

1.7 Rational Functions and End Behavior

Name: _____

Hour: _____ Date: _____

Directions: For each of the following rational functions write the **equation** of the asymptote. Then write the **left** and **right** limit statements to describe the end behavior.

$$1. f(x) = \frac{3x^2 - 1}{2x^2 + 5x + 7}$$

[Horizontal]

$$\text{Equation: } y = \frac{3}{2}$$

$$\text{Left: } \lim_{x \rightarrow -\infty} f(x) = \frac{3}{2}$$

$$\text{Right: } \lim_{x \rightarrow \infty} f(x) = \frac{3}{2}$$

$$2. h(x) = \frac{5x^3 - 2x^2 - 1}{x^4 - 6}$$

[Horizontal]

$$\text{Equation: } y = 0$$

$$\text{Left: } \lim_{x \rightarrow -\infty} h(x) = 0$$

$$\text{Right: } \lim_{x \rightarrow \infty} h(x) = 0$$

$$3. p(x) = \frac{(3x-1)^2}{2x^2 + 3x + 5}$$

[Horizontal]

$$\text{Equation: } y = \frac{9}{2}$$

$$\text{Left: } \lim_{x \rightarrow -\infty} p(x) = \frac{9}{2}$$

$$\text{Right: } \lim_{x \rightarrow \infty} p(x) = \frac{9}{2}$$

$$4. f(x) = \frac{x^2 + x - 6}{x - 1}$$

$$\text{[Slant]} \quad x - 1 = 0$$

$$x = 1$$

$$5. k(x) = \frac{6x^3 + 2x + 3}{2x^2 - 11x + 4}$$

[Slant]

$$6. f(x) = \frac{(x^2 - 1)(x + 2)}{x - 2}$$

[Slant] [Neither]

$$x^3 + 2x^2 - x - 2$$

$$\text{Equation: } \cancel{y = x^2}$$

$$y = x^2$$

$$\text{Left: } \lim_{x \rightarrow -\infty} f(x) = \infty$$

$$\text{Right: } \lim_{x \rightarrow \infty} f(x) = \infty$$

$$\text{Equation: } y = 3x + 16.5$$

$$\text{Left: } \lim_{x \rightarrow -\infty} k(x) = -\infty$$

$$\text{Right: } \lim_{x \rightarrow \infty} k(x) = \infty$$

$$\text{Equation: } \cancel{y = x^2} \quad y = x^2 + 4x + 7$$

$$\text{Left: } \lim_{x \rightarrow -\infty} f(x) = \infty$$

$$\text{Right: } \lim_{x \rightarrow \infty} f(x) = \infty$$

$$\begin{array}{r} 1 \ 1 \ -6 \\ \underline{1} \ 1 \ 0 \\ 0 \end{array}$$

$$1 \ 2 \ \cancel{-6}$$

$$x^2$$

$$\begin{array}{r} 2x^2 - 11x + 4 \) 6x^3 + 2x + 3 \\ \underline{6x^3 - 33x^2 + 12x} \\ -35x + 8 \end{array}$$

$$\begin{array}{r} 3x + 16.5 \\ 2x^2 - 11x + 4 \) 6x^3 + 0x^2 + 2x + 3 \\ \underline{6x^3 - 33x^2 + 12x} \\ +33x^2 - 10x + 3 \end{array}$$

$$\begin{array}{r} 1 \ 2 \ -1 \ -2 \\ \underline{2} \ 0 \ 2 \ 0 \\ 0 \end{array}$$

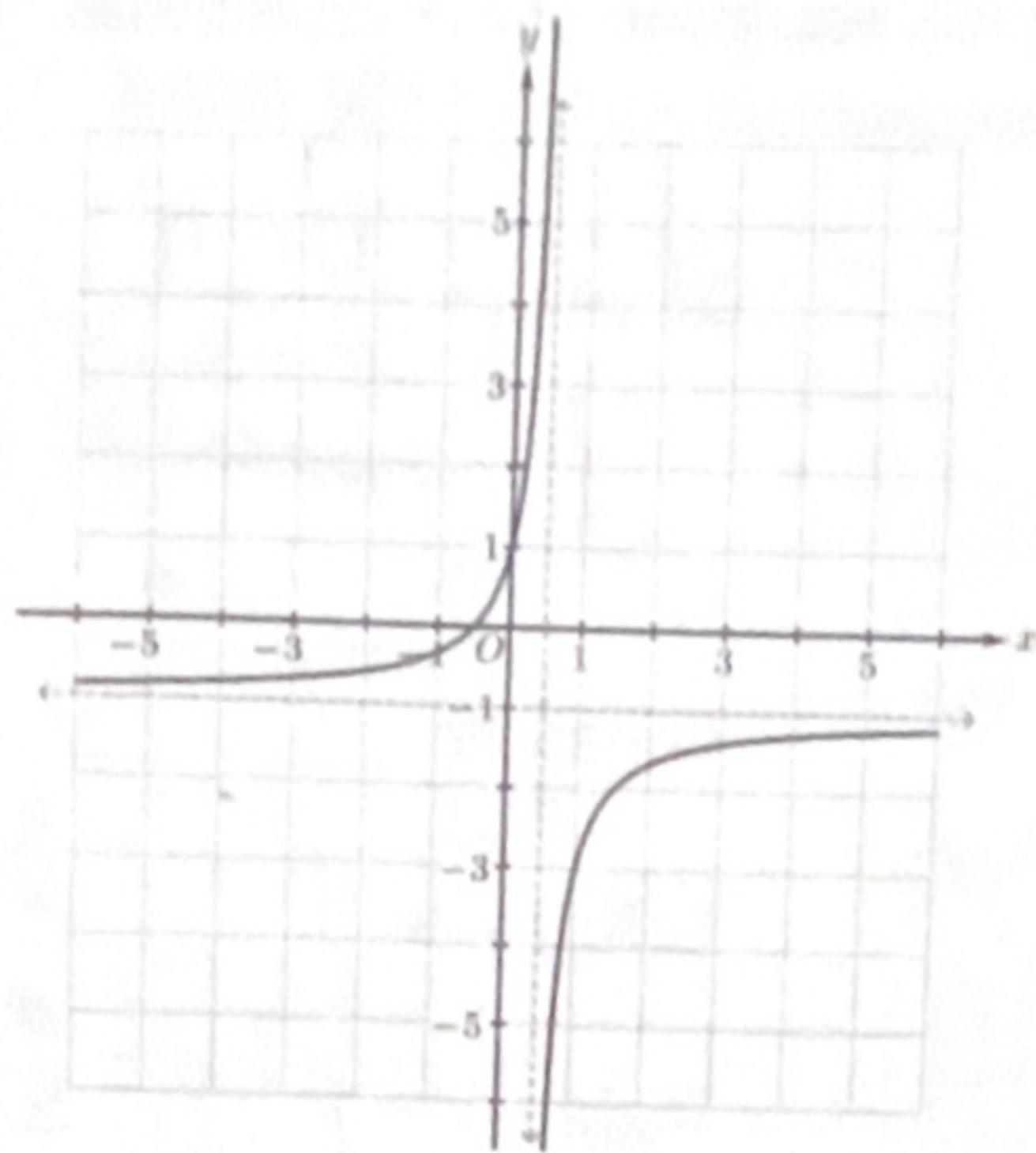
$$x^2 - 1$$

$$\begin{array}{r} 1 \ 2 \ -1 \ -2 \\ \underline{2} \ 8 \ 14 \\ 0 \end{array}$$

$$1 \ 4 \ 7 \ \underline{12}$$

Directions: Write a limit statement describing the output values for the following graphs and verbal descriptions of the input values.

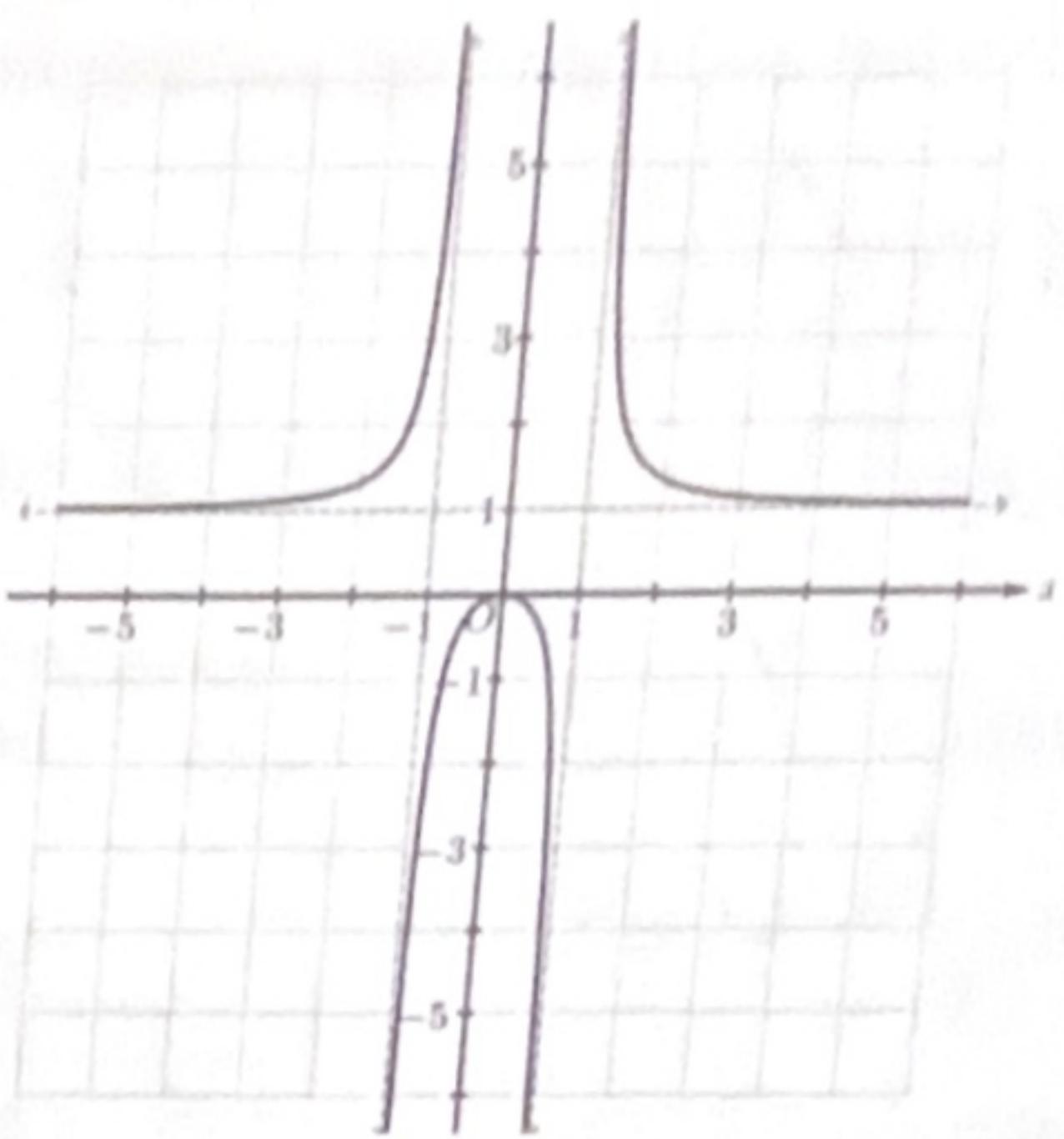
13. The input values decrease without bound



Graph of $f(x)$

13. Limit Statement: $\lim_{x \rightarrow -\infty} f(x) = -1$
 ~~$\lim_{x \rightarrow \infty} f(x) = -1$~~

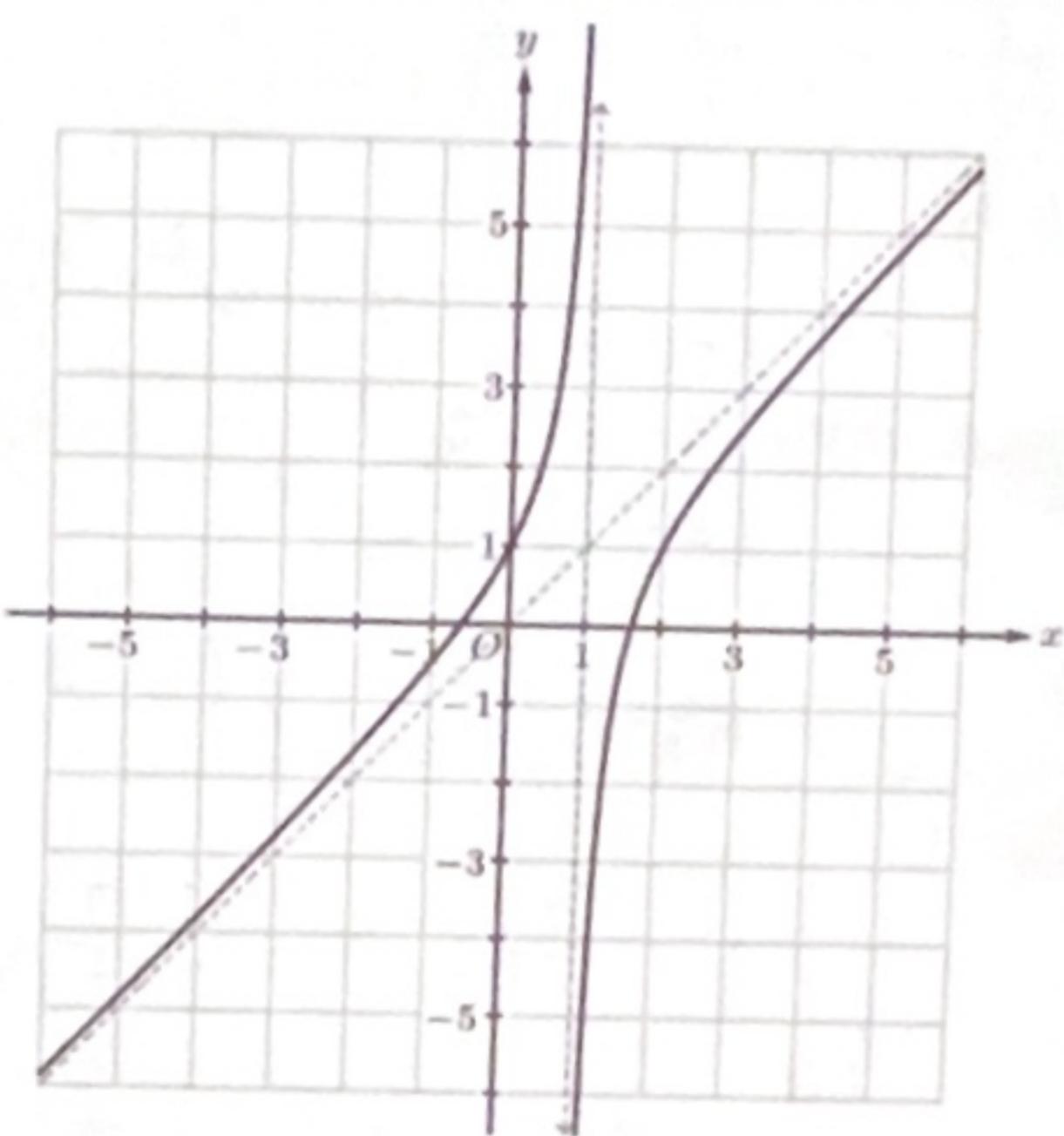
14. The input values increase without bound



Graph of $g(x)$

14. Limit Statement: $\lim_{x \rightarrow \infty} g(x) = 1$
 ~~$\lim_{x \rightarrow -\infty} g(x) = 1$~~

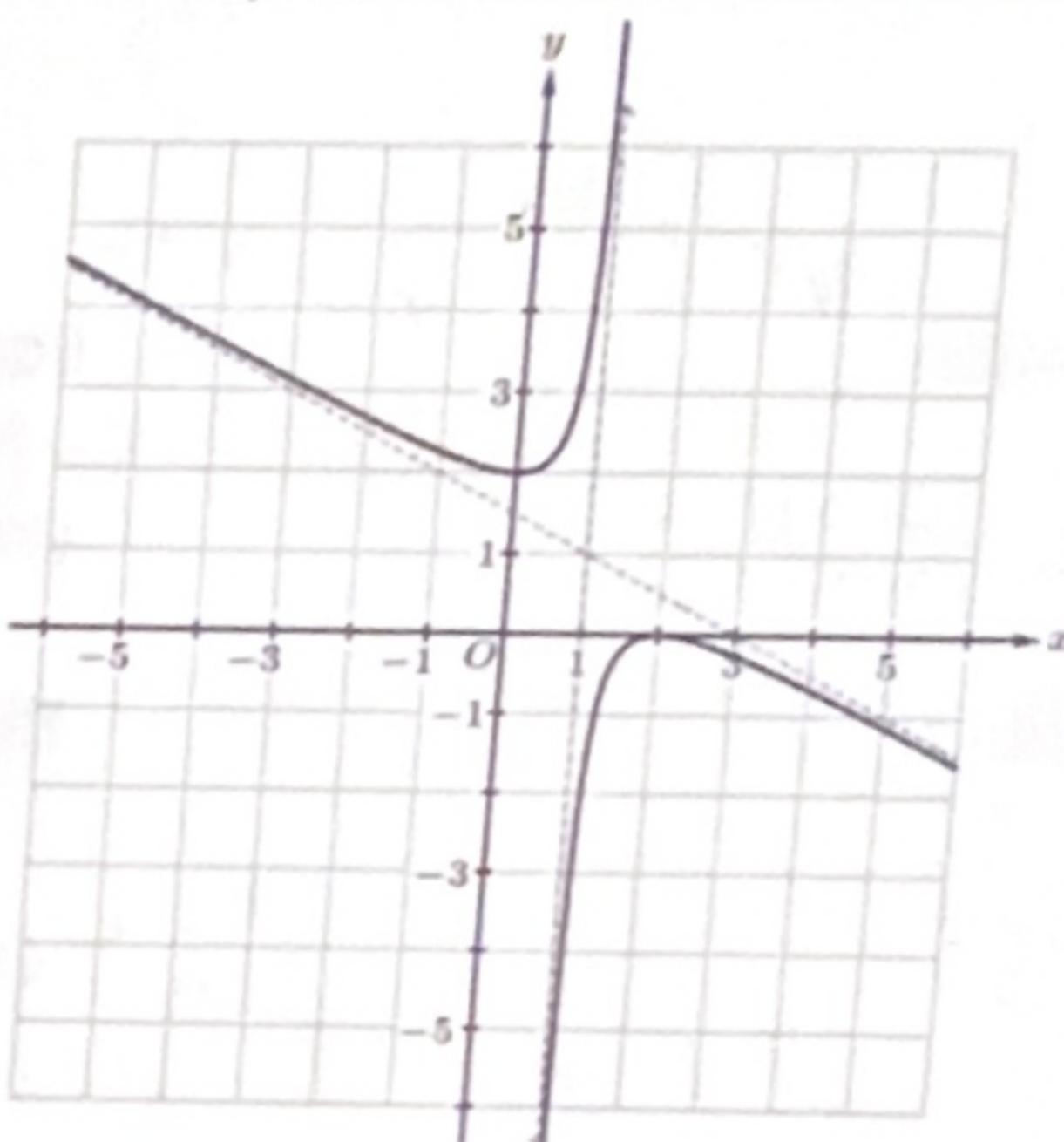
15. The input values increase without bound



Graph of $h(x)$

15. Limit Statement: $\lim_{x \rightarrow -\infty} h(x) = \infty$
 $\lim_{x \rightarrow \infty} h(x) = \infty$

16. The input values decrease without bound



Graph of $k(x)$

16. Limit Statement: $\lim_{x \rightarrow -\infty} k(x) = -1$
 ~~$\lim_{x \rightarrow \infty} k(x) = -1$~~