

## Universidade do Minho Departamento de Matemática

## Cálculo para a Engenharia

 $u:I\longrightarrow\mathbb{R}$  é uma função derivável num intervalo I, a é uma constante real apropriada e  $\mathcal C$  denota uma constante real arbitrária.

$$\int a \, dx = ax + \mathcal{C} \qquad \qquad \int u' \, u^\alpha \, dx = \frac{u^{\alpha+1}}{\alpha+1} + \mathcal{C} \, \left(\alpha \neq -1\right)$$

$$\int \frac{u'}{u} \, dx = \ln |u| + \mathcal{C} \qquad \qquad \int u' \, a^u \, dx = \frac{a^u}{\ln a} + \mathcal{C} \, \left(a \in \mathbb{R}^+ \setminus \{1\}\right)$$

$$\int u' \, \cos u \, dx = \sin u + \mathcal{C} \qquad \qquad \int u' \, \sin u \, dx = -\cos u + \mathcal{C}$$

$$\int u' \, tg \, u \, dx = -\ln |\cos u| + \mathcal{C} \qquad \qquad \int u' \, \cot u \, dx = \ln |\sin u| + \mathcal{C}$$

$$\int \frac{u'}{\cos^2 u} \, dx = tg \, u + \mathcal{C} \qquad \qquad \int \frac{u'}{\sin^2 u} \, dx = -\cot u + \mathcal{C}$$

$$\int \frac{u'}{\sqrt{1-u^2}} \, dx = \arcsin u + \mathcal{C} \qquad \qquad \int \frac{u'}{\sqrt{1-u^2}} \, dx = \arccos u + \mathcal{C}$$

$$\int \frac{u'}{1+u^2} \, dx = \arctan u + \mathcal{C} \qquad \qquad \int \frac{-u'}{1+u^2} \, dx = \arccos u + \mathcal{C}$$

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$$\int u' \, \cosh u \, dx = \sinh u + \mathcal{C} \qquad \qquad \int u' \, \coth u \, dx = \ln(\sinh u) + \mathcal{C}$$

$$\int \frac{u'}{\cos^2 u} \, dx = \tanh u + \mathcal{C} \qquad \qquad \int \frac{u'}{\sin^2 u} \, dx = -\coth u + \mathcal{C}$$

$$\int \frac{u'}{\sqrt{u^2+1}} \, dx = \operatorname{argsenh} u + \mathcal{C} \qquad \qquad \int \frac{u'}{\sqrt{u^2-1}} \, dx = \operatorname{argcosh} u + \mathcal{C}$$

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