Lab 4: Non-linear regression on dependency trees

Rodrigo Arias Mallo

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1 Introduction

A list of datasets with information of syntactic dependency trees are used in this report to derive conclusions about the relation of a metric and the size of the sentence n.

1.1 Selection of the metric

For selecting the metric, I built a small python program, that receives as input a list of elements, and a number. The program concatenate the list and the number by using; as separator, and a MD5 hash is computed over the resulting string. Finally, an element of the list is chosen by using the first byte of the hexadecimal hash, converted to a index modulus the size of the list. Then the item with the corresponding index is selected.

The last digit of my identification number is used as the input number, so the output is unique for me.

% python choice.py 64718 degree 2nd moment

Finally the chosen metric is the degree 2nd moment $\langle k^2 \rangle$.

2 Results

All the analysis has been made in python, by using numeric and statistical packages. The datasets were read and the test

$$4 - 6/n \le \langle k^2 \rangle \le n - 1$$

was failed in some elements, because the rounding errors. After allowing a small error $\epsilon=5\times10^{-6}$ the test

$$4 - 6/n - \epsilon \le \langle k^2 \rangle \le n - 1 + \epsilon$$

was succesfully passed in all languages.

2.1 Summary

In the table 1 a summary of the properties of the degree sequences is shown. The sample mean and standard deviation of the metric x are represented by \overline{x} and s_x respectively.

Language	N	\overline{n}	s_n	\overline{x}	s_x
Arabic	4108	26.958	20.647	4.160	1.275
Basque	2933	11.335	6.527	4.143	1.089
Catalan	15053	25.572	13.618	4.962	0.824
Chinese	54238	6.249	3.310	3.218	1.066
Czech	25037	16.428	10.721	4.293	1.299
English	18779	24.046	11.223	5.170	0.802
Greek	2951	22.820	14.379	4.600	1.070
Hungarian	6424	21.660	12.565	5.956	1.706
Italian	4144	18.407	13.344	4.340	1.170
Turkish	6030	11.102	8.281	3.759	0.934

Table 1: The measures of the datasets.

2.2 Models

The models tested are presented in the table 2. The model 0 is used as reference, and has no parameters.

Model	Function	Parameters
0	f(n) = (1 - 1/n)(5 - 6/n)	
1	$f(n) = (n/2)^b$	b
2	$f(n) = an^b$	a, b
3	$f(n) = ae^{cn}$	a, c
4	$f(n) = a \log n$	a
5	$f(n) = an^b e^{cn}$	a,b,c
1+	$f(n) = (n/2)^b + d$	b, d
2+	$f(n) = an^b + d$	a,b,d
3+	$f(n) = ae^{cn} + d$	a, c, d
4+	$f(n) = a \log n + d$	a, d
5+	$f(n) = an^b e^{cn} + d$	a,b,c,d

Table 2: The list of models to test.

2.3 Non-linear regression

The proposed R function nls is the abreviature of Nonlinear Least-Squares. The basic procedure is to modify the parameters of the model in order to reduce the sum of the square distance between the data points and the predicted points of the model.

This function is available in the python package scipy.optimize as least_squares. However the wrap function curve_fit let us use it more easily, and is what has been used in order to fit the models.

The initial parameters are set by default to 1. Except in models 2+ and 3+ which had been modified a bit, but with no luck. The default parameters are defined in the model function:

```
def m2d(n, a=0.06, b=0.8, d=1): return a*n**b + d
def m3d(n, a=-1, c=-0.05, d=13): return a*np.exp(c*n) + d
```

Some models can't find a optimum value and a exception is returned. In this case a second attempt is made, in order to find better parameters for the model. The function differential_evolution let us use an evolutionary algorithm to find values where the least-squares fails. It takes a bit more, but almost always improves the parameters.

In the tables 3 and 4 the difference AIC metric is shown, with respect to the best model in each case. Note that the metric can be affected by the value of the outliers if we use the aggregate mean, so the full dataset is used to get the best parameters. We see that the model 5+ seems to better fit the data,

Language	0	1	2	3	4	5
Arabic	210.1	6276.8	2446.3	5436.0	2290.0	1426.9
Basque	2003.9	5476.5	1626.6	3417.0	1143.0	600.7
Catalan	12644.6	26268.4	3326.8	8266.6	7741.9	1329.2
Chinese	11896.5	85699.6	30496.7	74717.7	10359.2	8129.4
Czech	6340.2	25546.9	5039.1	15949.9	3661.5	4014.9
English	18717.1	28508.2	2309.5	5793.3	7775.1	1207.6
Greek	1673.5	5279.4	1450.1	3211.2	1596.4	713.5
Hungarian	6888.6	4987.7	258.3	1271.2	138.3	155.4
Italian	1736.1	7250.8	1995.7	4642.6	1860.2	936.9
Turkish	920.2	14390.5	4259.5	7868.1	5634.7	1773.2

Table 3: The $\triangle AIC$ of the first models.

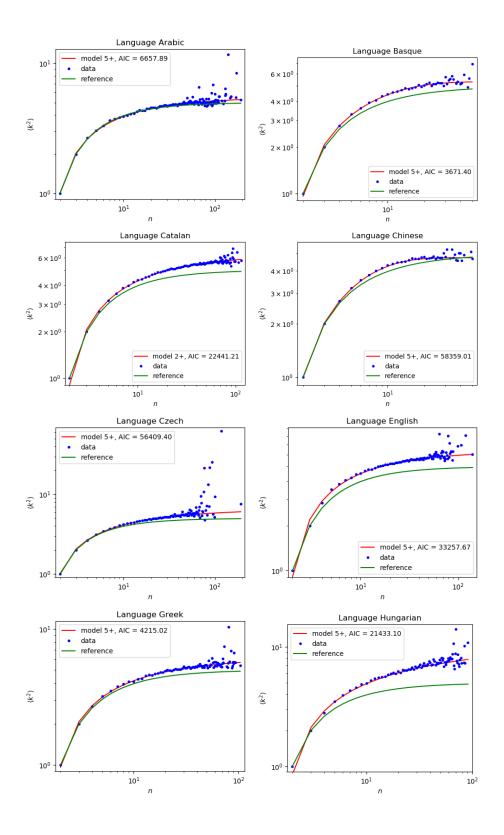
Language	1+	2+	3+	4+	5+
Arabic	3053.3	1.0	392.9	1353.7	0.0
Basque	2095.3	14.2	1457178.6	804.9	0.0
Catalan	4427.3	0.0	737.0	2134.3	1.0
Chinese	38903.3	816.2	26797895.7	10347.4	0.0
Czech	7082.3	13.1	1349.5	1859.7	0.0
English	3075.1	1.2	619.7	1590.0	0.0
Greek	1878.8	0.4	278.1	813.4	0.0
Hungarian	467.4	4.1	54.2	52.8	0.0
Italian	2602.5	0.0	239.9	1022.1	1.9
Turkish	5139.7	38.8	3717244.6	2851.8	0.0

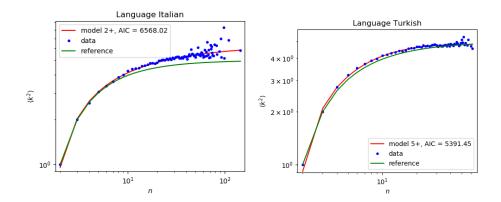
Table 4: The $\triangle AIC$ of the models with a constant parameter.

followed by the 2+ model.

3 Plots of the models

The best model has been selected to be plotted along with the reference model 0, and the aggregate mean data points. The logarithmic scale is enabled in both axis.





3.1 Model parameters

TBD: Fix second table of parameters.

Language	1.b	2.a	2.b	3.a	3.c	4.a	5.a	5.b	5.c
Arabic	0.5	2.0	0.2	3.6	0.0	1.4	1.3	0.5	-0.0
Basque	0.8	1.9	0.3	3.2	0.0	1.8	1.1	0.7	-0.0
Catalan	0.6	2.7	0.2	4.2	0.0	1.6	1.9	0.4	-0.0
Chinese	0.9	1.3	0.5	2.2	0.1	1.9	0.7	1.2	-0.1
Czech	0.7	2.0	0.3	3.4	0.0	1.6	1.3	0.6	-0.0
English	0.6	3.0	0.2	4.4	0.0	1.7	2.1	0.3	-0.0
Greek	0.6	2.3	0.2	3.9	0.0	1.6	1.5	0.5	-0.0
Hungarian	0.7	2.5	0.3	4.6	0.0	2.0	1.8	0.5	-0.0
Italian	0.6	2.1	0.3	3.6	0.0	1.6	1.4	0.5	-0.0
Turkish	0.7	2.0	0.3	3.2	0.0	1.7	1.3	0.6	-0.0

Table 5: The models parameters.

Language	1+.b	1+.d	2+.a	2+.b	2+.d	3+.a	3+.c	3+.d	4+.a	4+.d	5+.a	5+.b	5+
Arabic	0.4	1.6	-7.0	-0.6	5.5	-5.2	-0.2	4.8	1.1	1.0	-7.0	-0.7	-0.
Basque	0.6	1.7	-8.4	-0.6	6.4	5.0	5.0	5.0	1.5	0.7	-7.4	-0.5	-0.
Catalan	0.4	2.5	-8.2	-0.6	6.4	-4.6	-0.1	5.4	1.0	1.9	-7.9	-0.6	-0.
Chinese	0.7	1.0	-8.1	-0.6	6.4	5.0	5.0	5.0	1.9	0.0	-6.9	-0.3	-0.
Czech	0.5	1.7	-8.0	-0.5	6.5	-5.4	-0.2	5.2	1.3	0.8	-7.9	-0.5	-0.
English	0.4	2.7	-8.6	-0.7	6.3	-4.7	-0.1	5.5	0.9	2.2	-8.5	-0.7	-0.
Greek	0.4	2.0	-7.8	-0.6	6.2	-5.3	-0.2	5.2	1.1	1.3	-7.8	-0.6	-0.
Hungarian	0.5	2.6	-12.0	-0.3	10.3	-5.9	-0.1	7.4	1.7	0.9	-11.0	-0.4	-0.
Italian	0.4	1.8	-7.9	-0.5	6.4	-5.5	-0.2	5.2	1.2	1.0	-7.4	-0.6	-0.
Turkish	0.5	1.7	-7.8	-0.8	5.3	5.0	5.0	5.0	1.2	1.2	-7.3	-0.7	-0.

Table 6: The models parameters.

- 4 Results
- 5 Discussion
- 6 Methods