Chapter 1
Proofs of Parser Laws

The approach taken to prove the following parser laws for parsley is via equational reasoning on gigaparsec semantics, under the assumption that their semantics are equivalent. While there is no formal proof of this equivalence at the present, gigaparsec was designed to have semantics equivalent to parsley's.

1.1   Left absorption for `fmap`

```
    f <$> empty
=   { applicative functor law }
    pure f <*> empty
=   { definition of <*> }
    liftA2 ($) (pure f) empty
=   { semantics of liftA2 }
    Parsec $ λst ok err →
      let ok' x st' = (unParsec empty) st' (ok . (x $)) err
      in (unParsec $ pure f) st ok' err
=   { semantics of empty }
    Parsec $ λst ok err →
      let ok' x st' = (unParsec $ raise (`emptyErr` 0)) st' (ok . (x $)) err
      in (unParsec $ pure f) st ok' err
=   { semantics of raise }
    Parsec $ λst ok err →
      let ok' x st' = (unParsec $ Parsec $ λst'' _ bad →
        useHints bad (emptyErr st'' 0) st') st' (ok . (x $)) err
      in (unParsec $ pure f) st ok' err
=   { β-reduction }
    Parsec $ λst ok err →
      let ok' x st' = useHints err (emptyErr st' 0) st'
      in (unParsec $ pure f) st ok' err
=   { semantics of pure }
    Parsec $ λst ok err →
      let ok' x st' = useHints err (emptyErr st' 0) st'
      in (unParsec $ Parsec $ λst'' ok'' _ → ok'' f st'') st ok' err
=   { β-reduction }
    Parsec $ λst ok err →
      let ok' x st' = useHints err (emptyErr st' 0) st'
      in ok' f st
=   { inline ok' }
    Parsec $ λst ok err → useHints err (emptyErr st 0) st
=   { rearrange and α-conversion }
    Parsec $ λst _ bad → useHints bad ((`emptyErr` 0) st) st
=   { fold definition of raise }
    raise (`emptyErr` 0)
=   { fold definition of empty }
    empty
```