

## 1.8 Rational Functions and Zeros

Name: \_\_\_\_\_

Hour: \_\_\_\_\_ Date: \_\_\_\_\_

**Directions:** Find the zeros and domain for the following rational functions.

$$1. y = \frac{(x+3)(x-2)}{(x-1)(x+5)}$$

-3      2  
1      -5

Zeros:  $(-3, 0), (2, 0)$ Domain:  $\mathbb{R} \setminus \{1, -5\}$ 

$$2. y = \frac{x^2}{(x-1)(x+2)}$$

0  
1      -2

Zeros:  $(0, 0)$ Domain:  $\mathbb{R} \setminus \{-2, 1\}$ 

$$3. y = \frac{(x-3)(x-6)}{(x-6)(x-2)}$$

Zeros:  $(3, 0)$   ~~$(6, 0)$~~ Domain:  $\mathbb{R} \setminus \{6, 2\}$ 

$$4. h(x) = \frac{x^2 - x - 20}{x^2 + x - 20}$$

5      -4  
(x-5)(x+4)  
-5      4

Zeros:  $(5, 0), (-4, 0)$ Domain:  $\mathbb{R} \setminus \{-5, 4\}$ 

$$5. f(x) = \frac{x^2 - 9}{x^2 - 2x - 15}$$

3      -3  
x-5      x+3  
5      -3

Zeros:  $(3, 0)$ Domain:  $\mathbb{R} \setminus \{5, -3\}$ 

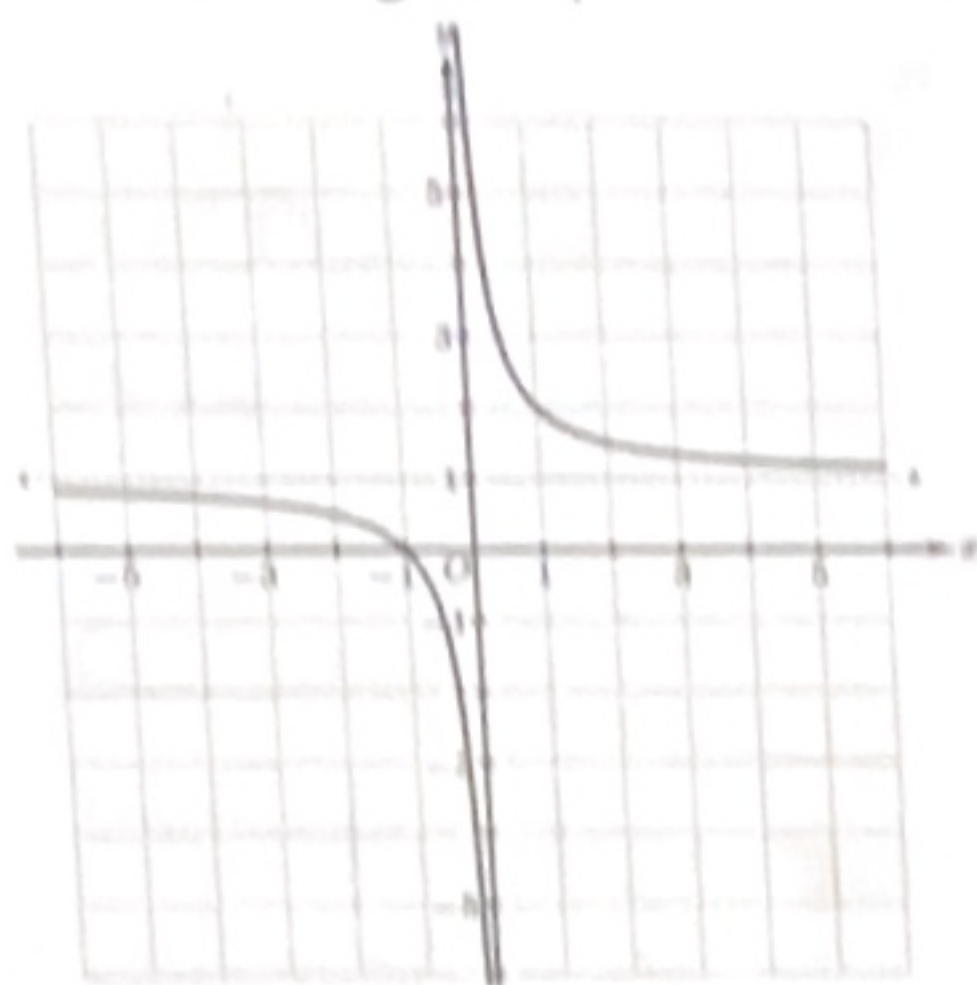
Numerator 0 are done 0 8 -4

$$6. g(x) = \frac{x^3 - 4x^2 - 32x}{2x^2 + 7x - 4}$$

x(x-8)(x+4)  
2x-1      x+4  
-4

Zeros:  $(0, 0)$   $(0, -8)$ Domain:  $\mathbb{R} \setminus \{\frac{1}{2}, -4\}$ 

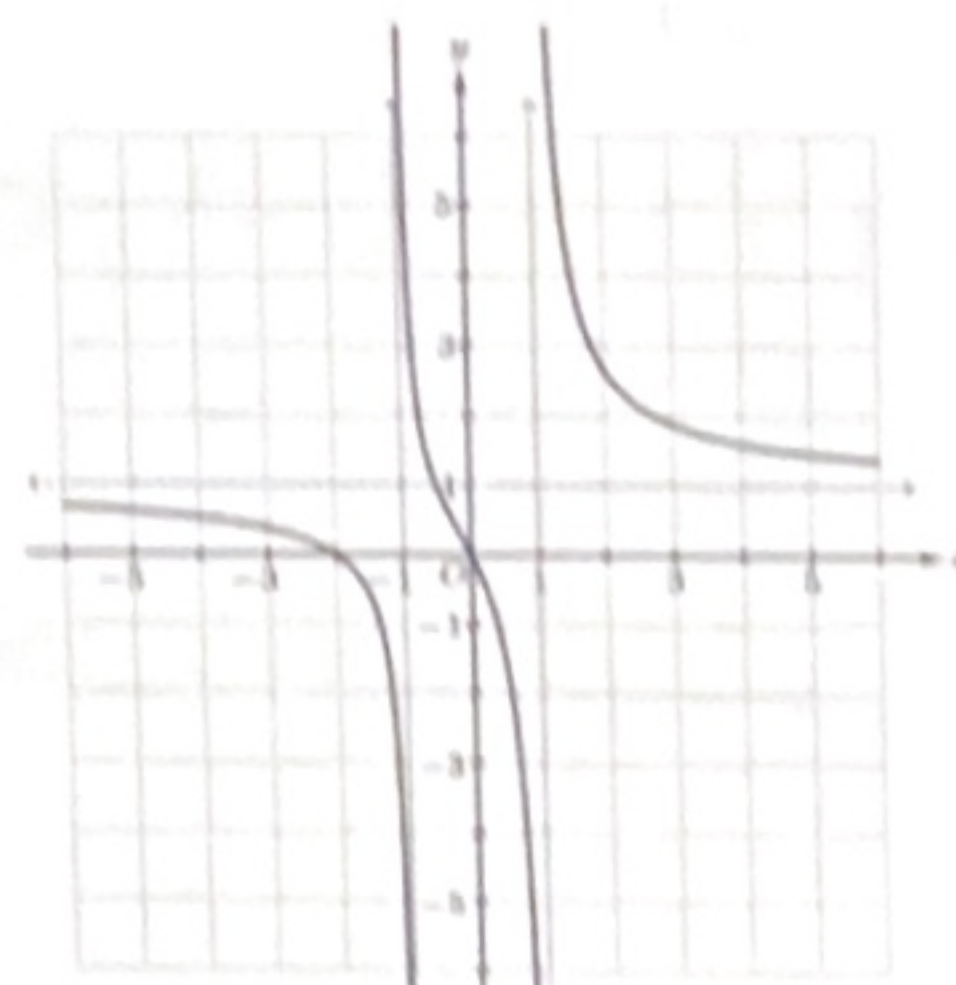
**Directions:** The graphs of several rational functions are given below. Use the graphs to solve the following inequalities.

Graph of  $f$ 

7.  $f(x) > 0$

 $(-\infty, 1) \cup (0, \infty)$ Graph of  $g$ 

8.  $g(x) \leq 0$

 $(-1, 1]$ Graph of  $h$ 

9.  $h(x) \geq 0$

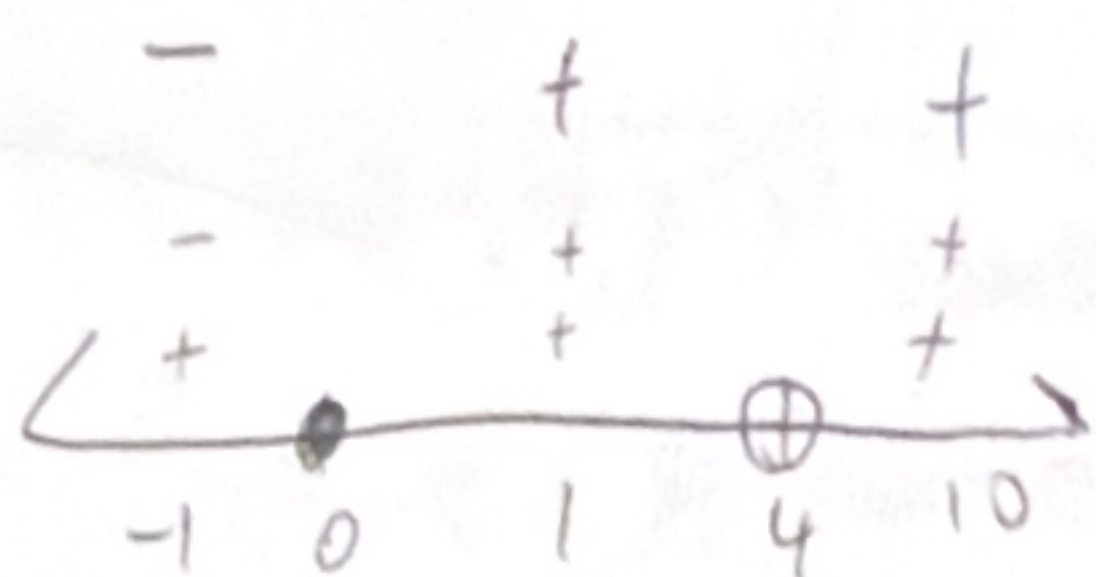
 $(-\infty, -2] \cup (-1, 0] \cup (1, \infty)$



**Directions:** Solve the following inequalities. Show a sign chart & write your answers using interval notation.

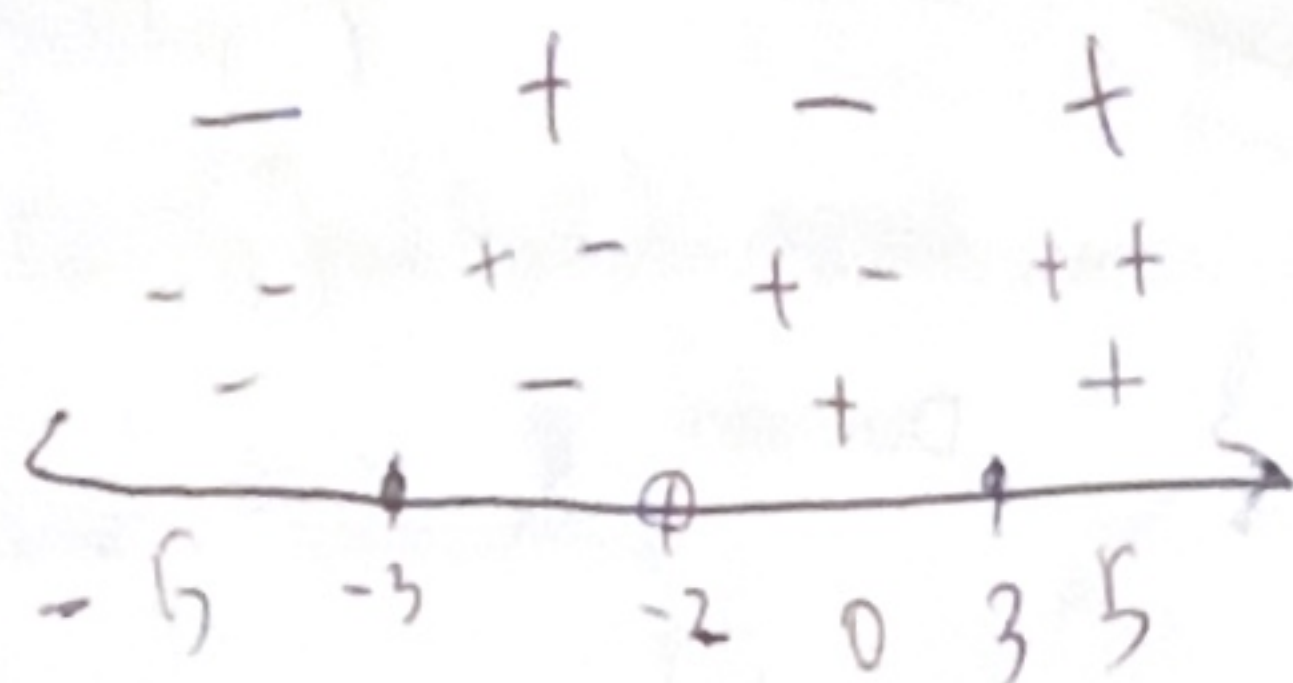
10.  $\frac{x}{(x-4)^2} < 0$

$(-\infty, 0)$



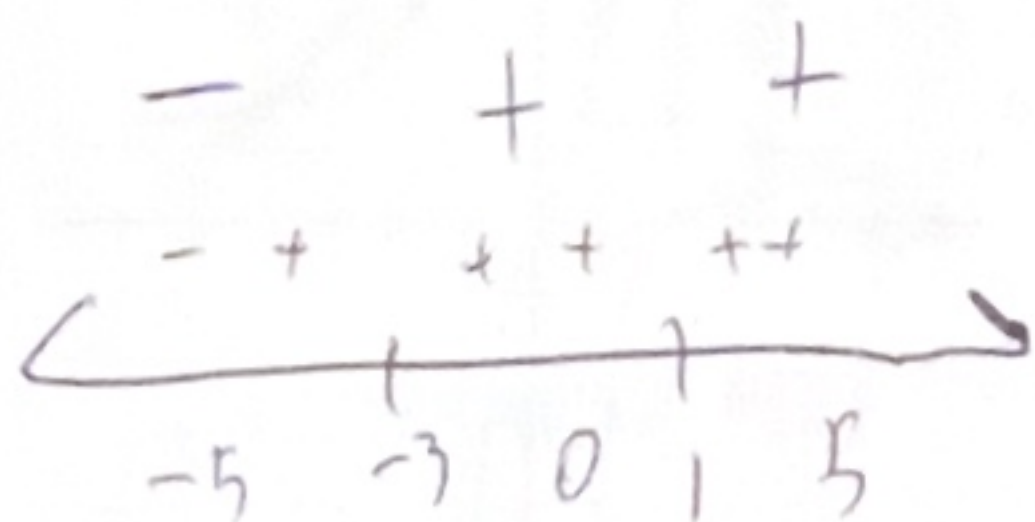
12.  $\frac{x^2-9}{x+2} > 0$

$(-\infty, -3) \cup (-2, 3)$



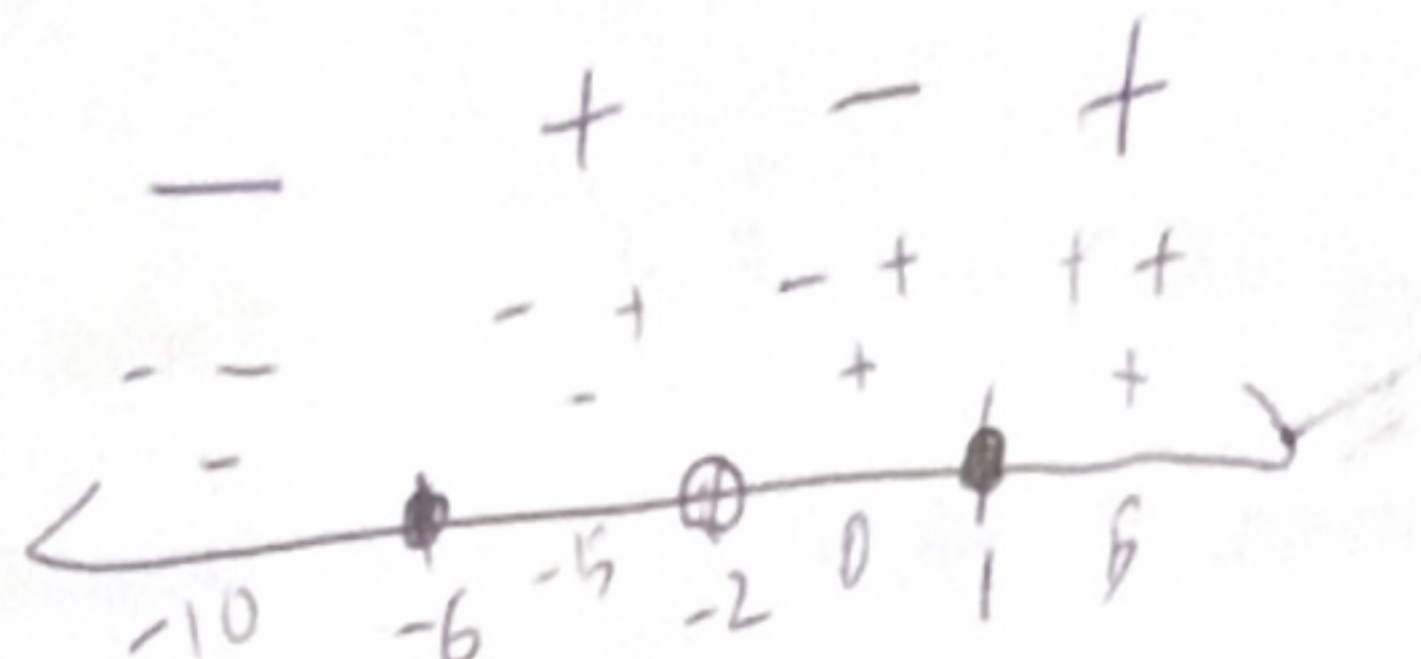
14.  $(x+3)|x-1| \geq 0$

$[-3, \infty)$



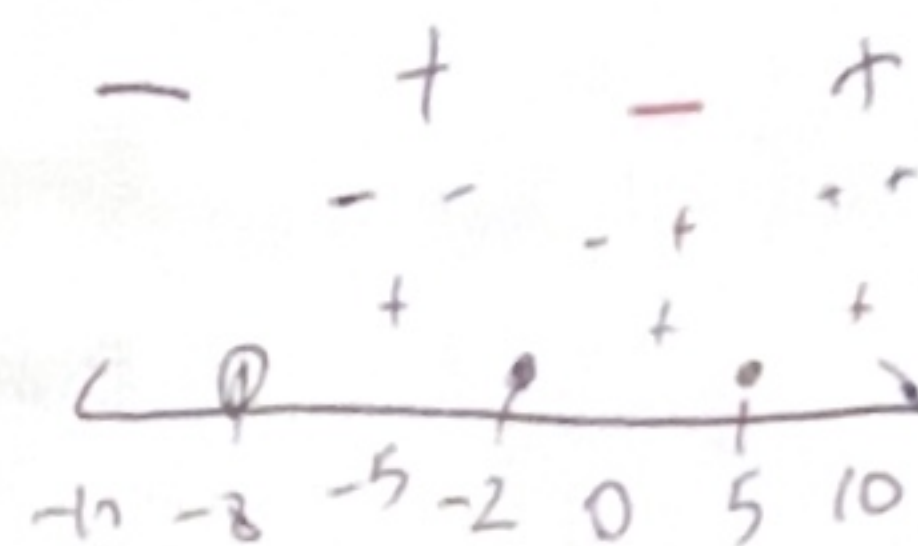
11.  $\frac{(x-1)(x+6)}{x+2} \leq 0$

$(-\infty, -6] \cup (-2, 1)$



13.  $\frac{x^2-3x-10}{x+8} < 0$

$(-\infty, -8) \cup (-2, 5)$



15.  $\frac{(x-5)|x-2|}{\sqrt{2x-3}} \geq 0$

$[5, \infty)$

