

LIE GROUP NOTATIONS

position – orientation	standard representation $\mathbf{g} = \begin{pmatrix} \mathbf{R} & \mathbf{u} \\ 0 & 1 \end{pmatrix} \in SE(3)$	Adjoint and coAdjoint representation $Ad_{\mathbf{g}} = \begin{pmatrix} \mathbf{R} & 0 \\ \tilde{\mathbf{u}}\mathbf{R} & \mathbf{R} \end{pmatrix}, Ad_{\mathbf{g}}^* = \begin{pmatrix} \mathbf{R} & \tilde{\mathbf{u}}\mathbf{R} \\ 0 & \mathbf{R} \end{pmatrix} \in \mathbb{R}^{6 \times 6}$
velocity (body frame)	Lie Algebra element $\mathbf{g}^{-1}\dot{\mathbf{g}} = \hat{\boldsymbol{\eta}} = \begin{pmatrix} \tilde{\mathbf{w}} & \mathbf{v} \\ 0 & 0 \end{pmatrix} \in \mathfrak{se}(3)$	adjoint and coadjoint map $ad_{\boldsymbol{\eta}} = \begin{pmatrix} \tilde{\mathbf{w}} & 0 \\ \tilde{\mathbf{v}} & \tilde{\mathbf{w}} \end{pmatrix}, ad_{\boldsymbol{\eta}}^* = \begin{pmatrix} \tilde{\mathbf{w}} & \tilde{\mathbf{v}} \\ 0 & \tilde{\mathbf{w}} \end{pmatrix} \in \mathbb{R}^{6 \times 6}$
	twist vector $\boldsymbol{\eta} = \begin{bmatrix} \mathbf{w} \\ \mathbf{v} \end{bmatrix} \in \mathbb{R}^6$	
strain (body frame)	Lie Algebra element $\mathbf{g}^{-1}\mathbf{g}' = \hat{\boldsymbol{\xi}} = \begin{pmatrix} \tilde{\mathbf{k}} & \mathbf{p} \\ 0 & 0 \end{pmatrix} \in \mathfrak{se}(3)$	adjoint and coadjoint map $ad_{\boldsymbol{\xi}} = \begin{pmatrix} \tilde{\mathbf{k}} & 0 \\ \tilde{\mathbf{p}} & \tilde{\mathbf{k}} \end{pmatrix}, ad_{\boldsymbol{\xi}}^* = \begin{pmatrix} \tilde{\mathbf{k}} & \tilde{\mathbf{p}} \\ 0 & \tilde{\mathbf{k}} \end{pmatrix} \in \mathbb{R}^{6 \times 6}$
	twist vector $\boldsymbol{\xi} = \begin{bmatrix} \mathbf{k} \\ \mathbf{p} \end{bmatrix} \in \mathbb{R}^6$	

