

Relational Algebra and SQL

Please see the associated file: RelationalAlgebraAndSQL.sql

Why Relational Algebra?

Adapted From Pritam Mitra

(https://www.doc.ic.ac.uk/~pjm/teaching/student_projects/pm105_report.pdf)

Often lecturers introduce Relational Algebra as conceptual operations which can be performed by actual query languages. Such presentations lead students to believe that Relational Algebra plays no important role in the actual implementation of database applications. Students may fail to realize that SQL queries are declarative and only tell the Database Management Systems (DBMS) what they want and not how to get it.

Relational Algebra on the other hand is procedural since it is concerned with operations on relations. It is very important that students understand Relational Algebra as it allows them to understand and compare database operations

Examples of Relational Algebra and SQL

Operand

| Relational Algebra Operation | Relational Algebra Operator Symbol | Relational Algebra Example | SQL Example | Result | | | | | | | | | | |
|------------------------------|------------------------------------|----------------------------|-----------------|--|----|----|---|---|---|---|---|---|---|---|
| | | R | SELECT * FROM R | <table><tr><th>C1</th><th>C2</th></tr><tr><td>1</td><td>B</td></tr><tr><td>2</td><td>A</td></tr><tr><td>3</td><td>B</td></tr><tr><td>4</td><td>A</td></tr></table> | C1 | C2 | 1 | B | 2 | A | 3 | B | 4 | A |
| C1 | C2 | | | | | | | | | | | | | |
| 1 | B | | | | | | | | | | | | | |
| 2 | A | | | | | | | | | | | | | |
| 3 | B | | | | | | | | | | | | | |
| 4 | A | | | | | | | | | | | | | |
| | | S | SELECT * FROM S | <table><tr><th>C1</th><th>C2</th></tr><tr><td>2</td><td>A</td></tr><tr><td>4</td><td>B</td></tr><tr><td>6</td><td>C</td></tr></table> | C1 | C2 | 2 | A | 4 | B | 6 | C | | |
| C1 | C2 | | | | | | | | | | | | | |
| 2 | A | | | | | | | | | | | | | |
| 4 | B | | | | | | | | | | | | | |
| 6 | C | | | | | | | | | | | | | |
| | | T | SELECT * FROM T | <table><tr><th>C1</th></tr><tr><td>1</td></tr><tr><td>3</td></tr></table> | C1 | 1 | 3 | | | | | | | |
| C1 | | | | | | | | | | | | | | |
| 1 | | | | | | | | | | | | | | |
| 3 | | | | | | | | | | | | | | |

Operations

| Relational Algebra Operation | Relational Algebra Operator Symbol | Relational Algebra Example | SQL Example | Result | | | | | | | | | | | | | | |
|------------------------------|------------------------------------|----------------------------|---|--|----|----|---|---|---|---|---|---|---|---|---|---|---|---|
| Union | \cup | $R \cup S$ | SELECT * FROM R <u>UNION</u> SELECT * FROM S | <table><tr><th>C1</th><th>C2</th></tr><tr><td>1</td><td>B</td></tr><tr><td>2</td><td>A</td></tr><tr><td>3</td><td>B</td></tr><tr><td>4</td><td>A</td></tr><tr><td>4</td><td>B</td></tr><tr><td>6</td><td>C</td></tr></table> | C1 | C2 | 1 | B | 2 | A | 3 | B | 4 | A | 4 | B | 6 | C |
| C1 | C2 | | | | | | | | | | | | | | | | | |
| 1 | B | | | | | | | | | | | | | | | | | |
| 2 | A | | | | | | | | | | | | | | | | | |
| 3 | B | | | | | | | | | | | | | | | | | |
| 4 | A | | | | | | | | | | | | | | | | | |
| 4 | B | | | | | | | | | | | | | | | | | |
| 6 | C | | | | | | | | | | | | | | | | | |
| Intersect | \cap | $R \cap S$ | SELECT * FROM R <u>INTERSECT</u> SELECT * FROM S | <table><tr><th>C1</th><th>C2</th></tr><tr><td>2</td><td>A</td></tr></table> | C1 | C2 | 2 | A | | | | | | | | | | |
| C1 | C2 | | | | | | | | | | | | | | | | | |
| 2 | A | | | | | | | | | | | | | | | | | |
| Difference | $-$ | $R - S$ | SELECT * FROM R <u>EXCEPT</u> SELECT * FROM S | <table><tr><th>C1</th><th>C2</th></tr><tr><td>1</td><td>B</td></tr><tr><td>3</td><td>B</td></tr><tr><td>4</td><td>A</td></tr></table> | C1 | C2 | 1 | B | 3 | B | 4 | A | | | | | | |
| C1 | C2 | | | | | | | | | | | | | | | | | |
| 1 | B | | | | | | | | | | | | | | | | | |
| 3 | B | | | | | | | | | | | | | | | | | |
| 4 | A | | | | | | | | | | | | | | | | | |
| Rename | ρ | $\rho_{K1/C1}(R)$ | SELECT C1 <u>AS</u> K1, C2 FROM R | <table><tr><th>K1</th><th>C2</th></tr><tr><td>1</td><td>B</td></tr><tr><td>2</td><td>A</td></tr><tr><td>3</td><td>B</td></tr><tr><td>4</td><td>A</td></tr></table> | K1 | C2 | 1 | B | 2 | A | 3 | B | 4 | A | | | | |
| K1 | C2 | | | | | | | | | | | | | | | | | |
| 1 | B | | | | | | | | | | | | | | | | | |
| 2 | A | | | | | | | | | | | | | | | | | |
| 3 | B | | | | | | | | | | | | | | | | | |
| 4 | A | | | | | | | | | | | | | | | | | |
| Select | σ_{φ} | $\sigma_{C2='B'}(R)$ | SELECT * FROM R <u>WHERE C2 = 'B'</u> | <table><tr><th>C1</th><th>C2</th></tr><tr><td>1</td><td>B</td></tr><tr><td>3</td><td>B</td></tr></table> | C1 | C2 | 1 | B | 3 | B | | | | | | | | |
| C1 | C2 | | | | | | | | | | | | | | | | | |
| 1 | B | | | | | | | | | | | | | | | | | |
| 3 | B | | | | | | | | | | | | | | | | | |
| Project | π | $\pi_{C1}(R)$ | SELECT <u>C1</u> FROM R | <table><tr><th>C1</th></tr><tr><td>1</td></tr><tr><td>2</td></tr><tr><td>3</td></tr><tr><td>4</td></tr></table> | C1 | 1 | 2 | 3 | 4 | | | | | | | | | |
| C1 | | | | | | | | | | | | | | | | | | |
| 1 | | | | | | | | | | | | | | | | | | |
| 2 | | | | | | | | | | | | | | | | | | |
| 3 | | | | | | | | | | | | | | | | | | |
| 4 | | | | | | | | | | | | | | | | | | |

| Cartesian Product | X | R X S | SELECT * FROM <u>R, S</u> | <table><tr><th>R.C1</th><th>R.C2</th><th>S.C1</th><th>S.C2</th></tr><tr><td>1</td><td>B</td><td>2</td><td>A</td></tr><tr><td>1</td><td>B</td><td>4</td><td>B</td></tr><tr><td>1</td><td>B</td><td>6</td><td>C</td></tr><tr><td>2</td><td>A</td><td>2</td><td>A</td></tr><tr><td>2</td><td>A</td><td>4</td><td>B</td></tr><tr><td>2</td><td>A</td><td>6</td><td>C</td></tr><tr><td>3</td><td>B</td><td>2</td><td>A</td></tr><tr><td>3</td><td>B</td><td>4</td><td>B</td></tr><tr><td>3</td><td>B</td><td>6</td><td>C</td></tr><tr><td>4</td><td>A</td><td>2</td><td>A</td></tr><tr><td>4</td><td>A</td><td>4</td><td>B</td></tr><tr><td>4</td><td>A</td><td>6</td><td>C</td></tr></table> | R.C1 | R.C2 | S.C1 | S.C2 | 1 | B | 2 | A | 1 | B | 4 | B | 1 | B | 6 | C | 2 | A | 2 | A | 2 | A | 4 | B | 2 | A | 6 | C | 3 | B | 2 | A | 3 | B | 4 | B | 3 | B | 6 | C | 4 | A | 2 | A | 4 | A | 4 | B | 4 | A | 6 | C |
|-------------------|---------------------------------|---------------------------|---|--|------|------|------|------|---|---|---|---|---|---|---|---|------|------|------|------|---|---|------|------|------|------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| | | | | R.C1 | R.C2 | S.C1 | S.C2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | | 1 | B | 2 | A | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | | 1 | B | 4 | B | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | | 1 | B | 6 | C | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | | 2 | A | 2 | A | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | | 2 | A | 4 | B | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | | 2 | A | 6 | C | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | | 3 | B | 2 | A | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | | 3 | B | 4 | B | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | | 3 | B | 6 | C | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | | 4 | A | 2 | A | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | | 4 | A | 4 | B | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 4 | A | 6 | C | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Join (theta Join) | \bowtie_{φ} | $R \bowtie_{R.C1=S.C1} S$ | SELECT * FROM R <u>JOIN S ON R.C1=S.C1</u> | <table><tr><th>R.C1</th><th>R.C2</th><th>S.C1</th><th>S.C2</th></tr><tr><td>2</td><td>A</td><td>2</td><td>A</td></tr><tr><td>4</td><td>A</td><td>4</td><td>B</td></tr></table> | R.C1 | R.C2 | S.C1 | S.C2 | 2 | A | 2 | A | 4 | A | 4 | B | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| R.C1 | R.C2 | S.C1 | S.C2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 2 | A | 2 | A | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 4 | A | 4 | B | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Natural Join | \bowtie | $R \bowtie S$ | SELECT <u>R.C1 AS C1, R.C2 AS C2</u> FROM R <u>JOIN S ON R.C1=S.C1 AND R.C2=S.C2</u> | <table><tr><th>C1</th><th>C2</th></tr><tr><td>2</td><td>A</td></tr></table> | C1 | C2 | 2 | A | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| C1 | C2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 2 | A | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Left Join | $\bowtie_{\varphi} \rightarrow$ | $R \bowtie_{R.C1=S.C1} S$ | SELECT * FROM R <u>LEFT JOIN S ON R.C1=S.C1</u> | <table><tr><th>R.C1</th><th>R.C2</th><th>S.C1</th><th>S.C2</th></tr><tr><td>2</td><td>A</td><td>2</td><td>A</td></tr><tr><td>4</td><td>A</td><td>4</td><td>B</td></tr><tr><td>1</td><td>B</td><td>NULL</td><td>NULL</td></tr><tr><td>3</td><td>B</td><td>NULL</td><td>NULL</td></tr></table> | R.C1 | R.C2 | S.C1 | S.C2 | 2 | A | 2 | A | 4 | A | 4 | B | 1 | B | NULL | NULL | 3 | B | NULL | NULL | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| R.C1 | R.C2 | S.C1 | S.C2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 2 | A | 2 | A | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 4 | A | 4 | B | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 1 | B | NULL | NULL | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 3 | B | NULL | NULL | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Right Join | $\bowtie_{\varphi} \leftarrow$ | $R \bowtie_{R.C1=S.C1} S$ | SELECT * FROM R <u>RIGHT JOIN S ON R.C1=S.C1</u> | <table><tr><th>R.C1</th><th>R.C2</th><th>S.C1</th><th>S.C2</th></tr><tr><td>2</td><td>A</td><td>2</td><td>A</td></tr><tr><td>4</td><td>A</td><td>4</td><td>B</td></tr><tr><td>NULL</td><td>NULL</td><td>6</td><td>C</td></tr></table> | R.C1 | R.C2 | S.C1 | S.C2 | 2 | A | 2 | A | 4 | A | 4 | B | NULL | NULL | 6 | C | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| R.C1 | R.C2 | S.C1 | S.C2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 2 | A | 2 | A | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 4 | A | 4 | B | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| NULL | NULL | 6 | C | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Full Join | $\bowtie_{\varphi} \ltimes$ | $R \bowtie_{R.C1=S.C1} S$ | SELECT * FROM R <u>FULL JOIN S ON R.C1=S.C1</u> | <table><tr><th>R.C1</th><th>R.C2</th><th>S.C1</th><th>S.C2</th></tr><tr><td>2</td><td>A</td><td>2</td><td>A</td></tr><tr><td>4</td><td>A</td><td>4</td><td>B</td></tr><tr><td>1</td><td>B</td><td>NULL</td><td>NULL</td></tr><tr><td>3</td><td>B</td><td>NULL</td><td>NULL</td></tr><tr><td>NULL</td><td>NULL</td><td>6</td><td>C</td></tr></table> | R.C1 | R.C2 | S.C1 | S.C2 | 2 | A | 2 | A | 4 | A | 4 | B | 1 | B | NULL | NULL | 3 | B | NULL | NULL | NULL | NULL | 6 | C | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| R.C1 | R.C2 | S.C1 | S.C2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 2 | A | 2 | A | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 4 | A | 4 | B | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 1 | B | NULL | NULL | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 3 | B | NULL | NULL | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| NULL | NULL | 6 | C | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

| Left Semi Join* | \ltimes_{φ} | $R \bowtie_{R.C1=S.C1} S$ | SELECT <u>R.C1</u> , <u>R.C2</u> FROM R <u>JOIN S ON R.C1=S.C1</u> | <table><tr><th>R.C1</th><th>R.C2</th></tr><tr><td>2</td><td>A</td></tr><tr><td>4</td><td>A</td></tr></table> | R.C1 | R.C2 | 2 | A | 4 | A | | | | | | | | | | |
|------------------|--------------------------------|----------------------------------|---|---|------|------|----|----|---|---|---|---|---|---|---|---|---|---|---|---|
| R.C1 | R.C2 | | | | | | | | | | | | | | | | | | | |
| 2 | A | | | | | | | | | | | | | | | | | | | |
| 4 | A | | | | | | | | | | | | | | | | | | | |
| Right Semi Join* | \Join_{φ} | $R \Join_{R.C1=S.C1} S$ | SELECT <u>S.C1</u> , <u>S.C2</u> FROM R <u>JOIN S ON R.C1=S.C1</u> | <table><tr><th>S.C1</th><th>S.C2</th></tr><tr><td>2</td><td>A</td></tr><tr><td>4</td><td>B</td></tr></table> | S.C1 | S.C2 | 2 | A | 4 | B | | | | | | | | | | |
| S.C1 | S.C2 | | | | | | | | | | | | | | | | | | | |
| 2 | A | | | | | | | | | | | | | | | | | | | |
| 4 | B | | | | | | | | | | | | | | | | | | | |
| Anti-Join* | $\not\triangleright_{\varphi}$ | $R \triangleright_{R.C1=S.C1} S$ | SELECT * FROM R <u>EXCEPT</u> <u>SELECT R.C1, R.C2 FROM R</u> <u>JOIN S ON R.C1=S.C1</u> | <table><tr><th>R.C1</th><th>R.C2</th></tr><tr><td>1</td><td>B</td></tr><tr><td>3</td><td>B</td></tr></table> | R.C1 | R.C2 | 1 | B | 3 | B | | | | | | | | | | |
| R.C1 | R.C2 | | | | | | | | | | | | | | | | | | | |
| 1 | B | | | | | | | | | | | | | | | | | | | |
| 3 | B | | | | | | | | | | | | | | | | | | | |
| Self-Join | | $\rho_{R/S}(S) \Join_{2=S.C1} S$ | SELECT * FROM S AS R JOIN S ON 2 = S.C1 | <table><tr><th>C1</th><th>C2</th><th>C1</th><th>C2</th></tr><tr><td>2</td><td>A</td><td>2</td><td>A</td></tr><tr><td>4</td><td>B</td><td>2</td><td>A</td></tr><tr><td>6</td><td>C</td><td>2</td><td>A</td></tr></table> | C1 | C2 | C1 | C2 | 2 | A | 2 | A | 4 | B | 2 | A | 6 | C | 2 | A |
| C1 | C2 | C1 | C2 | | | | | | | | | | | | | | | | | |
| 2 | A | 2 | A | | | | | | | | | | | | | | | | | |
| 4 | B | 2 | A | | | | | | | | | | | | | | | | | |
| 6 | C | 2 | A | | | | | | | | | | | | | | | | | |
| Division | \div | $R \div T$ | SELECT C2 FROM R <u>EXCEPT</u> SELECT C2 FROM (SELECT * FROM T, (SELECT C2 FROM R) AS U <u>EXCEPT</u> SELECT * FROM R) AS U | <table><tr><th>C2</th></tr><tr><td>B</td></tr></table> | C2 | B | | | | | | | | | | | | | | |
| C2 | | | | | | | | | | | | | | | | | | | | |
| B | | | | | | | | | | | | | | | | | | | | |

Here, the definitions of Left Semi Join, Right Semi Join, and Anti Join are variations of the Theta-Join. Left Semi Join, Right Semi Join, and Anti Join are actually variations on the rarely-used natural join.

Some Links:

Relational Database derives from relational algebra: http://en.wikipedia.org/wiki/Relational_algebra,
http://en.wikipedia.org/wiki/Relational_database

Self join: <http://stackoverflow.com/questions/3362038/what-is-self-join-and-when-would-you-use-it>

Joins: [http://en.wikipedia.org/wiki/Join_\(SQL\)](http://en.wikipedia.org/wiki/Join_(SQL))