

# Lecture «Robot Dynamics»: Legged Robots

151-0851-00 V

lecture: CAB G11

Tuesday 10:15 – 12:00, every week

exercise: **HG E1.2**

Wednesday 8:15 – 10:00, according to schedule (about every 2nd week)

office hour: LEE H303

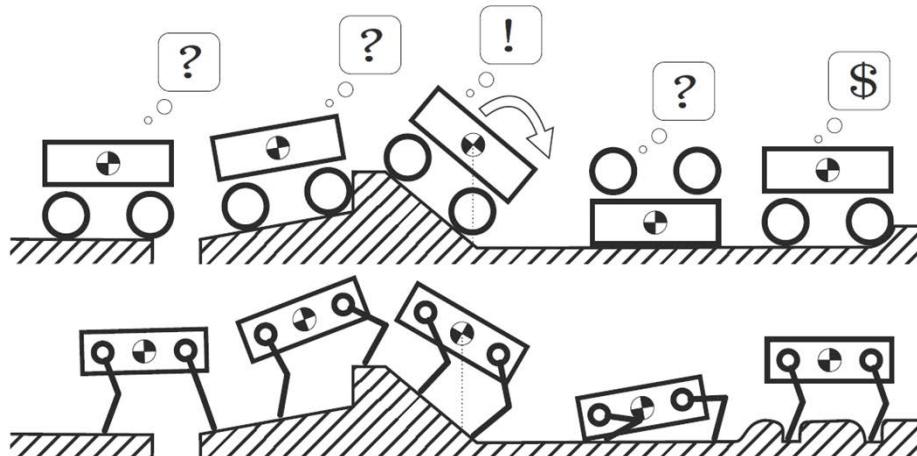
Friday 12.15 – 13.00

Marco Hutter, Roland Siegwart, and Thomas Stastny

	<b>Topic</b>		<b>Title</b>
20.09.2016	Intro and Outline	L1	Course Introduction; Recapitulation Position, Linear Velocity, Transformation
27.09.2016	Kinematics 1	L2	Rotation Representation; Introduction to Multi-body Kinematics
28.09.2016	Exercise 1a	E1a	Kinematics Modeling the ABB arm
04.10.2016	Kinematics 2	L3	Kinematics of Systems of Bodies; Jacobians
05.10.2016	Exercise 1b	L3	Differential Kinematics and Jacobians of the ABB Arm
11.10.2016	Kinematics 3	L4	Kinematic Control Methods: Inverse Differential Kinematics, Inverse Kinematics; Rotation Error; Multi-task Control
12.10.2016	Exercise 1c	E1b	Kinematic Control of the ABB Arm
18.10.2016	Dynamics L1	L5	Multi-body Dynamics
19.10.2016	Exercise 2a	E2a	Dynamic Modeling of the ABB Arm
25.10.2016	Dynamics L2	L6	Dynamic Model Based Control Methods
26.10.2016	Exercise 2b	E2b	Dynamic Control Methods Applied to the ABB arm
01.11.2016	Legged Robots	L7	Case Study and Application of Control Methods
08.11.2016	Rotorcraft 1	L8	Dynamic Modeling of Rotorcraft I
15.11.2016	Rotorcraft 2	L9	Dynamic Modeling of Rotorcraft II & Control
16.11.2016	Exercise 3	E3	Modeling and Control of Multicopter
22.11.2016	Case Studies 2	L10	Rotor Craft Case Study
29.11.2016	Fixed-wing 1	L11	Flight Dynamics; Basics of Aerodynamics; Modeling of Fixed-wing Aircraft
30.11.2016	Exercise 4	E4	Aircraft Aerodynamics / Flight performance / Model derivation
06.12.2016	Fixed-wing 2	L12	Stability, Control and Derivation of a Dynamic Model
07.12.2016	Exercise 5	E5	Fixed-wing Control and Simulation
13.12.2016	Case Studies 3	L13	Fixed-wing Case Study
20.12.2016	Summery and Outlook	L14	Summery; Wrap-up; Exam

# Why legged robots?

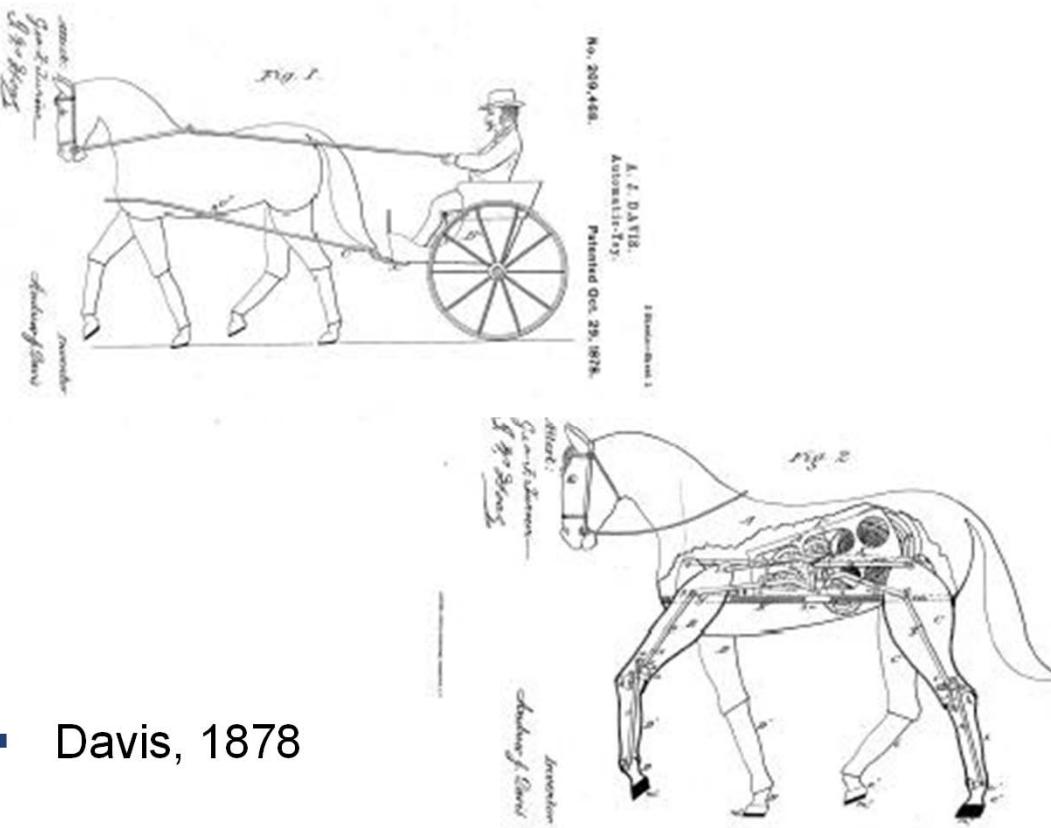
- Legged systems can overcome many obstacles



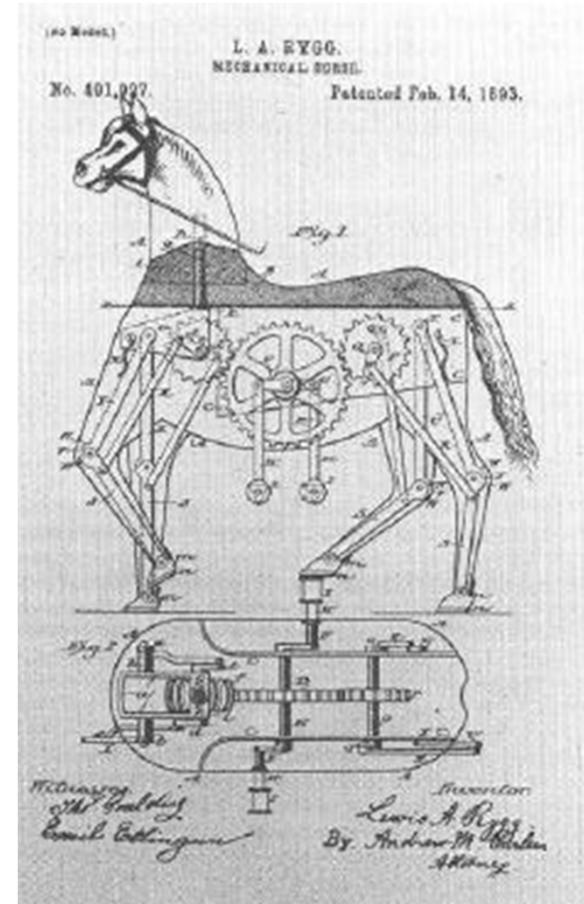
- But it is quite hard to achieve this since
  - many DOFs must be **controlled** in a coordinated way
  - the robot must **interact** with (uncertain) terrain

# History of Legged Robotics

## Walking Mechanism – First patents

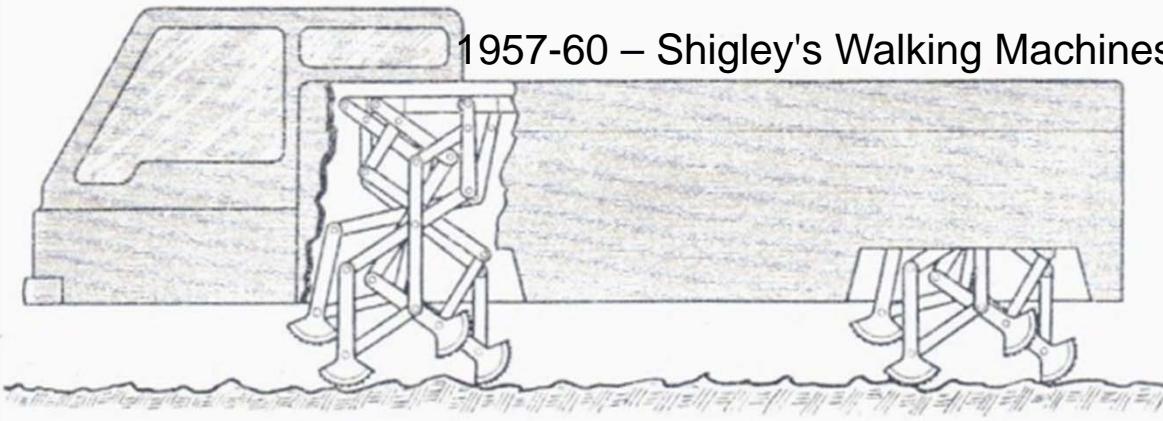


- Davis, 1878



Rygg, 1893

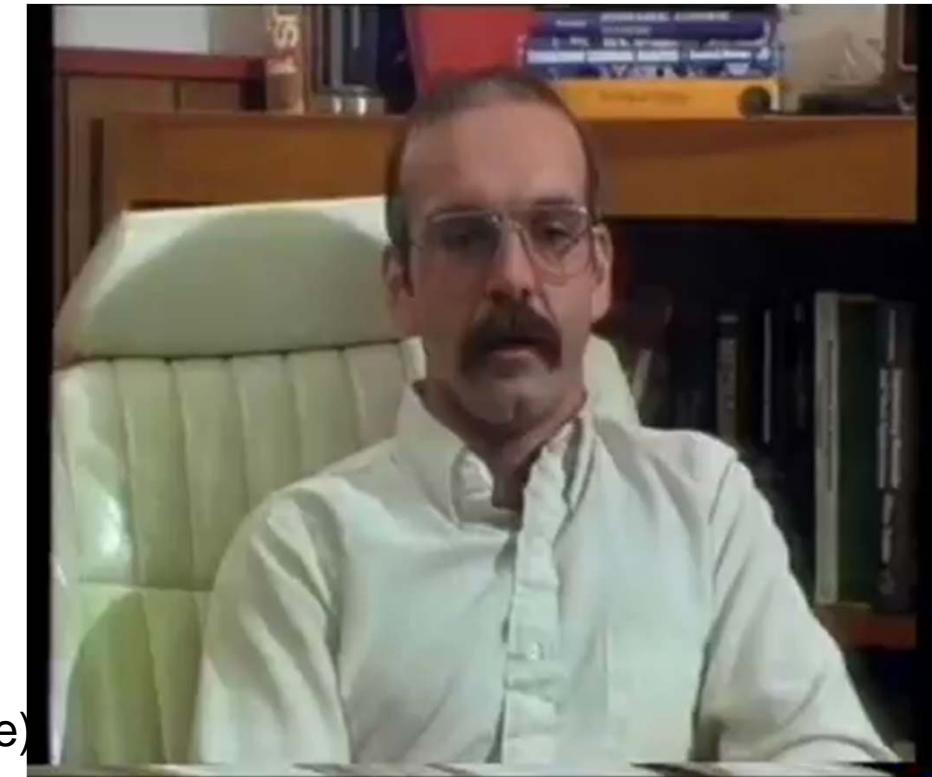
# Walking Mechanisms



1957-60 – Shigley's Walking Machines



1984 - OSU ASV  
(Adaptive Suspension Vehicle)



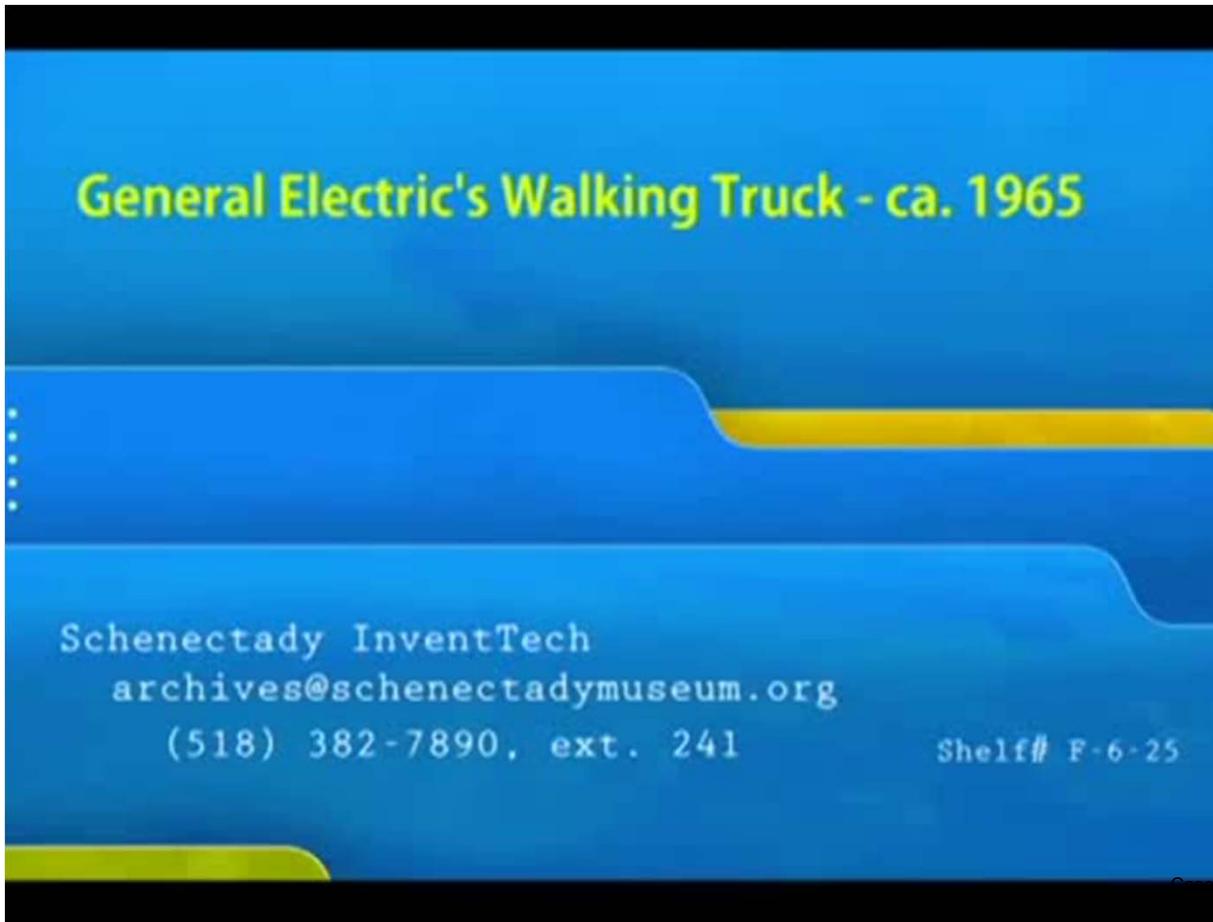
# Walking Mechanism

## Theo Jansen



# History of Legged Robotics

GE Walking Truck – human controlled 4-ped



# Large Scale Legged Locomotion and Manipulation

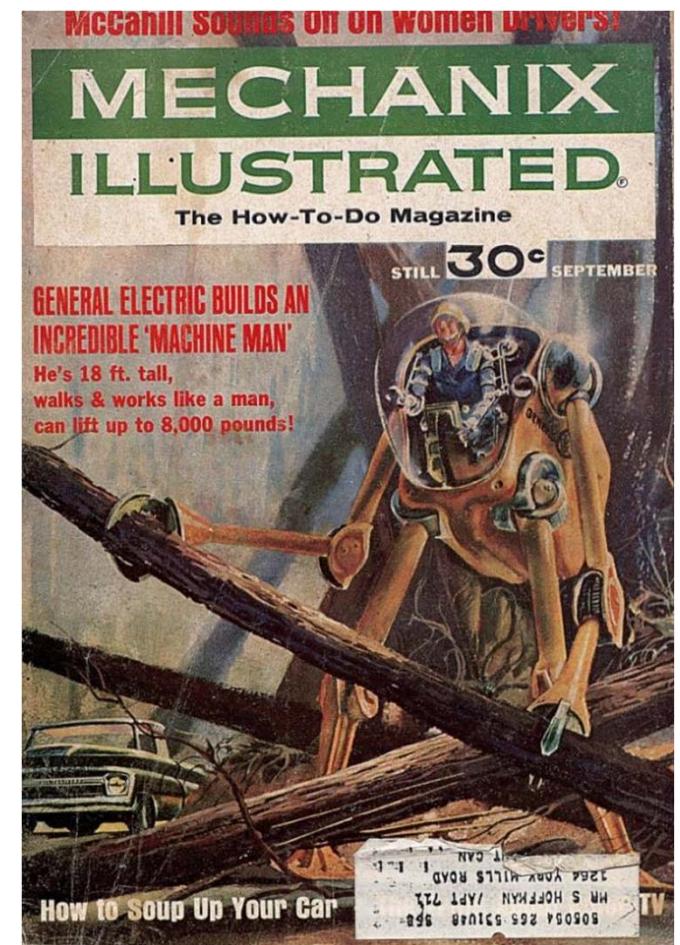
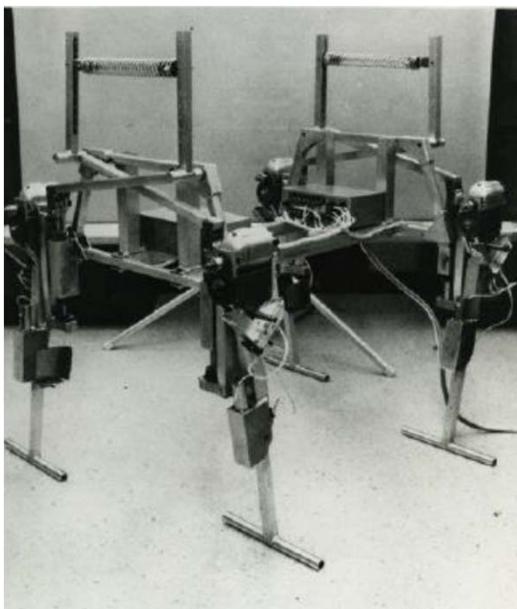
Youtube:  
menzi muck extreme



# History of Legged Robotics

Phony Pony, GE Hardiman and many more...

- More on <http://cyberneticzoo.com/>
  - steam-actuated humans
  - mechanical elephants
  - ...



# History of Legged Robotics

## Humanoid robots after 2000

- Honda Asimo



- Toyota Humanoid



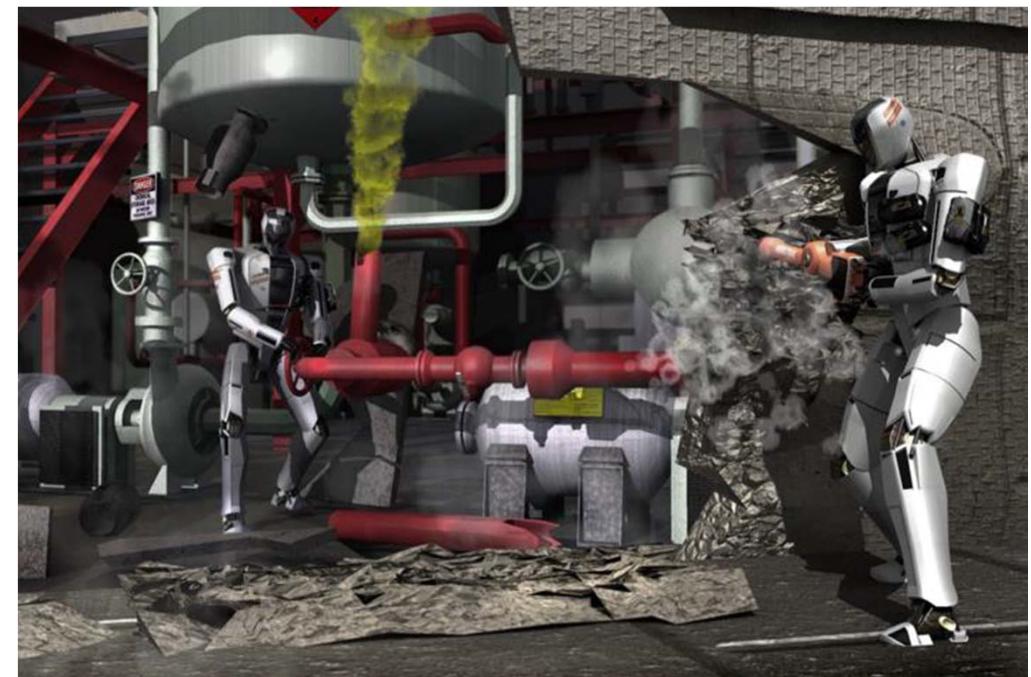
# History of Legged Robotics

## Humanoid robots after 2000

- Fukushima 2011



- DARPA Robotics Challenge 2012



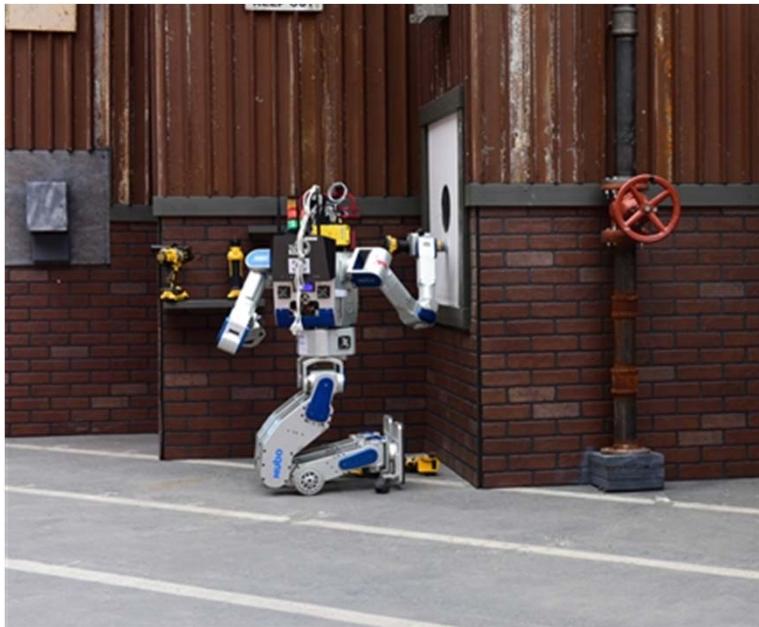
# Legged Robotics

Where are we really and what are the challenges?

# DARPA Robotics Challenge

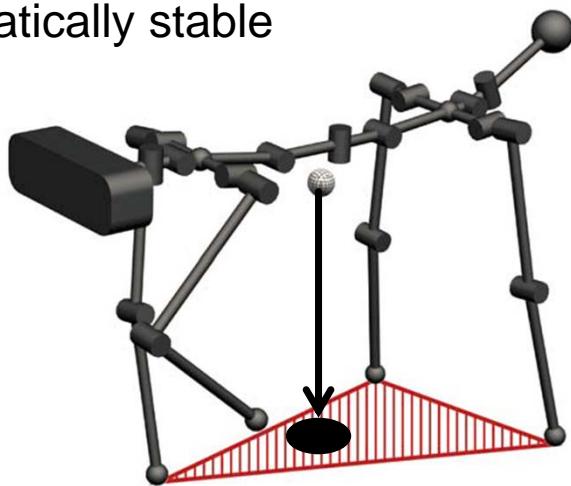
... and a thing we learned after the DRC Finals

- Walking is still difficult



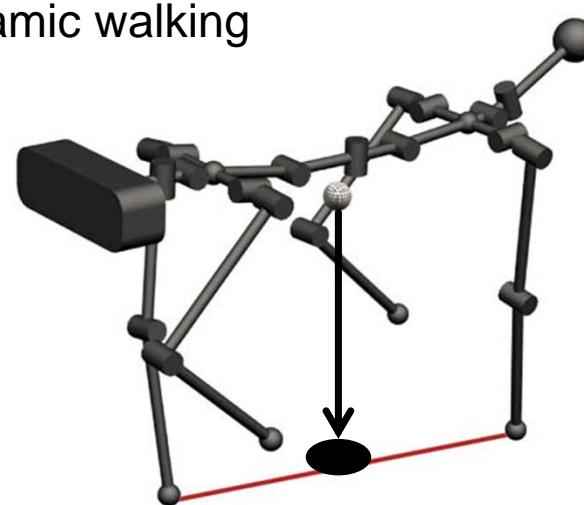
## Static vs. Dynamic Stability

- Statically stable



- Bodyweight supported by at least three legs
- Even if all joints 'freeze' instantaneously, the robot will not fall
- Safe, slow and inefficient

- Dynamic walking

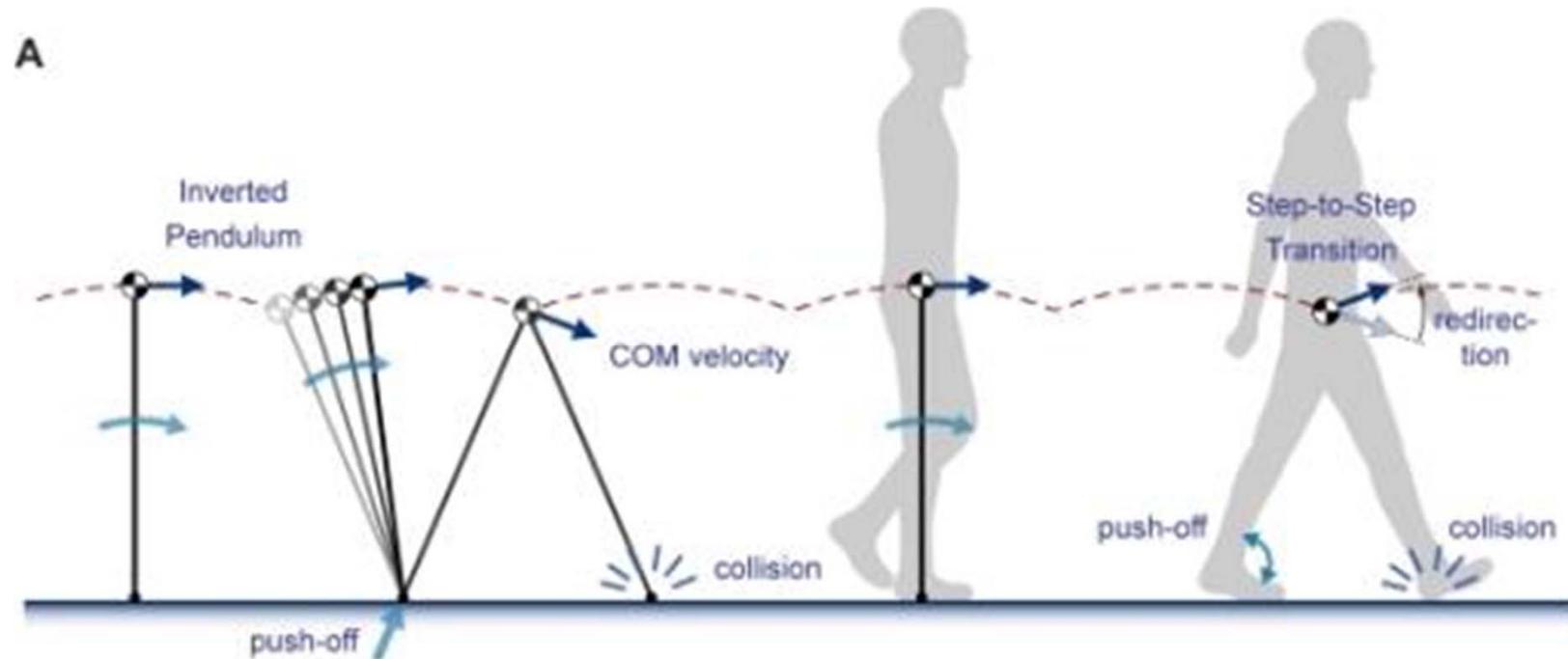


- The robot will fall if not continuously moving
- Less than three legs can be in ground contact
- fast, efficient and demanding for actuation and control

# Static walking principles

## Inverted Pendulum

- Static walking can be represented by inverted pendulum



# Static walking principles

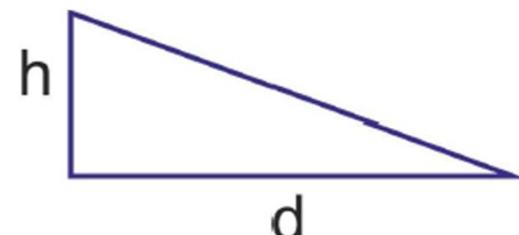
## Inverted Pendulum

- Static walking can be represented by inverted pendulum
- Exploit this in so-called passive dynamic walkers



Energetically very efficient

$$COT = \frac{E_{used}}{m \cdot g \cdot d} = \frac{m \cdot g \cdot h}{m \cdot g \cdot d} = \frac{h}{d}$$



# Static walking principles

## Inverted Pendulum

- Static walking can be represented by inverted pendulum
- Exploit this in so-called passive dynamic walkers
- Add small actuation to walk on flat ground



### Cornell Ranger

Total distance: 65.24 km  
Total time: 30:49:02  
Power: 16.0 W  
COT: 0.28

# Dynamic locomotion

## Leg Structure

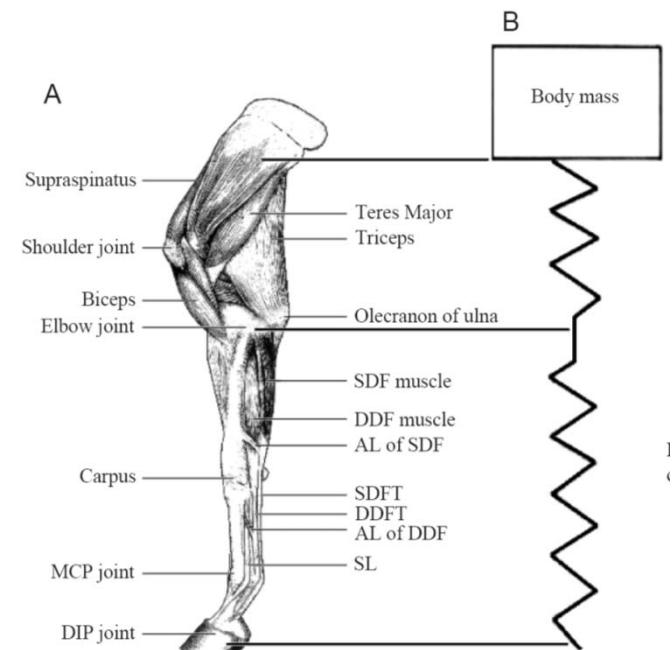


# Dynamic locomotion

## Leg Structure

- Leg during running is NOT and inverted pendulum
- Spring loaded inverted pendulum (SLIP)
  - are robust against collisions
  - can better handle uncertainties
  - can temporarily store energy
  - reduce peak power

[Alexander 1988, 1990, 2002, 2003]

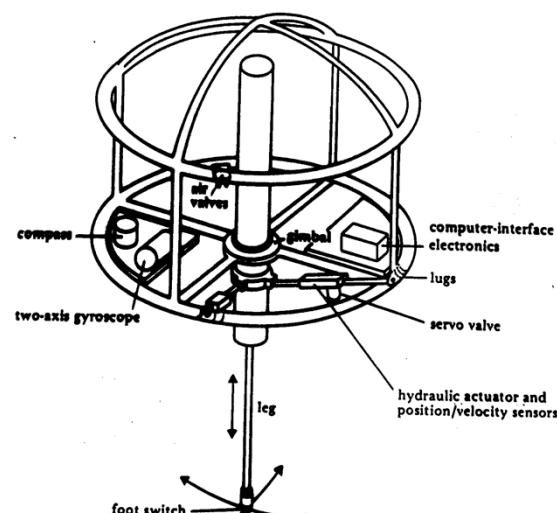
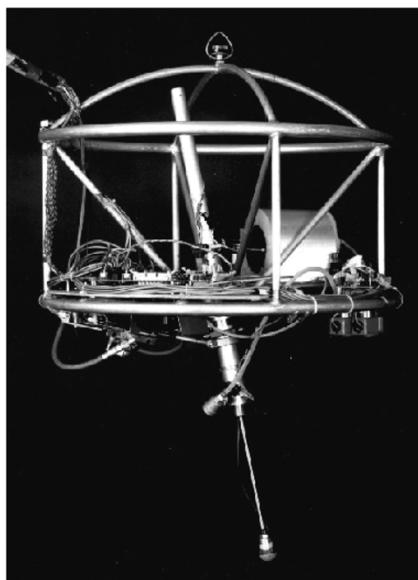


McGuigan & Wilson, 2003 – *J. Exp. Bio.*

# Dynamic Locomotion

## SLIP principles in robotics

- Early Raibert hoppers (MIT leg lab) [1983]
  - Pneumatic piston
  - Hydraulic leg “angle” orientation



# From Raibert Hopper to Humanoids and Quadrupeds

## MIT and CMU Leg Lab (1980ies)

The Leg Laboratory

Robotics Institute

Carnegie-Mellon University



Marc Raibert, Gill Pratt, Jerry Pratt, Hugh Herr, Russ Tedrake, Jessica Hodgins, Martin Bühler,...

# From Raibert Hopper to Humanoids and Quadrupeds

## Boston Dynamics

- Founded 1992
- Big Dog V1 (2005), Big Dog V2 (2008)



By JONATHAN BERR / MONEYWATCH / December 16, 2013, 1:18 PM

## Google buys 8 robotics companies in 6 months: Why?

4 Comments / 224 Shares / 91 Tweets / Stumble / @ Email More +

Google's (GOOG) acquisition of military robotics maker Boston Dynamics has certainly gotten tongues wagging but has left one key question unanswered: Why? Media reports about the deal didn't provide much insight other than to note that Boston Dynamics makes cool stuff. The search engine giant has named Andy Rubin, who oversaw the development of the Android operating system, to head its robotics endeavors, which the company has without irony called a "moonshot." A spokesman for Google confirmed the acquisition but declined to answer any questions.

The deal is also the clearest indication yet that Google is intent on building a new class of autonomous systems that might do anything from warehouse work to package delivery and even elder care," according to the New York Times.

Google, which has a market capitalization topping \$357 billion, probably didn't break a sweat buying Boston Dynamics, which is based in the Boston suburb of Waltham, or the seven other robotics companies it has acquired in the past six months. The company has been making a splash with its robotics research for a while. It has been testing driverless cars since 2010 and according to its research



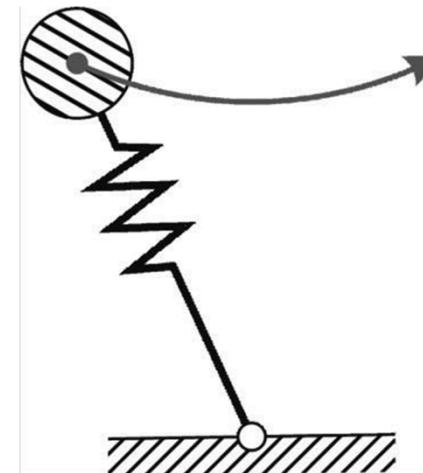
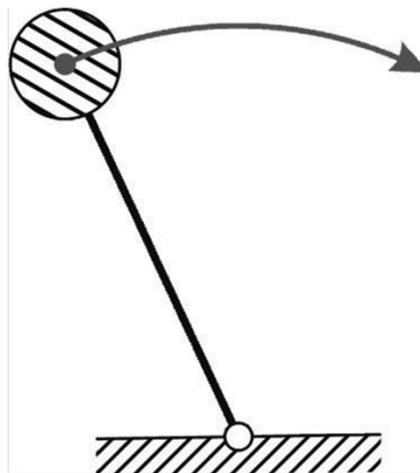


Boston Dynamics

# Understanding Locomotion

## Summary

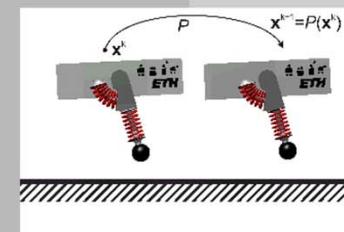
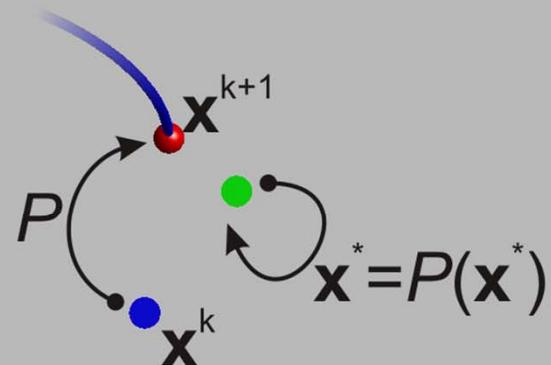
- Static locomotion (IP)       $\Leftrightarrow$       Dynamic Locomotion (SLIP)



- How to determine stability?
- How to control (actively stabilize)?

# Analyzing Stability through Limit Cycles

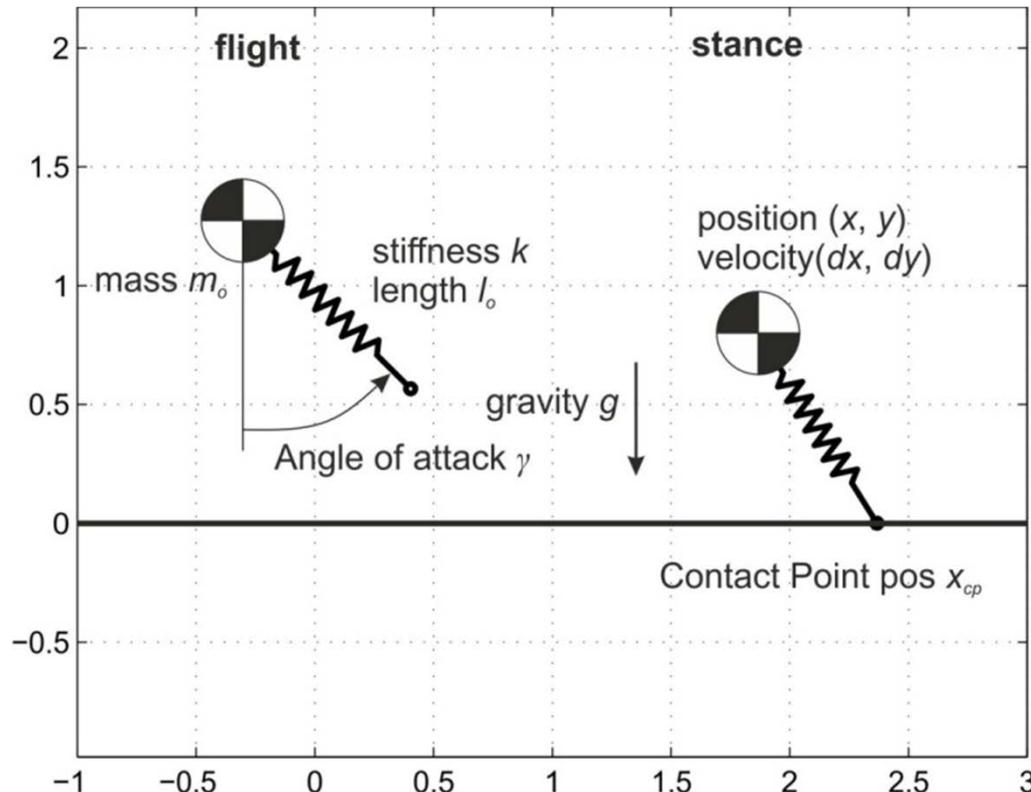
- Poincaré Map  $\mathbf{x}_{k+1} = P(\mathbf{x}_k)$
- Fix-Point  $\mathbf{x}^* = P(\mathbf{x}^*)$
- Linearization of mapping  $\Delta\mathbf{x}_{k+1} = \frac{\partial P}{\partial \mathbf{x}} \Delta\mathbf{x}_k = \Phi \Delta\mathbf{x}_k$
- The system is stable iff:  $\lambda_i(\Phi) < 1$



[C. David Remy, 2011]

# Dynamic Locomotion

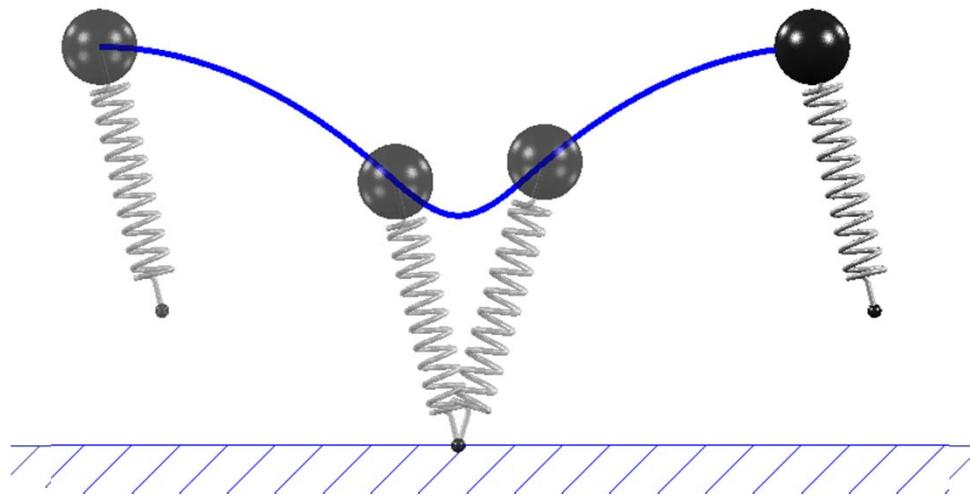
## Stability Analysis



- Point mass:  $\mathbf{q} = \begin{bmatrix} x \\ y \end{bmatrix}$
  - Equation of Motion:
    - flight
$$\ddot{\mathbf{q}} = \begin{bmatrix} \ddot{x} \\ \ddot{y} \end{bmatrix} = \begin{bmatrix} 0 \\ -g \end{bmatrix}$$
  - stance
- $$\ddot{\mathbf{q}} = \begin{bmatrix} \ddot{x} \\ \ddot{y} \end{bmatrix} = \begin{bmatrix} \frac{-F_{spring}^x}{m_o} \\ \frac{F_{spring}^y}{m_o} - g \end{bmatrix}$$
- $F_{spring} = f(\gamma, k, l)$

# Stability of Locomotion

## Limit Cycle Analysis



- Point mass:  $\mathbf{q} = \begin{bmatrix} x \\ y \end{bmatrix}$

- Equation of Motion:
  - flight

$$\ddot{\mathbf{q}} = \begin{bmatrix} \ddot{x} \\ \ddot{y} \end{bmatrix} = \begin{bmatrix} 0 \\ -g \end{bmatrix}$$

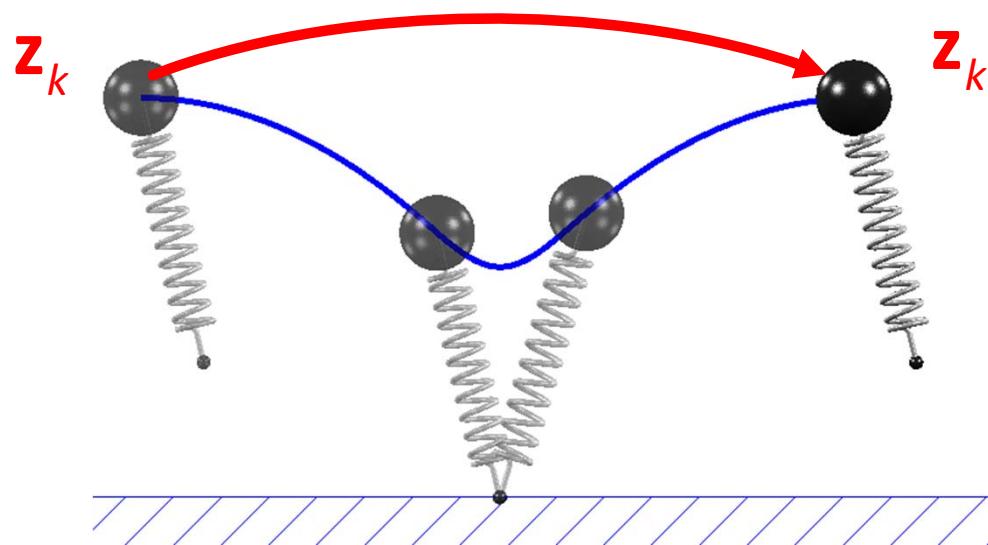
- stance

$$\ddot{\mathbf{q}} = \begin{bmatrix} \ddot{x} \\ \ddot{y} \end{bmatrix} = \begin{bmatrix} \frac{-F_{spring}^x}{m_o} \\ \frac{F_{spring}^y}{m_o} - g \end{bmatrix}$$

$$\mathbf{F}_{spring} = f(\gamma, k, l)$$

# Stability of Locomotion

## Limit Cycle Analysis



- Point mass:  $\mathbf{q} = \begin{bmatrix} x \\ y \end{bmatrix}$
- System state  
$$\mathbf{z} = \begin{bmatrix} x \\ y \\ \dot{x} \\ \dot{y} \end{bmatrix} \xrightarrow{\text{analysis at apex}} \mathbf{z} = \begin{bmatrix} y \\ \dot{x} \end{bmatrix}$$
- How does the state propagate from one apex to the next?

# Stability of Locomotion

## Limit Cycle Analysis

- Given the Poincaré mapping from one apex to the next

$$\mathbf{z}_{k+1} = P(\mathbf{z}_k)$$

- P includes differential equations that cannot be analytically solved!

- Analyze periodic stability of a fixed point

$$\mathbf{z}^* = P(\mathbf{z}^*)$$

- How can we do this? Linearization...

$$\mathbf{z}_{k+1} = \mathbf{z}^* + \Delta\mathbf{z}_{k+1} = P(\mathbf{z}^* + \Delta\mathbf{z}_k) = \underbrace{P(\mathbf{z}^*)}_{\mathbf{z}^*} + \frac{\partial P}{\partial \mathbf{x}} \Big|_{\mathbf{x}=\mathbf{x}^*} \cdot \Delta\mathbf{z}_k + \frac{\partial^2 P}{\partial \mathbf{x}^2} \Big|_{\mathbf{x}=\mathbf{x}^*} \cdot \Delta\mathbf{z}_k^2 + \dots \approx 0$$

$$\Delta\mathbf{z}_{k+1} = \frac{\partial P}{\partial \mathbf{z}} \Delta\mathbf{z}_k = \Phi \Delta\mathbf{z}_k$$

?

# Stability of Locomotion

## Numerical Limit Cycle Analysis

- Find the linearization of the Poincaré map around fix-point

$$\begin{bmatrix} \Delta y_{k+1} \\ \Delta \dot{x}_{k+1} \end{bmatrix} = \frac{\partial P}{\partial \mathbf{x}} \Big|_{\mathbf{x}=\mathbf{x}^*} \cdot \begin{bmatrix} \Delta y_k \\ \Delta \dot{x}_k \end{bmatrix}$$

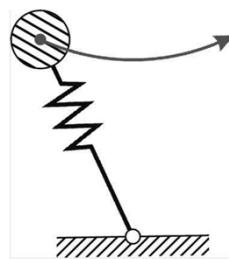
- Choose  $\Delta \mathbf{z}_k = \begin{bmatrix} \Delta y_k \\ \Delta \dot{x}_k \end{bmatrix} = \begin{bmatrix} 1 \\ 0 \end{bmatrix} h$ , with a small  $h$
- Simulate until the next apex, starting from
- Calculate  $\frac{\partial P}{\partial \mathbf{x}} \Big|_{\mathbf{x}=\mathbf{x}^*} = \begin{bmatrix} \frac{y_{k+1} - y^*}{h} & * \\ \frac{\dot{x}_{k+1} - \dot{x}^*}{h} & * \end{bmatrix}$
- Do the same thing for  $\Delta \mathbf{z}_k = \begin{bmatrix} \Delta y_k \\ \Delta \dot{x}_k \end{bmatrix} = \begin{bmatrix} 0 \\ 1 \end{bmatrix} h$

$$\begin{bmatrix} y_{k+1} \\ \dot{x}_{k+1} \end{bmatrix} = P \left( \mathbf{z}^* + \begin{bmatrix} 1 \\ 0 \end{bmatrix} h \right)$$

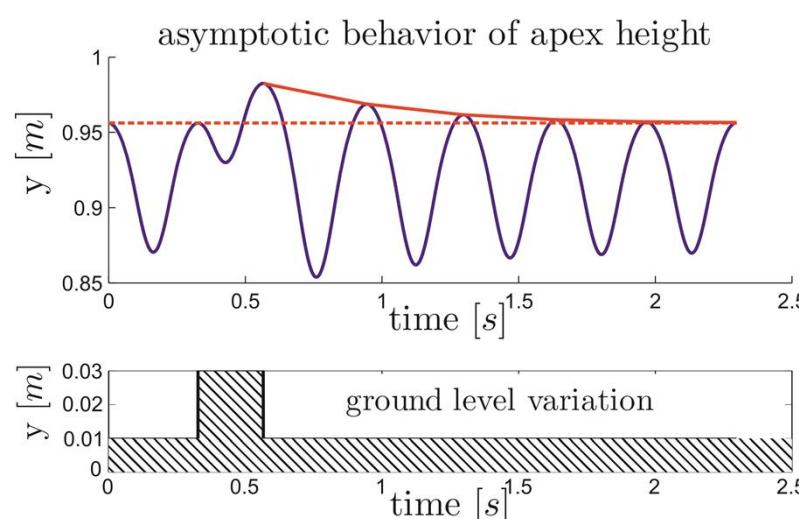
# Stability of Locomotion

## Numerical Limit Cycle Analysis

- The previous evaluation results in a 2x2 matrix
- Eigenvalue analysis:
  - System is energy conservative:  $\lambda_1 = 1$
  - System can be
    - stable  $|\lambda_2| < 1$
    - unstable:  $|\lambda_2| > 1$



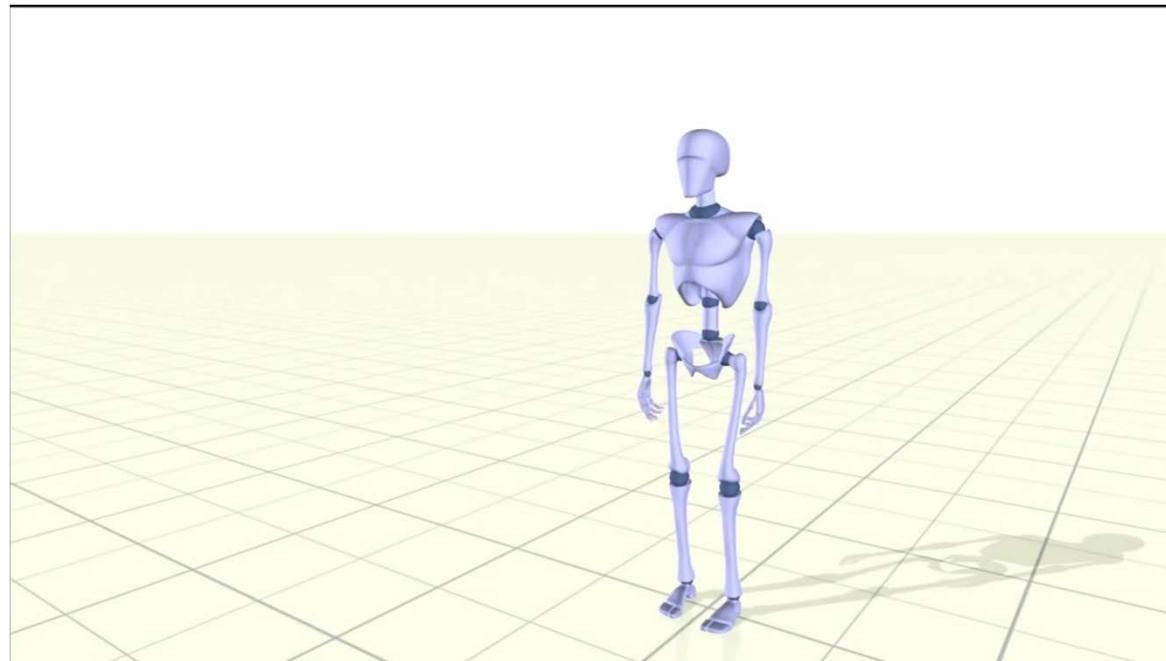
$$\left. \frac{\partial P}{\partial \mathbf{x}} \right|_{\mathbf{x}=\mathbf{x}^*}$$



# Stability and Control of Locomotion

## Example of a biped

- External disturbances lead to instability

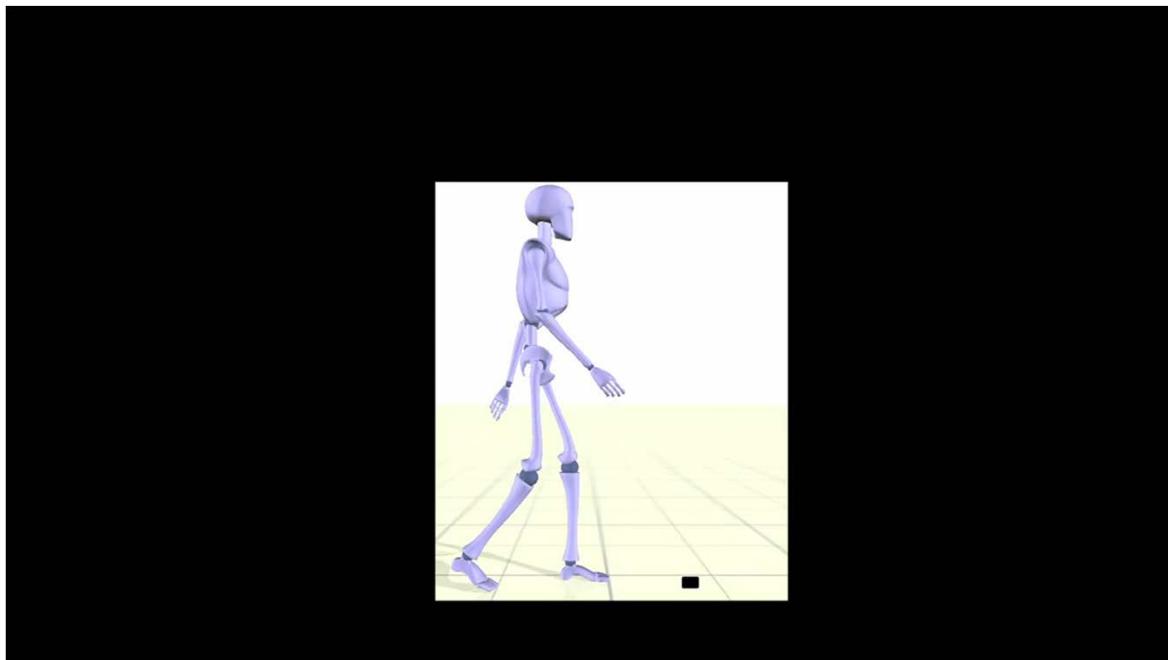


[Coros 2012]

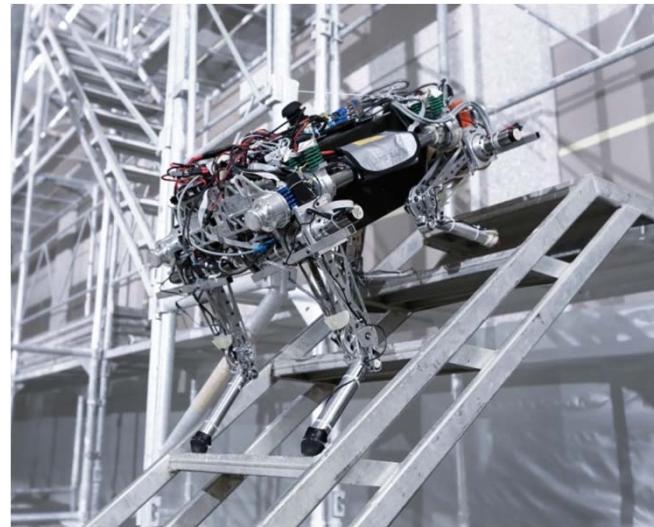
# Stability and Control of Locomotion

## Example of a biped

- External disturbances lead to instability
- Foot step control for fall recovery



[Coros 2012]



# Legged Robots for Challenging Environments

**Marco Hutter**

Robotic Systems Lab, ETH Zurich

28.10.2016

# Legged Robots for Challenging Environments

- Macerata, 2 days ago



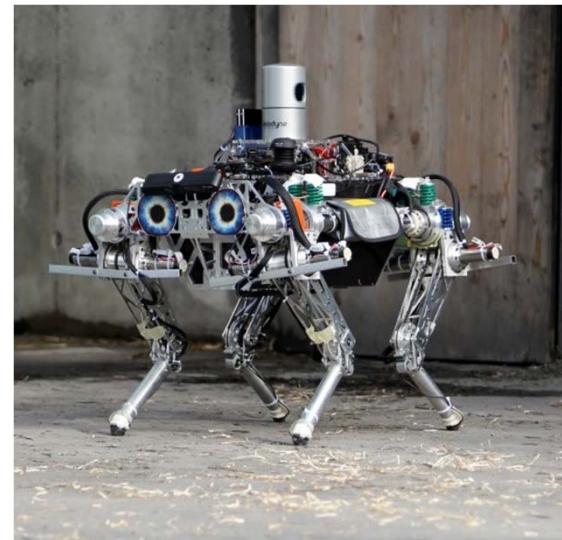
# Legged Robotics Research at ETH

2009



ALoF

2012



StarlETH

2015

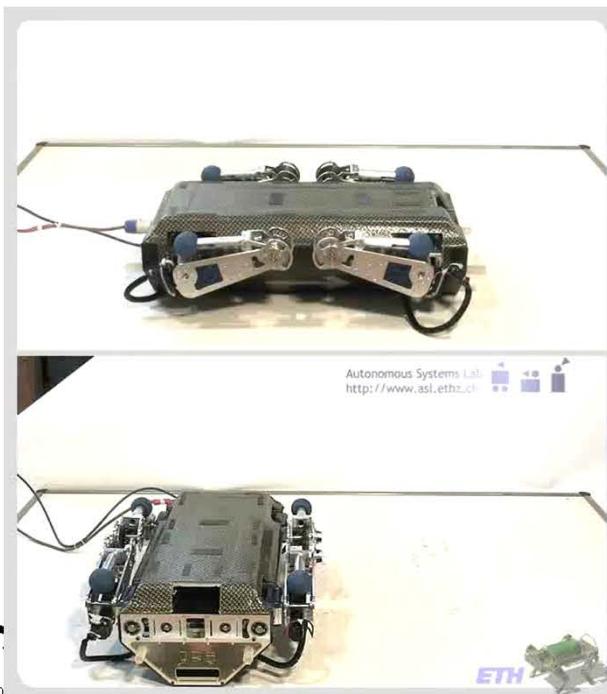


ANYmal

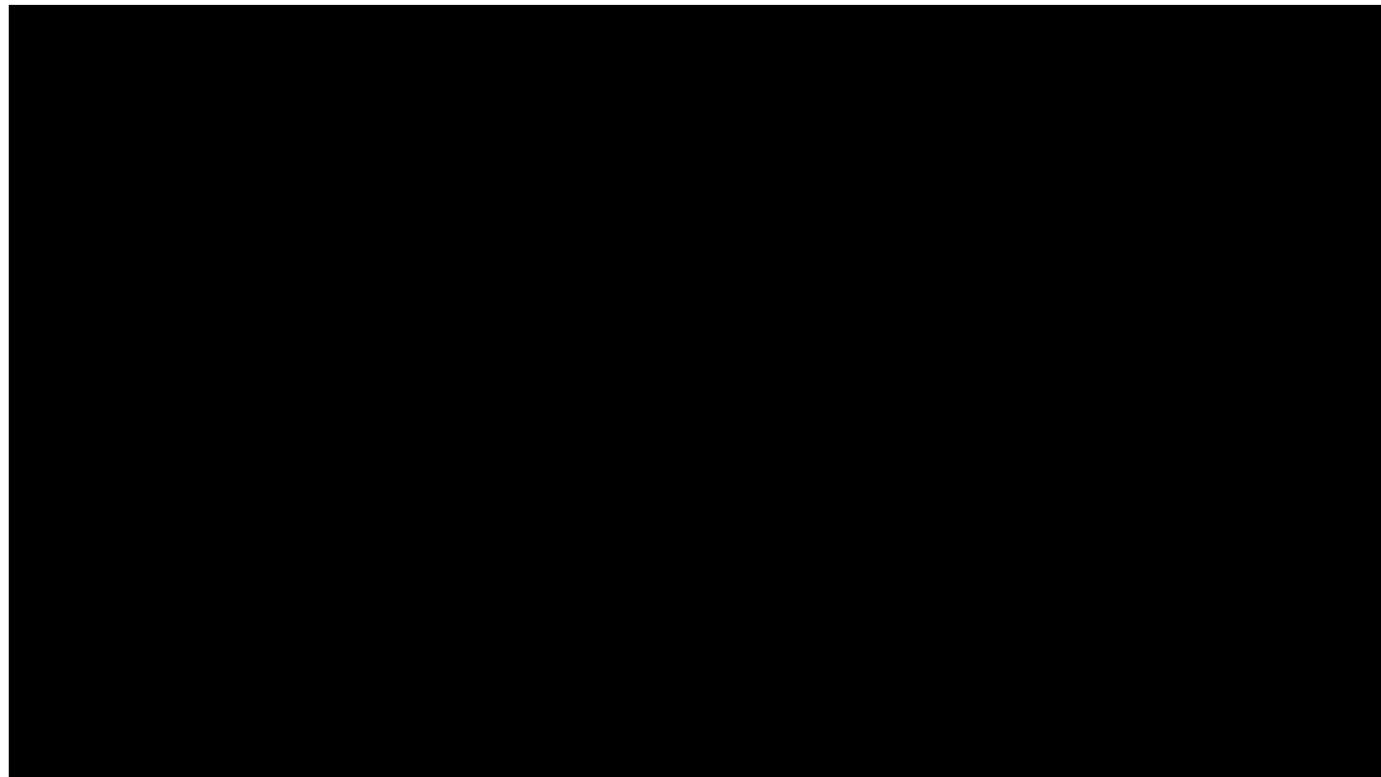
# ALOF

## a versatile quadruped robot

- High mobility
  - Clever design
  - Precise kinematic planning



# How to engineer a dog



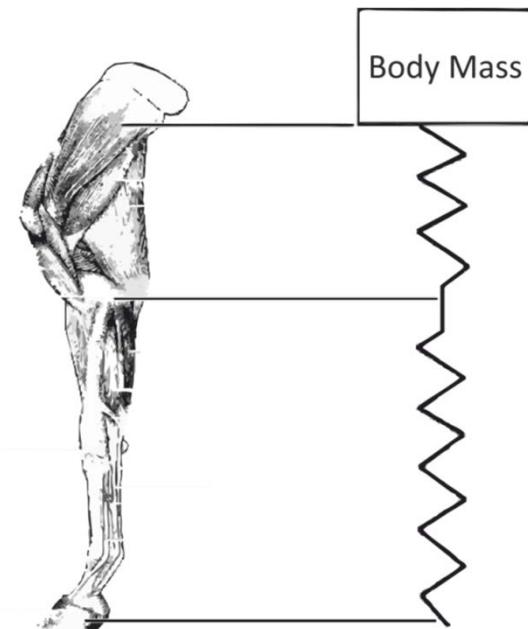


# Biomechanics of Animals

## Compliance in muscles and tendons

- Muscle/tendon (mech. compliance)
  - Robustness
  - Energy storage
  - Power/speed amplification
  - Force control instead of position

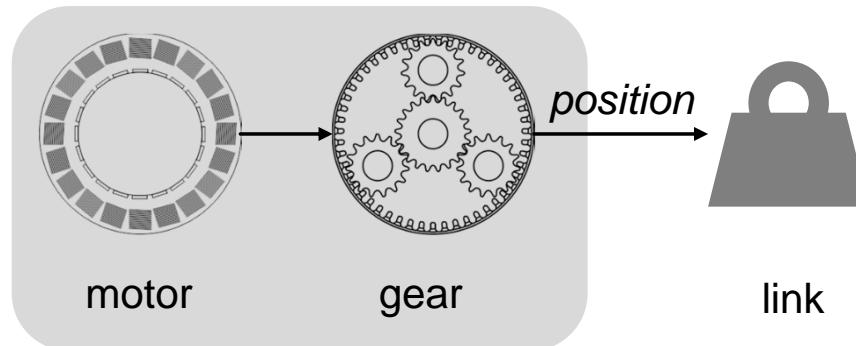
[Alexander 1988, 1990, 2002, 2003]



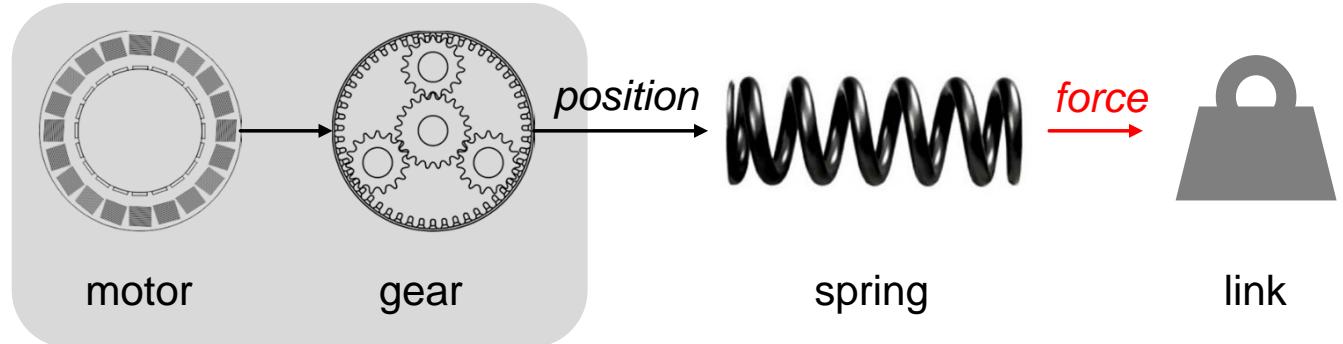
# From Position to Force Controlled Systems

## Compliance in robotic actuation

- Kinematic, position control



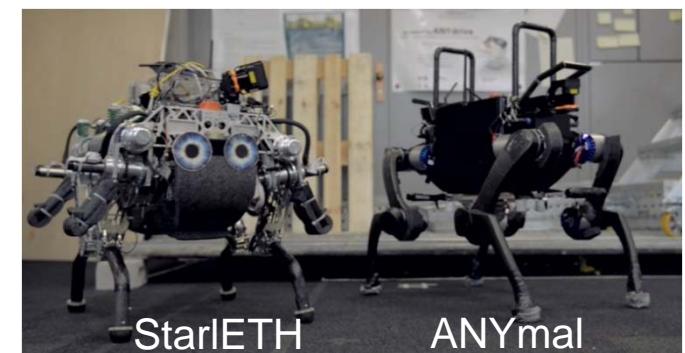
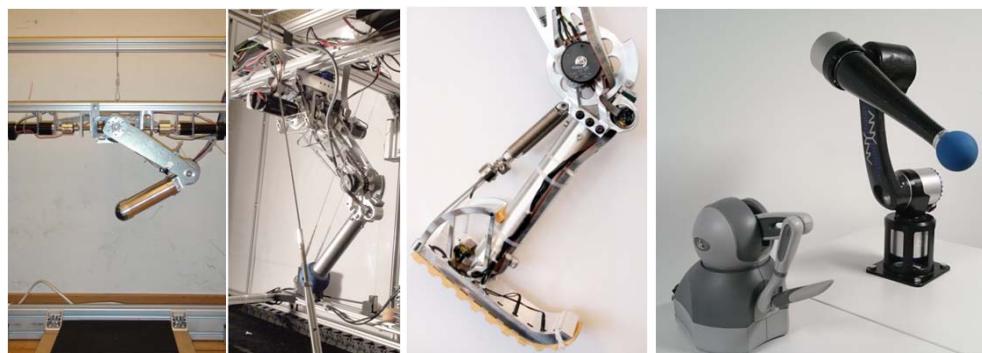
- Dynamic, force control



# High-performance Series Elastic Actuators

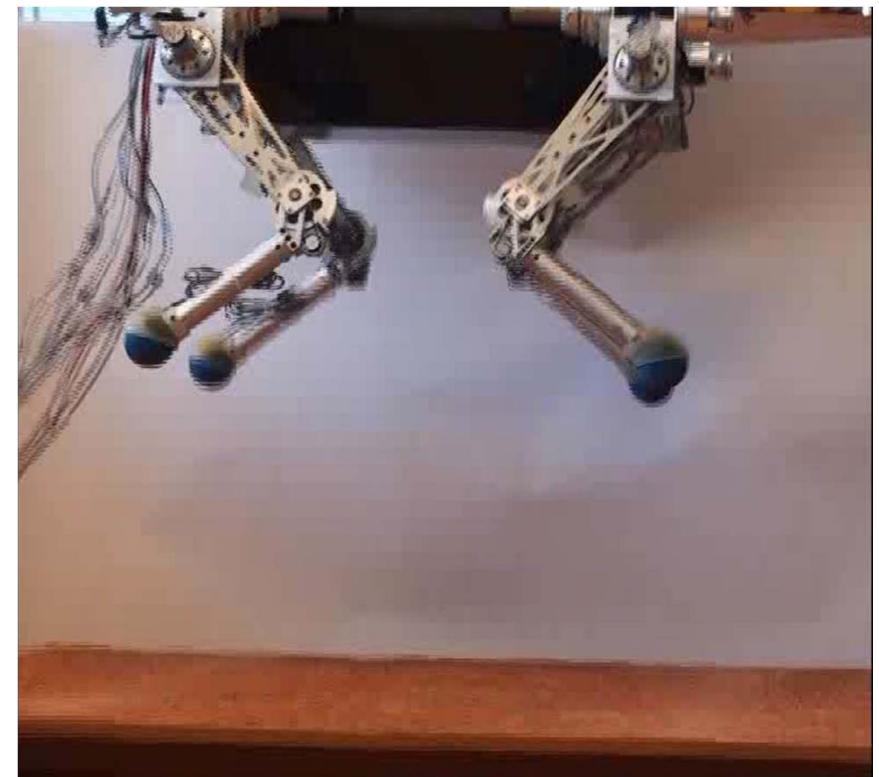
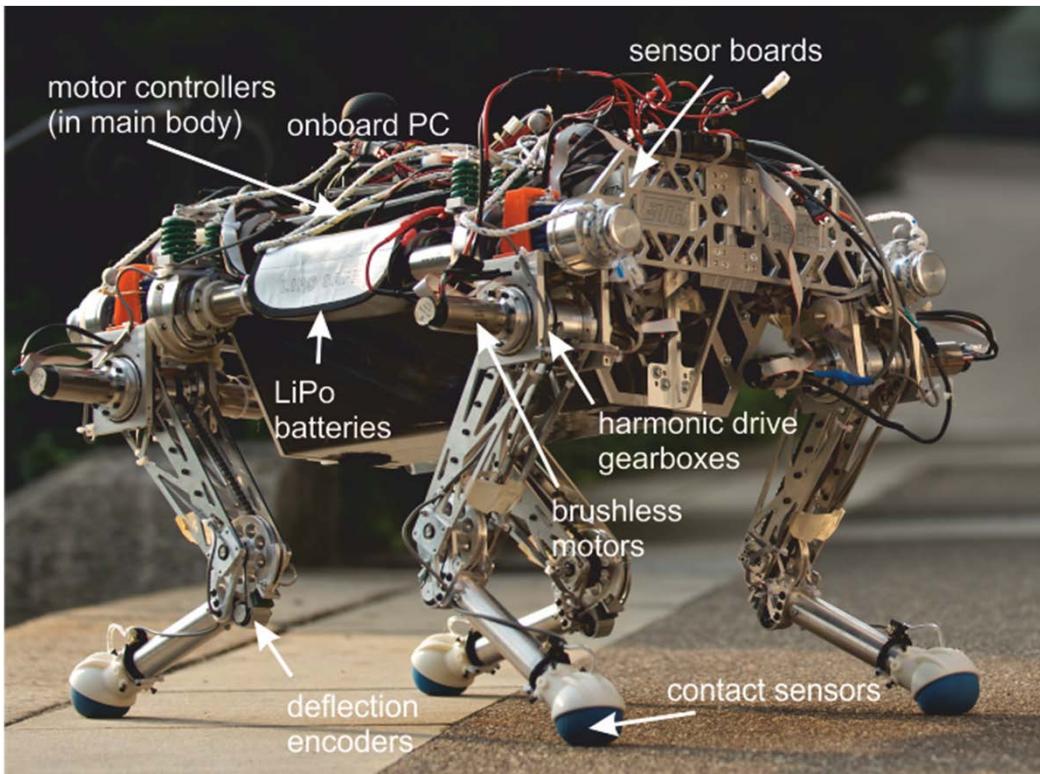
## Driving dynamic robots

- How to
  - ... **select** the optimal compliance?
  - ... mechanically **integrate** this compliance?
  - ... optimally **exploit** the compliance?
  - ... **control** systems with integrated compliance?



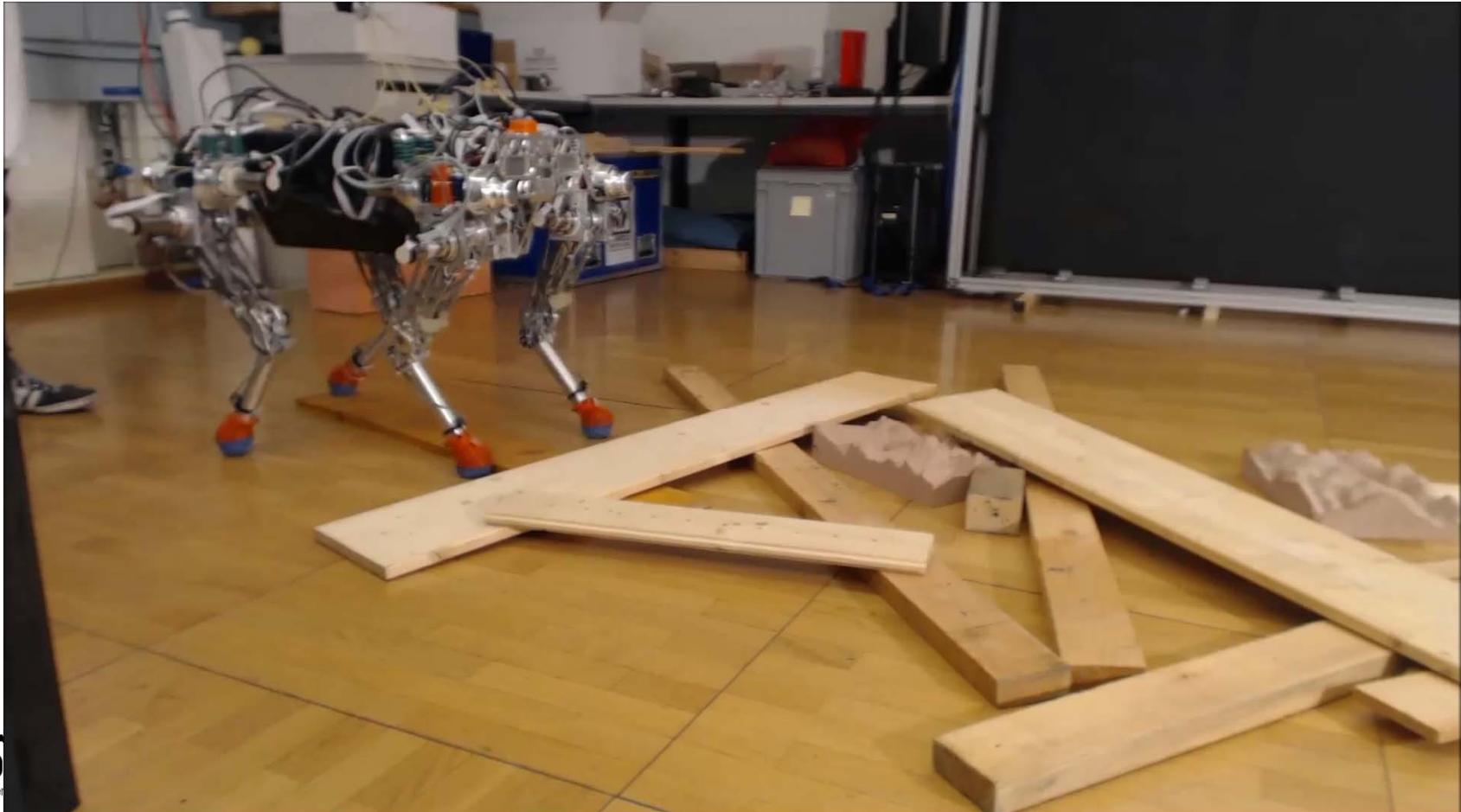
# StarIETH

## A compliant quadrupedal robot



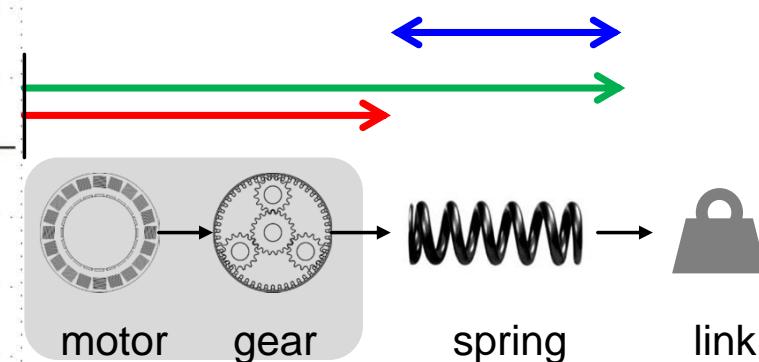
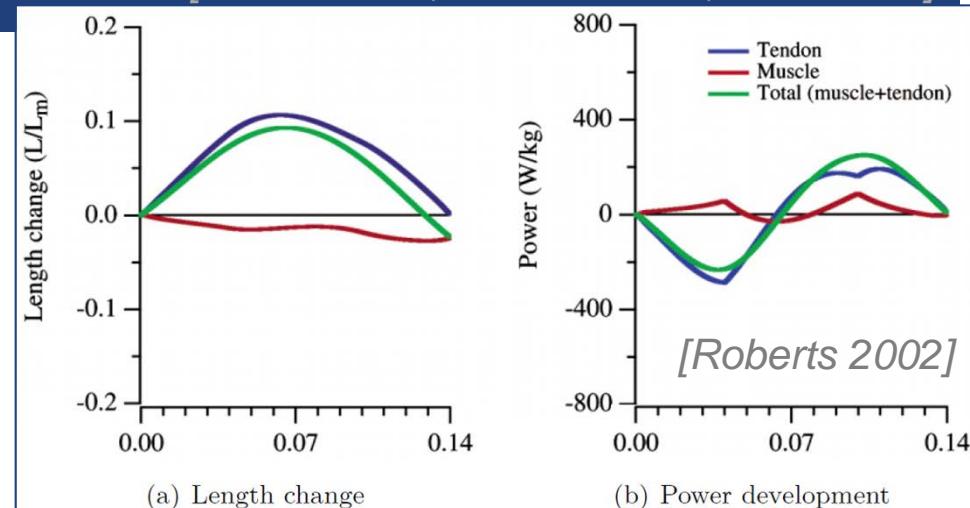
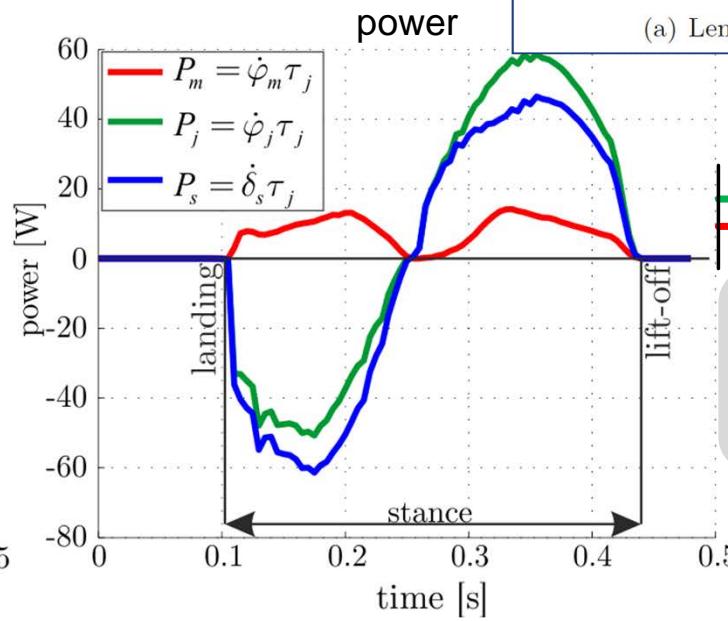
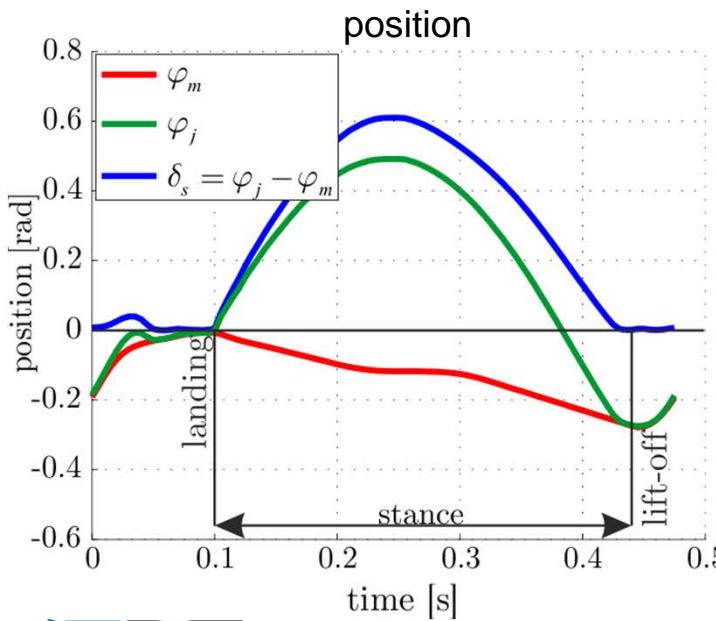
# StarIETH – a Compliant Quadrupedal Robot

## Towards autonomous running and climbing



# Exploitation of Passive Dynamics

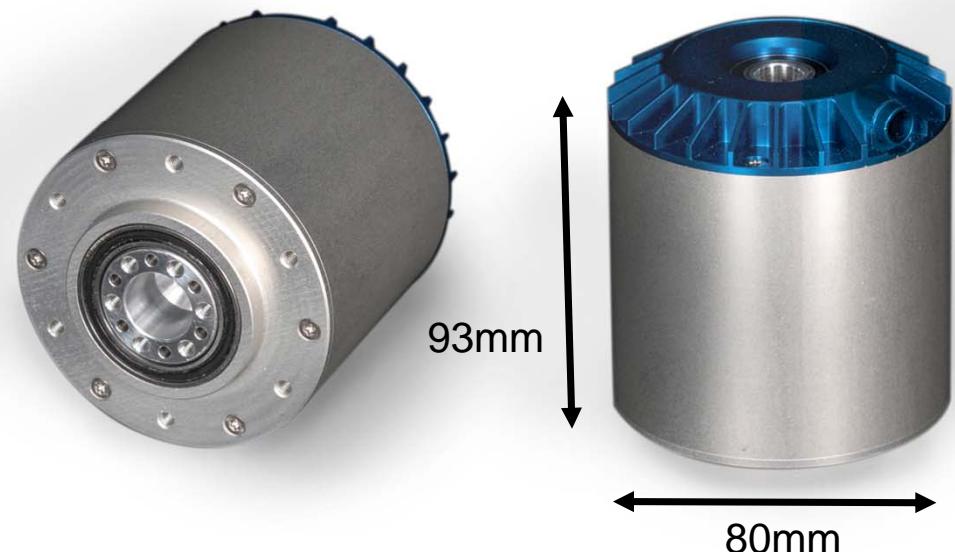
- 64% passive energy recovery
- Speed amplification 4.7, power amplification 4.1



## ANYdrive

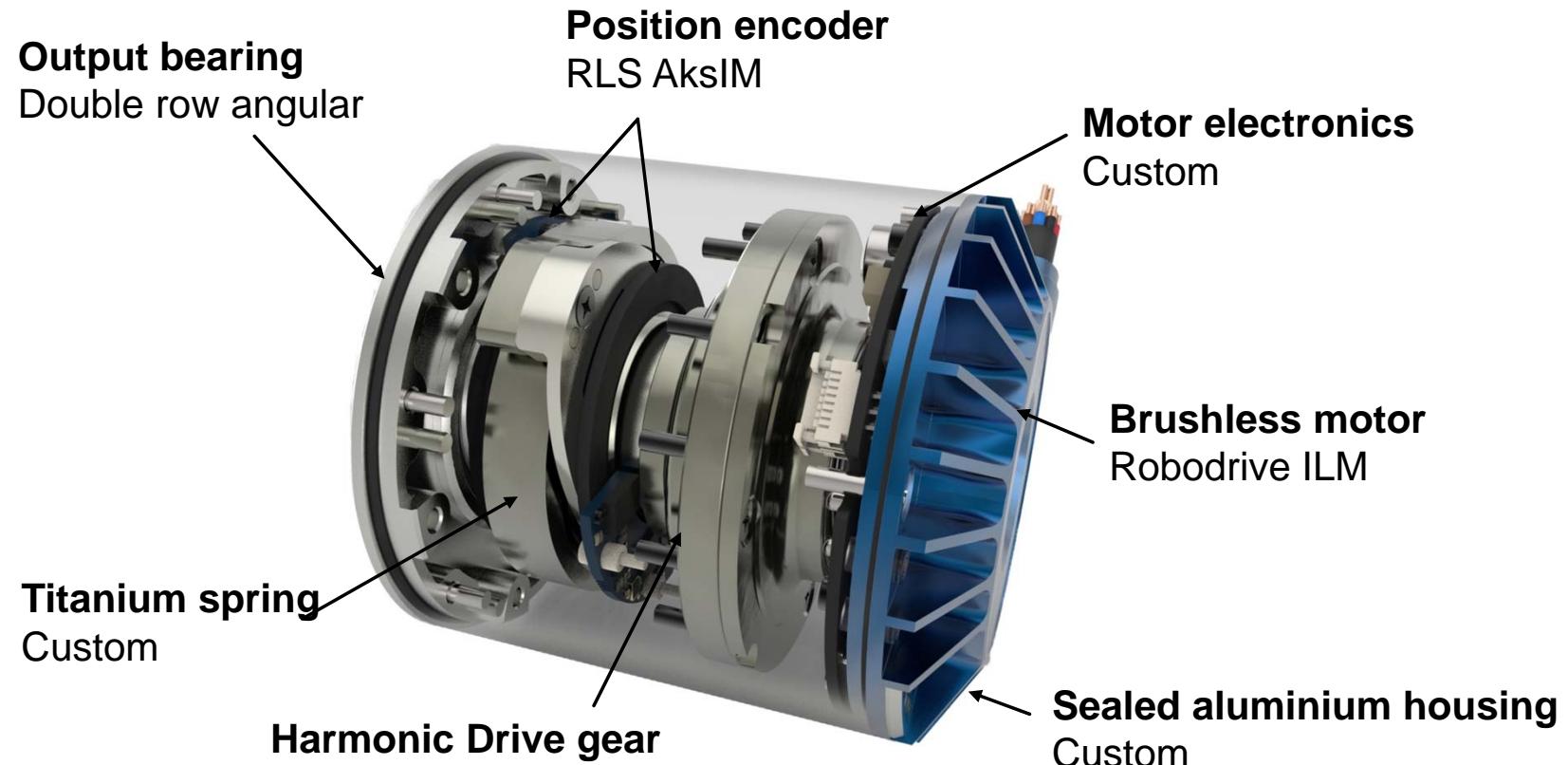
A robust and force controllable robot joint unit

- Fully integrate SEAs
  - Custom motor control and sensing (no communication delay)
  - CAN (future EtherCAT) and power interface
  - Precise absolute output position and torque control
  - Hollow shaft for cabling
  - Large output load bearing
  - IP67



# ANYdrive

## Setup



torque control



tracking



impact robustness



safe interaction



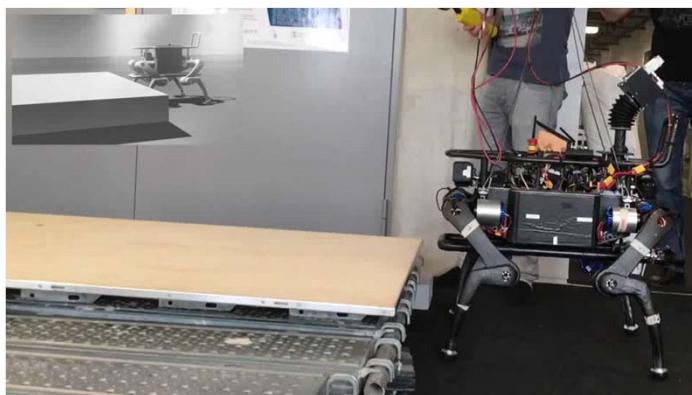
# ANYmal – System overview



- High mobility
  - Extensive range of motion
  - Various maneuvers (climb)
- Powerful, dynamic & efficient
  - Different gaits (walk, trot, jump,...)

# ANYmal

## Combining dynamic motion skills with large mobility



# ANYmal – System overview



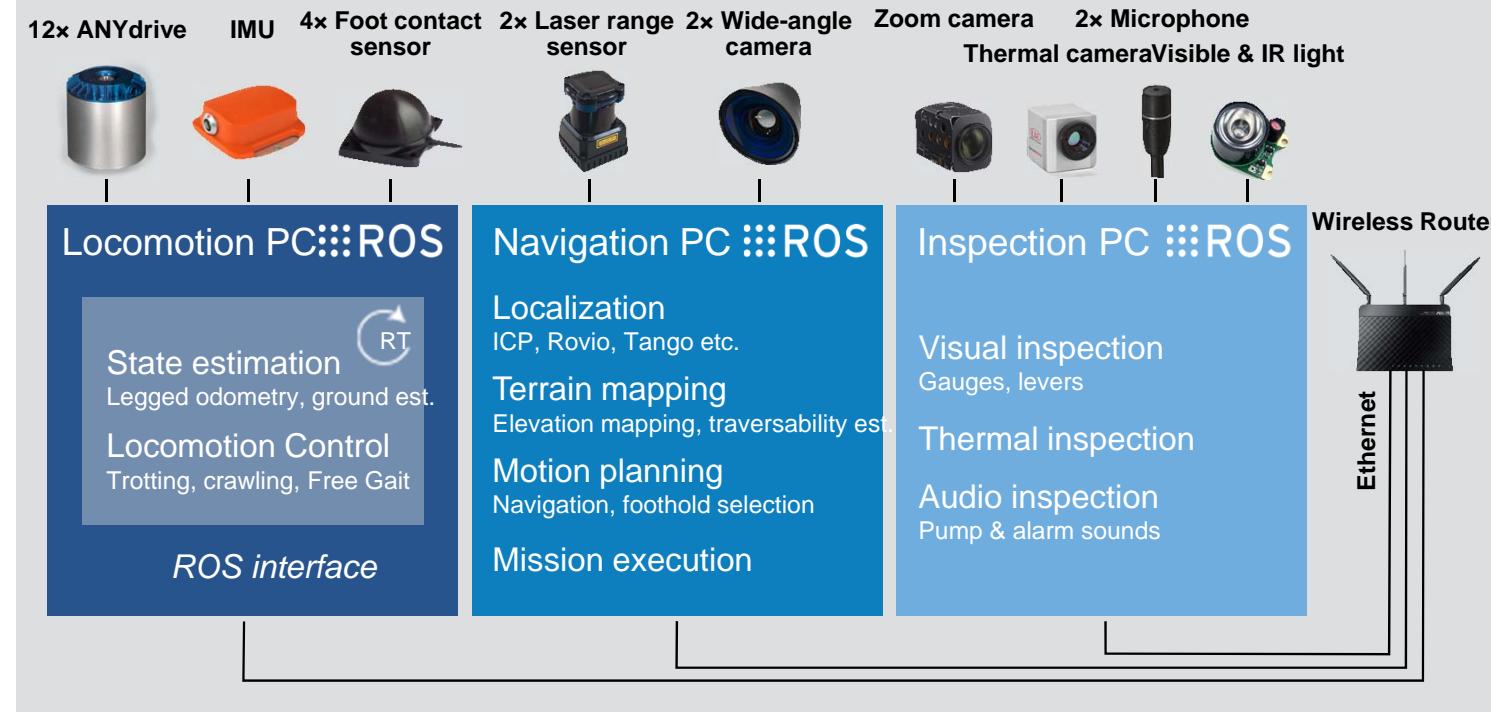
## Fully autonomous

- Onboard localization, mapping, planning, and control
- Modular sensor payload

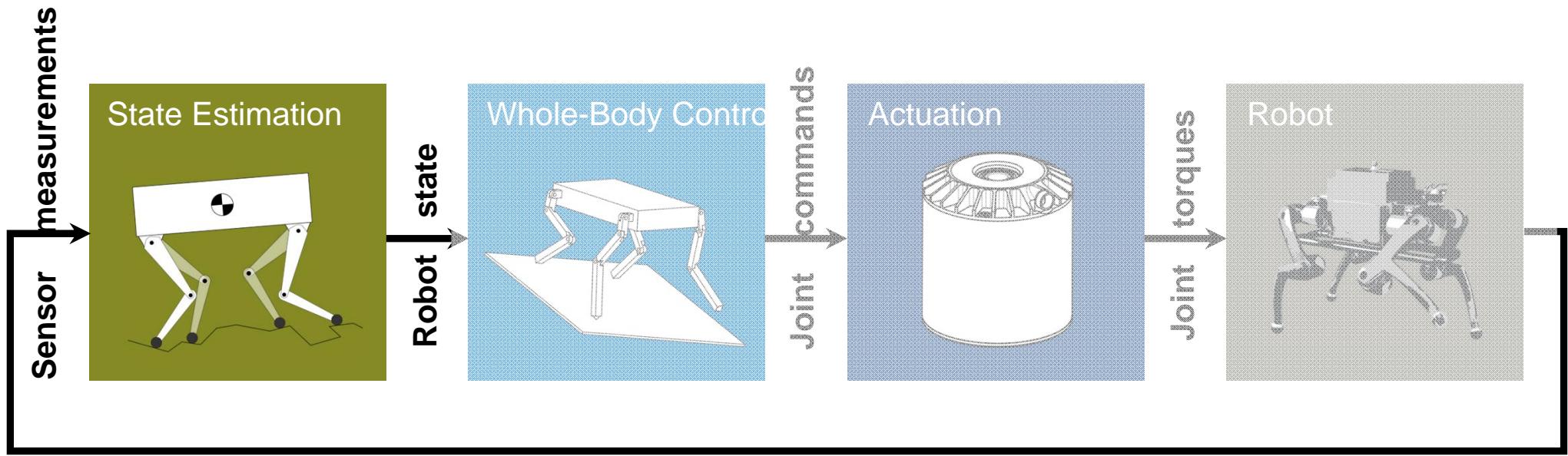
## Field-ready

- Water-proof
- 2–3 h endurance (280W avg power)
- 1-person operation (30kg)
- GUI for intuitive tele-operation
- Fall-safe

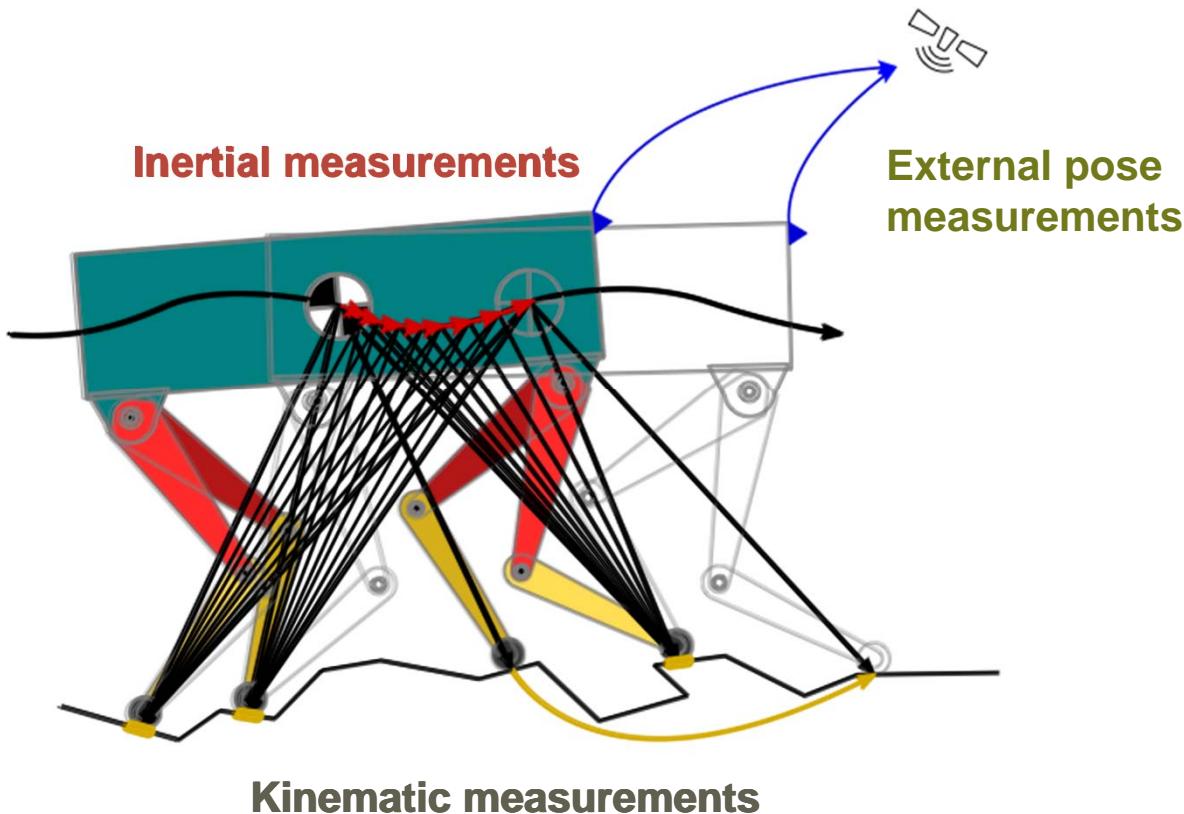
# Software and Electronics Architecture



# Locomotion



# State Estimation

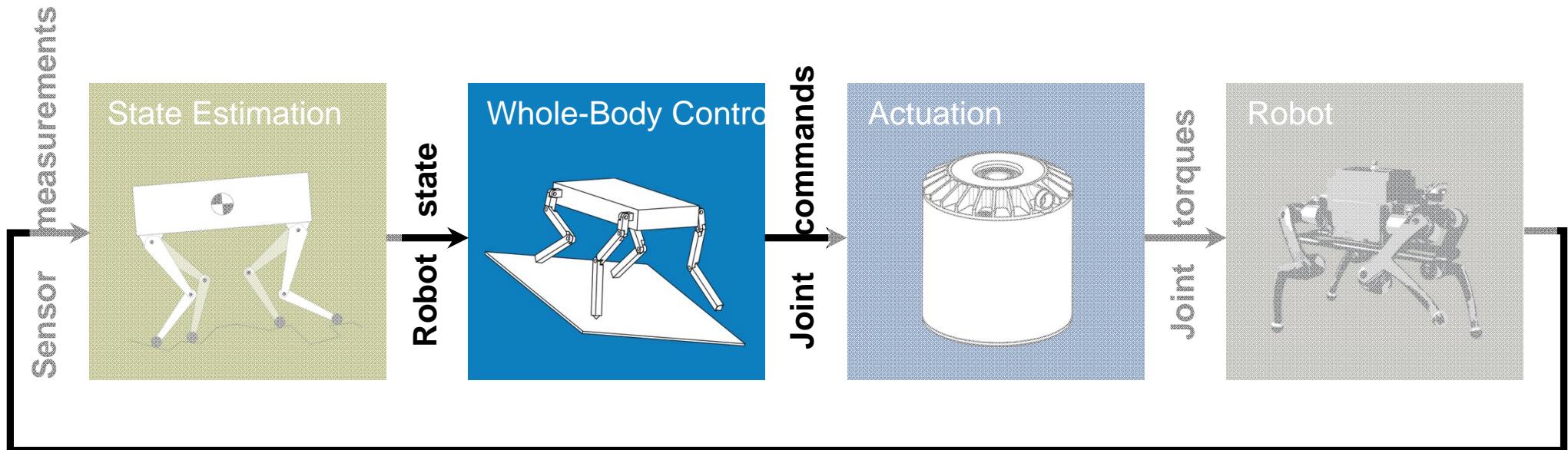


## Extended Kalman Filter

- No assumption on terrain
- Kinematic measurements (encoders) for legs in contact
- Fused with inertial measurements (IMU)
- Error < 5% over distance
- Optionally combined with external pose (GPS, laser, vision, etc.)

M. Bloesch, C. Gehring, P. Fankhauser, M. Hutter, M. A. Hoepflinger and R. Siegwart, “**State Estimation for Legged Robots on Unstable and Slippery Terrain**”, in International Conference on Intelligent Robots and Systems (IROS), 2013.

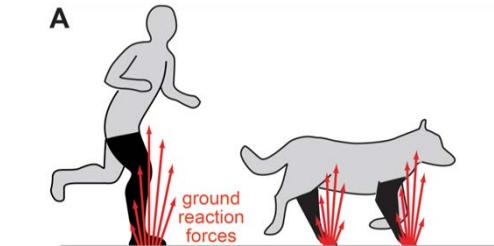
# Locomotion



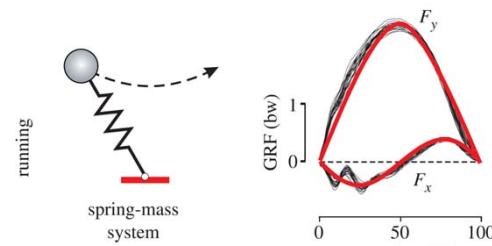
# Foot Placement Control

## Balance from stepping

- Biomechanical studies suggest SLIP models to describe complex running behaviors



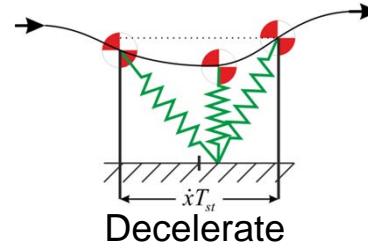
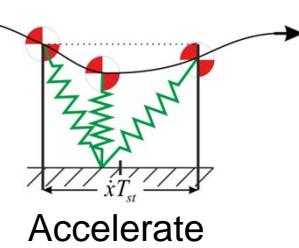
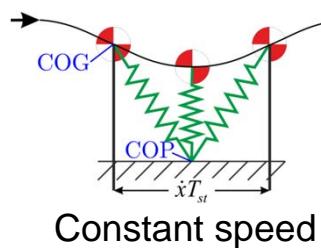
[Dickinson, Farley, Full 2000]



[Geyer 2006]

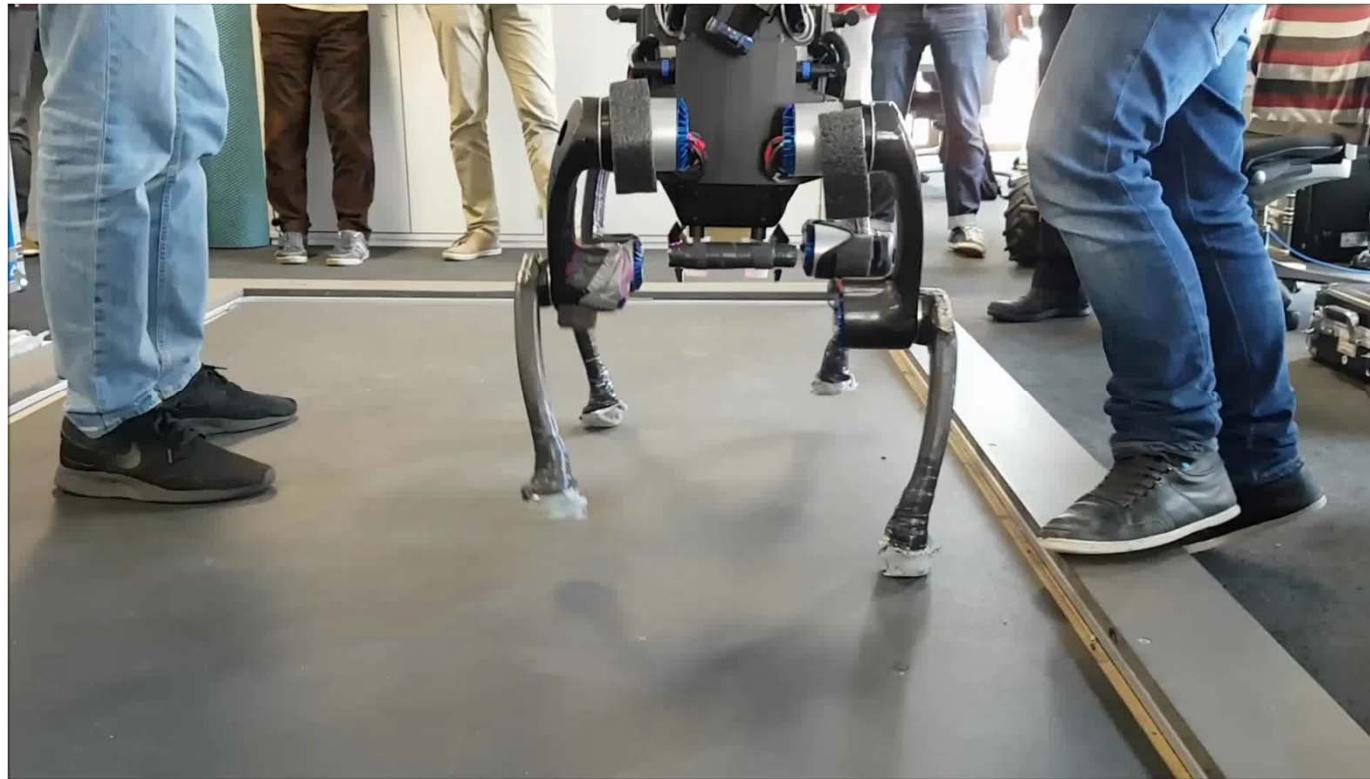
- Simple step-length rule to adjust the velocity

$$\mathbf{r}_F = \frac{1}{2} \dot{\mathbf{r}}_{HC,des} T_{st} + k_R^{FB} (\dot{\mathbf{r}}_{HC,des} - \dot{\mathbf{r}}_{HC}) \sqrt{h_{HC}} \quad [Raibert 1986]$$



# Foot Placement Control

## Balance from stepping



# Kinematics and Dynamics in Control

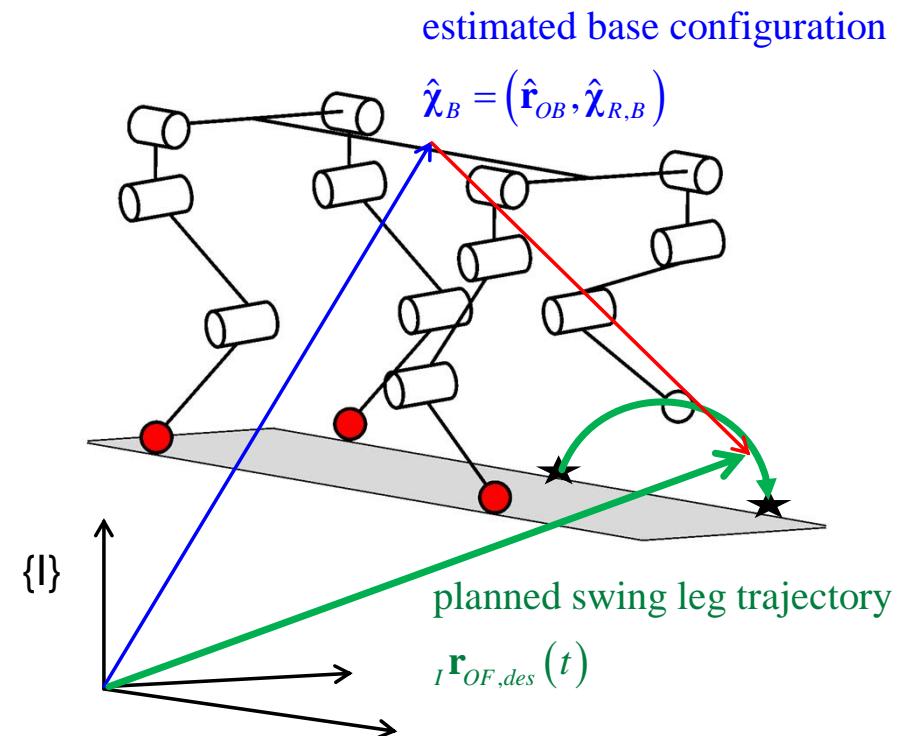
## Inverse kinematics for swing leg control

- Foot point in base frame

$$\mathbf{r}_{BF,des} = \mathbf{r}_{OF,des} - \hat{\mathbf{r}}_{OB}$$

- Expressed in world frame  ${}_I\mathbf{r}_{BF} = {}_I\mathbf{r}_{BF}(\mathbf{q}_r, \boldsymbol{\chi}_B)$
- Expressed in body frame  ${}_B\mathbf{r}_{BF} = {}_B\mathbf{r}_{BF}(\mathbf{q}_r)$
- => inverse kinematics in body frame

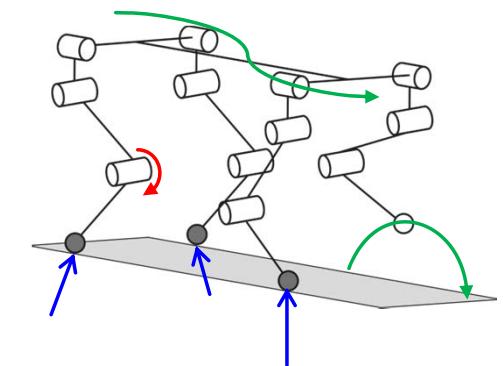
$${}_B\mathbf{r}_{BF,des} = \mathbf{R}_{BI}(\hat{\boldsymbol{\chi}}_{R,B}) {}_I\mathbf{r}_{OF,des} - {}_B\hat{\mathbf{r}}_{OB} = {}_B\mathbf{r}_{BF,des}(\mathbf{q}_{r,swing\ leg})$$



# Whole-body Control of a Legged Robot

- Equations of motion
- Contact constraint
- Desired motion optimization
- Contact force optimization
- Joint torque optimization

motion  $\xleftarrow{\text{causes}}$  actuation  
 $\downarrow$                    $\downarrow$   
 $\mathbf{M}\ddot{\mathbf{q}} + \mathbf{b} + \mathbf{g} + \mathbf{J}_s^T \mathbf{F}_s = \mathbf{S}^T \boldsymbol{\tau}$   
 $\uparrow$  contact force  
 $\mathbf{J}_s \ddot{\mathbf{q}} + \dot{\mathbf{J}}_s \dot{\mathbf{q}} = \mathbf{0}$



$$\min \|\ddot{\mathbf{r}}_i(\mathbf{q}) - \ddot{\mathbf{r}}_{des}\|_2 \text{ or } \ddot{\mathbf{r}}_i < \ddot{\mathbf{r}}_{i,\max}$$

$$\min \|\mathbf{W}_s \mathbf{F}_s - \mathbf{b}_F\|_2 \text{ or } \mathbf{F}_{s_i} < \mathbf{F}_{s,\max}$$

$$\min \|\mathbf{W}_\tau \boldsymbol{\tau} - \mathbf{b}_\tau\|_2 \text{ or } \boldsymbol{\tau} < \boldsymbol{\tau}_{\max}$$

Whole-body control = large scale simultaneous optimization of  $\ddot{\mathbf{q}}, \mathbf{F}_s, \boldsymbol{\tau}$

# Kinematics and Dynamics in Control

## (simple) whole body control

- Adjust joint torques to
  - track the swing leg
  - to move the base
  - ensure contact constraint

$$\ddot{\mathbf{r}}_{OF} = \mathbf{J}_F \ddot{\mathbf{q}} + \dot{\mathbf{J}}_F \dot{\mathbf{q}} = \ddot{\mathbf{r}}_{OF,des}(t)$$

$$\dot{\mathbf{w}}_B = \mathbf{J}_B \ddot{\mathbf{q}} + \dot{\mathbf{J}}_B \dot{\mathbf{q}} = \dot{\mathbf{w}}_{B,des}(t)$$

$$\ddot{\mathbf{r}}_c = \mathbf{J}_c \ddot{\mathbf{q}} + \dot{\mathbf{J}}_c \dot{\mathbf{q}} = \mathbf{0}$$

⇒ fully defines the motion of the system

12 actuated + 6 unactuated = 18 DOF

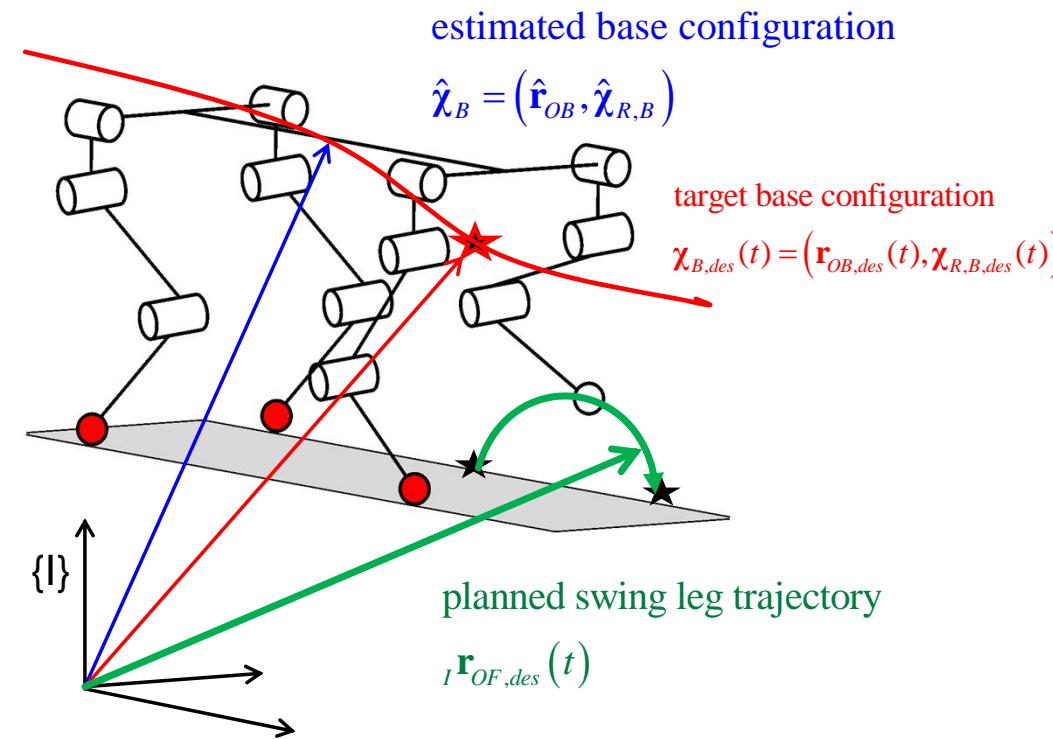
6 motion + 9 constraints + 3 swing leg = 18

If more tasks,  
use pseudo-inverse

$$\ddot{\mathbf{q}}_{des} = \begin{bmatrix} \mathbf{J}_F \\ \mathbf{J}_B \\ \mathbf{J}_c \end{bmatrix} \mathbf{T}^{-1} \begin{bmatrix} \ddot{\mathbf{r}}_{OF}(t) \\ \dot{\mathbf{w}}_B(t) \\ 0 \end{bmatrix} - \begin{bmatrix} \dot{\mathbf{J}}_F \\ \dot{\mathbf{J}}_B \\ \dot{\mathbf{J}}_c \end{bmatrix} \dot{\mathbf{q}}$$

- Inverse dynamics control

$$\boldsymbol{\tau} = (\hat{\mathbf{N}}_c^T \mathbf{S}^T)^+ \hat{\mathbf{N}}_c^T (\hat{\mathbf{M}} \ddot{\mathbf{q}}_{des} + \hat{\mathbf{b}} + \hat{\mathbf{g}})$$



# Locomotion as Optimization Problem

- Write inverse dynamics as constraint (prioritized) optimization

- Step 1: move base

s.t.

$$\begin{aligned} \min_{\ddot{\mathbf{q}}} & \| \dot{\mathbf{w}}_{B,des}(t) - \mathbf{J}_B \ddot{\mathbf{q}} - \dot{\mathbf{J}}_B \dot{\mathbf{q}} \| \\ \text{s.t. } & \mathbf{M}\ddot{\mathbf{q}} + \mathbf{b} + \mathbf{g} + \mathbf{J}_c \mathbf{F}_c = \mathbf{S}^T \boldsymbol{\tau} \\ & \mathbf{J}_B \ddot{\mathbf{q}} + \dot{\mathbf{J}}_B \dot{\mathbf{q}} = \mathbf{0} \\ & \mathbf{F}_{c,n_i} > F_{n,\min} \\ & \mu \mathbf{F}_{c,n_i} > \|\mathbf{F}_{c,t_i}\|_2 \end{aligned}$$

<= equation of motion holds  
 <= contact constraint holds  
 <= minimal normal contact force  
 <= contact force in friction cone

- Step 2: move swing leg

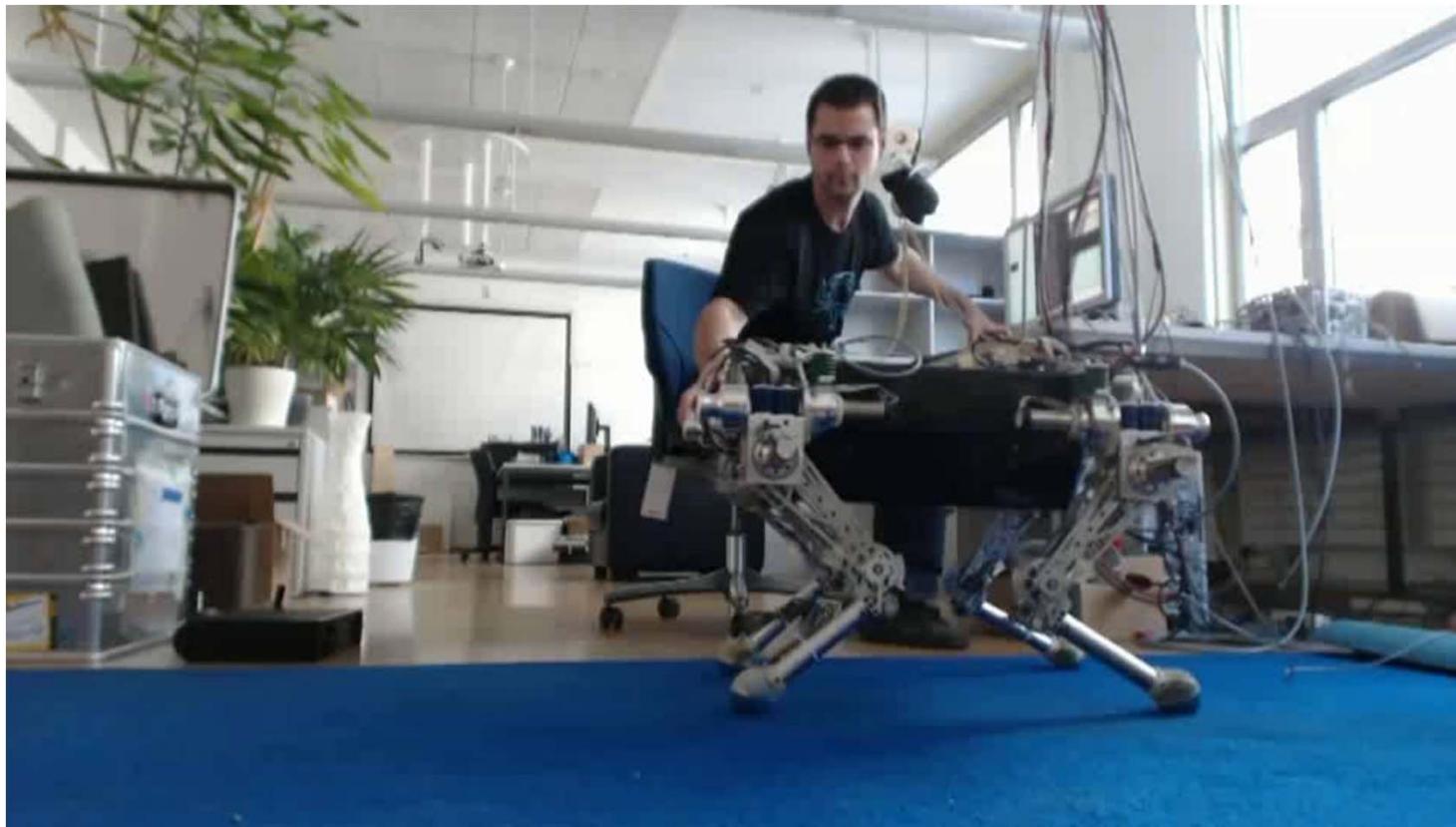
s.t.

$$\begin{aligned} \min_{\ddot{\mathbf{q}}} & \| \ddot{\mathbf{r}}_{OF,des}(t) - \mathbf{J}_F \ddot{\mathbf{q}} - \dot{\mathbf{J}}_F \dot{\mathbf{q}} \| \\ & c_1 = \ddot{\mathbf{x}}_{B,des}(t) - \mathbf{J}_B \ddot{\mathbf{q}} - \dot{\mathbf{J}}_B \dot{\mathbf{q}} \\ \text{s.t. } & \mathbf{M}\ddot{\mathbf{q}} + \mathbf{b} + \mathbf{g} + \mathbf{J}_c \mathbf{F}_c = \mathbf{S}^T \boldsymbol{\tau} \\ & \mathbf{F}_{c,n_i} > F_{n,\min} \\ & \mu \mathbf{F}_{c,n_i} > \|\mathbf{F}_{c,t_i}\|_2 \end{aligned}$$

<= higher priority task is not influenced  
 <= equation of motion holds  
 <= minimal normal contact force  
 <= contact force in friction cone

- Last step: minimize e.g. torque  $\min \|\boldsymbol{\tau}\|$  or tangential contact forces  $\min \|\mathbf{F}_{s,t_i}\|$   
 s.t. all other tasks are still fulfilled

# Static Walking with Compliant Behavior



# Static Walking – Force/Torque Optimization

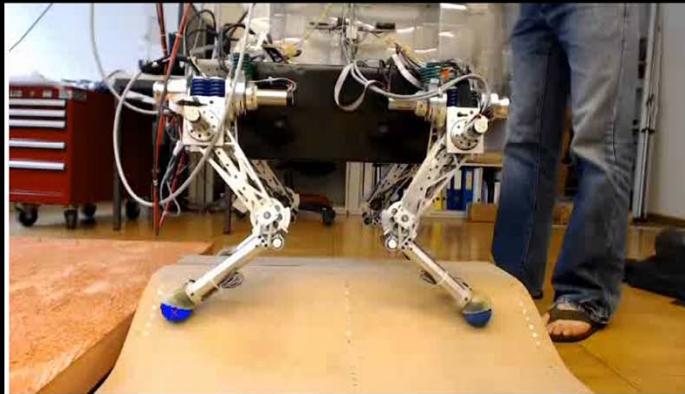
- Different force and torque optimization strategies:
  - Reduced energy consumption by torque minimization  $\mathbf{W}_\tau = \mathbf{I}$
  - Reduction of risk of slippage by contact force alignment  $\mathbf{W}_F = \text{diag}(\mathbf{t}_i)$

		Torque minimization	Tangential force minimization
Energy consumption	$E_\tau = \int \boldsymbol{\tau}^T \boldsymbol{\tau} dt$ [N <sup>2</sup> m <sup>2</sup> s]	4701	5544
Risk of slippage	$\bar{\mu} = \text{mean} \left( \frac{F_{tan}(t)}{F_{norm}(t)} \right)$ [-]	0.2	0.04
Average tracking error	$\bar{\Delta r} = \text{mean} \  \mathbf{r}(t) - \mathbf{r}_{des}(t) \ $ [mm]	7.7	3.3

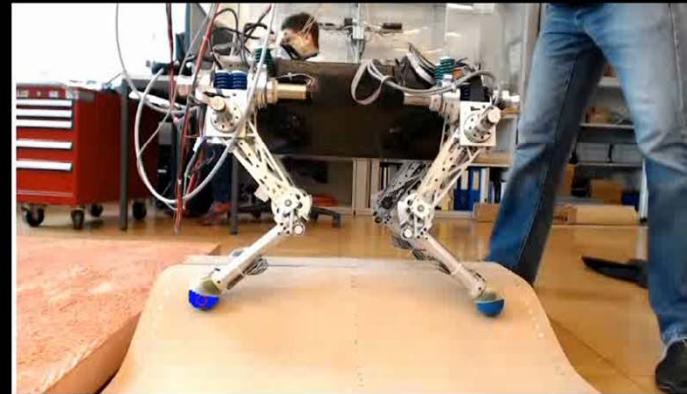
# Static Walking – Force/Torque Optimization

- Different force and torque optimization strategies:
  - Reduced energy consumption by torque minimization  $\mathbf{W}_\tau = \mathbf{I}$
  - Reduction of risk of slippage by contact force alignment  $\mathbf{W}_F = \text{diag}(\mathbf{t}_i)$

standard force distribution

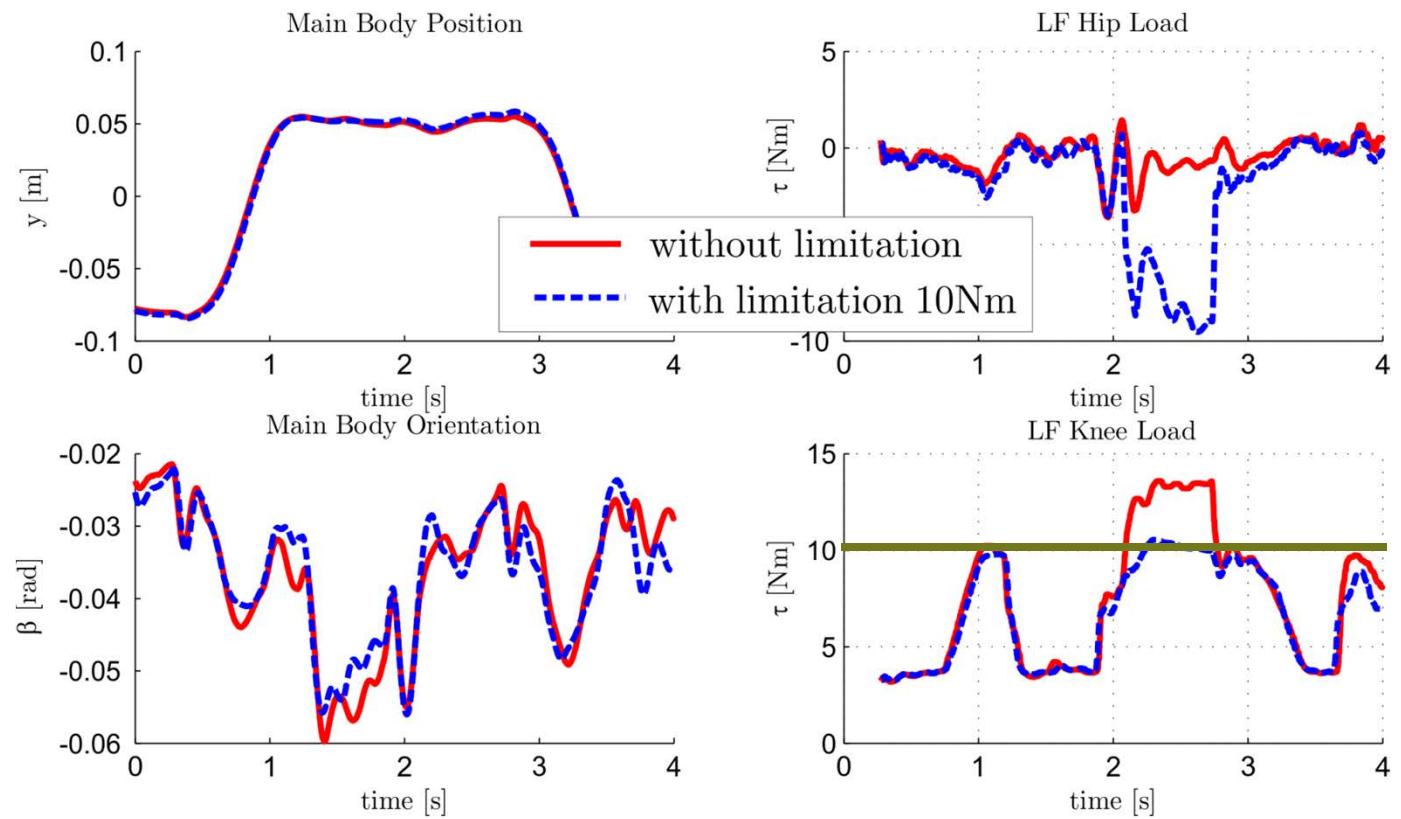


contact force optimization



# Joint Torque Limitations

- Inequality tasks



# Joint Position Limitation

$$\mathbf{A}_i \mathbf{x} \leq \mathbf{b}_i$$

- Base shifting
- Joint Limitation = Inequality constraint

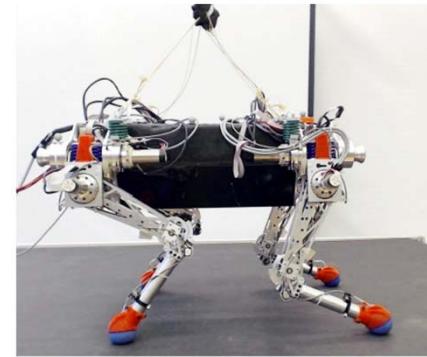
$P_1^q$  : contact constraints

$P_2^q$  : angle limitation

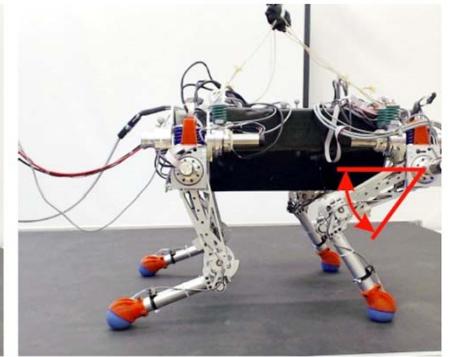
$P_3^q$  : xy body position

$P_4^q$  : body orientation

$P_5^q$  : ground clearance



(a) Start configuration



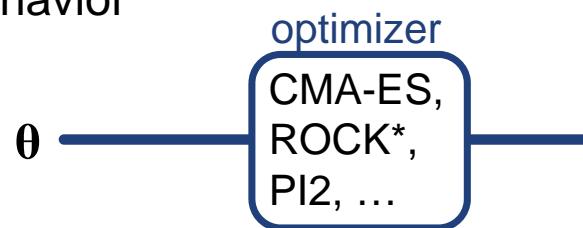
(b) No joint limitation

# Task Prioritization (Bellicoso, Humanoids 2016)

Priority	Task
1	Equations of Motion
2	No contact motion
3	Torque limits
4	Friction cone and $\lambda$ modulation
5	Desired torso $x, y$ position
6	Swing foot motion tracking
7	Limb kinematic limits
8	Main body yaw
9	Main body height
10	Main body roll and pitch
11	Contact force minimization

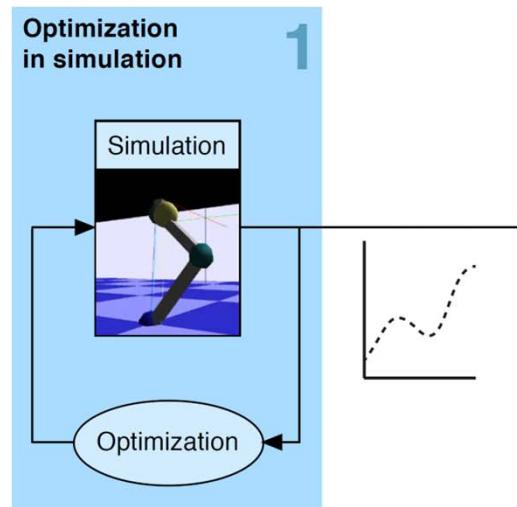
# Motion Synthesis from Optimization

- Parameterization of behavior
  - Motion primitives
  - Gait pattern
  - Control gains
  - ...



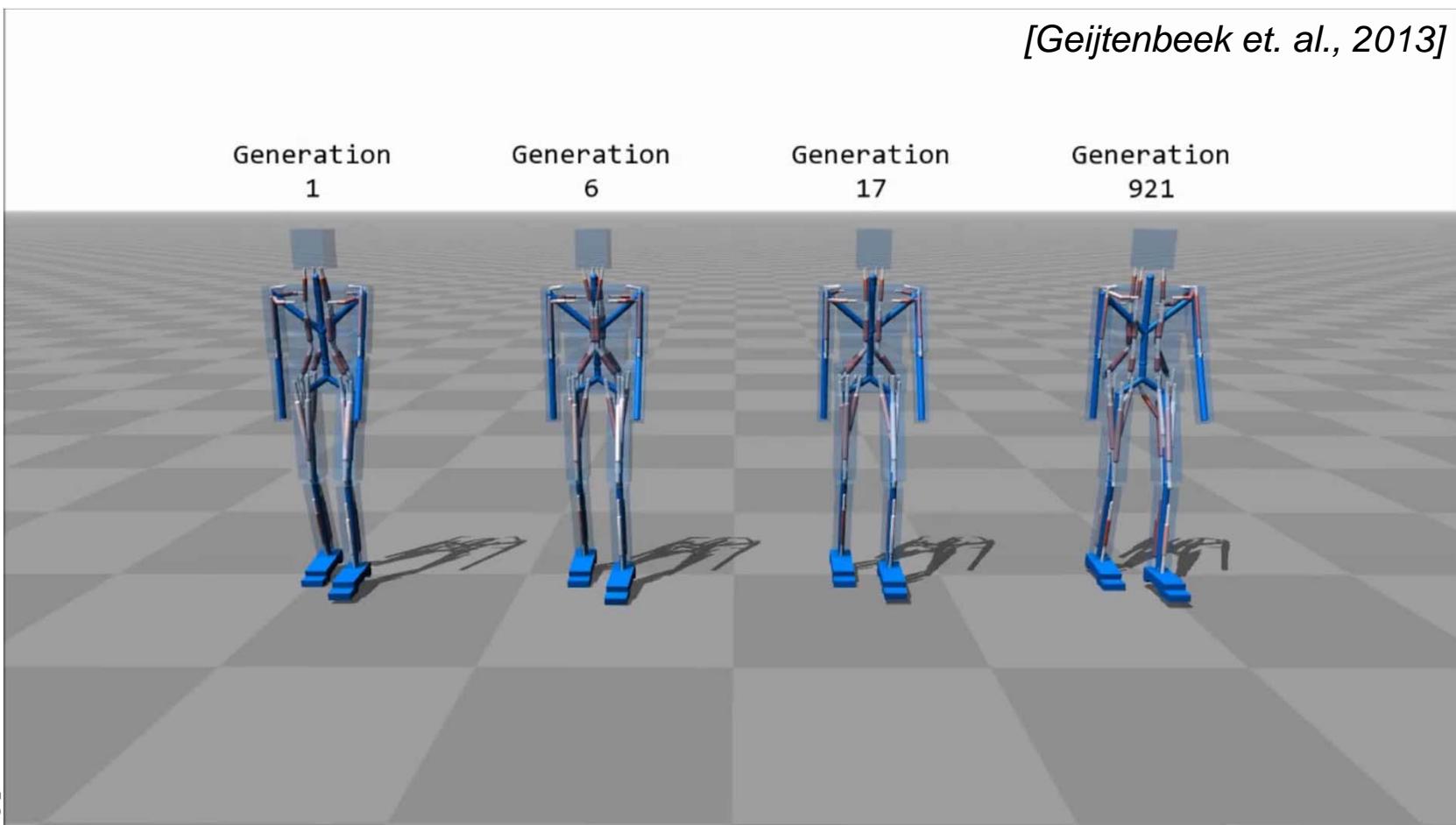
Target behavior = cost function

$$\theta^* = \arg \min_{\theta} \sum w_i \cdot C_i(\theta, q, \dot{q}, \tau)$$



# Motion Synthesis from Optimization

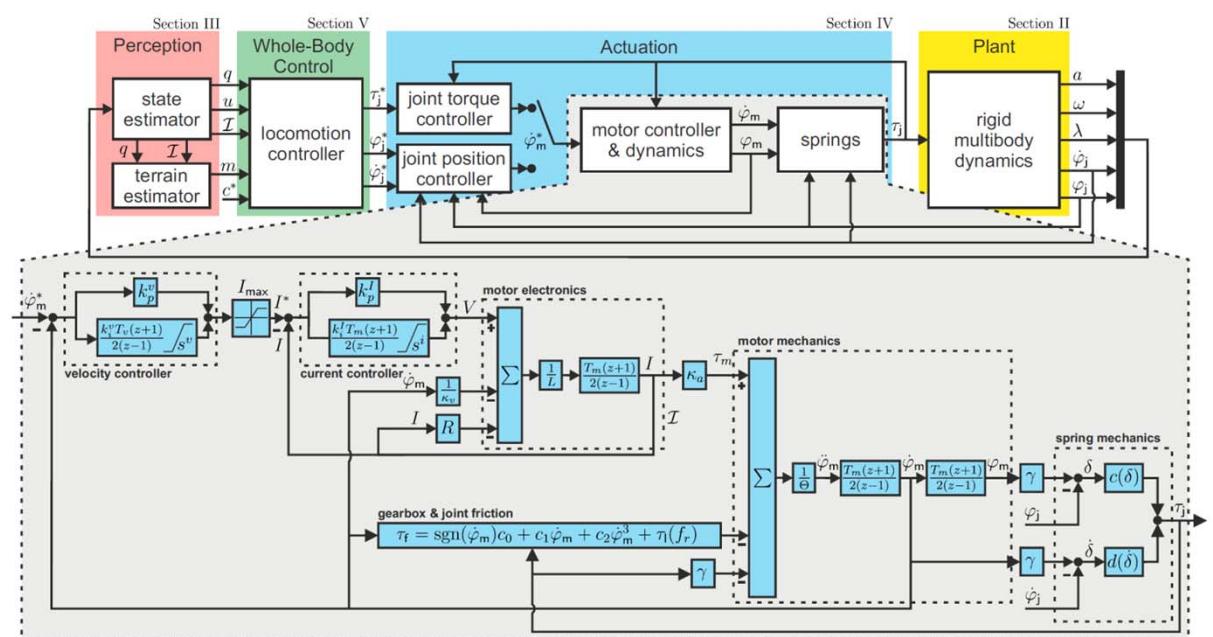
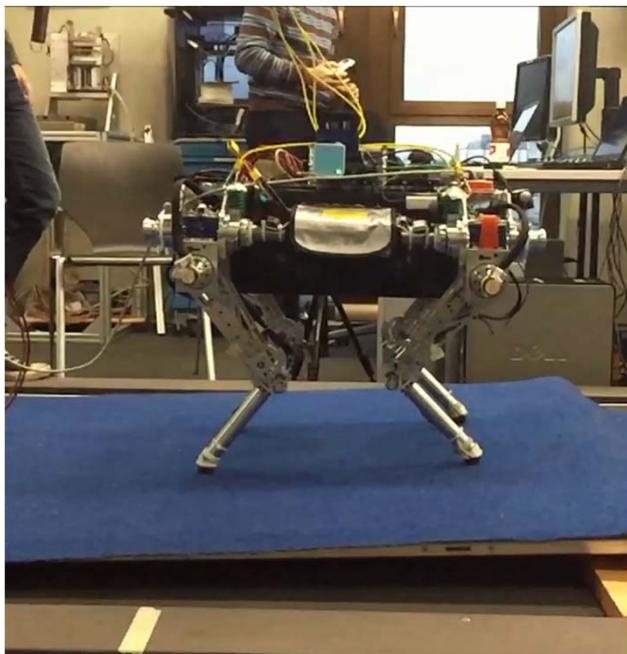
[Geijtenbeek et. al., 2013]



# Emerging Behaviors

## High jumping manoeuvre

- Model ENTIRE system (including actuator dynamics and mechanical elasticity) allows reaching maximum performance



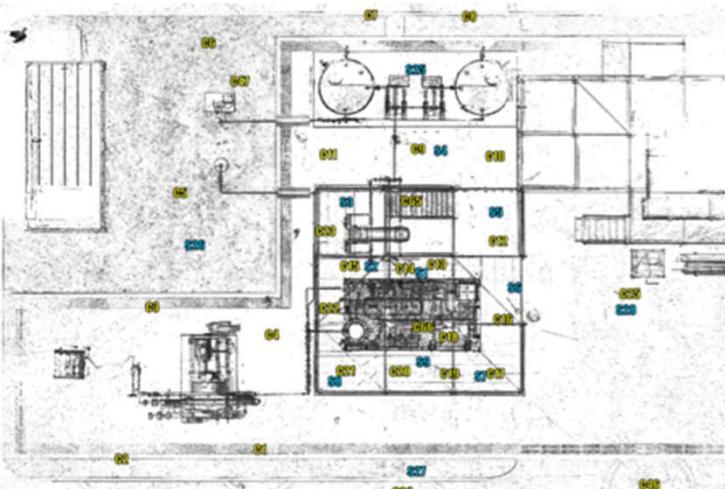
# ANYmal – Application in real-world scenarios



- ARGOS challenge
  - Autonomous inspection of oil and gas sites
- NCCR rescue robotics
  - S&R application together with UAVs

# ARGOS Challenge

## Autonomous Inspection of Oil and Gas Sites



ANR

**ARGOS**  
CHALLENGE  
LOGGING THE FIRST AUTONOMOUS ROBOT FOR DANGEROUS OIL SITES

**TOTAL**  
COMMITTED TO BETTER ENERGY

### Requirement 3 (Detection and analysis)

For the 2<sup>nd</sup> competition the robot must be able to detect, by its own means, and react to:

- General Platform Alarm - GPA (3-1):  
a GPA situation has to be detected by the robot system itself using its audio sensors. The GPA is not activated by the operator (except in simulation condition, see remarks).
- Acoustic leak detection (3-2):  
gas leaks emit in the ultra-sonic range (25kHz-70kHz, dynamic range 58-104dB SPL).
- Checkpoints:  
checkpoints will have to be detected around their expected position, and their absence reported.
  - Pressure gauge (3-6)
  - Water level (3-7)
  - Valve (3-8)
  - The most important point (3-10)
- Abnormal noises of pump (3-3):  
The robot will have to detect, in the close vicinity of the pump, if the sound produced matches the expected nominal sound.
- Unexpected heat sources (3-11):  
The robot will have to detect unexpected heat sources in the facility (refer to requirement 4 - Sources of high temperatures, page 22).
- Obstacles (3-12):  
unexpected obstacles during the 2<sup>nd</sup> competition can be objects or part of structure, on the ground (positive obstacles) or out of the ground (suspended obstacles), or holes (negative obstacles), refer to requirement 7, page 24.

Associated reactions and behaviours to these stimuli detection are listed in requirement 18 (autonomous reactions).

Testing the implementations of detection and reaction to the following stimuli are not planned for the 2<sup>nd</sup> competition:

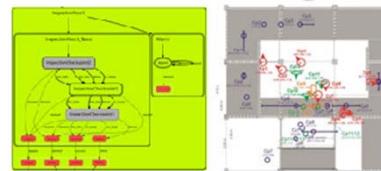
- Gas leak - IR detection (3-5):  
gas leak detection and detection based on the point IR detector.
- Safety equipment - extinguishers (3-4):  
the robot has to detect whether the extinguishers are present in their expected localization.
- Absence of plug (3-9):  
monitoring the environment to identify missing plugs on open pipes.

### Remarks:

In order to allow simulation of GPA, for testing purpose only, the operator should be able to simulate a detection of a GPA by the robot through the control room's HMI.

# ARGOS Challenge

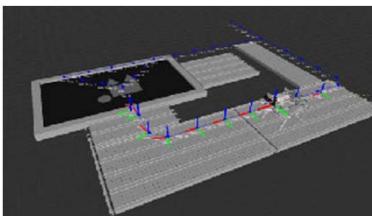
## Autonomous Inspection of Oil and Gas Sites



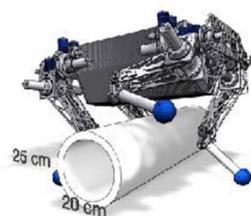
**Mission planning**  
Mission layout, decision making, user interface ...



**Inspection**  
Gauges, water levels, levers, heat sources, alarm sounds ...



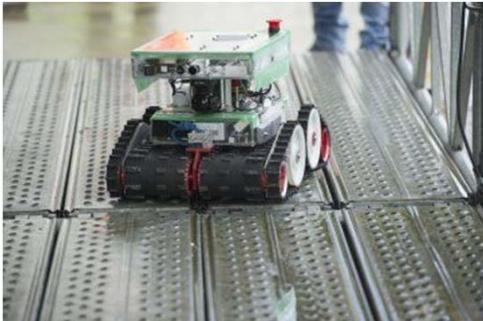
**Navigation**  
Path planning, localization, obstacle avoidance  
...



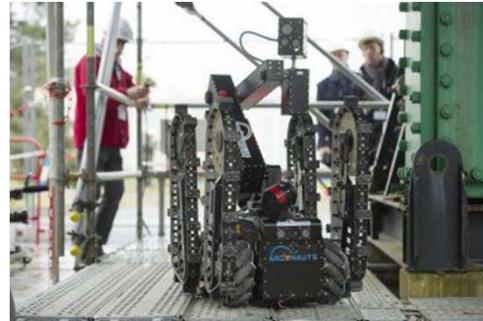
**Climbing**  
Steps, Pipes, Stairs ...

# ARGOS Challenge

5 International Teams (Industry + Academia)



**AIR-K**  
Japan



**ARGONAUTS**  
Austria & Germany



**FOXIRIS**  
Spain & Portugal



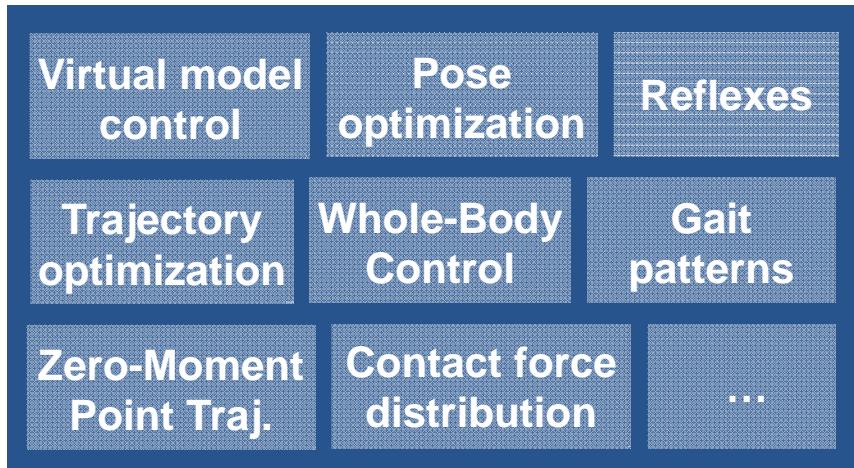
**VIKINGS**  
France



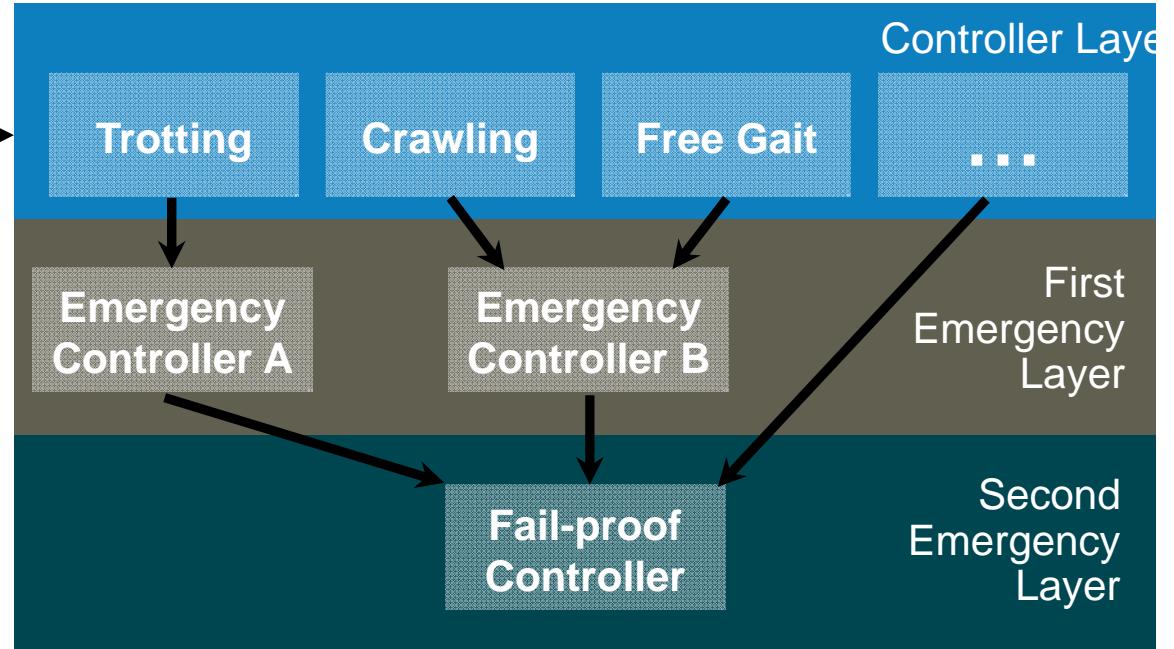
**LIO**  
Switzerland

# Locomotion Control

Locomotion Controller Modules (Loco)



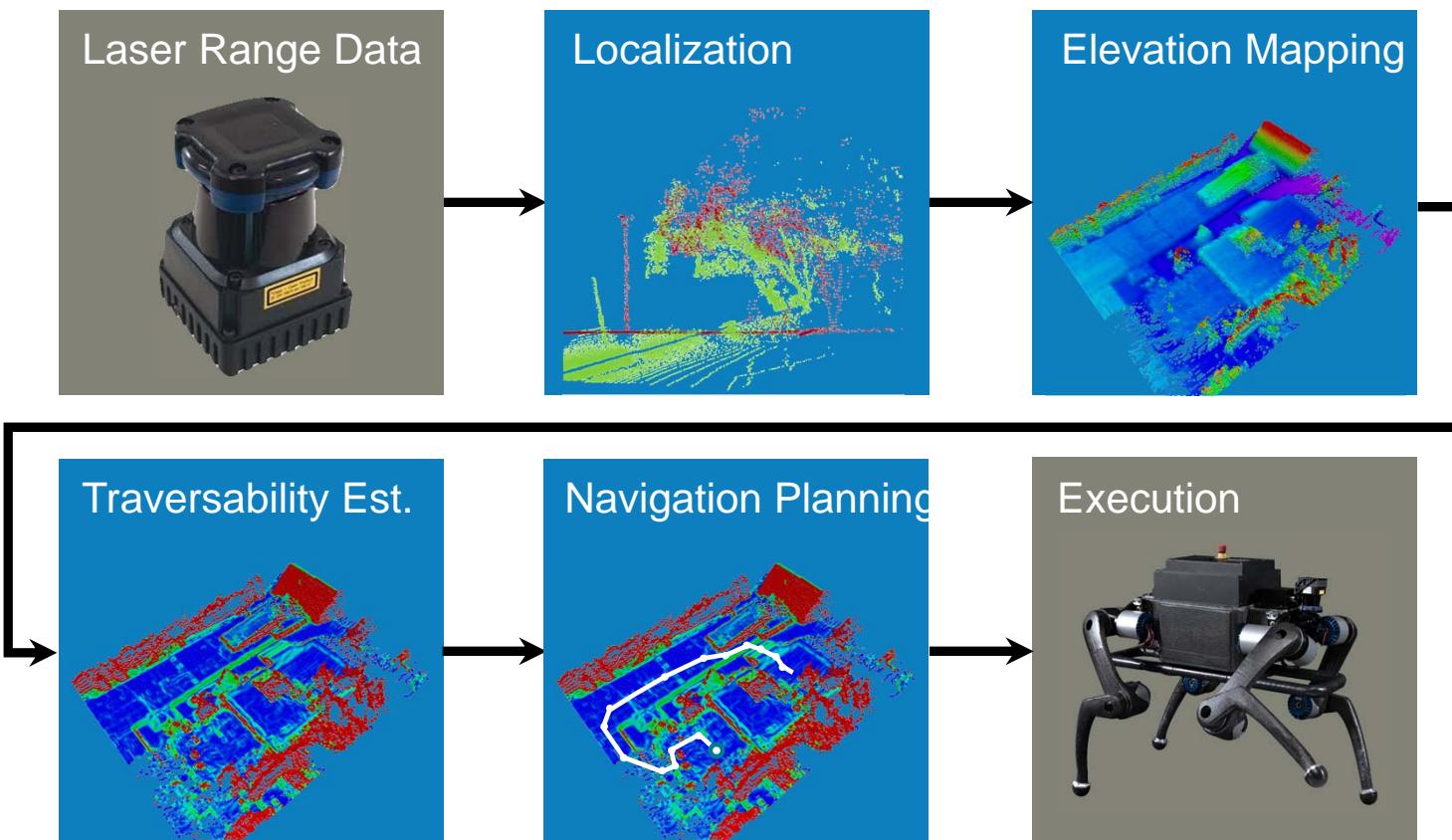
Robot Controller Manager (Rocoma)



C. Gehring, S. Coros, M. Hutter, D. Bellicoso, H. Heijnen, R. Diethelm, M. Bloesch, P. Fankhauser, J. Hwangbo, M. A. Hoeplinger, and R. Siegwart, “**Practice Makes Perfect: An Optimization-Based Approach to Controlling Agile Motions for a Quadruped Robot.**”, in IEEE Robotics & Automation Magazine, 2016.

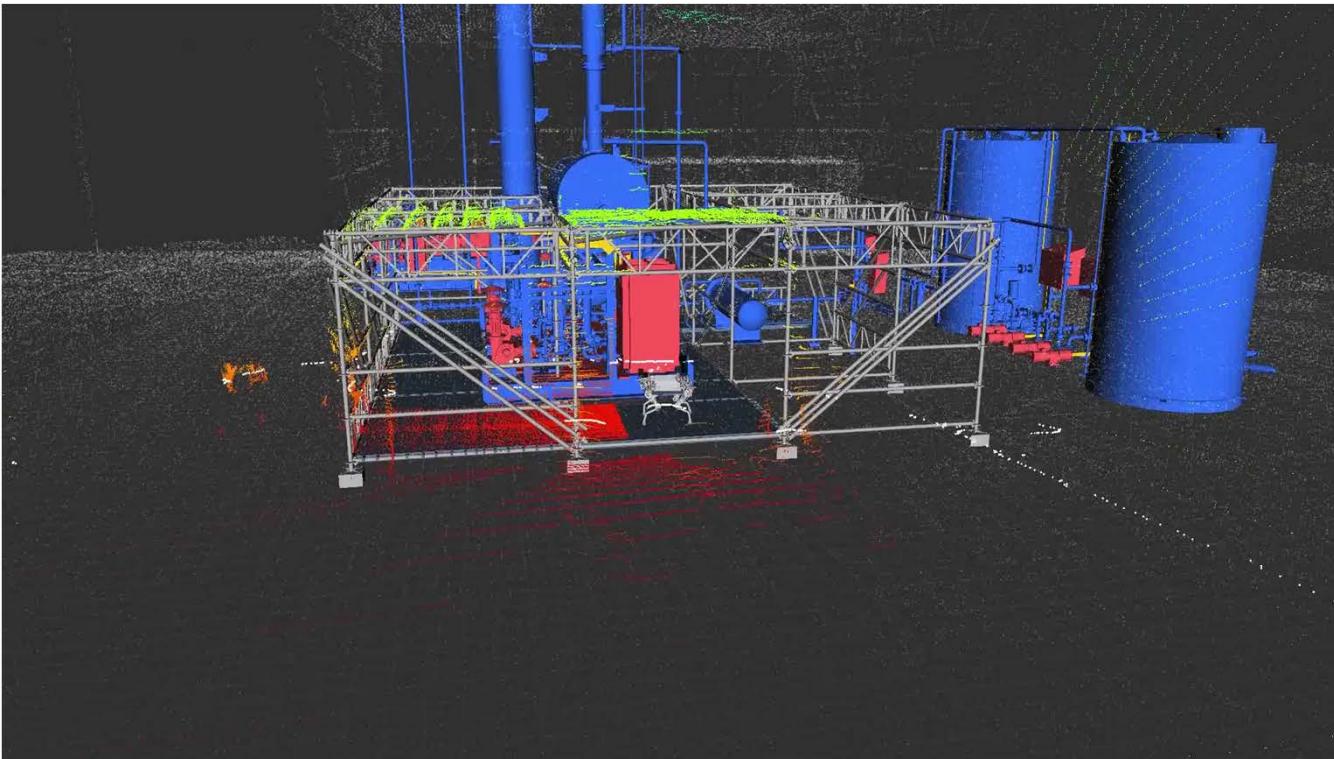
C. Dario Bellicoso, C. Gehring, J. Hwangbo, P. Fankhauser, M. Hutter, “**Emerging Terrain Adaptation from Hierarchical Whole Body Control,**” in IEEE Internal Conference on Humanoid Robots (Humanoids), 2016.

# Navigation



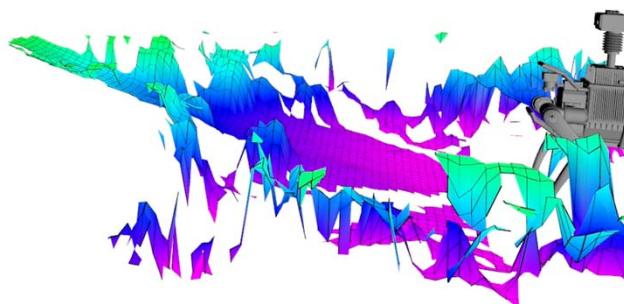
# Navigation

## ICP Localization



- Point cloud registration for localization in reference map
- Full rotation of LiDAR is aggregated for point cloud
- Use of existing maps or online mapping

# Navigation Elevation Mapping – Dense Terrain Mapping

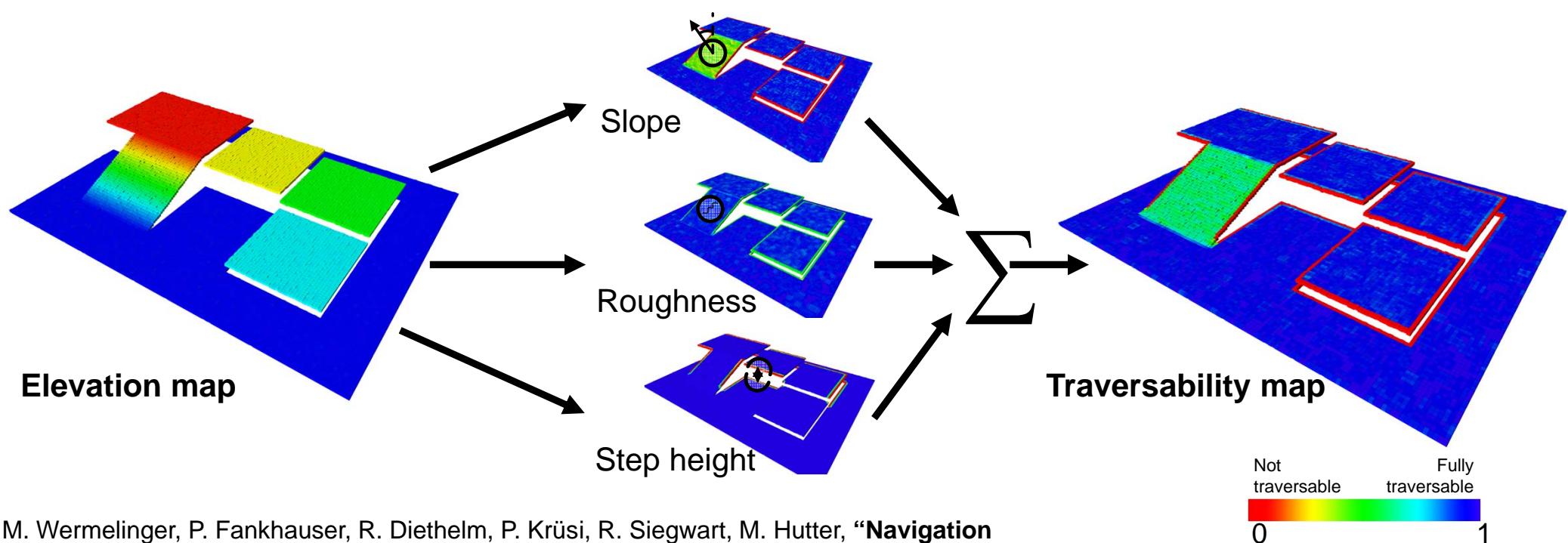


- Probabilistic fusion of range measurements and pose estimation
- Explicitly handles drift of state estimation (robot-centric)
- Input data from laser, Kinect, stereo cameras, Velodyne etc.

P. Fankhauser, M. Bloesch, C. Gehring, M. Hutter, R. Siegwart “**Robot-Centric Elevation Mapping with Uncertainty Estimates**,” in International Conference on Climbing and Walking Robots (CLAWAR), 2014.

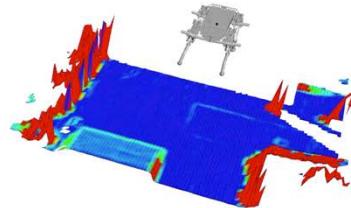
# Navigation

## Traversability estimation



M. Wermelinger, P. Fankhauser, R. Diethelm, P. Krüsi, R. Siegwart, M. Hutter, “**Navigation Planning for Legged Robots in Challenging Terrain**,” in IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS), 2016.

# Navigation Planning



- Online navigation planning based on RRT\* (OMPL)
- Works with and without initial map
- Continuous for changing environments

M. Wermelinger, P. Fankhauser, R. Diethelm, P. Krüsi, R. Siegwart, M. Hutter, “**Navigation Planning for Legged Robots in Challenging Terrain**,” in IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS), 2016.

# Collaborative Navigation

## Vision based localization



# Inspection

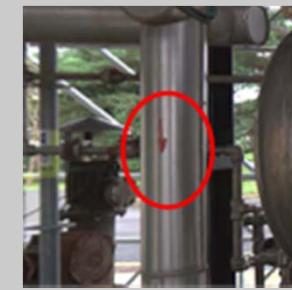
Visual inspection



Pressure &amp; Level gauges



Thermal Inspection



Thermal points



Pumps



Gas leaks

Platform alarm

Auditive Inspection

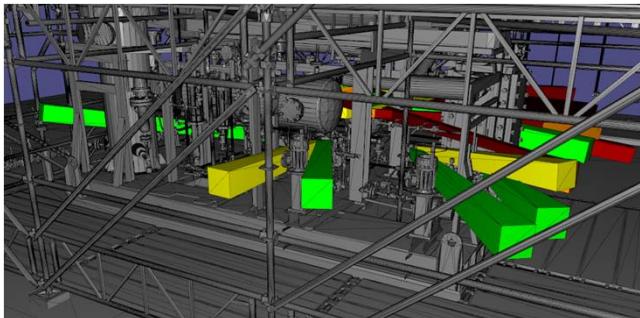


Microphones (audible and ultra-sonic)

# Inspection

## Visual inspection of pressure gauges

Automatic view point generation



Visual servoing



Indicator reading



→ Reading ok

Whole-body camera positioning

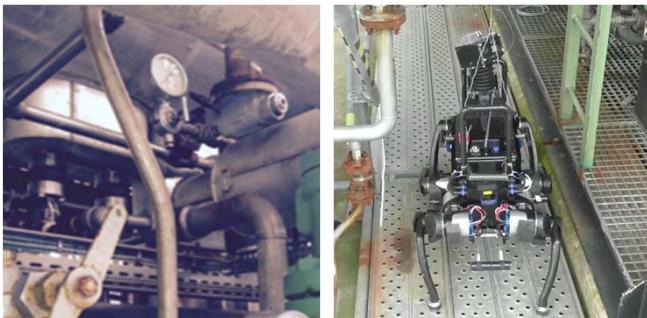
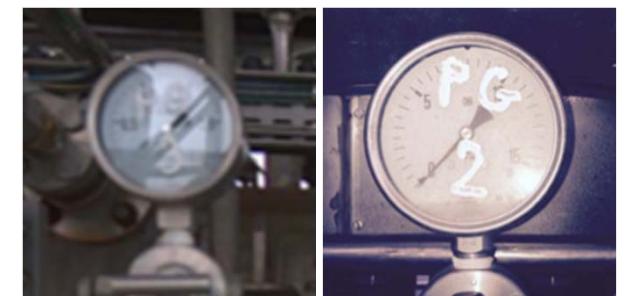
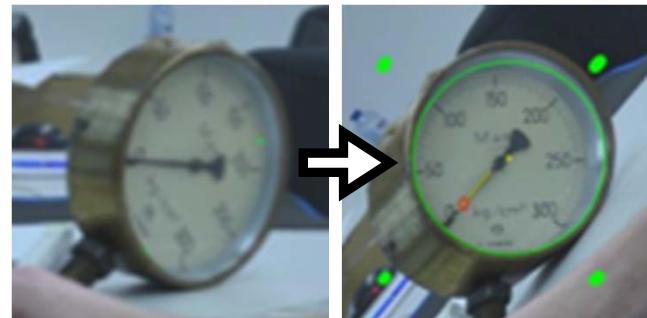


Image de-warping



→ Reading unsuccessful, try alternative position or report as unknown

S. Bachmann, "Visual Inspection of Manometers and Valve Levers", Master's Thesis, ETH Zurich, 2015.