

Artificiële Intelligentie

RCA AIG 04Q6 01 APRIL 2021



*Computational Foundations of
Machine Learning [ML]
with Python*

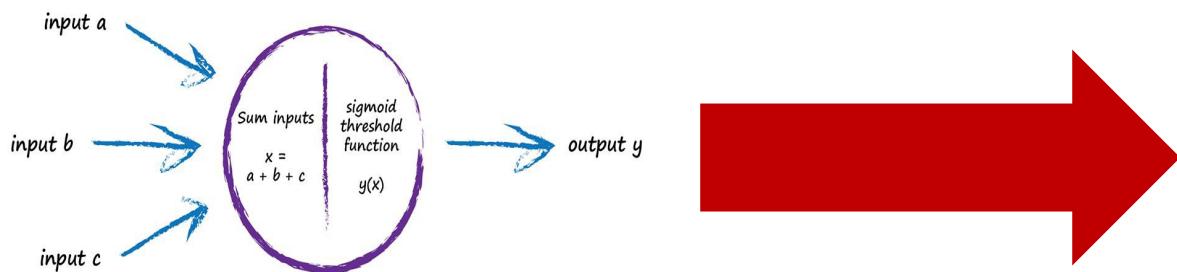
CONTEXT

- **Prerequisites:** basics in linear algebra, probability, and analysis of algorithms.
- **Workload:** homework assignments
- **GitHub:** Start a ML repository at GitHub

Lecture 03

- Basic definitions and concepts of Machine Learning (ML) PART02.
- How to get from ML concepts & Models to Python code.

THE DOT PRODUCT



```
import numpy as np
import matplotlib.pyplot as plt

class Perceptron(object):

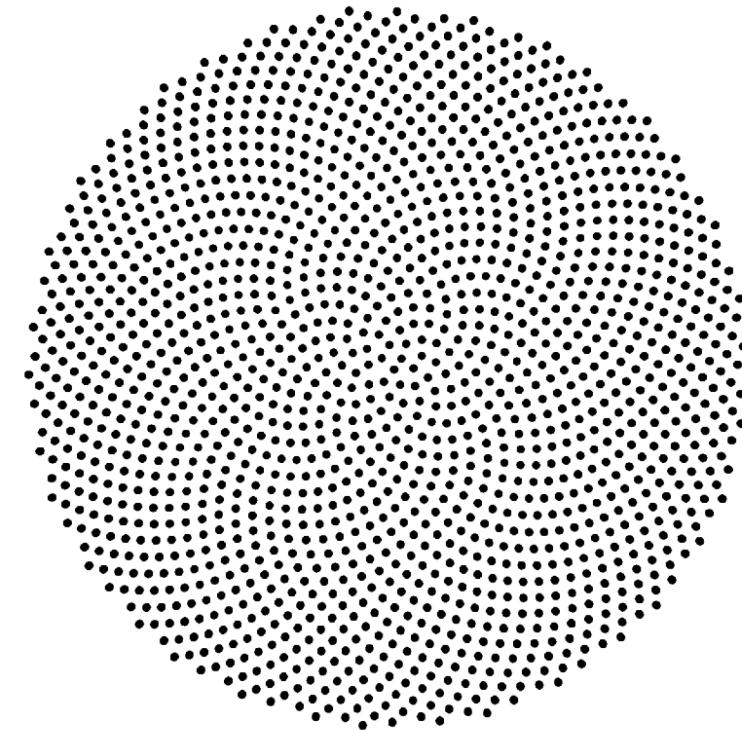
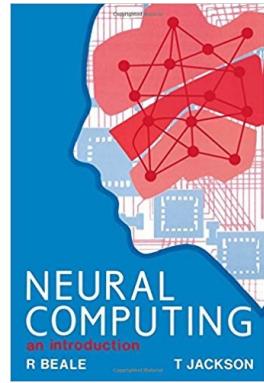
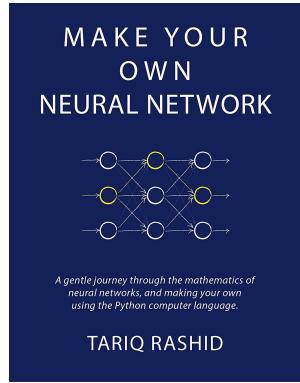
    def __init__(self, no_of_inputs, no_of_training_epochs=20, learning_rate=0.01):
        self.no_of_training_epochs = no_of_training_epochs
        self.learning_rate = learning_rate
        self.weights = np.random.normal(0, 10, no_of_inputs + 1)
        self.bias = self.weights[0]
        self.epoch_list = []
        self.error_history = []

    def step_function(self, inputs):
        netto_summation = np.dot(inputs, self.weights[1:]) + self.bias
        if netto_summation > 0:
            activation = 1
        else:
            activation = 0
        return activation

    def train(self, training_inputs, teacher_labels):
        epoch = 0;
        i = 0;
        for _ in range(self.no_of_training_epochs):
            epoch += 1
            for inputs, teacher in zip(training_inputs, teacher_labels):
                activated_perceptron_output = self.step_function(inputs)
                error = (teacher - activated_perceptron_output)
                self.weights[1:] += self.learning_rate * (error) * inputs
                self.bias += self.learning_rate * error
                #print(teacher, activated_perceptron_output)
                i += 1
            self.epoch_list.append(epoch)
            self.error_history.append(np.sum(np.abs(error)))
            #print("iteration = ", i, " epoch = ", epoch, ' error: ', error, ' weights: ', self.weights[1:])
```

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Fundamentals



Key-words / Concepts / Labels

Artificial neuron === Model of single biological neuron / Perceptron

Feedforward / Feed-backward / Hebbian learning

Bias / Threshold

Weights /adjustable parameters / Memory

Unit / Node / Activation Functions (Sigmoid / Step)

Input / Output / Layers / Input vs Output Space

Target / Teacher / Error / learningrate

Iterations / Epochs / Baches

Logical functions AND / OR / XOR (Boolean Algebra)

PYTHON MODULES

```
import Numpy as np  
import Matlibplot.pyplot as plt
```

```
class  
def return  
for (loops)  
if else  
zip  
print  
list  
append  
  
+ =
```

Matrix Calculus

```
np.zeros  
np.random.normal  
np.dot
```

Plotting

```
plt.subplots()  
plt.subplot(221)  
plt.plot(epoch, error)  
plt.xlabel('Epoch')  
plt.ylabel('Error')
```

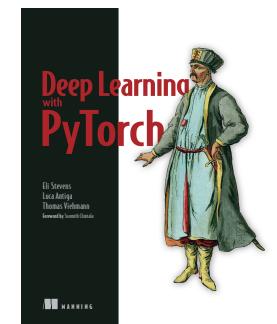
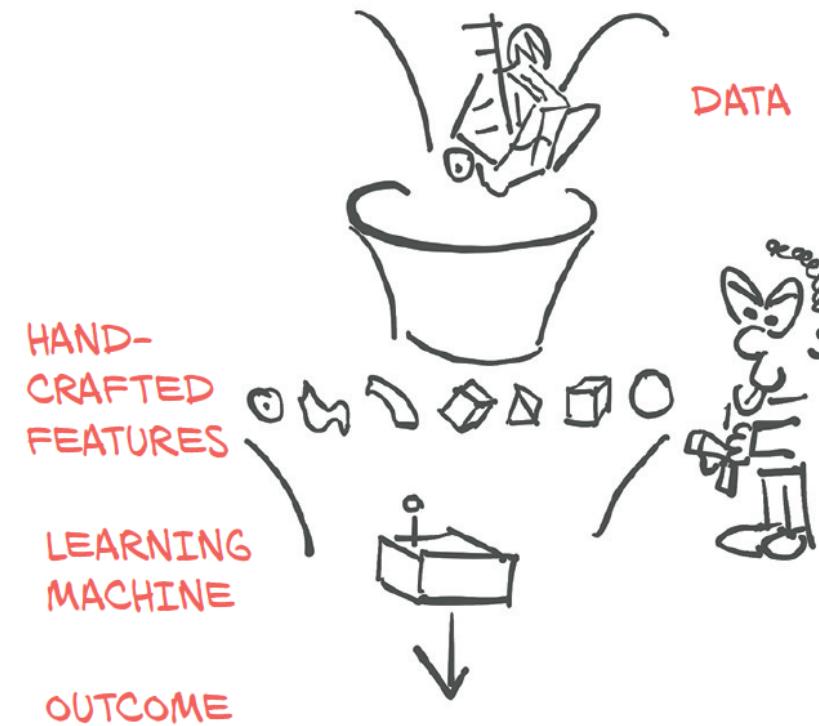
The PERCEPTRON

The perceptron was very promising, but it was soon discovered that it has serious limitations as it only works for linearly-separable classes.

In 1969, Marvin Minsky and Seymour Papert demonstrated that it could not learn even a simple logical function such as XOR.

This led to a significant decline in the interest in perceptron's and Machine learning as a whole.

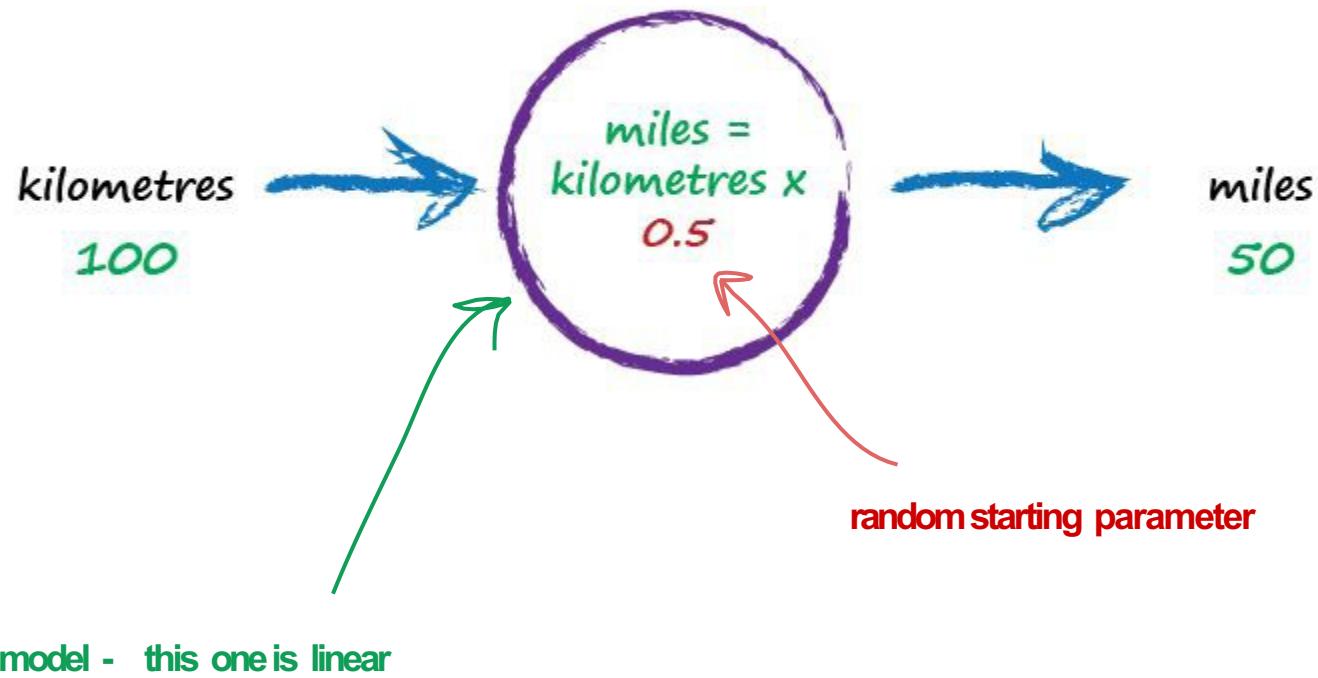
MACHINE LEARNING [ML]



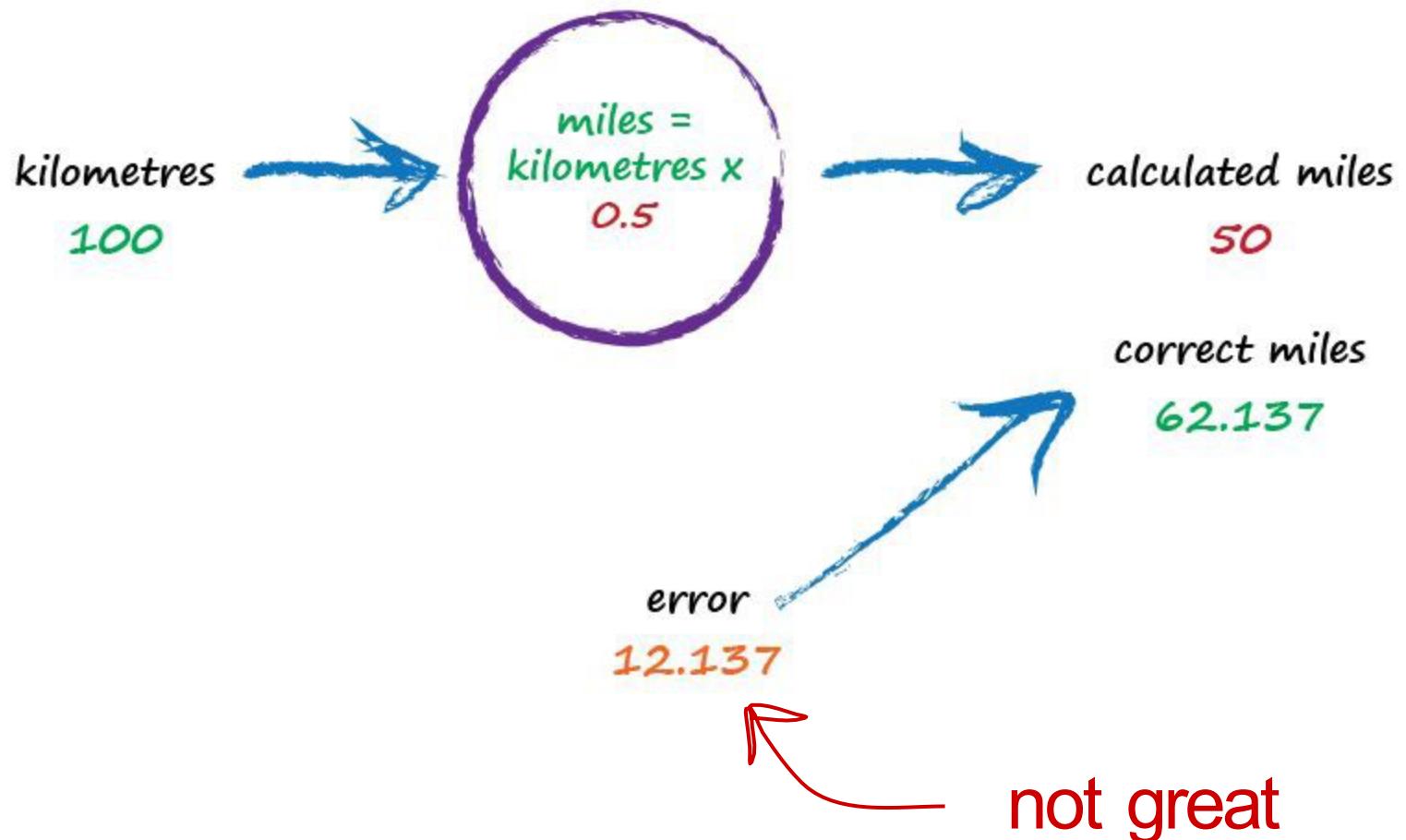
The Concept of Machine Learning



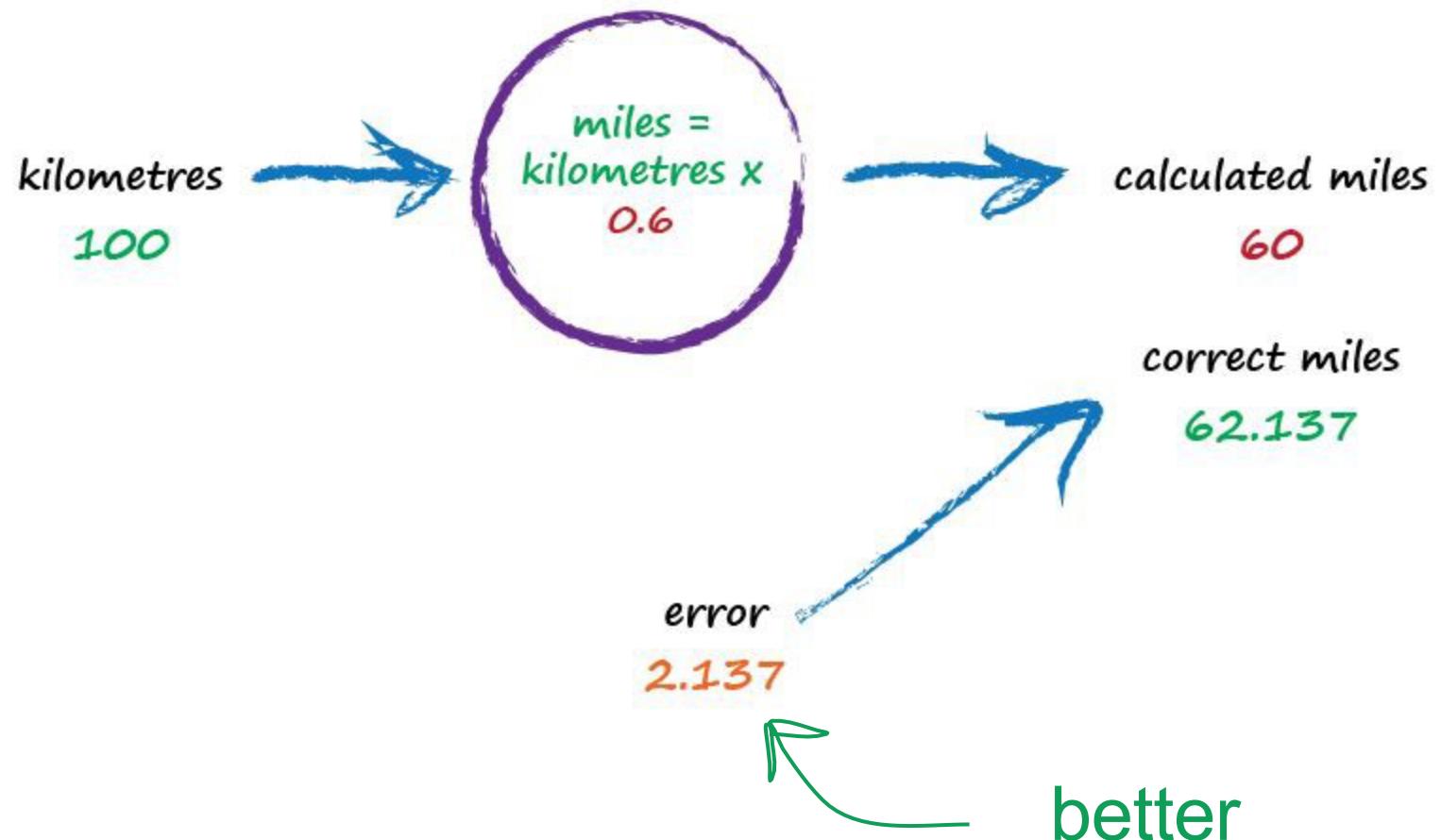
The Concept of Machine Learning



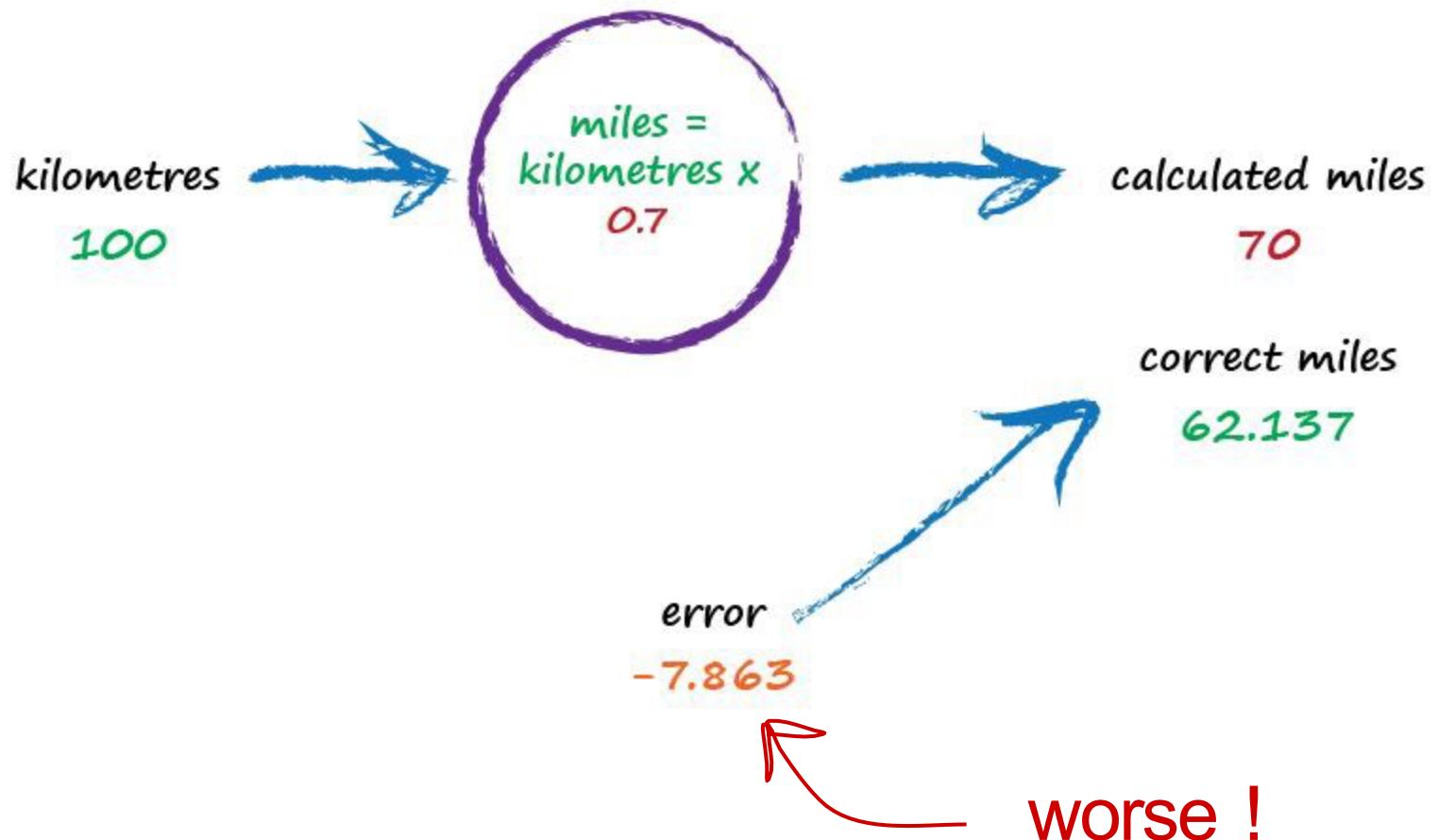
The Concept of Machine Learning



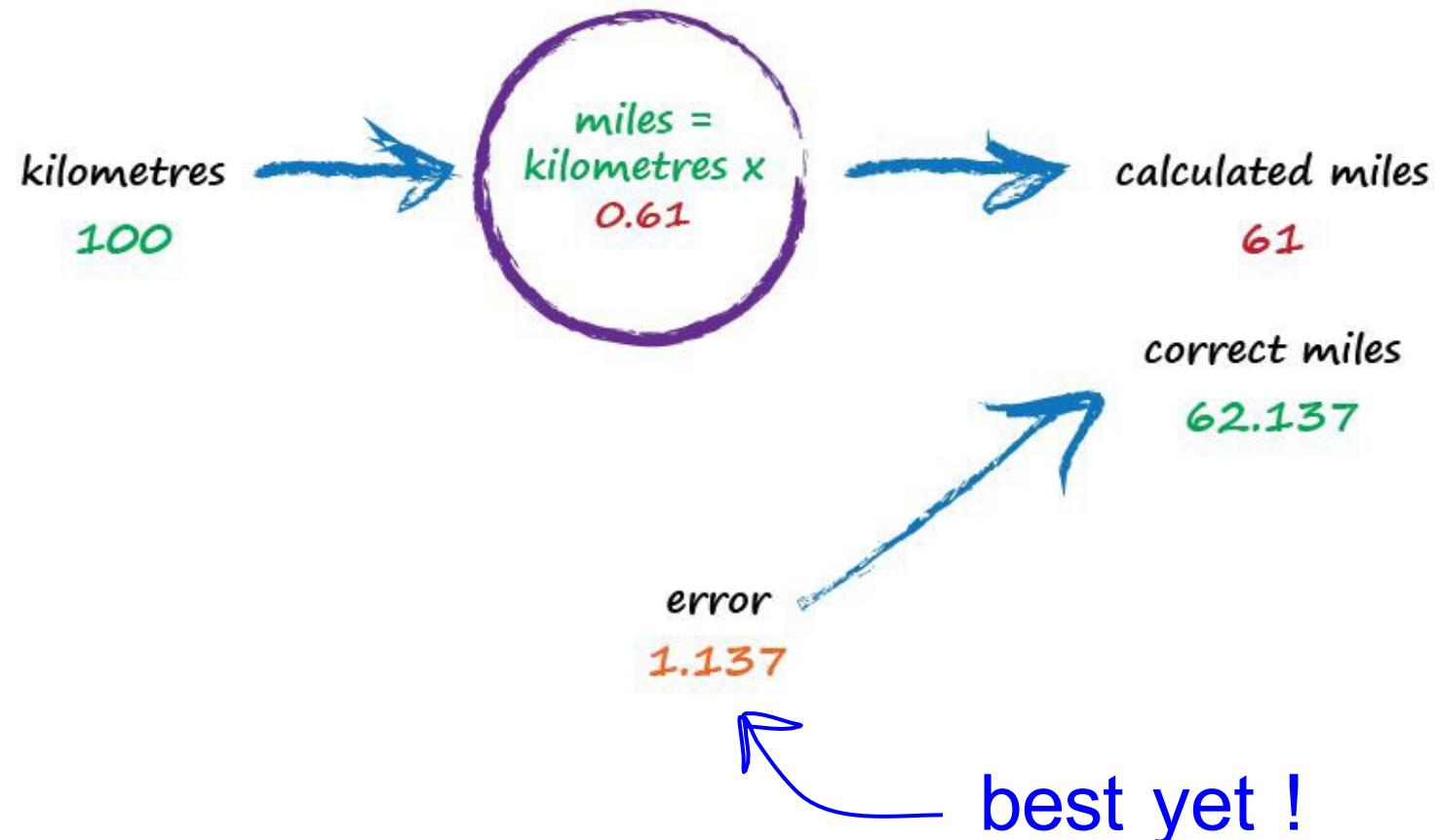
The Concept of Machine Learning



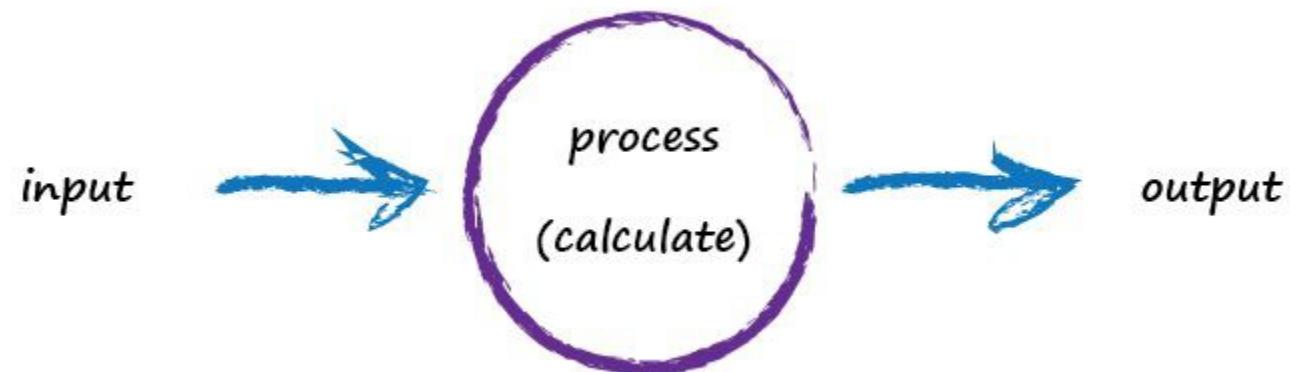
The Concept of Machine Learning



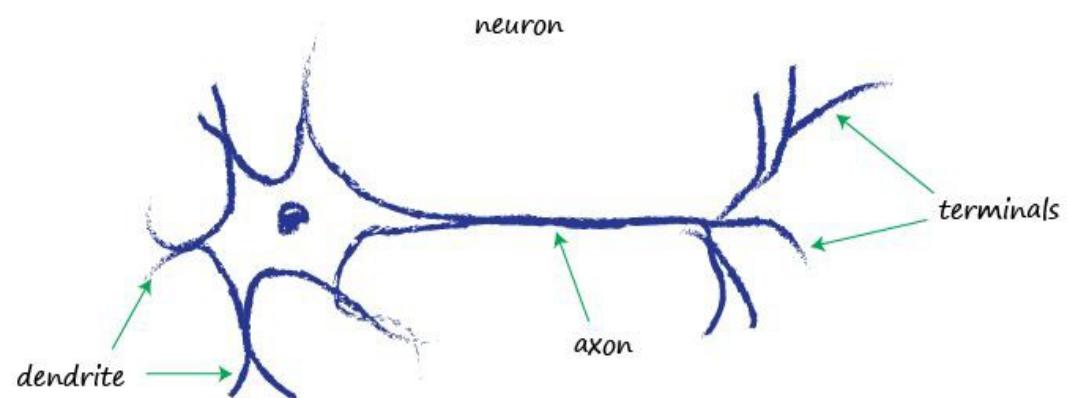
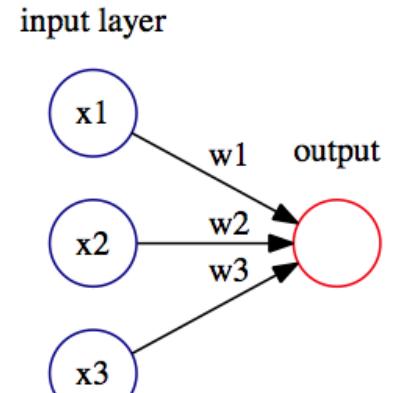
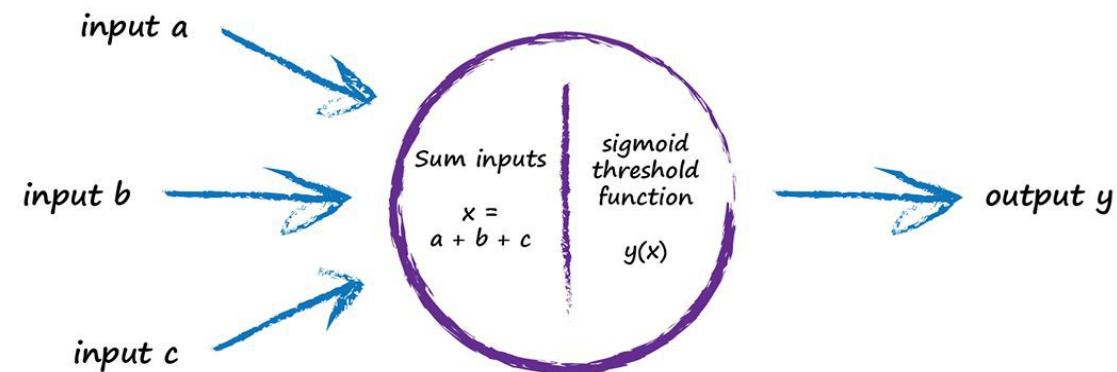
Basic Concept of Machine Learning (ML) is iterative in nature; requires a teacher & memory



The Concept of Input / Output model



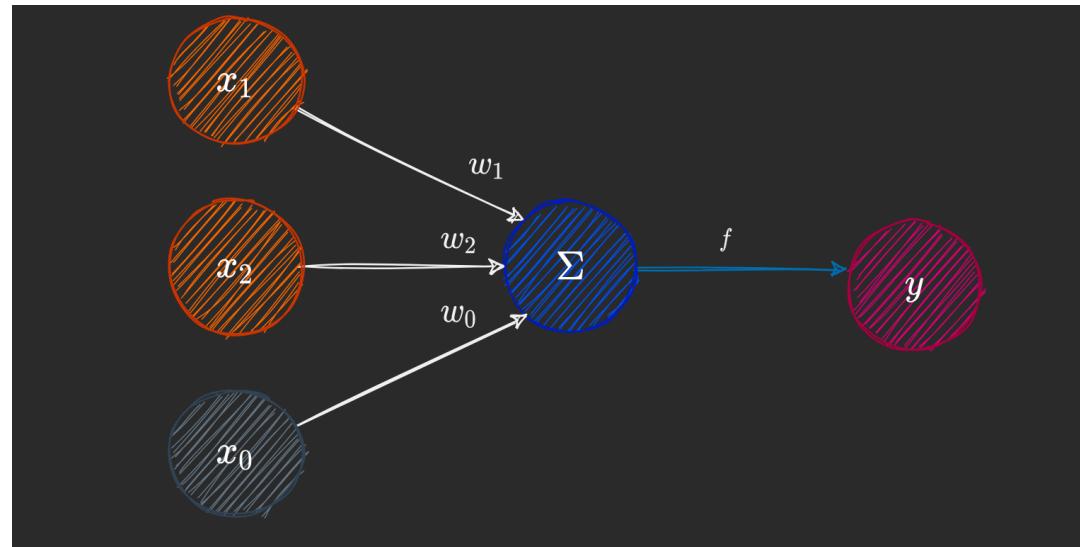
Artificial Neuron Model: input vs output



Artificial Neuron Model: PERCEPTRON structure

Perceptron Components :

- Input nodes $x_0 \dots X_n$
- Output node y
- An activation function
- Weights and biases
- Summation
- Activation Function f



FEED FORWARD
CALCULATION:

The output calculation is straightforward.

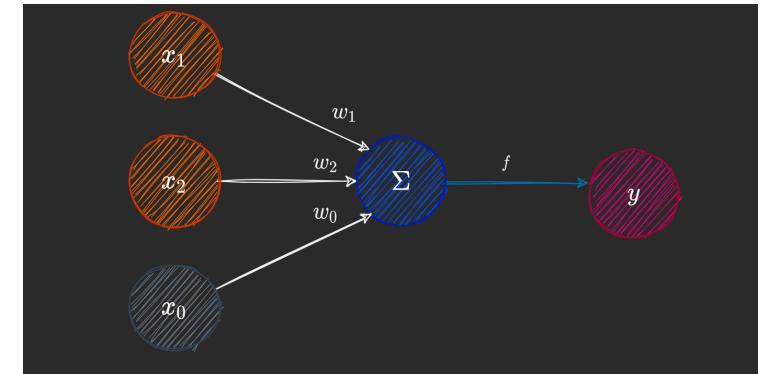
Compute the DOT PRODUCT of the input $[x_1 \ x_2]$ and weight vector $[w_1 \ w_2]$

The bias b equals w_0

Apply the activation function.

Artificial Neuron Model: PERCEPTRON maths

$$y = f(w \cdot X + b)$$



Feedforward computation:
(DOT PRODUCT is a form of mathematical summation)

$$y = f(x_1 \cdot w_1 + x_2 \cdot w_2 + b)$$

Artificial Neuron Model: PERCEPTRON maths

weights incoming signals

The diagram illustrates the mathematical operation of a perceptron. It shows two vectors: 'weights' (represented by a 2x2 matrix) and 'incoming signals' (represented by a 2x1 vector). A green arrow labeled 'weights' points to the first column of the matrix. Another green arrow labeled 'incoming signals' points to the first column of the vector. An equals sign follows the multiplication, leading to the resulting vector where each element is the sum of the products of corresponding elements from the weight matrix and the incoming signal vector.

$$\begin{pmatrix} w_{1,1} & w_{2,1} \\ w_{1,2} & w_{2,2} \end{pmatrix} \begin{pmatrix} \text{input_1} \\ \text{input_2} \end{pmatrix} = \begin{pmatrix} (\text{input_1} * w_{1,1}) + (\text{input_2} * w_{2,1}) \\ (\text{input_1} * w_{1,2}) + (\text{input_2} * w_{2,2}) \end{pmatrix}$$

$$\mathbf{W} \cdot \mathbf{I} = \mathbf{X}$$

dot product

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Fundamentals

"Dot Product"

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix} \times \begin{bmatrix} 7 & 8 \\ 9 & 10 \\ 11 & 12 \end{bmatrix} = \begin{bmatrix} 58 \end{bmatrix}$$

The "Dot Product" is where we **multiply matching members**, then sum up:

$$(1, 2, 3) \bullet (7, 9, 11) = 1 \times 7 + 2 \times 9 + 3 \times 11 \\ = 58$$

We match the 1st members (1 and 7), multiply them, likewise for the 2nd members (2 and 9) and the 3rd members (3 and 11), and finally sum them up.

Want to see another example? Here it is for the 1st row and **2nd column**:

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix} \times \begin{bmatrix} 7 & 8 \\ 9 & 10 \\ 11 & 12 \end{bmatrix} = \begin{bmatrix} 58 & 64 \end{bmatrix}$$

$$(1, 2, 3) \bullet (8, 10, 12) = 1 \times 8 + 2 \times 10 + 3 \times 12 \\ = 64$$

np.dot()**1D + Scalar**

[1 2 3] ✘ 10

[10 20 30]

1D + 1D[-1
-2
-3]

[1 2 3] ✘

-14

1D + 2D[[2 2 2]
[1 1 1]]

[1 -1]

✘

[1 1 1]

2D + 2D[[-1 -1]
[1 1]][[2 2]
[1 1]]

✘

[[0 0]
[0 0]]

$$a \cdot b = \begin{bmatrix} a_1 & a_2 & a_3 & a_4 & a_5 \end{bmatrix}_{(1 \times n)} \begin{bmatrix} b_1 \\ b_2 \\ b_3 \\ b_4 \\ b_5 \end{bmatrix}_{(n \times 1)} = \left\{ a_1b_1 + a_2b_2 + a_3b_3 + a_4b_4 + a_5b_5 \right\}$$

Dot Product

```
a = np.array([3, 5, 6])
b = np.array([23, 15, 1])

np.dot(a, b)
```

Boolean Logic

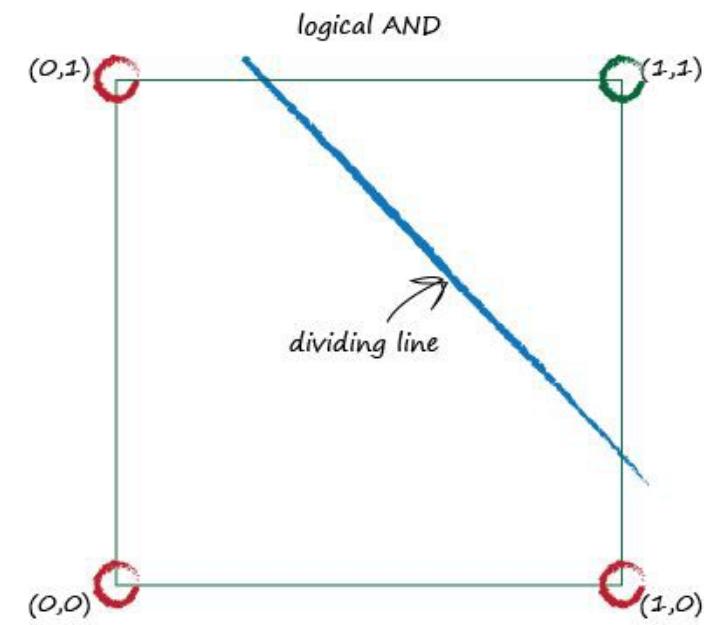


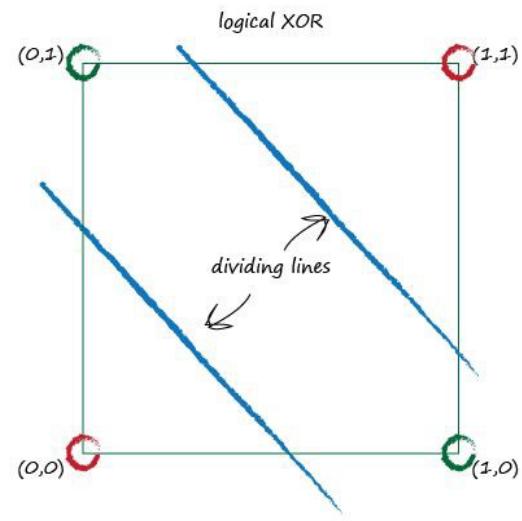
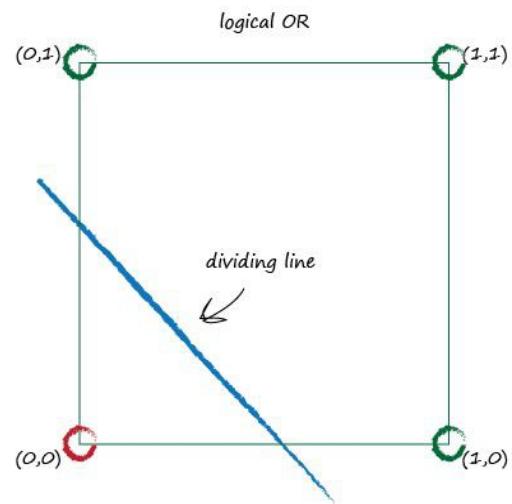
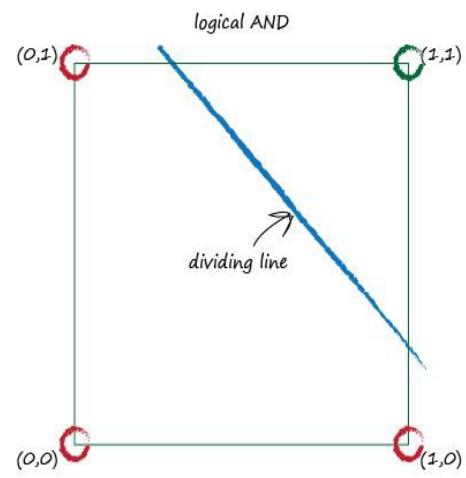
IF I have eaten my vegetables **AND** I am still hungry
THEN I can have ice cream.

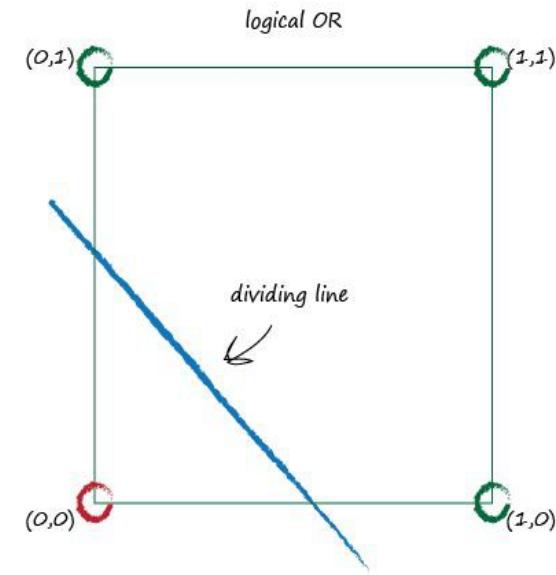
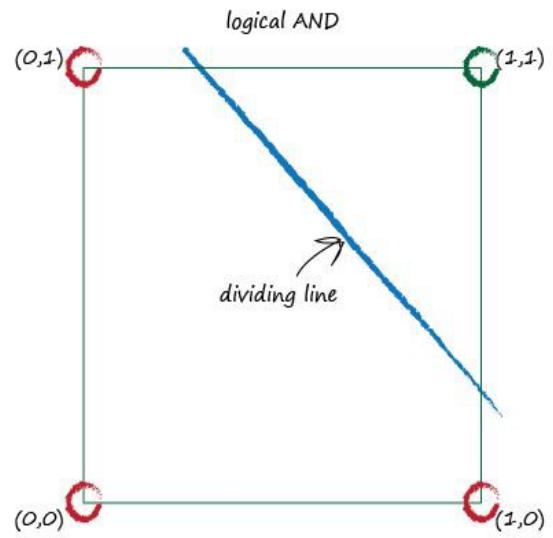
IF it's the weekend **OR** I am on annual leave **THEN** I'll go to the park.

Input A	Input B	AND	OR
0	0	0	0
0	1	0	1
1	0	0	1
1	1	1	1

Input x1	Input x2	AND y
0	0	0
0	1	0
1	0	0
1	1	1







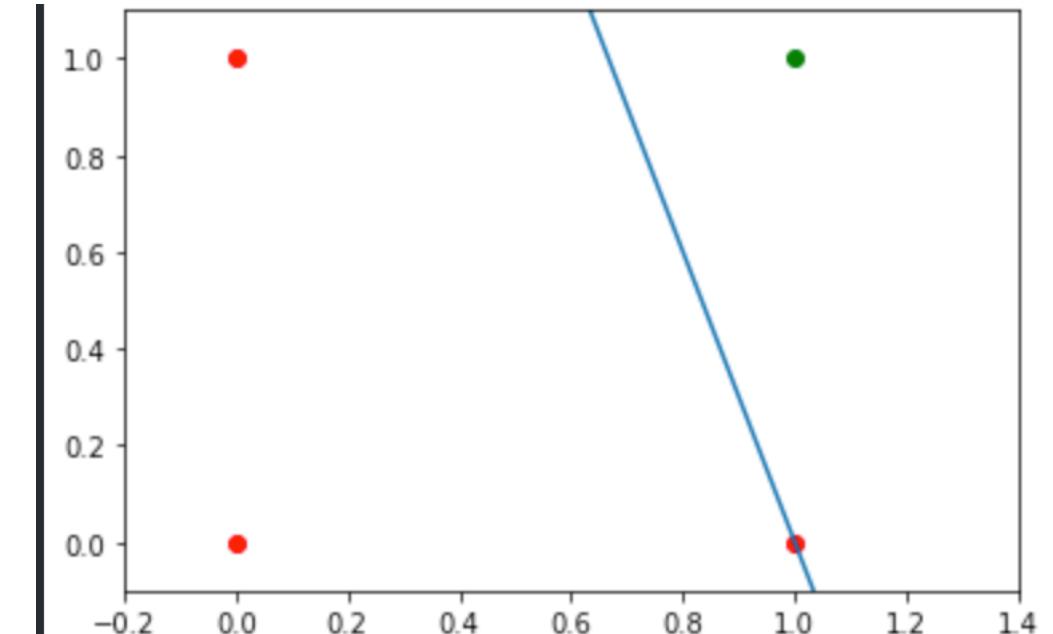
Class₁: $w \cdot X + b \geq 0$

Class₂: $w \cdot X + b < 0$

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Fundamentals

```
p = Perceptron(weights=[0.3, 0.3, 0.3],  
                learning_rate=0.2)  
  
for in_data, label in labelled_samples(30):  
    p.adjust(label,  
             in_data)  
  
test_data, test_labels = list(zip(*labelled_samples(30)))  
  
evaluation = p.evaluate(test_data, test_labels)  
print(evaluation)  
  
  
fig, ax = plt.subplots()  
xmin, xmax = -0.2, 1.4  
X = np.arange(xmin, xmax, 0.1)  
ax.scatter(0, 0, color="r")  
ax.scatter(0, 1, color="r")  
ax.scatter(1, 0, color="r")  
ax.scatter(1, 1, color="g")  
ax.set_xlim([xmin, xmax])  
ax.set_ylim([-0.1, 1.1])  
m = -p.weights[0] / p.weights[1]  
c = -p.weights[2] / p.weights[1]  
print(m, c)  
ax.plot(X, m * X + c )  
plt.plot()
```



PYTHON PERCEPTRON MODEL code

```
import Numpy as np  
import Matlibplot.pyplot as plt
```

Learn how to specify: input/output relationship

Initialize weights

Forward computation

```

import numpy as np
import matplotlib.pyplot as plt

class Perceptron(object):

    def __init__(self, no_of_inputs, no_of_training_epochs=20, learning_rate=0.01):
        self.no_of_training_epochs = no_of_training_epochs
        self.learning_rate = learning_rate
        self.weights = np.random.normal(0, 10, no_of_inputs + 1)
        self.bias = self.weights[0]
        self.epoch_list = []
        self.error_history = []

    def step_function(self, inputs):
        netto_summation = np.dot(inputs, self.weights[1:]) + self.bias
        if netto_summation > 0:
            activation = 1
        else:
            activation = 0
        return activation

    def train(self, training_inputs, teacher_labels):
        epoch = 0;
        i = 0;
        for _ in range(self.no_of_training_epochs):
            epoch += 1
            for inputs, teacher in zip(training_inputs, teacher_labels):
                activated_perceptron_output = self.step_function(inputs)
                error = (teacher - activated_perceptron_output)
                self.weights[1:] += self.learning_rate * (error) * inputs
                self.bias += self.learning_rate * error
            i += 1
            self.epoch_list.append(epoch)
            self.error_history.append(np.sum(np.abs(error)))

```

PYTHON PERCEPTRON MODEL code

import Numpy as np
 import Matlibplot.pyplot as plt

Where are input & ouput specified?

Where are the weights initialized?

How is the Forward computation specified?

To Do:

Change the code as to print
 Iteration number

Bach number

Error

And weights

PYTHON INPUT / OUTPUT relationship code

```
import Numpy as np
import Matlibplot.pyplot as plt

import numpy as np

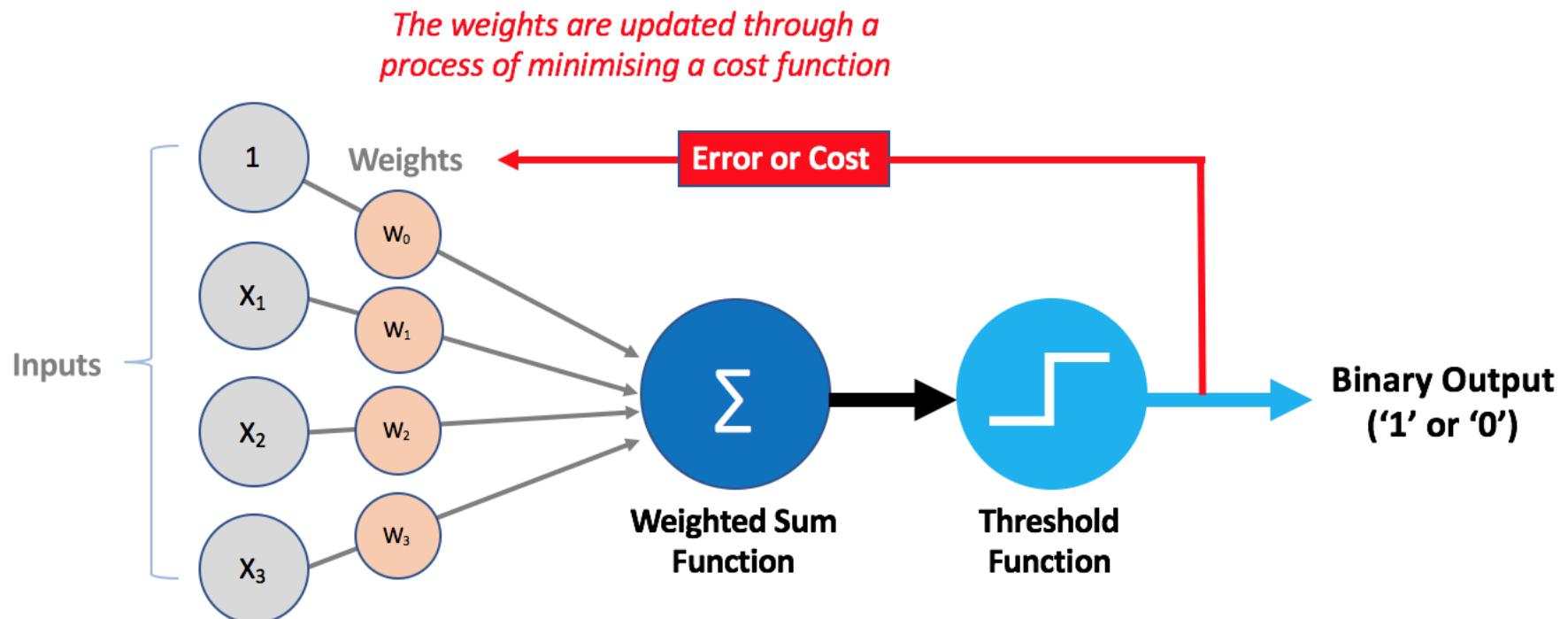
inputs = []
inputs.append(np.array([1, 1]))
inputs.append(np.array([1, 0]))
inputs.append(np.array([0, 1]))
inputs.append(np.array([0, 0]))

teacher = np.array([1, 0, 0, 0])
```

USING ZIP

```
print([inputs for teacher in zip(inputs, teacher)])  
print([i for i in zip(inputs, teacher)])
```

NEXT WEEK:



Artificial Neuron Model: PERCEPTRON maths

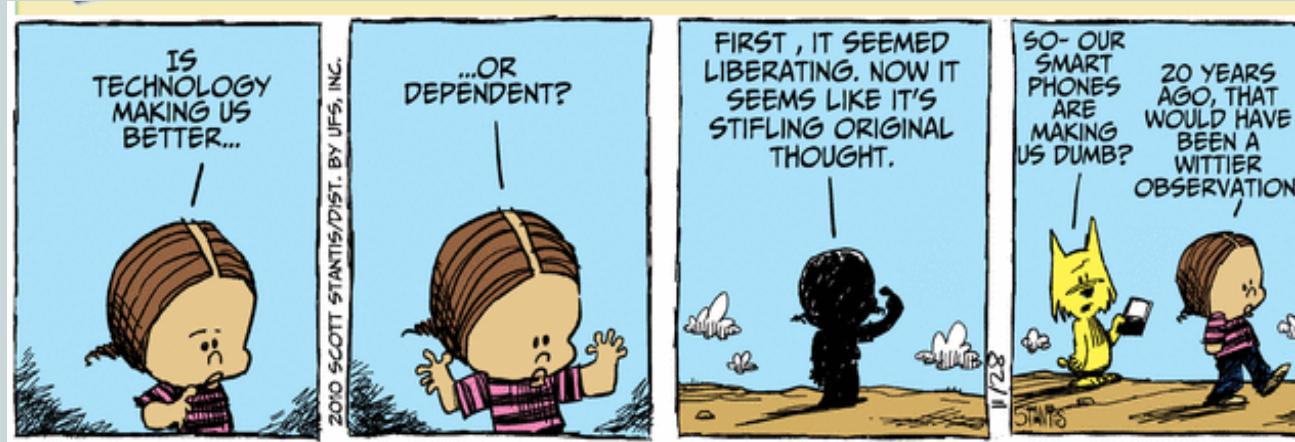
$$\Delta w = node \cdot (actual - computed)$$

Error calculation

Artificial Neuron Model: PERCEPTRON maths

$$\cancel{w_{updated} = w_{old} + lr \cdot \Delta w}$$

FEED FORWARD calculation



This lesson was developed by:

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OKT 2020

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