## Chapter 1

## **Proofs of Parser Laws**

The approach taken to prove the following parser laws for parsley is via equational reasoning on gigaparsec semantics, under the assumption that their semantics are equivalent. While there is no formal proof of this equivalence at the present, gigaparsec was designed to have semantics equivalent to parsley's.

## 1.1 Left absorption for fmap

```
f <$> empty
{ applicative functor law }
pure f <*> empty
{ definition of <*> }
liftA2 ($) (pure f) empty
{ semantics of liftA2 }
Parsec \$ \lambdast ok err \rightarrow
  let ok' x st' = (unParsec empty) st' (ok . (x $)) err
  in (unParsec $ pure f) st ok' err
  { semantics of empty }
Parsec \$ \lambdast ok err \rightarrow
  let ok' x st' = (unParsec $ raise (`emptyErr` 0)) st' (ok . (x $)) err
  in (unParsec $ pure f) st ok' err
  { semantics of raise }
Parsec \$ \lambdast ok err \rightarrow
  let ok' x st' = (unParsec \ Parsec \ \lambdast'' \ bad \rightarrow
    useHints bad (emptyErr st'' 0) st') st' (ok . (x \$)) err
  in (unParsec $ pure f) st ok' err
  { \beta-reduction }
Parsec \$ \lambdast ok err \rightarrow
  let ok' x st' = useHints err (emptyErr st' 0) st'
  in (unParsec $ pure f) st ok' err
 { semantics of pure }
Parsec \$ \lambdast ok err \rightarrow
  let ok' x st' = useHints err (emptyErr st' 0) st'
  in (unParsec $ Parsec $ \lambda st'' \circ k'' \longrightarrow ok'' f st'') st ok' err
  \{\beta-reduction \}
Parsec \$ \lambdast ok err \rightarrow
  let ok' x st' = useHints err (emptyErr st' 0) st'
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Rocco Jiang

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in ok' f st

= { inline ok' }

Parsec $ \( \) \( \) \( \) to \( \) err → \( \) useHints \( \) err (\( \) emptyErr \( \) st \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \( \) \(
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