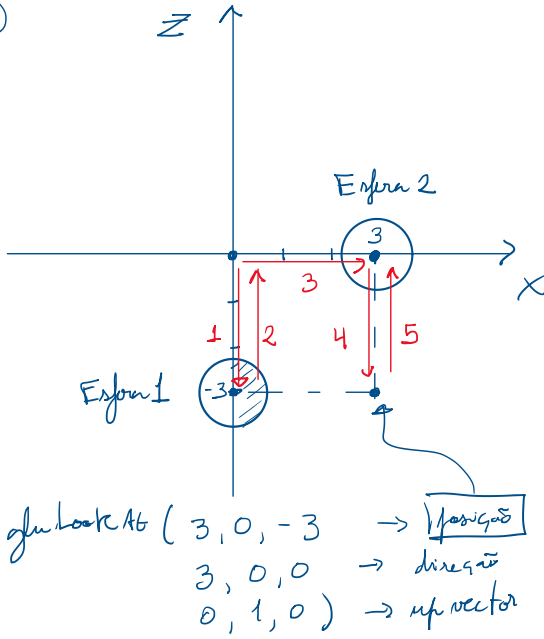
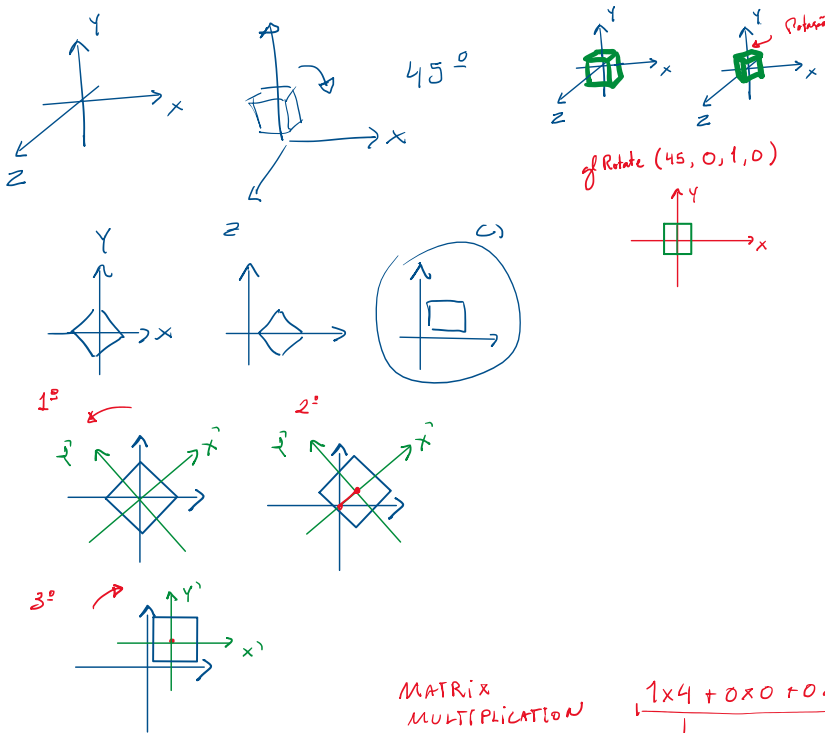


①



②



③ a)

$$\begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 4 & 0 & 0 & 0 \\ 0 & 4 & 0 & 0 \\ 0 & 0 & 4 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 4 & 0 & 0 & 1 \\ 0 & 4 & 0 & 1 \\ 0 & 0 & 4 & 1 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

MATRIX MULTIPLICATION ...

$1 \times 4 + 0 \times 0 + 0 \times 0 + 1 \times 0$

R: Incorreta

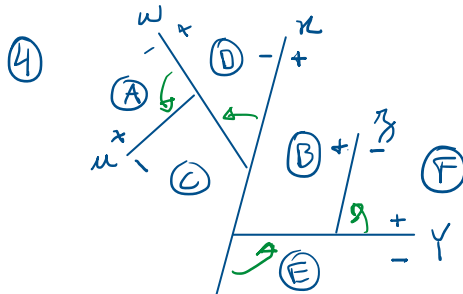
Devia ser = a 4

b)

$$\begin{bmatrix} 1 & 0 & 0 & 4 \\ 0 & 1 & 0 & 4 \\ 0 & 0 & 1 & 4 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} 4 & 0 & 0 & 0 \\ 0 & 4 & 0 & 0 \\ 0 & 0 & 4 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 4 & 0 & 0 & 4 \\ 0 & 4 & 0 & 4 \\ 0 & 0 & 4 & 4 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

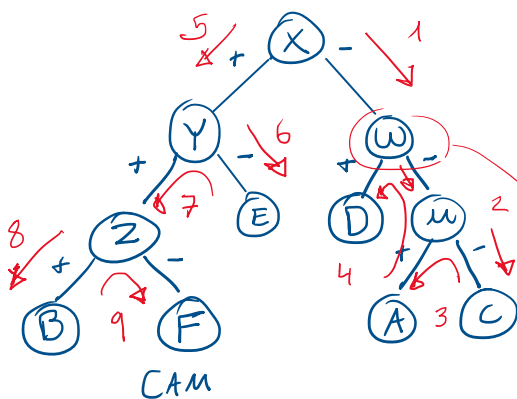
R: Correta

$$C) \begin{bmatrix} 4 & 0 & 0 & 0 \\ 0 & 4 & 0 & 0 \\ 0 & 0 & 4 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} \dots \end{bmatrix}$$



(Acho que não importam os lados dos sinais)

Binary Space Partition



• Desenhar primeiro o lado oposto à câmara

De que lado do plano W é que está a câmara  
 $\rightarrow \oplus$   
 $\rightarrow$  ir pelo  $\ominus$  primeiro

- 1º C
- 2º A
- 3º D
- 4º E
- 5º B
- 6º F

$\rightarrow$  6º elemento a ser desenhado é o que está mais próximo da câmara

## • Parte II

5. Método Casteljau

$$t = 0.75$$

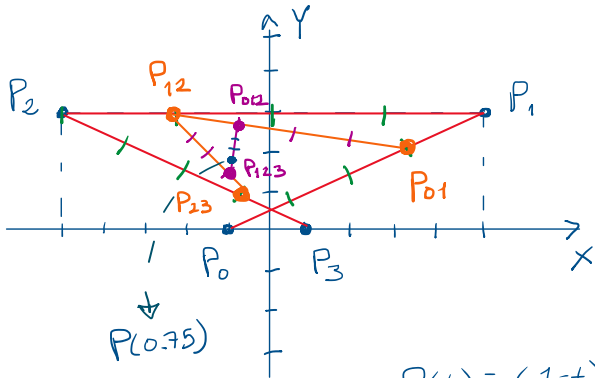
Ponto de uma trajetória  
 cúbica de bezier

$$P_0 = (-1, 0)$$

$$P_1 = (5, 3)$$

$$P_2 = (-5, 3)$$

$$P_3 = (1, 0)$$



$$P(t) = (1-t)A$$

$$\begin{array}{l}
 P_0 \xrightarrow{1-t} \\
 P_1 \xrightarrow[t]{t} P_{01} \xrightarrow{1-t} \\
 P_2 \xrightarrow[t]{t} P_{12} \xrightarrow[t]{t} P_{012} \xrightarrow{1-t} \\
 P_3 \xrightarrow[t]{t} P_{23} \xrightarrow[t]{t} P_{123} \xrightarrow[t]{t} P(t)
 \end{array}$$

$$\Rightarrow P(0.75) = 0.25 P_{012} + 0.75 P_{123}$$

$$= 0.25(0.25P_{01} + 0.75P_{12}) + 0.75(0.25P_{12} + 0.75P_{23})$$

$$= 0.25(0.25(0.25P_0 + 0.75P_1) + 0.75(0.25P_1 + 0.75P_2)) +$$

$$+ 0.75(0.25(0.25P_1 + 0.75P_2) + 0.75(0.25P_2 + 0.75P_3))$$

$$P = (1-t)^3 P_1 + 3(1-t)^2 t P_2 + 3(1-t) t^2 P_3 + t^3 P_4$$

$$0.016 P_1 + 0.141 P_2 + 0.422 P_3 + 0.422 P_4$$

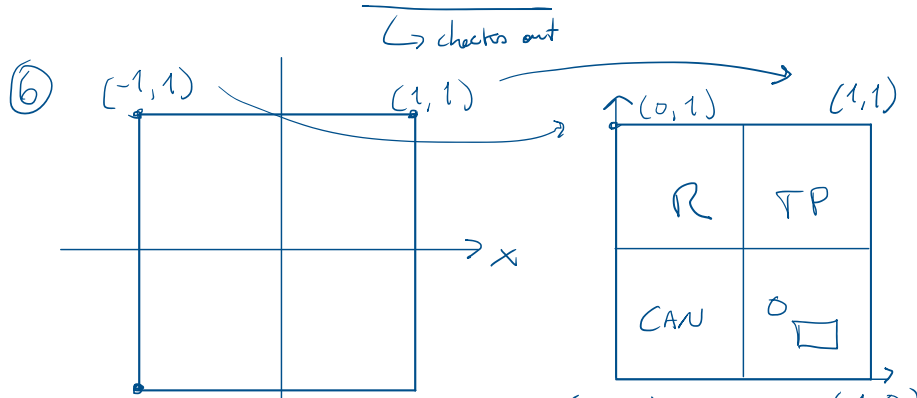
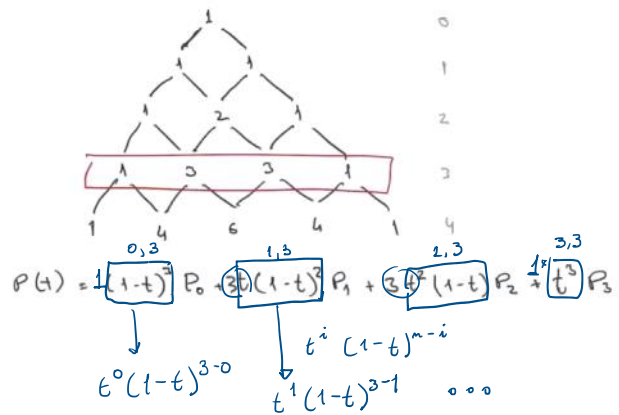
$$= (-0.016, 0)$$

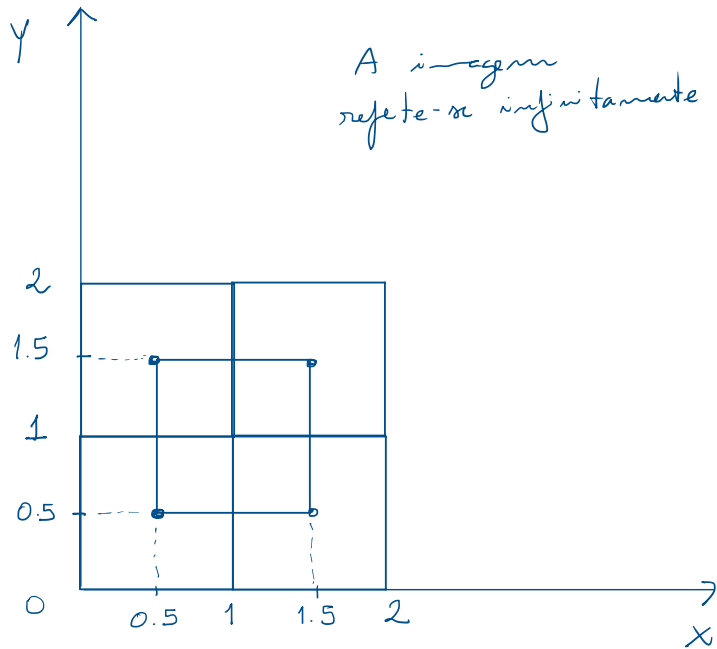
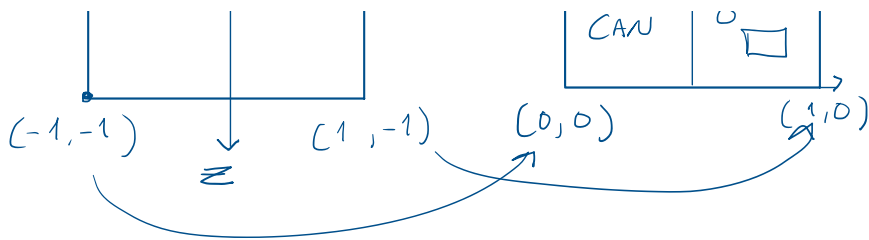
$$+ (0.705, 0.423)$$

$$+ (-2,11, 1,266)$$

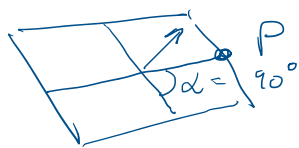
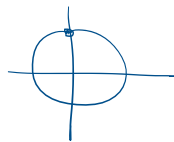
$$+ (0,422, 0)$$

$$= (-0,999, 1,689) \approx (-1, 1.7) \quad \checkmark$$





- $(0.5, 0.5)$
- $(1.5, 0.5)$
- $(0.5, 1.5)$
- $(1.5, 1.5)$

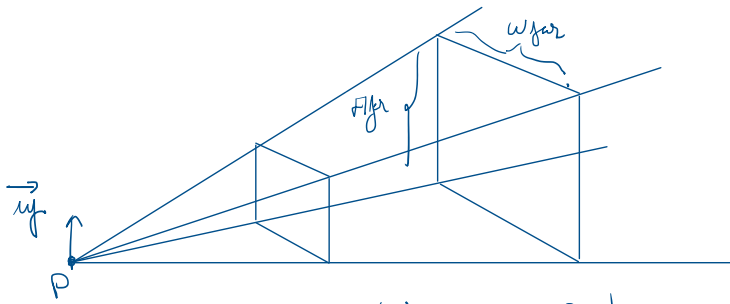


$$\vec{a} \times \vec{b} = |\vec{a}| |\vec{b}| \underbrace{\sin(\alpha)}_{=1} \vec{n}$$

$$\Rightarrow M = |P_3 - P_2| |P_1 - P_2|$$

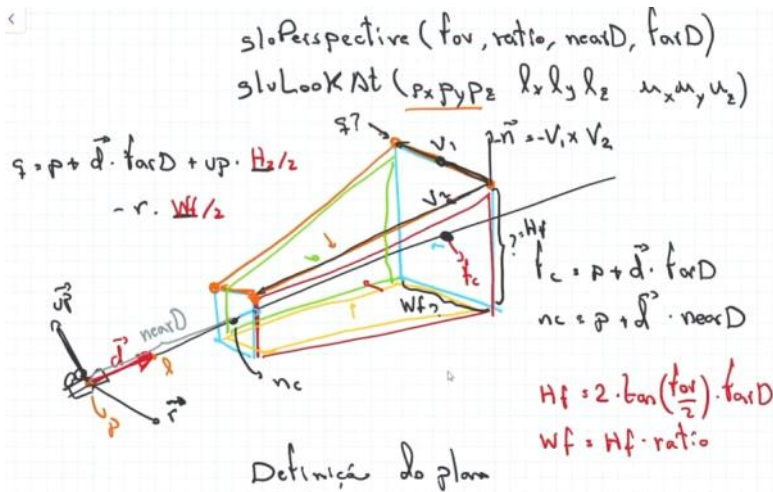
$$\vec{n} = \frac{M}{|M|}$$

8



$$a) H_{far} = 2 \cdot \tan\left(\frac{fov}{2}\right) \cdot farDistance$$

$$w_{far} = H_f \cdot ratio$$



$$b) \vec{r} = \vec{UP} \times \vec{L}$$

$$\vec{q}_c = \vec{P} + \vec{L} \times farD$$

$$\vec{q}_{cd} = \vec{q}_c + (-\vec{up}) \times \frac{H_{far}}{2}$$

$$\vec{q}_{br} = \vec{q}_{cd} + \vec{r} \times \frac{w_{far}}{2}$$