# coursera





Representation

### **Logistic Regression Model**

#### **Multiclass Classification**

#### **Review**

## Solving the Problem of Overfitting

- Video: The Problem of Overfitting
  9 min
- Reading: The Problem of Overfitting
  3 min
- Video: Cost Function
  10 min
- Reading: Cost Function 3 min
- Video: Regularized Linear Regression
  10 min
- Reading: Regularized Linear Regression
  3 min
- Video: Regularized Logistic Regression 8 min
- Reading: Regularized Logistic Regression 3 min

#### **Review**

- Reading: Lecture Slides
  10 min
- Quiz: Regularization 5 questions
- Programming Assignment:
  Logistic Regression
  3h

# 

# Regularized Linear Regression

**Note:** [8:43 - It is said that X is non-invertible if  $m \le n$ . The correct statement should be that X is non-invertible if m < n, and may be non-invertible if m = n.

We can apply regularization to both linear regression and logistic regression. We will approach linear regression first.

#### **Gradient Descent**

We will modify our gradient descent function to separate out  $\theta_0$  from the rest of the parameters because we do not want to penalize  $\theta_0$ .

$$egin{aligned} ext{Repeat } \{ & heta_0 := heta_0 - lpha \ rac{1}{m} \ \sum_{i=1}^m (h_ heta(x^{(i)}) - y^{(i)}) x_0^{(i)} \ & heta_j := heta_j - lpha \left[ \left( rac{1}{m} \ \sum_{i=1}^m (h_ heta(x^{(i)}) - y^{(i)}) x_j^{(i)} 
ight) + rac{\lambda}{m} \, heta_j 
ight] \ & j \in \{1, 2...n\} \ \} \end{aligned}$$

The term  $\frac{\lambda}{m}\theta_j$  performs our regularization. With some manipulation our update rule can also be represented as:

$$heta_j := heta_j (1 - lpha rac{\lambda}{m}) - lpha rac{1}{m} \sum_{i=1}^m (h_ heta(x^{(i)}) - y^{(i)}) x_j^{(i)}$$

The first term in the above equation,  $1-\alpha\frac{\lambda}{m}$  will always be less than 1. Intuitively you can see it as reducing the value of  $\theta_j$  by some amount on every update. Notice that the second term is now exactly the same as it was before.

## **Normal Equation**

Now let's approach regularization using the alternate method of the non-iterative normal equation.

To add in regularization, the equation is the same as our original, except that we add another term inside the parentheses:

$$heta = \left( X^T X + \lambda \cdot L 
ight)^{-1} X^T y$$
  $ext{where } L = egin{bmatrix} 0 & & & & \ & 1 & & & \ & & 1 & & \ & & \ddots & & \ & & & & 1 \end{bmatrix}$ 

L is a matrix with 0 at the top left and 1's down the diagonal, with 0's everywhere else. It should have dimension (n+1)×(n+1). Intuitively, this is the identity matrix (though we are not including  $x_0$ ), multiplied with a single real number  $\lambda$ .

Recall that if m < n, then  $X^TX$  is non-invertible. However, when we add the term  $\lambda \cdot L$ , then  $X^TX + \lambda \cdot L$  becomes invertible.

✓ Complete

Go to next item

