Problem Set 1

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Due: September 30, 2024

Instructions

- Please show your work! You may lose points by simply writing in the answer. If the problem requires you to execute commands in R, please include the code you used to get your answers. Please also include the .R file that contains your code. If you are not sure if work needs to be shown for a particular problem, please ask.
- Your homework should be submitted electronically on GitHub.
- This problem set is due before 23:59 on Monday September 30, 2024. No late assignments will be accepted.

Question 1: Education

A school counselor was curious about the average of IQ of the students in her school and took a random sample of 25 students' IQ scores. The following is the data set:

1. Find a 90% confidence interval for the average student IQ in the school.

```
1 ymean <- mean(y) #mean 98.44
2 df <- length(y)-1
3 ystderr <- sd(y)/sqrt(length(y)) # standard error 2.618575
4 confidence <- qt((.9)+ (1-.9)/2, df) # confidence 1.710882
5 upper_90 <- (ymean + (confidence)*ystderr) # 102.9201
6 lower_90 <- (ymean - (confidence)*ystderr) # 93.95993</pre>
```

2. Next, the school counselor was curious whether the average student IQ in her school is higher than the average IQ score (100) among all the schools in the country. Using the same sample, conduct the appropriate hypothesis test with $\alpha = 0.05$.

The Null Hypothesis is that the mean is <= 100 The Alternative Hypothesis is that mean > 100

Step 3: Calculate the Test Statistic The test statistic is -0.5957439.

Code:

```
1 \text{ test\_stat} \leftarrow ((\text{ymean} - 100)/\text{ystderr})
```

Step 4: Calculate the P-Value
The p-value is 0.7215383.

Code:

```
1 \text{ pvalue} \leftarrow (1-\text{pt}(\text{test\_stat}, \text{df}))
```

Step 5:

Based on sufficient evidence, the p-value (0.7215) is greater than the alpha (0.05), we fail to reject the null hypothesis that the average IQ score is less than or equal to 100

Question 2: Political Economy

Researchers are curious about what affects the amount of money communities spend on addressing homelessness. The following variables constitute our data set about social welfare expenditures in the USA.

```
State | 50 states in US
Y | per capita expenditure on shelters/housing assistance in state
X1 | per capita personal income in state
X2 | Number of residents per 100,000 that are "financially insecure" in state
X3 | Number of people per thousand residing in urban areas in state
Region | 1=Northeast, 2= North Central, 3= South, 4=West
```

Explore the expenditure data set and import data into R.

```
expenditure <- read.table("https://raw.githubusercontent.com/ASDS-TCD/StatsI_Fall2024/main/datasets/expenditure.txt", header=T)
head(expenditure)
```

• Please plot the relationships among Y, X1, X2, and X3? What are the correlations among them (you just need to describe the graph and the relationships among them)?

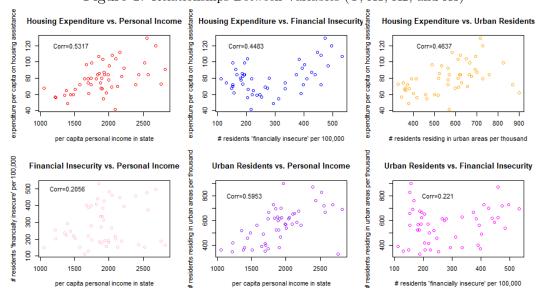


Figure 1: Relationships Between Variables (Y, X1, X2, and X3)

Relationships:

Housing Expenditure vs. Personal Income (top left) shows

a linear relationship with a strong, positive correlation. As personal income per capita in state increases so does the expenditure per capita on housing assistance in state.

Housing Expenditure vs. Financial Insecurity (top middle) has a nonlinear relationship with a weak correlation.

Housing Expenditure vs. Urban Residents (top right) showcases a linear relationship with a weak, positive correlation.

This shows there is an effect in expenditure on housing assistance as urban areas grow.

Financial Insecurity vs. Personal Income (bottom left) has a nonlinear relationship with little to no correlation. The variables of personal income and financial insecurity have little impact on eachother.

Urban Residents vs. Personal Income (bottom middle) has a linear relationship with a strong, positive correlation. There is a possible connection between increased personal income in state and increasing urban populations.

Urban Residents vs. Financial Insecurity (bottom right) has a nonlinear with little to no correlation. This shows that these variables have little impact in relation to each other.

Code:

```
par(mfrow = c(2,3))
plot (expenditure $X1, expenditure $Y, col='red',
       xlab = "per capita personal income in state",
       ylab = "expenditure per capita on housing assistance",
       main = "Housing Expenditure vs. Personal Income",
       text(1450,120, sprintf("Corr=%s", round(cor(expenditure$X1,
     expenditure $Y), 4)))
7 plot (expenditure $X2, expenditure $Y, col='blue',
       xlab = "# residents 'financially insecure' per 100,000",
       ylab = "expenditure per capita on housing assistance",
9
       main = "Housing Expenditure vs. Financial Insecurity",
       text (200, 120, sprintf ("Corr=%s", round (cor (expenditure $X2,
     expenditure $Y), 4))))
plot (expenditure $X3, expenditure $Y, col='orange',
       xlab = "# residents residing in urban areas per thousand",
13
       ylab = "expenditure per capita on housing assistance",
14
       main = "Housing Expenditure vs. Urban Residents",
       text (500, 120, sprintf ("Corr=%s", round (cor (expenditure $X3,
```

```
expenditure (Y), (4))
  plot (expenditure $X1, expenditure $X2, col='pink',
       xlab = "per capita personal income in state",
18
       ylab = "# residents 'financially insecure' per 100,000",
19
       main = "Financial Insecurity vs. Personal Income",
20
       text (1400, 500, sprintf ("Corr=%s", round (cor (expenditure $X1,
21
      expenditure \$X2, 4))))
  plot(expenditure$X1, expenditure$X3, col='purple',
       xlab = "per capita personal income in state",
23
       ylab = "# residents residing in urban areas per thousand",
24
       main = "Urban Residents vs. Personal Income"
25
       text (1400, 800, sprintf ("Corr=%s", round (cor (expenditure $X1,
      expenditure (X3), (4))
  plot (expenditure $X2, expenditure $X3, col='magenta',
       xlab = "# residents 'financially insecure' per 100,000",
28
       ylab = "# residents residing in urban areas per thousand",
29
       main = "Urban Residents vs. Financial Insecurity",
30
       text (250, 800, sprintf ("Corr=%s", round (cor (expenditure $X2,
     expenditure X3, X
```

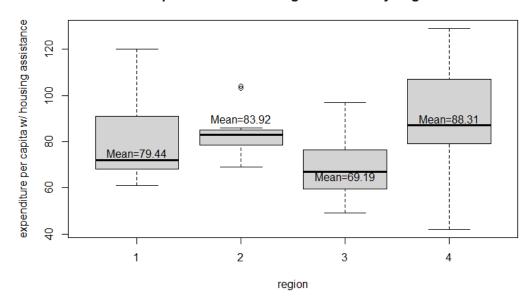
• Please plot the relationship between Y and Region? On average, which region has the highest per capita expenditure on housing assistance?

On average, the West (Region 4) has the highest per capita expenditure on housing assistance at 88.31.

Code:

Figure 2: Relationship between Y and Region

Expenditure on Housing Assistance by Region



• Please plot the relationship between Y and X1? Describe this graph and the relationship. Reproduce the above graph including one more variable Region and display different regions with different types of symbols and colors.

Region 1 and 3 have a positive linear relationship and a wide data spread with strong correlations.

Region 2 and 4 have a nonlinear relationship with a central distribution of data and little to no correlation between variables. This means, according to these basic correlation tests, that states in the Northeast and the South generally see an increase in expenditure per capita on housing assistance when personal income percapita increases as well, however, this cannot be said for the North Central and West.

Code:

```
title = "Region")

cor(expenditure$X1[expenditure$Region == "1"], expenditure$Y[expenditure$Region == "1"])

cor(expenditure$X1[expenditure$Region == "2"], expenditure$Y[expenditure$Region == "2"],

Region == "2"])

cor(expenditure$X1[expenditure$Region == "3"], expenditure$Y[expenditure$Region == "3"])

cor(expenditure$X1[expenditure$Region == "4"], expenditure$Y[expenditure$Region == "4"])
```

Figure 3: Relationship between Y and X1 based on Region

Housing Expenditure vs. Personal Income

