in the DSL. ERepTy is a type family associated to the ERep type class, which represents a "canonical form" of the given type. This canonical form can be immediately constructed in the EDSL. Canonical form types crucially include Either and (,), which allow all combinations of basic sum types and product types to be encoded, in the manner described at the beginning of Section 2.

With GHC Generics, any data type T with a Generic instance has a corresponding Rep T type, which gives a generic representation of T. Conversion between values of this type and values of the original type T is given by the functions to and from. The generic representation Rep T can be traversed by functions which operate solely on the structure of the data type. This generic representation contains additional metadata which we do not need. However, we can automatically generate a ERep instance for any type which has a Generic instance.

As Generic instances are automatically generated, this provides a simple mechanism to automaticly generate ERep instances.

This information is brought into the E type via the constructor ConstructRep. The E also contains constructors representing Either and (,) values:

```
data E t where
...
ConstructRep ::
   (Typeable a, ERep a)
   => E (ERepTy a) -> E a

LeftExp :: E a -> E (Either a b)
RightExp :: E b -> E (Either a b)

PairExp :: E a -> E b -> E (a, b)
...
```

ERep and ERepTy provide an interface for transferring values between the EDSL expression language and the source Haskell language:

```
class Typeable t => ERep t where
```

```
331
       type ERepTy t
332
333
       construct :: t -> E (ERepTy t)
334
335
       rep :: t -> E t
336
337
       default rep ::
338
         (ERep (ERepTy t))
         => t -> E t
340
       rep x = ConstructRep (construct x)
341
       {-# INLINABLE rep #-}
342
343
       unrep' :: ERepTy t -> t
344
345
346
       rep' :: t -> ERepTy t
347
       The key algebraic instances mentioned before are as fol-
348
     lows:
349
350
     instance (ERep a, ERep b)
351
       => ERep (Either a b) where
352
353
       type ERepTy (Either a b) = Either a b
355
       rep (Left x) = LeftExp (rep x)
356
       rep (Right y) = RightExp (rep y)
357
358
359
       unrep' = id
360
             = id
       rep'
361
362
     instance (ERep a, ERep b)
363
       => ERep (a, b) where
364
365
       type ERepTy(a, b) = (a, b)
366
367
       rep (x, y) = PairExp (rep x) (rep y)
368
       unrep' = id
369
       rep'
               = id
370
371
372
     3 Representing pattern matches
373
```

Within the E expression language, a pattern match is represented by the CaseExp constructor:

```
data E t where
...
CaseExp ::
   (ERep t, ERepTy (ERepTy t) ~ ERepTy t)
   => ERep t
        -> E (SumMatch (ERepTy t) r)
        -> E r
```

The equality constraint ensures that a canonical type is its own canonical type.

```
TODO: Should we make a synonym for this constraint since it is used in multiple places? Like this:

type CanonicalIsIdem t =
```

```
ERepTy (ERepTy t) ~ ERepTy t
```

(The above code block is a slight simplification of the actual implementation, which has an additional type variable which is used at an "intermediate" point. The expanded form is in place to simplify the Core transformation.)

The type SumMatch is defined as

```
newtype SumMatch a b =
  MkSumMatch { runSumMatch :: a -> b }
```

For the moment, we will primarily use this type as a type tag and ignore the values it can take on.

A value of type E (SumMatch a b) represents a computation within the EDSL which destructures a value of type E a and produces a value of type E b. Therefore, E (SumMatch (ERepTy t) r) represents a computation which destructures a value of type E (ERepTy t) and produces a value of type E b.

3.1 E (SumMatch a b)

The overall structure of a E (SumMatch a b) value is a (heterogeneous) list of E (ProdMatch \times b) values. Each item of this list corresponds exactly to one branch in the original case match.

The following constructors generate SumMatch-tagged values in the expression language:

```
data E t where
...
SumMatchExp ::
    (ERep a, ERep b, ERepTy b ~ b)
    => E (ProdMatch a r)
        -> E (SumMatch b r)
        -> E (SumMatch (Either a b) r)

OneSumMatch ::
    (ERep a, ERep b, ERepTy a ~ a)
    => E (ProdMatch a b)
        -> E (SumMatch a b)

EmptyMatch ::
    (ERep b) => E (SumMatch Void b)
...
```

Note the ERepTy a \sim a constraints. This constraint ensures that the type a is already in canonical form (that is, consists entirely of Either, (,) and base types).

3.2 E (ProdMatch s t)

E (ProdMatch x y) is equivalent to a curried function from x to y in the expression language. Note that s is a (potentially nested) pair type. For example, E (ProdMatch (a, (b, c)) r) is equivalent to E $(a \rightarrow E (b \rightarrow E (c \rightarrow E r)))$.

```
data E t where
```

```
ProdMatchExp ::
    (ERep a, ERep b)
    => E (a -> ProdMatch b r)
        -> E (ProdMatch (a, b) r)

NullaryMatch ::
    (ERep a)
    => E r -> E (ProdMatch a r)

OneProdMatch ::
    (ERep a)
    => E (a -> b) -> E (ProdMatch a b)
...
```

The ProdMatch type is defined similarly to the SumMatch type and is similarly used primarily as a type tag:

```
newtype ProdMatch a b =
  MkProdMatch { runProdMatch :: a -> b }
```

3.3 Connection to Church encodings

TODO: Work on this subsection. Maybe this shouldn't be a separate section at all and maybe its contents should be incorporated throughout the rest of the paper.

Algebraic datatypes can be represented as lambda calculus terms using *Church encodings*. For example, the pair constructor can be represented as

```
church_mkPair
    :: a -> b -> (a -> b -> r) -> r
church_mkPair x y = \ f -> f x y
```

Coproducts can be represented with the constructors

```
church_mkLeft
    :: a -> (a -> r) -> (b -> r) -> r
church_mkLeft x = \ f g -> f x

church_mkRight
    :: b -> (a -> r) -> (b -> r) -> r
```

```
church_mkRight y = \ f g -> g y
```

In this representation:

 A pair of type A and type B is represented with a value of type forall r. (A -> B -> r) -> r. A coproduct of type A and type B is represented with a value of type forall r. (A -> r) -> (B -> r) -> r.

Both of those representations represent the type as a function that performs the corresponding case analysis. A deep embedding of the operations churchMkPair, church_mkLeft and church_mkRight is given by the type

```
data Church r where
  ChurchPair
    :: a -> b -> (a -> b -> r) ->
        Church r

ChurchLeft
    :: a -> (a -> r) -> (b -> r) ->
        Church r

ChurchRight
    :: b -> (a -> r) -> (b -> r) ->
        Church r
```

with the evaluation function

```
churchEval :: Church r -> r
churchEval (ChurchPair x y f) = f x y
churchEval (ChurchLeft x f g) = f x
churchEval (ChurchRight y f g) = g y
```

However, we only want to keep track of the functions used for elimination. By moving the values actually being contained in the products and coproducts out to the evaluation function, we arrive at

```
data Church' t r where
  ChurchPair'
    :: (a -> b -> r) ->
        Church' (a, b) r

ChurchEither'
    :: (a -> r) -> (b -> r) ->
        Church' (Either a b) r

churchEval' :: Church' t r -> t -> r
churchEval' (ChurchPair' f) (x, y) = f x y
churchEval' (ChurchEither' f g) e =
  case e of
    Left x -> f x
    Right y -> g y
```

TODO: Figure out how recursive types fit into this framework. Church encodings can handle recursive types and so can our representation. This is also the case for Scott encodings, etc, and is the difference between Church and Scott encodings.

Does our way of handling recursive types correspond to how any of those encodings handle recursive types?

Maybe this is relevant: Generalized Church encoding is the Curry-Howard of Knaster-Tarski

3.4 An aside on ProdMatch and SumMatch values

Though ProdMatch and SumMatch are used throughout this EDSL as type tags, they do have values and they are not trivial values. The reason for this is that it connects the encoded pattern matches (values from the E) type to their semantics. A value of type E (SumMatch a b) is an expression which takes in a value of type a (embedded within the expression language), internally performs some pattern matching, and produces a value of type b (again, embedded within the expression language). This is exactly the semantics of a function from a to b. Likewise for ProdMatch a b.

Recall the previously mentioned function

```
abs :: E a -> a
```

Now consider at the type of abs when it is specialized to take E (SumMatch a b) values:

```
abs :: E (SumMatch a b) -> SumMatch a b
```

If we postcompose with runSumMatch, we get:

```
runSumMatch . abs
    :: E (SumMatch a b) -> (a -> b)
```

The SumMatch a b value which abs returns is exactly the function which pattern matches according to its input value. Likewise for ProdMatch a b values.

4 Representing tail recursion

Tail recursion is given a direct-style representation using a simple sum type, using the technique described in [Grebe et al. 2017].

Consider a tail recursive function of the type f :: a -> b. Each recursive call can be seen as a simple "update" of the values of the arguments, since these calls are all in tail position. This is why tail recursive functions can be easily compiled to simple loops or conditional jumps.

We can take advantage of this view by transforming a tail recursive function $f::a \rightarrow b$ into a function $f'::a \rightarrow b$ a. Iter b a is a type which can either correspond to an argument "update" (in the sense mentioned previously) or a final result. This type is implemented as a sum of the types a and b. Recursive calls are transformed to

Step applications and non-recursive branches are wrapped in Done applications.

```
data Iter a b = Step b | Done a
  deriving (Functor, Generic)
```

To use the new f' function, we repeatedly call it until it gives a Done value. If it gives a Step value, we pass the the value wrapped in the Step back into f' and continue.

The function runIter provides the standard semantics for executing such a function representing a tail recursive function:

```
runIter :: (ERep a, ERep b)
    => (a -> Iter b a)
        -> (a -> b)
runIter f = go
    where
        go x =
            case f x of
            Done r -> r
            Step x' -> go x'
```

TODO: runIter has the following alternate implementation. Would this be useful to use somewhere?

```
runIter f = getDone . fix (f >=>)
getDone :: Iter b a -> b
getDone (Done x) = x
getDone _ = error "getDone"
```

where Iter is given a standard Monad instance (essentially the same as the Either Monad instance).

Maybe this could be useful in some proofs or derivations somewhere (in this paper or elsewhere)? Note that error is never called under any circumstance in this implementation of runIter.

This technique can be contrasted with the more traditional trampolining technique for implementing tail recursion. Conventional trampolining uses a sum type of the result type and a thunk with the code necessary to continue execution. [Ganz et al. 1999]

In the technique presented here, we do not need to allocate thunks or closures. We actually do not to use higher-order functions at all in this tail recursion representation.

In the E type, this is used to represent tail recursion by the following constructors:

```
data E t where
   ...
   StepExp :: E b -> E (Iter a b)
   DoneExp :: E a -> E (Iter a b)
```

```
661
662
663
664
665
666
667
668
```

```
TailRec :: (ERep a, ERep b)
=> E (b -> Iter a b)
-> E (b -> a)
...
```

5 Representing lambdas

This representation of pattern matching depends on the ability to bring function values into the expression language. This is accomplished with the following constructors:

```
data E t where
...
Lam ::
    (ERep a, Typeable a)
    => Name a -> E b -> E (a -> b)

Var :: (Typeable a) => Name a -> E a
```

The Typeable constraints are necessary to lookup correctly typed values in the variable binding environment later on.

The Name t type represents a lambda variable identifier together with its type t (Note that the ScopedTypeVariables extension is enabled):

newtype Name a = Name Int

In the Core transformation, each lambda is given a Name with a globally unique Int, sidestepping any name capture issues.

-> Nothing

The following datatypes are used to represent a variable binding environment of typed names to expression language values:

```
data EnvMapping where
  (:=>) :: forall a.
   Typeable a
   => Name a -> E a -> EnvMapping
```

This type encodes a single variable binding, with values of the form n :=> v, where n is a typed name and v is the value it is bound to.

These bindings are grouped together in the Env type:

```
newtype Env = Env [EnvMapping]
emptyEnv :: Env
emptyEnv = Env []
extendEnv :: Env -> EnvMapping -> Env
extendEnv (Env maps) m = Env (m:maps)
envLookup :: Typeable a
  => Env -> Name a -> Maybe (E a)
envLookup (Env maps) = go maps
  where
    go []
                         = Nothing
    go ((n' :=> e):rest) =
      case namesEq n n' of
        Just Refl -> Just e
                  -> go rest
        Nothing
```

6 Recovering standard semantics for pattern matches

The standard semantics for the EDSL is given by abs. Two helper functions, sumMatchAbs and prodMatchAbs, are used to provide the standard semantics for matches on sum types and matches on product types, respectively. These helper functions are based on the mechanism described in section 3.4.

```
abs :: forall t. E t -> t
abs = absEnv emptyEnv

sumMatchAbs ::
   (ERepTy (ERepTy s) ~ ERepTy s, ERep s)
   => Env
      -> E (SumMatch (ERepTy s) t)
     -> s
     -> t
...

prodMatchAbs :: (ERep s)
   => Env
     -> E (ProdMatch s t)
     -> s
     -> t
```

See Appendix A for more implementation details of absEnv.

7 C Backend

TODO: Should this section be expanded?

The C backend makes use of a small EDSL for generating C code. See Appendix B for implementation details of this ESDL.

This backend is based on a globally unique name generator. Similar to SSA form, a new C variable is created for each Haskell subexpression. It differs from SSA, however, in that these variables can be assigned multiple times. In particular, a variable can be assigned in multiple branches of an if statement or inside of a while loop. This simplifies the implementation, as ϕ nodes are not needed.

The following structs provide the C representation for Haskell expressions:

```
783
     typedef enum var_type_tag {
784
       EXPR_INT
785
     , EXPR_PAIR
786
787
788
     , EXPR_UNIT
789
     } var_type_tag;
790
791
     typedef enum semantic_type_tag {
792
       NO_SEMANTIC_TAG
793
       EXPR_COMPLEX
                           // Complex numbers
794
     } semantic_type_tag;
795
     struct closure_t;
797
798
     typedef struct var_t {
799
800
       var_type_tag tag;
801
       semantic_type_tag semantic_tag;
802
       void* value;
803
     } var_t;
804
805
     typedef struct closure_t {
806
       var_t* fv_env;
807
       var_t (*fn)(var_t, struct closure_t*);
808
     } closure_t;
809
```

The semantic_tag allows type information preserved by the Typeable constraints in the EDSL to be brought over to the generated C code. In our implementation, this is used to distinguish between pairs of Doubles and Complex Double values. In the case of a Complex Double, the var_t would have a tag field with the value EXPR_PAIR and a semantic_tag field with the value EXPR_COMPLEX.

8 Core Plugin

The Core plugin translates marked expressions. Expressions are marked by the externalize function:

```
externalize :: a -> E a
```

For example, externalize x marks the expression x.

If an expression already has an EDSL type (a type of the form E a for some a), then the marking procedure ignores it and does not wrap it with externalize (see *M* in Section 8.2).

In the flowchart given in Figure 1, the names in parentheses in a node refers to the names of transformations given in the rewrite rules in Figure 2. Calls to unrep :: E a -> a are only used internally and will not exist in the final result of the transformation.

Note that:

- The tail recursion transformation given by D, T'_f and T_f is completely independent of the E type and the transformations associated to the E type. As a result, the tail recursion transformation can be used on its own
- The total number of marks introduced is upper bounded by the number of subexpressions in the original Core given to the transformation by GHC and each full transformation step (that is, *C*) eliminates one mark. Therefore, the transformation will terminate.

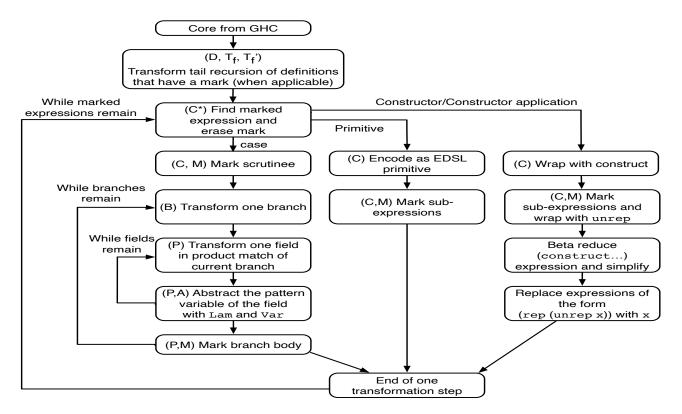


Figure 1. Control Flow of the Core Plugin

```
991
            D(f x = internalize (externalize (case s of { ... })))
992
                \Longrightarrow \begin{cases} \text{f = internalize } C^*(\text{externalize (runIter } (\lambda x \to \text{case s of } \{\ T'_{\text{f}}(\dots)\ \}))) & \text{if f occurs free in } \{\ \dots\ \} \\ \text{f x = internalize } C^*(\text{externalize (case s of } \{\ \dots\ \})) & \text{otherwise} \end{cases}
993
994
995
996
            T'_{\mathfrak{s}}(\mathsf{K} \ \mathsf{x0} \ \ldots_{U} \ \mathsf{xN} \to \mathsf{case} \ \mathsf{s} \ \mathsf{of} \ \{ \ \ldots_{V} \ \}; \ \ldots_{W})
997
                \Longrightarrow K x0 ... U xN \to T_{\rm f}({\rm case \ s \ of \ \{ \ ... \ V \ \}}); \ T_{\rm f}'(\ ... W\ )
998
            T'_{\mathfrak{f}}(\mathsf{K} \ \mathsf{x0} \ \ldots_{U} \ \mathsf{xN} \ \to \ \mathsf{body0}; \ \ldots_{V})
999
1000
                \Longrightarrow \begin{cases} \mathsf{K} \ \mathsf{x0} \ \ldots_U \ \mathsf{xN} \to \mathsf{body0}[\mathsf{f} \mapsto \mathsf{Step}]; \ T_\mathsf{f}'(\ \ldots_V\ ) & \text{if f occurs free in body0} \\ \mathsf{K} \ \mathsf{x0} \ \ldots_U \ \mathsf{xN} \to \mathsf{Done} \ \mathsf{body0}; \ T_\mathsf{f}'(\ \ldots_V\ ) & \text{otherwise} \end{cases}
1001
1002
1003
            T_{\mathfrak{s}}'(\varepsilon) \Longrightarrow \varepsilon (Note: \varepsilon represents the empty string
1004
            T_{\rm f}({\sf case \ s \ of \ \{\ \dots\ \}})
1005
                \Longrightarrow \begin{cases} \text{case s of } \{ T'_{\mathsf{f}}( \dots ) \} & \text{if f occurs free in } \{ \dots \} \\ \text{Done (case s of } \{ \dots \} ) & \text{otherwise} \end{cases}
1006
1007
           C^*(x) \Longrightarrow \begin{cases} x & \text{if x has no subexpressions marked with externalize} \\ C^*(C(y)) & \text{if externalize y is the first marked subexpression of x} \end{cases}
1009
1010
1011
1012
1013
            C(\text{runIter } x) \Longrightarrow \text{TailRec } M(x)
1014
            C(x + y) \Longrightarrow Add M(x) M(y)
1015
1016
            C(\text{case scrutinee of } \{ \dots \}) \Longrightarrow \text{CaseExp } M(\text{scrutinee}) \ B( \dots )
1017
            C(\lambda x \rightarrow body) \Longrightarrow A(\lambda x \rightarrow body)
1018
            C(K \times 0 \dots \times N) \Longrightarrow \text{construct}(K \text{ (unrep } M(\times 0)) \dots \text{ (unrep } M(\times N))) (Where K is a constructor)
1019
            C(f x) \Longrightarrow App M(f) M(x)
1020
1021
1022
            B(K \times \emptyset \dots_U \times N \to body\emptyset; \dots_V) \Longrightarrow SumMatchExp P(x\emptyset \dots_U \times N \to body\emptyset) B(\dots_V)
1023
            B(K \times \emptyset \dots \times N \to body) \Longrightarrow OneSumMatchExp P(x \emptyset \dots \times N \to body)
1024
            B(\varepsilon) \Longrightarrow \mathsf{EmptyMatch}
1025
1026
1027
            P(x0 x1 ... xN \rightarrow body) \Longrightarrow ProdMatchExp A(\lambda x0 \rightarrow P(x1 ... xN \rightarrow body))
1028
            P(x \rightarrow body) \Longrightarrow OneProdMatchExp A(\lambda x \rightarrow body)
1029
            P(\rightarrow body) \Longrightarrow NullaryMatch M(body)
1030
1031
1032
            A(\lambda(x :: a) \rightarrow body) \Longrightarrow Lam (Name @a uniq) M(body[x \mapsto unrep (Var @a uniq)])
1033
                  (where uniq is a globally unique identifier)
1034
1035
1036
1037
            M(\mathbf{x} :: \mathbf{a}) \Longrightarrow \begin{cases} \mathbf{externalize} \ \mathbf{x} & \text{if } \nexists t, a \sim E \ t \\ \mathbf{x} & \text{if } \exists t, a \sim E \ t \end{cases}
1038
1039
1040
1041
```

Figure 2. Rewrite rules

9 Related Work

TODO: Does this need more fleshing out?

A similar EDSL-oriented representation of pattern matching is given in [Atkey et al. 2009, Section 3.3]. In that paper, patterns were given their own representation which allows for compound patterns. This is useful in the context of that work, as the programmer works directly with these patterns.

In the present paper, however, the representation is generated automatically by a compiler plugin. As a result of GHC's desugared Core (which does not have compound patterns), there is no need to directly express compound patterns at the representation-level.

There is other recent work using deep embeddings in functional languages for system development. One example is the Ivory language [Elliott et al. 2015] which provides a deeply embedded DSL for use in programming high assurance systems, However, it's syntax is typical of a deep EDSL and requires additional keywords and structures above idiomatic Haskell.

The Feldspar project [Axelsson et al. 2010; Svenningsson and Axelsson 2013] is a Haskell embedding of a monadic interface that targets C, and focuses on high-performance. Both Feldspar and our work use some form of monadic reification technology [Persson et al. 2012; Sculthorpe et al. 2013; Svenningsson and Svensson 2013].

Svenningsson and Axelsson [Svenningsson and Axelsson 2013] explored combining deep and shallow embedding. They used a deep embedding as a low level language, then extended the deep embedding with a shallow embedding written on top of it. Haskell type classes were used to minimize the effort of adding new features to the language.

Yin-Yang [Jovanovic et al. 2014] provides a framework for DSL embedding in Scala which uses Scala macros to provide the translation from a shallow to deep embedding. Yin-Yang goes beyond the translation by also providing autogeneration of the deep DSL from the shallow DSL. The focus of Yin-Yang is in generalizing the shallow to deep transformations, and does not include recursive transformations.

Forge [Sujeeth et al. 2013] is a Scala based meta-EDSL framework which can generate both shallow and deep embeddings from a single EDSL specification. Embeddings generated by Forge use abstract Rep types, analogous to our EDSL's E types. Their shallow embedding is generated as a pure Scala library, while the deeply embedded version is generated as an EDSL using the Delite [Sujeeth et al. 2014] framework.

Elliott developed GHC plugins [Elliott 2015a] [Elliott 2016] for compiling Haskell to hardware [Elliott 2015b], using worker-wrapper style transformations [Gill and Hutton 2009] equivalent to the abs and rep transformations described in Section 1.2. These plugins were later generalized to enable additional interpretations [Elliott 2017].

References

Robert Atkey, Sam Lindley, and Jeremy Yallop. 2009. Unembedding Domain-Specific Languages. In Proceedings of the 2nd ACM SIGPLAN Symposium on Haskell (Edinburgh, Scotland) (Haskell '09). Association for Computing Machinery, New York, NY, USA, 37–48. https://doi.org/10.1145/1596638. 1596644

Emil Axelsson, Koen Claessen, Gergely Dévai, Zoltán Horváth, Karin Keijzer, Bo Lyckegård, Anders Persson, Mary Sheeran, Josef Svenningsson, and Andras Vajdax. 2010. Feldspar: A domain specific language for digital signal processing algorithms.. In MEMOCODE'10. 169–178.

Conal Elliott. 2015a. https://github.com/conal/lambda-ccc

Conal Elliott. 2015b. https://github.com/conal/talk-2015-haskell-to-hardware

Conal Elliott. 2016. https://github.com/conal/reification-rules

Conal Elliott. 2017. Compiling to categories. *Proc. ACM Program. Lang.* 1, ICFP, Article 48 (Sept. 2017), 24 pages. https://doi.org/10.1145/3110271

Conal Elliott. 2018. The simple essence of automatic differentiation. In *Proceedings of the ACM on Programming Languages (ICFP)*. http://conal.net/papers/essence-of-ad/

Conal Elliott. 2019. Generalized convolution and efficient language recognition (extended version). CoRR abs/1903.10677 (2019). https://arxiv.org/abs/1903.10677

Trevor Elliott, Lee Pike, Simon Winwood, Pat Hickey, James Bielman, Jamey Sharp, Eric Seidel, and John Launchbury. 2015. Guilt free ivory. In Proceedings of the 8th ACM SIGPLAN Symposium on Haskell. ACM, 189–200

Steven E. Ganz, Daniel P. Friedman, and Mitchell Wand. 1999. Trampolined Style. In Proceedings of the Fourth ACM SIGPLAN International Conference on Functional Programming (Paris, France) (ICFP '99). Association for Computing Machinery, New York, NY, USA, 18–27. https://doi.org/10. 1145/317636.317779

Andy Gill and Graham Hutton. 2009. The worker/wrapper transformation. Journal of Functional Programming 19, 2 (March 2009), 227–251.

Mark Grebe, David Young, and Andy Gill. 2017. Rewriting a Shallow DSL Using a GHC Compiler Extension. In *Proceedings of the 16th ACM SIG-PLAN International Conference on Generative Programming: Concepts and Experiences* (Vancouver, BC, Canada) (*GPCE 2017*). ACM, New York, NY, USA, 246–258. https://doi.org/10.1145/3136040.3136048

Vojin Jovanovic, Amir Shaikhha, Sandro Stucki, Vladimir Nikolaev, Christoph Koch, and Martin Odersky. 2014. Yin-Yang: Concealing the Deep Embedding of DSLs. In Proceedings of the 2014 International Conference on Generative Programming: Concepts and Experiences (Västerås, Sweden) (GPCE 2014). Association for Computing Machinery, New York, NY, USA, 73–82. https://doi.org/10.1145/2658761.2658771

Anders Persson, Emil Axelsson, and Josef Svenningsson. 2012. Generic Monadic Constructs for Embedded Languages. In *Implementation and Application of Functional Languages*, Andy Gill and Jurriaan Hage (Eds.). Lecture Notes in Computer Science, Vol. 7257. Springer Berlin Heidelberg, 85–99.

Neil Sculthorpe, Jan Bracker, George Giorgidze, and Andy Gill. 2013. The Constrained-Monad Problem. In *Proceedings of the 18th ACM SIG-PLAN International Conference on Functional Programming* (Boston, Massachusetts). ACM, 287–298. http://dl.acm.org/citation.cfm?doid=2500365.2500602

Arvind K Sujeeth, Kevin J Brown, Hyoukjoong Lee, Tiark Rompf, Hassan Chafi, Martin Odersky, and Kunle Olukotun. 2014. Delite: A compiler architecture for performance-oriented embedded domain-specific languages. ACM Transactions on Embedded Computing Systems (TECS) 13, 4s (2014), 1–25.

```
1211
     Arvind K. Sujeeth, Austin Gibbons, Kevin J. Brown, HyoukJoong Lee, Tiark
                                                                                                                      1266
       Rompf, Martin Odersky, and Kunle Olukotun. 2013. Forge: Generat-
1212
                                                                                                                      1267
                                                              absEnv env (LeftExp x) =
       ing a High Performance DSL Implementation from a Declarative Spec-
1213
                                                                                                                      1268
                                                                 Left (absEnv env x)
       ification. In Proceedings of the 12th International Conference on Gen-
1214
                                                                                                                      1269
       erative Programming: Concepts & Experiences (Indianapolis, Indi-
1215
                                                                                                                      1270
       ana, USA) (GPCE '13). ACM, New York, NY, USA, 145-154. https:
                                                              absEnv env (RightExp y) =
1216
       //doi.org/10.1145/2517208.2517220
                                                                                                                      1271
                                                                 Right (absEnv env y)
     Josef Svenningsson and Emil Axelsson. 2013. Combining deep and shallow
1217
                                                                                                                      1272
       embedding for EDSL. In Trends in Functional Programming. Springer,
1218
                                                                                                                      1273
                                                              absEnv env (PairExp x y) =
1219
                                                                                                                      1274
     Josef David Svenningsson and Bo Joel Svensson. 2013. Simple and com-
                                                                 (absEnv env x, absEnv env y)
1220
                                                                                                                      1275
       positional reification of monadic embedded languages. In Proceedings
1221
                                                                                                                      1276
       of the 18th International Conference on Functional Programming. ACM,
                                                              absEnv env (ConstructRep x) =
       299-304.
1222
                                                                                                                      1277
                                                                 unrep' (absEnv env x)
                                                                                                                      1278
1224
     A Additional Code for Standard Haskell
                                                                                                                      1279
1225
                                                                                                                      1280
          Semantics Implementation
                                                              . . .
1226
                                                                                                                      1281
                                                              B A small EDSL for C code generation used
                                                                                                                      1282
1227
     absEnv :: forall t. Env -> E t -> t
1228
                                                                                                                      1283
     absEnv env (CaseExp x f) =
                                                                  internally by the C backend
1229
                                                                                                                      1284
        sumMatchAbs f (absEnv env x)
1230
                                                                                                                      1285
                                                              type CCode = String
1231
                                                                                                                      1286
                                                              type CName = String
     absEnv env (TailRec f) = \ x \rightarrow
1232
                                                                                                                      1287
        case absEnv env f x of
1233
                                                                                                                      1288
           Step x' -> absEnv env (TailRec f) x'
                                                              stmt :: CCode -> CCode
                                                                                                                      1289
          Done r -> r
                                                              stmt = (<> ";")
1235
                                                                                                                      1290
1236
                                                                                                                      1291
                                                              cCall :: CName -> [CCode] -> CCode
     absEnv env (Var v) =
1237
                                                                                                                      1292
                                                              cCall fnName args =
1238
        case envLookup env v of
                                                                                                                      1293
                                                                 fnName <> "(" <> intercalate ", " args <>
                                                                                                                      1294) "
1239
           Just x -> absEnv env
1240
          Nothing ->
1241
                                                              derefPtr :: CCode -> CCode
                                                                                                                      1296
             error
                                                                                                                      1297
                                                              derefPtr x = "*(" <> x <> ")"
                ("No_binding_for_name_"
1243
                                                                                                                      1298
                  ++ show v)
1244
                                                                                                                      1299
                                                              cCast :: CCode -> CCode -> CCode
1245
                                                                                                                      1300
                                                              cCast toType x =
     absEnv env (Lam (name :: Name a)
1246
                                                                                                                      1301
                                                                 "((" <> toType <> ")" <> x <> ")"
                          (body :: E b)) =
1247
                                                                                                                      1302
        \ (arg :: a) ->
1248
                                                                                                                      1303
           let go :: forall x. E x -> E x
                                                              cIndex :: CCode -> Int -> CCode
1249
                                                                                                                      1304
                                                              cIndex x i = "(" <> x <> ")[" <> show i <>
                go expr@(Var name2 :: E a') =
                                                                                                                      1305
1250
                  case namesEq name name2 of
                                                              (!) :: CCode -> Int -> CCode
1252
                     Just Refl -> rep arg
                                                                                                                      1307
                                                              (!) = cIndex
                                                                                                                      1308
1254
                                                                                                                      1309
                       case envLookup env name2 of
1255
                                                                                                                      1310
                                                              (=:) :: CCode -> CCode
                          Just v -> v
1256
                                                                                                                      1311
                          Nothing -> expr
                                                              x =: y = stmt (x <> "_=_" <> y)
                                                                                                                      1312
1258
                                                                                                                      1313
                -- [... traverse rest of expression cDecl :: CName -> CName -> CCode
                                                                                                                      1314
1259
                                                              cDecl cType v = stmt (cType <> "_" <> v)
                          in go ...]
                                                                                                                      1315
1260
           in
                                                                                                                      1316
1261
           absEnv (extendEnv env
                                                              (#) :: CCode -> CName -> CCode
                                                                                                                      1317
1262
                                                              x # fieldName = x <> "." <> fieldName
                                  (name :=> rep arg))
1263
                                                                                                                      1318
                    (go body)
1264
                                                                                                                      1319
1265
                                                                                                                      1320
                                                           12
```

On Adding Pattern Matching to Haskell-based Deeply Embedded Domain Specific Languages GPCE '20, November 15 - 20, 2020, Chicago, Illinois, United States Not For Distribution

```
1322
      macroDef :: CName -> [CName] -> [CCode] -> CCode
                                                                                                                                             1376
1323
                                                                                                                                             1377
      macroDef name args theLines =
1324
                                                                                                                                             1378
          unlines
1325
                                                                                                                                             1379
             [ "#define_" <> name
1326
                                                                                                                                             1380
                            <> "(" <>
1327
                                                                                                                                             1381
                               intercalate ", " args
1328
                                                                                                                                             1382
                            <> ")\\"
1329
                                                                                                                                             1383
             , "__do_{\\"
1330
             , unlines
1331
                                                                                                                                             1385
                   . map ("___"++)
1332
                                                                                                                                             1386
1333
                   . map (++"\\")
                                                                                                                                             1387
1334
                   $ theLines
                                                                                                                                             1388
             , "__}_while_(0);"
1335
                                                                                                                                             1389
1336
                                                                                                                                             1390
1337
                                                                                                                                             1391
1338
                                                                                                                                             1392
1339
                                                                                                                                             1393
1340
                                                                                                                                             1394
1341
                                                                                                                                             1395
1342
                                                                                                                                             1396
1343
                                                                                                                                             1397
1344
                                                                                                                                             1398
1345
1346
                                                                                                                                             1400
1347
                                                                                                                                             1401
1348
                                                                                                                                             1402
1349
                                                                                                                                             1403
1350
                                                                                                                                             1404
1351
                                                                                                                                             1405
1352
                                                                                                                                             1406
1353
                                                                                                                                             1407
1354
                                                                                                                                             1408
1355
                                                                                                                                             1409
1356
                                                                                                                                             1410
1357
                                                                                                                                             1411
1358
                                                                                                                                             1412
1359
                                                                                                                                             1413
1360
                                                                                                                                             1414
                                                                                                                                             1415
1362
                                                                                                                                             1416
1363
                                                                                                                                             1417
1364
                                                                                                                                             1418
1365
                                                                                                                                             1419
1366
                                                                                                                                             1420
1367
                                                                                                                                             1421
1368
                                                                                                                                             1422
1369
                                                                                                                                             1423
1370
                                                                                                                                             1424
1371
                                                                                                                                             1425
1372
                                                                                                                                             1426
1373
                                                                                                                                             1427
1374
                                                                                                                                             1428
1375
                                                                                                                                             1429
                                                                                                                                             1430
```