

1. int 32bits -2,147,483,648 to 2,147,483,647
long 64bits -9,223,372,036,854,775,808 to 9,223,372,036,854,775,807
2.
 - a. For the plus I just used the normal pencil procedure since it's easy to do this with the 2's components.
 - b. For subtract, I changed the sign of the second BigInt and then use the add method.
 - c. For multiply, I used the booth algorithm.
 - d. For factorial, I use a for-loop to call multiply.
3. I used the booth algorithm for multiply. It's better than paper/pencil version.

Booth algorithm:

The example of x: 0010 * y: 1111

x is 2, y is -1

-y: 0001

step	Upper	Lower	Multiplicand	Last digit of lower	Pre last digit of lower	
0	0000	0010	1111	0	0	Nothing
1	0000	0001	1111	1	0	subtract
1a	0001	0001	Make right shift			
2	1000	1000	1111	0	1	add
2a	0111	1000	Make right shift			
3	0011	1100	1111	0	0	Nothing
4	0001	1110	1111	0	0	Nothing

Always make a right shift for upper and lower, the last digit of lower becomes the first digit of upper.

How many bits then how many steps.

Last digit of lower and Pre last digit of lower:

00 and 11 do nothing.

01 add upper and y

10 subtract the y from upper.

1110 is -2. It's the answer.

I think this is much more efficient than the paper/pencil version because it only has adding and shifting. The shifting is really fast since I only need to move the heads and tails.

4. I used the unit test java file to test my code. I meet the overflow bugs for the multiplying method and fix it by double the bits before compute.
5. It's a good project to practice the 2's components and binary.
I learnt the booth algorithm, which is very smart way to solve the multiply problem.
It is also a great practice to optimize codes. I tried a lot to make it run faster. Now, it can compute the factorial of 2000 in about 2 seconds