

## Lab 2: Chaos Game

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Experiment goals:

- Study how changing the number of points and iterations we can vastly change how a resulting plot looks.
- Experiment with repeated patterns that generate fractals
- inspect implemented code to generate the famous Sierpinski's Triangle and Barnsley's Fern.

Why is this important?

- The field has many applications across natural sciences and pure mathematics
- Study of the code leads to greater insight on how the systems are generated and how to analyze them.

# Sierpinski's Triangle

The code used to generate the triangle was:

```
def midpoint(P, Q):  
    return (0.5*(P[0] + Q[0]), 0.5*(P[1] + Q[1]))
```

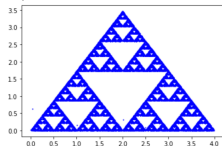
```
vertices = [(0, 0), (2, 2*np.sqrt(3)), (4, 0)]  
n = 25 # Change this value and see what happens
```

```
x = [0]*n  
y = [0]*n  
x[0] = random()  
y[0] = random()
```

```
for i in range(1, n):  
    x[i], y[i] = midpoint( vertices[randint(0, 2)], (x[i-1], y[i-1]) )
```

```
plt.scatter(x, y, color = 'b', s=1)
```

As the parameter  $n$  increases, The figure slowly approaches



# Barnsley's Fern

The code used to generate the fern was:

```
# Barnsley's Fern

# 1% of the time: x ← 0, y ← 0.16
# 85% of the time: x ← 0.85 x + 0.04, y ← -0.04 x + 0.05 y + 1.6
# 7% of the time: x ← 0.2 x - 0.26 y, y ← 0.23 x + 0.22 y + 1.6
# 7% of the time: x ← -0.15 x + 0.28 y, y ← 0.26 x + 0.24 y + 0.44

def pick(p):
    c = np.cumsum(p)
    return bisect(c, np.random.random() * c[-1])

p = np.array([0.01, 0.07, 0.07, 0.85])

eq = [np.array([[0, 0, 0], [0, 0.16, 0]]),
      np.array([[0.2, -0.26, 0], [0.23, 0.22, 1.6]]),
      np.array([[0.15, 0.28, 0], [0.26, 0.24, 0.44]]),
      np.array([[0.85, 0.04, 0], [-0.04, 0.85, 1.6]])]

n = 25 # Change this value and see what happens
x = np.zeros((n, 3))
x[:, 2] = 1

for i in range(1, n):
    x[i, :2] = np.matmul(eq[pick(p)], x[i-1, :])

plt.figure(figsize=(10, 10))
plt.scatter(x[:, 0], x[:, 1], s=3, c="g", marker="s", linewidths=0)
plt.axis("equal"), plt.axis("off")
```

As the parameter  $n$  increases, The figure slowly approaches



# Analysis and Conclusion

In conclusion, bounded randomness can generate very interesting images when iterated with itself, which changes and becomes more accurate as the number of iterations increase.