## Chapter 1

## **Proofs of Parser Laws**

The approach taken to prove the following parser laws for parsley is via equational reasoning on gigaparsec semantics, under the assumption that their semantics are equivalent. While there is no formal proof of this equivalence at the present, gigaparsec was designed to have semantics equivalent to parsley's.

## 1.1 Left absorption for fmap

```
f <$> empty
  { applicative functor law }
pure f <*> empty
 { definition of <*> }
liftA2 ($) (pure f) empty
  { semantics of liftA2 }
Parsec $\lambda st ok err \rightarrow
   let ok' x st' = (unParsec\ empty) st' (ok.(x \$)) err
   in (unParsec $ pure f) st ok' err
   { semantics of empty }
Parsec \$ \lambdast ok err \rightarrow
   let ok' x st' = (unParsec $ raise (`emptyErr` 0)) st' (ok . (x $)) err
   in (unParsec $ pure f) st ok' err
  { semantics of raise }
Parsec \$ \lambdast ok err \rightarrow
   let ok' x st' = (unParsec \ Parsec \ \lambdast'' \ bad \rightarrow
     useHints bad (emptyErr st'' 0) st') st' (ok . (x \$)) err
   in (unParsec $ pure f) st ok' err
   { \beta-reduction }
Parsec \$ \lambdast ok err \rightarrow
   let ok' x st' = useHints err (emptyErr st' 0) st'
   in (unParsec $ pure f) st ok' err
   { semantics of pure }
Parsec \$ \lambdast ok err \rightarrow
   let ok' x st' = useHints err (emptyErr st' 0) st'
   in (unParsec \ Parsec \ \lambda st'' ok'' \ \rightarrow ok'' \ st'') st ok' err
  { \beta-reduction }
Parsec \$ \lambdast ok err \rightarrow
   let ok' x st' = useHints err (emptyErr st' 0) st'
   in ok' f st
{ inline ok' }
Parsec \$ \lambdast ok err \rightarrow useHints err (emptyErr st 0) st
   { rearrange and \alpha-conversion }
Parsec $\lambda st \_ bad \rightarrow useHints bad ((`emptyErr` 0) st) st
   { fold definition of raise }
```

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