Annotated Type Rules

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1 Type system

Below you will find Figure 1, which describes the annotated type rules for the control flow analysis (CFA) for our extended lambda calculus language for the second assignment of Automatic Program Analysis at Utrecht University.

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\widehat{\Gamma} \vdash_{\text{CFA}} \underline{c} : \widehat{\tau}_c \ [con]
                                                                                                                                              \frac{\widehat{\Gamma}(x) = \widehat{\tau}}{\widehat{\Gamma} \vdash_{CFA} x : \widehat{\tau}} [var]
                                                                               \frac{\widehat{\Gamma}\left[x\mapsto\widehat{\boldsymbol{\tau}}_{x}\right]\vdash_{\mathrm{CFA}}e_{1}:\widehat{\boldsymbol{\tau}}_{0}}{\widehat{\Gamma}\vdash_{\mathrm{CFA}}\mathbf{f}\mathbf{n}_{\pi}\ x\Rightarrow e_{1}:\widehat{\boldsymbol{\tau}}_{x}\xrightarrow{\{\pi\}\cup\varphi}\widehat{\boldsymbol{\tau}}_{0}}\left[fn\right]
                                               \frac{\widehat{\Gamma}\left[f \mapsto \widehat{\tau_x} \xrightarrow{\{\pi\} \cup \varphi} \widehat{\tau_0}\right] \left[x \mapsto \widehat{\tau_x}\right] \vdash_{\text{CFA}} e_1 : \widehat{\tau_0}}{\widehat{\Gamma} \vdash_{\text{CFA}} \mathbf{fun}_{\pi} f \ x \Rightarrow e_1 : \widehat{\tau_x} \xrightarrow{\{\pi\} \cup \varphi} \widehat{\tau_0}} [fun]
                                                               \frac{\widehat{\Gamma} \vdash_{\text{CFA}} e_1 : \widehat{\tau}_2 \xrightarrow{\varphi} \widehat{\tau}_0 \qquad \widehat{\Gamma} \vdash_{\text{CFA}} e_2 : \widehat{\tau}_2}{\widehat{\Gamma} \vdash_{\text{CFA}} e_1 e_2 : \widehat{\tau}_0} [app]
                               \frac{\widehat{\Gamma} \vdash_{\text{CFA}} e_1 : \underline{\textit{Bool}} \qquad \widehat{\Gamma} \vdash_{\text{CFA}} e_2 : \widehat{\tau} \qquad \widehat{\Gamma} \vdash_{\text{CFA}} e_3 : \widehat{\tau}}{\widehat{\Gamma} \vdash_{\text{CFA}} \text{ if } e_1 \text{ then } e_2 \text{ else } e_3 : \widehat{\tau}} \left[ if \right]
                                                          \frac{\widehat{\Gamma} \vdash_{\text{CFA}} e_1 : \widehat{\pmb{\tau}_1} \qquad \widehat{\Gamma} \left[ x \mapsto \widehat{\pmb{\tau}_1} \right] \vdash_{\text{CFA}} e_2 : \widehat{\pmb{\tau}_2}}{\widehat{\Gamma} \vdash_{\text{CFA}} \mathbf{let} \ x = e_1 \ \mathbf{in} \ e_2 : \widehat{\pmb{\tau}_2}} \left[ \mathit{let} \right]
                                                                                \frac{\widehat{\Gamma} \vdash_{\text{CFA}} e_1 : \widehat{\tau}_{op}^1 \qquad \widehat{\Gamma} \vdash_{\text{CFA}} e_2 : \widehat{\tau}_{op}^2}{\widehat{\Gamma} \vdash_{\text{CFA}} e_1 \underset{op}{op} e_2 : \widehat{\tau}_{op}} [op]
\frac{\widehat{\Gamma} \vdash_{\text{CFA}} e_1 : \widehat{\boldsymbol{\tau}_1} \qquad \forall i :: \widehat{\Gamma} \vdash_{\text{CFA}} e_i : \widehat{\boldsymbol{\tau}_1} \qquad \forall j :: \widehat{\Gamma} \vdash_{\text{CFA}} e_j : \widehat{\boldsymbol{\tau}_0}}{\widehat{\Gamma} \vdash_{\text{CFA}} \mathbf{case} \ e_1 \ \mathbf{of} \ [e_i \ \mathbf{then} \ e_j]^+ : \widehat{\boldsymbol{\tau}_0}} \ [\mathit{case}]
                                                        \frac{\widehat{\Gamma} \vdash_{\text{CFA}} x : \widehat{\tau}_0 \qquad \widehat{\Gamma} \vdash_{\text{CFA}} xs : \widehat{\tau}_{list(\widehat{\tau}_0)}}{\widehat{\Gamma} \vdash_{\text{CFA}} (x : xs) : \widehat{\tau}_{list(\widehat{\tau}_0)}} \ [\textit{list-cons}]
                                                                                                                  \widehat{\Gamma} \vdash_{\text{CFA}} []: \widehat{\tau}_{list(\widehat{\tau}_0)} [list\text{-}nil]
                                                                                 \frac{\widehat{\Gamma} \vdash_{\text{CFA}} e_1 : \widehat{\tau}_1 \qquad \widehat{\Gamma} \vdash_{\text{CFA}} e_2 : \widehat{\tau}_2}{\widehat{\Gamma} \vdash_{\text{CFA}} (e_1, e_2) : \widehat{\tau}_{pair(\widehat{\tau}_0)}} \ [pair]
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Figure 1: Control Flow Analysis