

## 1.8 Rational Functions and Zeros

Name: \_\_\_\_\_

Hour: \_\_\_\_\_ Date: \_\_\_\_\_

**Directions:** Find the zeros and domain for the following rational functions.

$$1. \ y = \frac{(x+3)(x-2)}{(x-1)(x+5)}$$

-3      2  
|      -5

Zeros: (-3, 0), (2, 0)

Domain:  $\mathbb{R} \setminus \{-1, -5\}$ 

$$2. \ y = \frac{x^2}{(x-1)(x+2)}$$

0  
|      -2

Zeros: (0, 0)

Domain:  $\mathbb{R} \setminus \{-2, 1\}$ 

$$3. \ y = \frac{(x-3)(x-6)}{(x-6)(x-2)}$$

Zeros: (3, 0) ~~(6, 0)~~Domain:  $\mathbb{R} \setminus \{6, 2\}$ 

$$4. \ h(x) = \frac{x^2 - x - 20}{x^2 + x - 20}$$

5      -4  
|  
(x-5)(x+4)  
(x+5)(x-4)

Zeros: (-5, 0), (-4, 0)

Domain:  $\mathbb{R} \setminus \{-5, 4\}$ 

$$5. \ f(x) = \frac{x^2 - 9}{x^2 - 2x - 15}$$

3      x  
|  
x-3    x+4  
5      -3

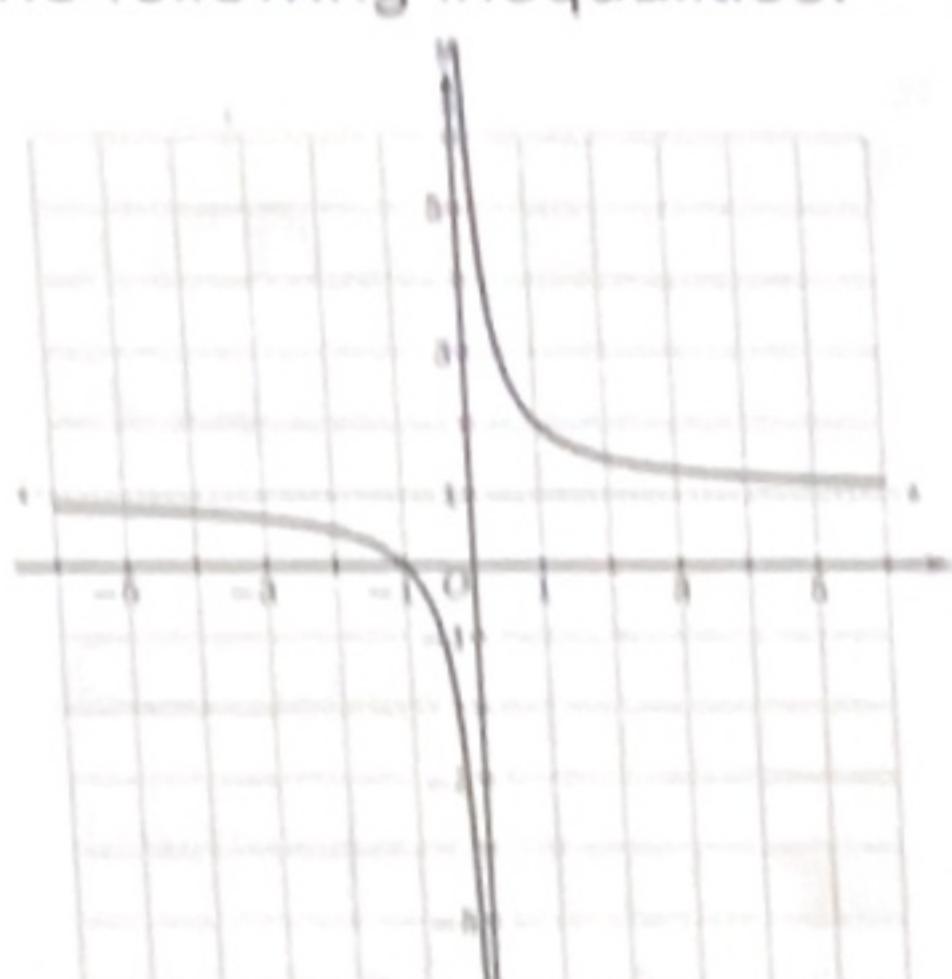
Zeros: (3, 0)

Domain:  $\mathbb{R} \setminus \{5, -3\}$ 

Numerator 0 at  $x = 0, 3, -3$   
Denominator 0 at  $x = 0, 8, -4$   
 $x(x-8)(x+4)$

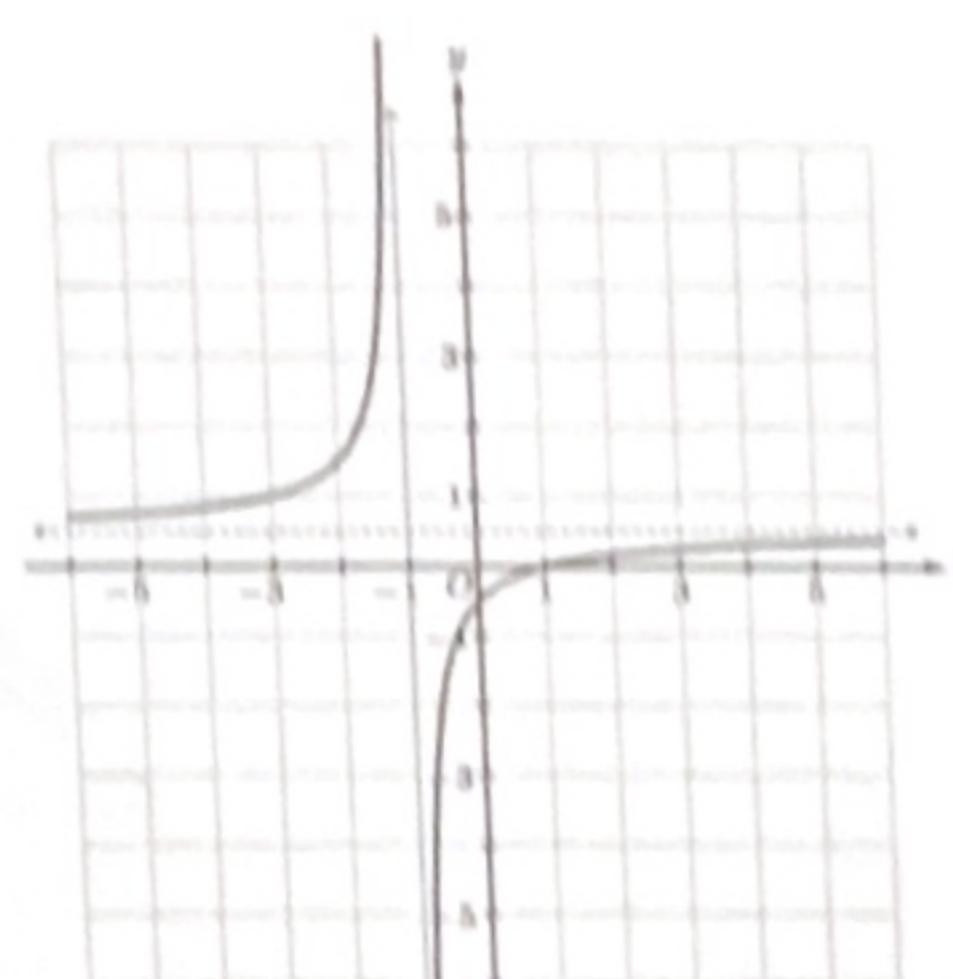
$$6. \ g(x) = \frac{x^3 - 4x^2 - 32x}{2x^2 + 7x - 4}$$

2      -4  
|  
(2x+1)(x+4)

Zeros: (0, 0) ~~(-1, 0)~~  
(0, -8)Domain:  $\mathbb{R} \setminus \{-\frac{1}{2}, -4\}$ **Directions:** The graphs of several rational functions are given below. Use the graphs to solve the following inequalities.Graph of  $f$ 

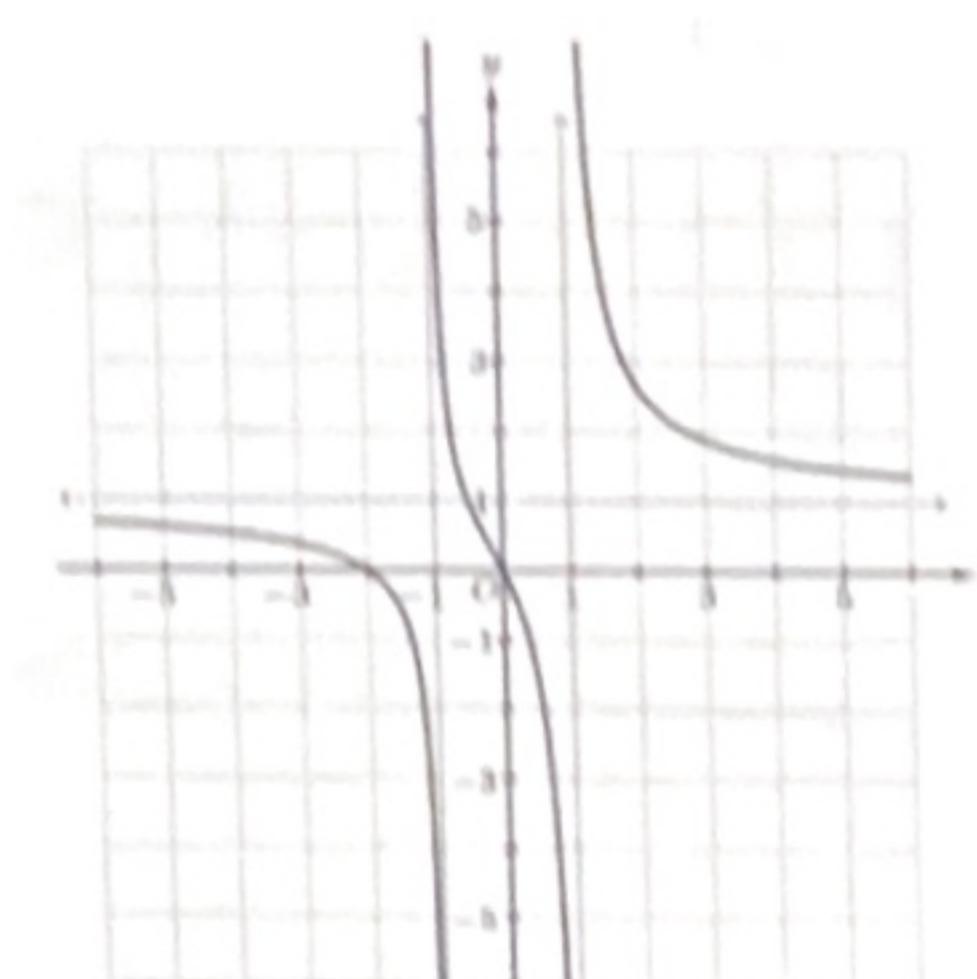
7.  $f(x) > 0$

$(-\infty, -5) \cup (0, \infty)$

Graph of  $g$ 

8.  $g(x) \leq 0$

$(-1, 1]$

Graph of  $h$ 

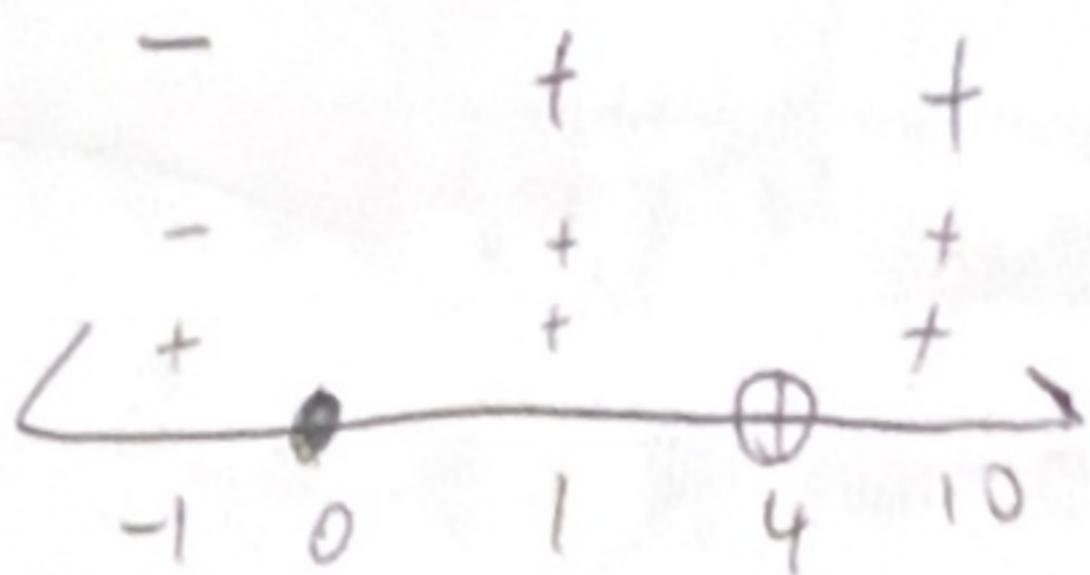
9.  $h(x) \geq 0$

$(-\infty, -2] \cup (-1, 0] \cup (1, \infty)$

**Directions:** Solve the following inequalities. Show a sign chart & write your answers using interval notation.

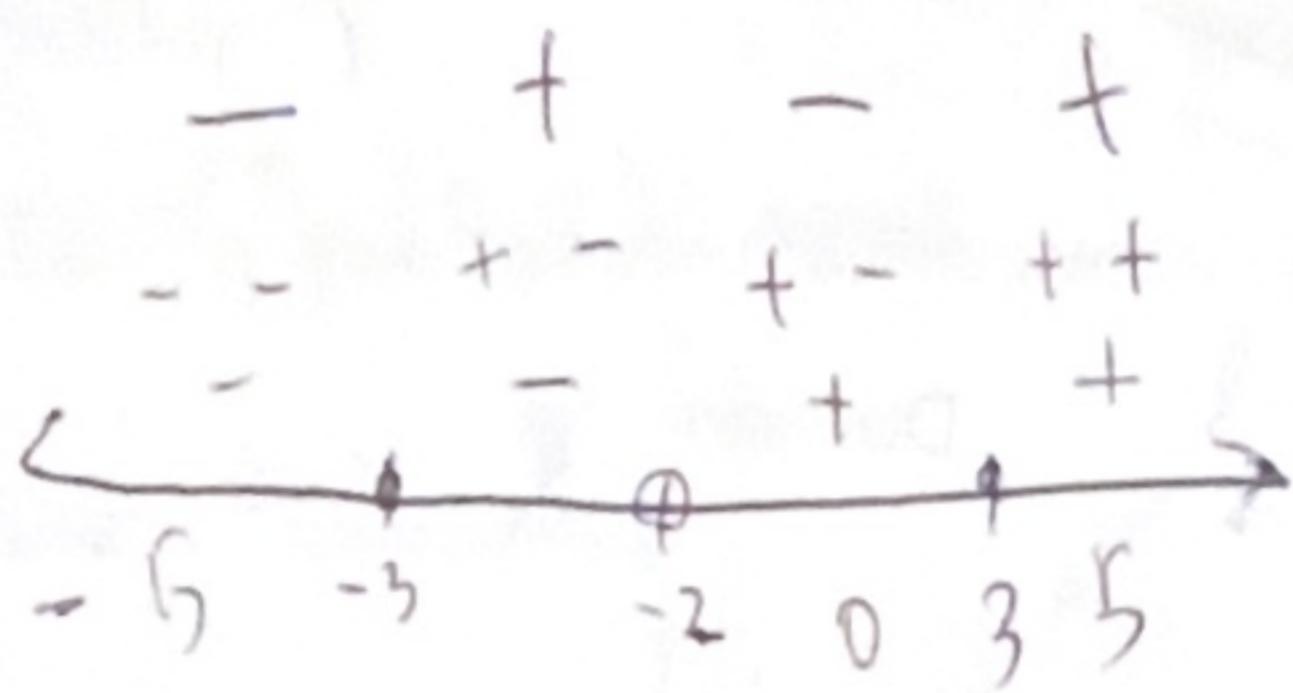
$$10. \frac{x}{(x-4)^2} < 0$$

$$(-\infty, 0)$$



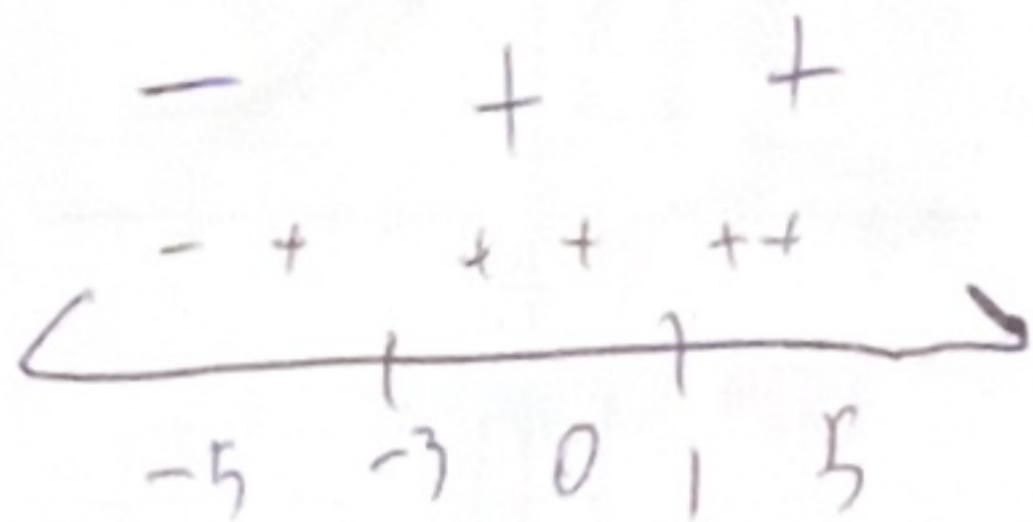
$$12. \frac{x^2-9}{x+2} > 0$$

$$(-\infty, -3) \cup (-2, 3)$$



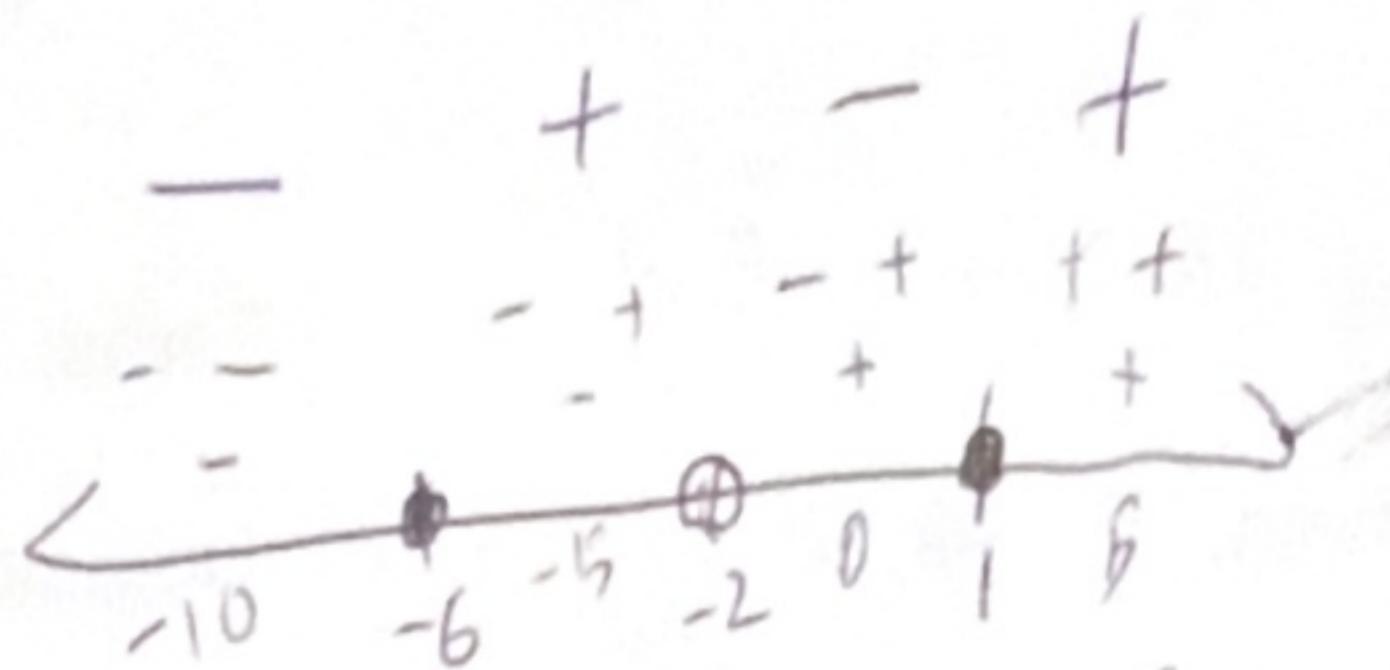
$$14. (x+3)|x-1| \geq 0$$

$$[-3, \infty)$$



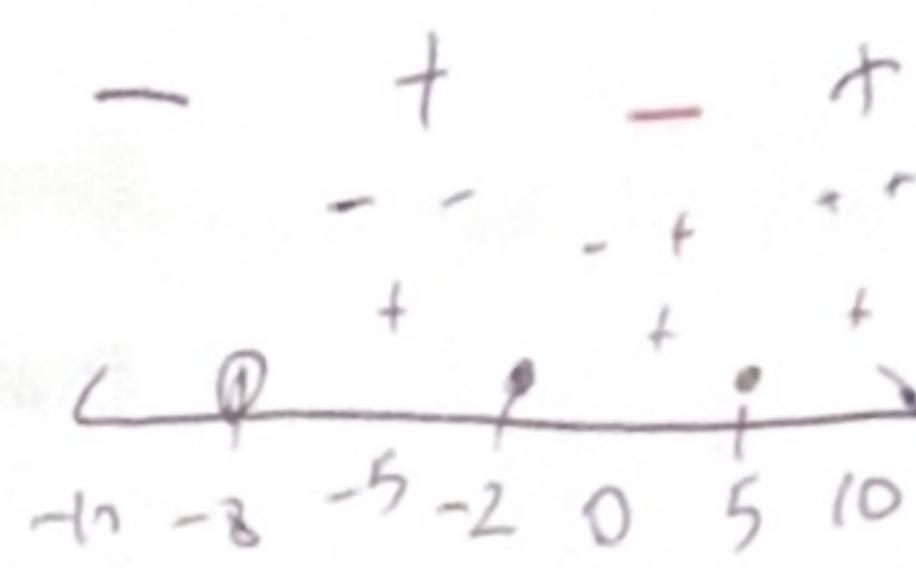
$$11. \frac{(x-1)(x+6)}{x+2} \leq 0$$

$$(-\infty, -6] \cup (-2, \infty)$$



$$13. \frac{x^2-3x-10}{x+8} < 0$$

$$(-\infty, -8) \cup (-2, 5)$$



$$15. \frac{(x-5)(x-2)^2}{\sqrt{2x-3}} \geq 0$$

$$[\frac{3}{2}, \infty)$$

