

Rodolphe RICHARD

Born the 3rd of June, **1984 French** citizen, UK **Settled** status

Mathematician

Work experience

	vvork experience		
Since 2024	Post-doctorant, University of Manchester, United Kingdom.		
2023 - 2024	Invited researcher, IHÉS, France.		
2019 - 2023 2016 - 2017			
2018 - 2019	Post-doctorant , University of Cambridge, United Kingdom. Research and Teaching in Mathematics.		
2014 - 2016	Post-doctorant , Universiteit Leiden, Netherland. Research and Teaching in Mathematics.		
2013 - 2014	Collaborator in Robotics,ÉPFL, Lausanne, Switzerland.Software development inside Clinical robotics team: $C++/Qt/SoQt$, $C\#$.		
2009 - 2013	Post-doctorant , ÉPFL, Lausanne and ETH, Zürich, Switzerland. Research and Teaching in Mathematics.		
2006 - 2009	PhD student "moniteur normalien", Université Rennes 1, France. Research and Teaching in Mathematics.		
2002 - 2006	Student employee "fonctionnaire stagiaire", ÉNS Paris, France.		
	Education and Degrees		
2014	Swiss teaching degree ; taught in Gymnase d'Yverdon.		
2009	PhD in mathematics, with Pr A. Chambert-Loir Université Rennes 1 Dynamics and Arithmetic Geometry		
2004 - 2005	Predoctoral year: Long stay in India , TIFR, Mumbaï; CMI Chennaï Research stay at TIFR and Teaching at CMI		
2004	DÉA/Master Algèbre et Géométrie Université Rennes 1 ranked 1 st , aged 19 , with a mean grade over 18,5/20		

2004 Agrégation in mathematics. (french higher teaching diploma)

Validated all courses for **BSc in physics** the same year. **2002** École normale supérieure de Paris, entered 2nd, the youngest. **2000 - 2002** French "Baccalauréat", preparatory school, University "DEUG" in mathematics **2000** Awards at "concours général de mathématiques 2000" (French olympiade)

Éns Paris

2003 BSc and "Maîtrise" (**MSc** 1st **year**) in mathematics

Teaching Experience

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Teaching degrees	Agrégation de Mathématiques,	France – 2004	
	Haute école pédagogique de Lausanne, Switzerland – 2014		
	Assistant teacher; Chief assistant; Supervisor; Head teacher.		
Levels	PhD — MSc (1st, 2nd years) — BSc (1st, 2nd, 3rd years) — Highschool		
Audience	Students in mathematics, mixed scientists, engineering, architecture; Highschool.		
2005	Calculus	Chennaï Math. Inst. (BSc)	
2006–2009	Affine Geometry Euclidean Geometry General mathematics for non-mathema Supervision	Univ. Rennes 1 (MSc) Univ. Rennes 1 (MSc) ticians Univ. Rennes 1 (BSc) Univ. Rennes 1 (BSc and MSc)	
2009–2012	Berkovich spaces and Modular curves Number Theory Functional analysis Descriptive geometry Calculus Linear Algebra	ÉPFL (PhD course) ÉPFL (MSc) ÉPFL (MSc) , ÉPFL (BSc Architecture)) ÉPFL (BSc Architecture) ÉPFL (BSc Engineering)	
2013–2014	Highschool Mathematics	Yverdon Highschool, Switzerland	
2014–2016	Galois theory Representation theory	Univ. Leiden (BSc) Univ. Leiden (MSc)	
2018-2019	Probability and Measure	Cambridge (BSc)	
2019–2023	Lie groups and Lie Algebras Number Theory	Univ. Coll. London (MSc) Univ. Coll. London (BSc)	
Remote Teaching	Experience in remote teaching: remote exams, remote lectures.		
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	Languages		
French	Native speaker	C2	
English	Fluent, Living in the UK for 6 years	C2	
Italian	Conversational	A2-B1	
	took courses several semesters at ÉPFL	.; numerous stays in Italy.	
	Computer experience		
Operating systems	GNU/Linux since Ubuntu 7.04, Windows since 95b, Android , OSX (Mac), Real-time extension for Windows (Ardence/Zero interval).		
Development	${\it C++/Qt/SoQt:Object}$ oriented, Graphic interface, Virtual reality. Software designed for rehabilitation of hemiplegic children, in in shape of a virtual reality game interacting with a robotic device inside Real-time extension of windows environment.		
Computer algebra	SAGE, Maple, Mathematica, MAGMA, PariGP, Scilab		
o Maple: implemented algorithm on formal solving of differential equation		solving of differential equations, 2002	
	o SAGE: devised and implemented algorithm	m on p-adic differential equations, 2013	
	o Magma/SAGE: devised and demonstrate	red algorithm in Number fields, 2021	
Document systems	ETEX : thesis report, research articles, t Knowledge in (X)HTML/CSS/PHP/SO	,	

Some of my Research interests Geometry, Number Theory, Algebra and Dynamics

Homogeneous Application of rigidity of unipotent dynamics (Ratners theorem) to dydynamics namical problems in lattices spaces.

> Keywords: Ratner theorems, homogeneous spaces, Bruhat-Tits buildings, algebraic groups, real and p-adic Lie groups

Arithmetic Applying the above to dynamics of Galois action in Shimura varieties, with **geometry** application to problem of André-Pink type and point counting. Studying variants of Zilber-pink conjectures: modulo p, over \mathbf{Z} , equidistribution. Keywords: Shimura varieties, Zilber-Pink, Unlikely intersections, equidistribution, André-Oort, André-Pink-Zannier, Manin-Mumford, Abelian varieties, o-minimality.

p-adic differential An explicit algebraic approach to Pulita's theory, and application to ef**equations** fective explicit algorithms and to p-adic theory of exponential sums. Keywords: p-adic differential equations, p-adic cohomology, exponential sums.

Berkovich space of Studying analogue dynamics of Galois action in the modular curve in the the modular curve associated p-adic analytic space.

> Keywords: Berkovich spaces, p-adic equidistribution, p-adic periods.

Arithmetic How the Arakelov-arithmetic form of Mumford stability can be used as a **stability** uniform approach to dynamical and arithmetic aspects of lattices spaces. Keywords: Geometric invariant theory, Symmetric spaces, Euclidean lattices.

Main Publications

- (submitted) 2024 Heights on 'Hybrid orbits' in Shimura varieties (with A. Yafaev), Submitted (2024) to the Proceedings of the LMS.
 - 2025 Generalised André-Pink-Zannier Conjecture for Shimura varieties of abelian type (with A. Yafaev).

Publications Mathématiques de l'IHÉS (2025), Vol. 141 pp. 249331, https://doi.org/10.1007/s10240-025-00154-4

2024 Height functions on Hecke orbits and the generalised André-Pink-Zannier conjecture (with A. Yafaev),

Composition Mathematica (2024), Volume 160(11):2531-2584.

https://doi:10.1112/S0010437X2400722X https://arxiv.org/abs/2109.13718

Équidistribution de sous-variétés spéciales et o-minimalité: André-Oort géométrique (with E. Ullmo, app. with J. Chen), **Annales de l'Institut Fourier (2024)** Volume 74 no. 6.
https://aif.centre-mersenne.org/articles/10.5802/aif.

(subm.) 2009–17 Homogeneous dynamics and Unlikely intersections

Publications

- (submitted) 2024 Heights on 'Hybrid orbits' in Shimura varieties. (with A. Yafaev), Submitted (2024) to the Proceedings of the LMS, https://arxiv.org/abs/2406.20013
 - (To Appear) A common generalisation of the André-Oort and André-Pink-Zannier conjectures. (with A. Yafaev), To Appear, LMS Lecture Notes Series. https://arxiv.org/abs/2401.03528
- (submitted) 2021 Manin-Mumford in arithmetic pencils . (with G. Baldi and E. Ullmo), Final stage of review at Crelle's Journal https://arxiv.org/abs/2105.12027
 - 2025 Generalised André-Pink-Zannier Conjecture for Shimura varieties of abelian type (with A. Yafaev), C. R. Acad. Sci. Paris., Vol. 363 (2025), p. 873-878 https://doi.org/10.5802/crmath.751
 - 2025 Generalised André-Pink-Zannier Conjecture for Shimura varieties of abelian type (with A. Yafaev).
 Publications Mathématiques de l'IHÉS (141), pp. 249331 (2025), https://doi.org/10.1007/s10240-025-00154-4
 - 2024 Height functions on Hecke orbits and the generalised André-Pink-Zannier conjecture . (with A. Yafaev),
 Composition Mathematica (2024), 160(11):2531-2584.
 https://doi:10.1112/S0010437X2400722X
 https://arxiv.org/abs/2109.13718
 - 2024 Équidistribution de sous-variétés spéciales et o-minimalité: André-Oort géométrique (with E. Ullmo, with an appendix with Jiaming Chen),
 Annales de l'Institut Fourier Volume 74 (2024) no. 6, pp. 2667-2721.
 https://aif.centre-mersenne.org/articles/10.5802/aif.
 - 2023 On The Generalised André-Pink-Zannier Conjecture (with A. Yafaev), C. R. Acad. Sci. Paris Vol. 361 (2023), pp. 1717-1722 https://doi.org/10.5802/crmath.491

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Expositiones Mathematicae Vol. 41(3), Sept. 2023,
     https://doi.org/10.1016/j.exmath.2023.05.004
2023 A two dimensional arithmetic André-Oort problem,
      Bull. of the London Mathematical Society Vol. 55(3), June 2023,
      https://doi.org/10.1112/blms.12804,
      https://arxiv.org/abs/1808.07900
     https://mathscinet.ams.org/article?mr=4618237
2023 Manin-Mumford topologique fort
      Annales de La Faculté des Sciences de Toulouse (To appear)
     https://afst.centre-mersenne.org/page/coming-issues/.
2022 Manin-Mumford par le critère de Weyl.
      Journal of Number Theory, Vol. 239, Oct. 2022,
      https://doi.org/10.1016/j.jnt.2021.11.007,
      https://mathscinet.ams.org/article?mr=4434490
2021 Constructing abelian extensions with prescribed norms.
     (with C. Frei),
      Mathematics of Computation, July 22, 2021 (2021)
     https://doi.org/10.1090/mcom/3663
     https://arxiv.org/abs/2006.08968
     https://mathscinet.ams.org/article?mr=4350543
2020 A mod p variant of the André-Oort conjecture (j/w B. Edixhoven),
      Rend. Circ. Mat. Palermo, II. Ser (2018).
      https://www.doi.org/10.1007/s12215-018-00392-y
     https://arxiv.org/abs/1807.03607
     https://mathscinet.ams.org/article?mr=4148780
2019 Stabilité analytique et Convergence locale de translatées en dy-
     namique homogène S-arithmétique.
     (with T. Zamojski),
      C. R. Acad. Sci. Paris, Ser. I, 357 (2019)
     https://doi.org/10.1016/j.crma.2019.02.005
2019 Topological and equidistributional refinement of the André-Pink-
      Zannier conjecture at finitely many places.
     (w. A. Yafaev).
      C. R. Acad. Sci. Paris, Ser. I, (2019)
     https://doi.org/10.1016/j.crma.2019.01.013
2018 Répartition Galoisienne Ultramétrique d'une classe d'isogenie de
      courbes elliptiques: Le cas de la mauvaise reduction. Application
      aux hauteurs locales,
      J. Th. Nombres Bordeaux 30 (2018), no. 1, 118.
     https://www.jstor.org/stable/26274045
     http://www.ams.org/mathscinet-getitem?mr=3809706
2017 Geometric results on linear actions of reductive Lie groups for appli-
      cations to homogeneous dynamics,
     (joint work with Nimish Shah),
      Ergodic Theory and Dynamical Systems 38 (2018), no. 7,
      https://doi.org/10.1017/etds.2016.138
      https://arxiv.org/abs/1305.6557
     http://www.ams.org/mathscinet-getitem?mr=3846726
2016 On \pi-exponentials II : Closed formula for the index,
      J. Th. Nombres Bordeaux, vol. 28 no. 2 (2016),
     https://www.jstor.org/stable/26274045
     https://arxiv.org/abs/1403.0615
     http://www.ams.org/mathscinet-getitem?mr=3509723
```

2023 Problèmes de type André-Oort en pinceau arithmétique,

2015 Des π -exponentielles I: vecteurs de Witt annulés par Frobenius et algorithme de (leur) rayon de convergence

Rendiconti del Seminario Matematico della Univ. di Padova 133.

https://doi.org/10.4171/RSMUP/133-7 https://arxiv.org/abs/1403.0610

http://www.ams.org/mathscinet-getitem?mr=3354948

2013–2014 Gap year in clinical robotics

2009–2017 Homogeneous dynamics and Unlikely intersections

https://arxiv.org/abs/1809.03802 A collection of **four articles** - 189 pages.

- 2017 Inner Galois Equidistribution and S-Hecke orbits (58 p.) (j/w A. Yafaev)
- 2016 Limit distribution of Translated pieces of possibly irrational leaves in S-arithmetic homogeneous spaces (84 p.) (j/w T. Zamojski)
- **2009** Résultat géométrique sur les représentations de groupe réductifs sur un corps ultramétrique (from PhD)
- **2009** On narrowness for translated algebraic probabilities in S-arithmetic homogeneous spaces (from PhD)

The above four articles have been submitted together as a 189 pp. book. Its **first and only submission is from 2017**. The editors and several reviewers encountered difficulties, and the **much delayed reviewing process is still ongoing**.

2013 Répartition galoisienne d'une classe disogénie de courbes elliptiques Int. J. Number Theory, 09, (2013), pp.517-543

https://doi.org/10.1142/S1793042112501199

http://www.ams.org/mathscinet-getitem?mr=3005563

2009 Répartition galoisienne d'une classe disogénie de courbes elliptiques [Hyperbolic Galois distribution of an isogeny class of elliptic curves], C. R. Acad. Sci. Paris, Ser. I 347 (2009)

https://doi.org/10.1016/j.crma.2008.12.008 http://www.ams.org/mathscinet-getitem?mr=2538097

PhD Thesis

Nov. 2009 Sur quelques questions d'équidistribution en géométrie arithmétique.

PhD thesis available in Open access at:

https://tel.archives-ouvertes.fr/tel-00438515/ Comprising six articles

- Répartition galoisienne d'une classe disogénie de courbes elliptiques [Hyperbolic Galois distribution of an isogeny class of elliptic curves],
 Published in C. R. Acad. Sci. Paris, Ser. I 347 (2009).
- Répartition galoisienne d'une classe disogénie de courbes elliptiques

Published in Int. J. Number Theory, 09, (2013), pp.517-543.

- Équidistribution et Variétés de Shimura
- Geometric result on representations of reductive Lie groups (joint work with Nimish Shah; a version augmented with newer results below is published in Erg. Th. Dyn. Syst.)
- Résultat géométrique sur les représentations de groupe réductifs sur un corps ultramétrique.

Open access available at https://arxiv.org/abs/1706.00301

 ${\rm \circ \ } On \ narrowness \ for \ translated \ algebraic \ probabilities \ in \ S-arithmetic \ homogeneous \ spaces$

References and previous managers

• Nimish Shah, Professor, Ohio state University.

Collaborator

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https://people.math.osu.edu/shah.595/

• Andrei Yafaev, Professor, University College London.

Collaborator and Manager 2017-2018 and 2019-2023

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http://www.ucl.ac.uk/~ucahaya/

• Emmanuel Ullmo, Professor (Univ. Paris-Saclay). Director (IHÉS)..

Collaborator

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• Antoine Chambert-Loir, Professor, Université Paris VII Denis Diderot.

Advisor (MSc and PhD)

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• Emmannuel Breuillard, Professor, Universität Münster.

PhD report reviewer, Manager 2018 - 2019

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• Antoine Ducros, Professor, Université Paris VII Jussieu.

MSc Teacher, Colleague

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- Bas Edixhoven, Leiden Universiteit.
- Philippe Michel, Professor, EPF Lausanne.

Manager 2009 - 2013

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• Gareth Jones, senior lecturer, University of Manchester...

Manager since 2023

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https://personalpages.manchester.ac.uk/staff/Gareth. Jones-3/index.php

• Martin Orr, Neumann Fellow, University of Manchester..

Manager since 2023

⊠ martin.orr@manchester.ac.uk

 $https://personal pages.\, manchester.\, ac.\, uk/staff/\, Martin.\, \\ \textit{Orr/}$

• Mohamed Bouri, Professor, EPF Lausanne.

Manager 2013 - 2014

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https://people.epfl.ch/mohamed.bouri