

Atrial Fibrillation Classification

The goal of this exercise is to train different neural networks to discriminate between atrial fibrillation and normal sinus rhythm from a sequence of interbeat intervals. We use interbeat intervals extracted from the Long Term AF Database (<https://physionet.org/content/ltafdb/1.0.0/>).

We will train the following models on windows of interbeat intervals:

- Logistic regression
- Multi-layer perceptron
- Convolutional neural network
- Recurrent neural network

In addition, the first two models will also be trained on simple features derived from each window of interbeat intervals.

First, we import all the required packages, define global constants, and seed the random number generators to obtain reproducible results.

```
In [1]: %matplotlib widget

import itertools
import logging
import operator
import pathlib
import warnings

import IPython.display
import matplotlib.pyplot as plt
import numpy as np
import pandas as pd
import pytorch_lightning as pl
import scipy.special
import seaborn as sns
import sklearn.metrics
import sklearn.model_selection
import torch

DATA_FILE = pathlib.Path('../data/ltafdb_intervals.npz')
LOG_DIRECTORY = pathlib.Path('../logs/af_classification')

# Disable Logging for PyTorch Lightning to avoid too long outputs.
logging.getLogger('pytorch_lightning').setLevel(logging.ERROR)

# Seed random number generators for reproducible results.
pl.seed_everything(42)
```

Seed set to 42

Out[1]: 42

Then, we load the windows of interbeat intervals and the corresponding labels. We also load the record identifiers. They will help to avoid using intervals from the same record for both training and testing.

```
In [2]: def load_data():
    with np.load(DATA_FILE) as data:
        intervals = data['intervals']
        labels = data['labels']
        identifiers = data['identifiers']
    return intervals, labels, identifiers

intervals, labels, identifiers = load_data()
targets = (labels == 'atrial_fibrillation').astype('float32')[:, None]
window_size = intervals.shape[1]

print(f'Number of windows: {intervals.shape[0]}')
print(f'Window size: {window_size}')
print(f'Window labels: {set(labels)}')
```

Number of windows: 25064

Window size: 32

Window labels: {'atrial_fibrillation', 'normal_sinus_rhythm'}

Here are a few examples of windows of interbeat intervals.

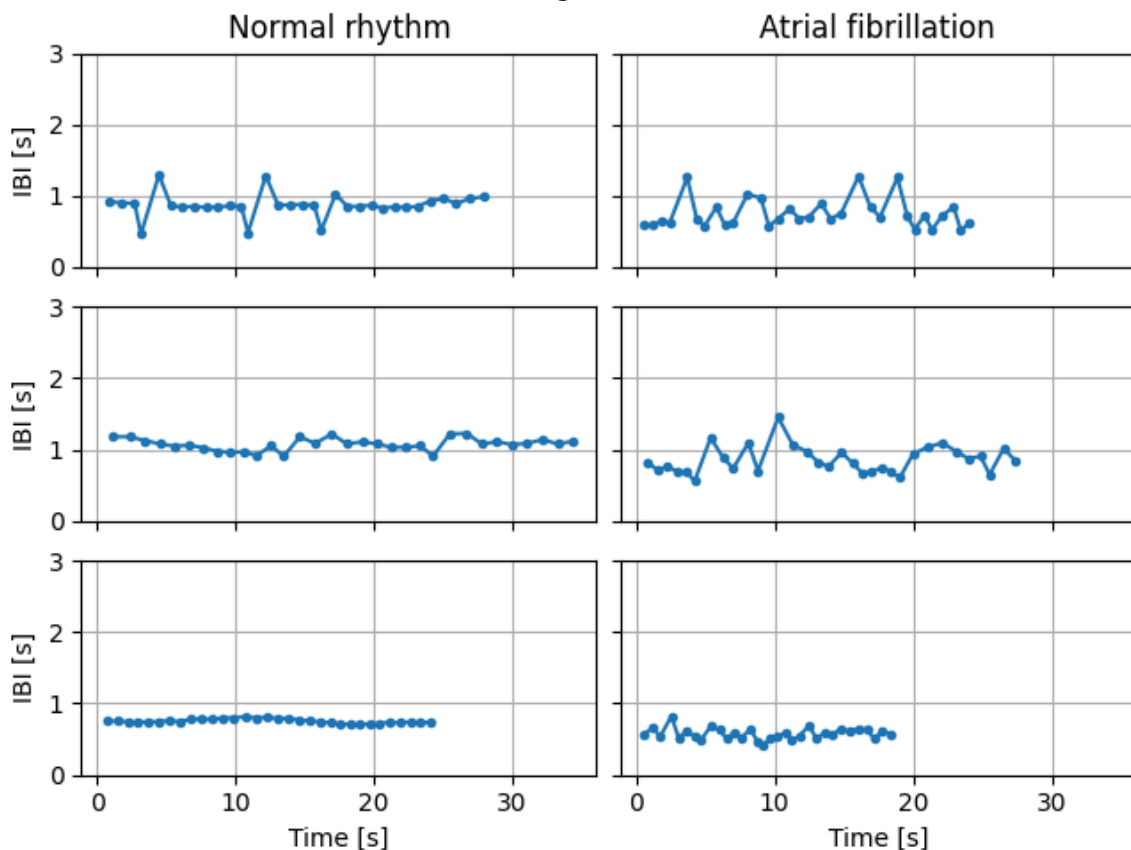
```
In [3]: def plot_interval_examples(intervals, targets, n_examples=3):
    normal_indices = np.random.choice(np.flatnonzero(targets == 0.0), n_examples)
    af_indices = np.random.choice(np.flatnonzero(targets == 1.0), n_examples, replace=True)

    def plot_intervals(ax, index):
        ax.plot(np.cumsum(intervals[index]), intervals[index], '-.')
        ax.grid(True)

    fig, axes = plt.subplots(n_examples, 2, sharex='all', sharey='all', squeeze=False)
    for i in range(n_examples):
        plot_intervals(axes[i, 0], normal_indices[i])
        plot_intervals(axes[i, 1], af_indices[i])
    plt.setp(axes, ylim=(0.0, 3.0))
    plt.setp(axes[-1, :], xlabel='Time [s]')
    plt.setp(axes[:, 0], ylabel='IBI [s]')
    axes[0, 0].set_title('Normal rhythm')
    axes[0, 1].set_title('Atrial fibrillation')

    plot_interval_examples(intervals, targets)
```

Figure



Question 1

Visually, what are the differences between the examples of the two classes?

Answer: During atrial fibrillation, the average interbeat interval is lower than during normal rhythm and features significantly more variation.

The next step is to split the dataset into subsets for training, validation, and testing stratified by labels. We use the record identifiers to avoid using windows from the same record in more than one subset.

```
In [4]: def split_data(identifiers, intervals, targets):
    splitter = sklearn.model_selection.StratifiedGroupKFold(n_splits=5)
    indices = list(map(operator.itemgetter(1), splitter.split(intervals, targets)))
    i_train = np.hstack(indices[:-2])
    i_val = indices[-2]
    i_test = indices[-1]

    assert not (set(identifiers[i_train]) & set(identifiers[i_val]))
    assert not (set(identifiers[i_train]) & set(identifiers[i_test]))
    assert not (set(identifiers[i_val]) & set(identifiers[i_test]))
    assert set(identifiers[i_train]) | set(identifiers[i_val]) | set(identifiers[i_test]) == set(identifiers)

    return i_train, i_val, i_test

i_train, i_val, i_test = split_data(identifiers, intervals, targets)

def build_summary(subsets, targets):
```

```

data = []
for subset, y in zip(subsets, targets):
    data.append({
        'subset': subset,
        'total_count': y.size,
        'normal_count': np.sum(y == 0.0),
        'af_count': np.sum(y == 1.0),
        'normal_proportion': np.mean(y == 0.0),
        'af_proportion': np.mean(y == 1.0),
    })
return pd.DataFrame(data)

```

```
IPython.display.display(build_summary(('training', 'validation', 'testing'), (ta
```

	subset	total_count	normal_count	af_count	normal_proportion	af_proportion
0	training	15000	6919	8081	0.461267	0.538733
1	validation	4964	2365	2599	0.476430	0.523570
2	testing	4964	2365	2599	0.476430	0.523570

To better understand the dataset, we extract two features from each window of interbeat intervals: the mean and the standard deviation. We then plot these two features for the two classes.

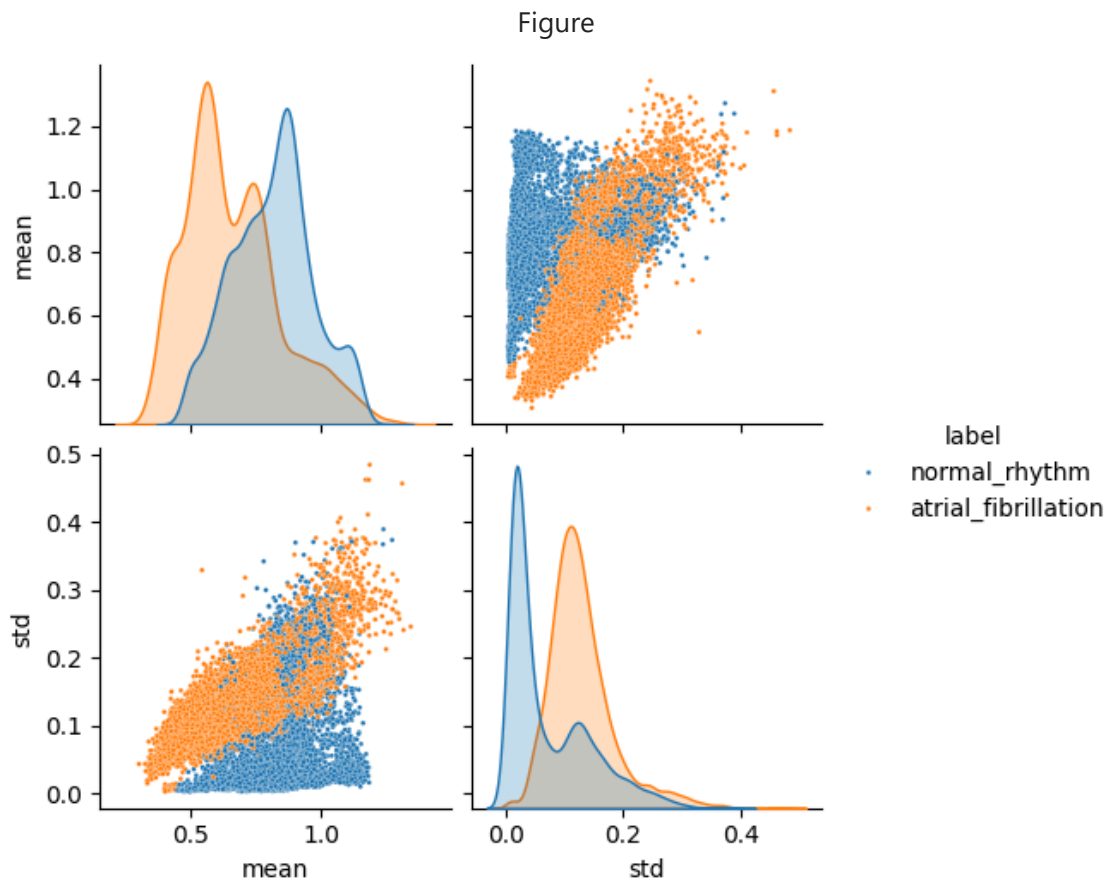
```

In [5]: features = np.vstack((
    np.mean(intervals, axis=1),
    np.std(intervals, axis=1),
)).T

def plot_features(f, y):
    data = pd.DataFrame({
        'label': y.ravel(),
        'mean': f[:, 0],
        'std': f[:, 1],
    })
    data['label'] = data['label'].map({0.0: 'normal_rhythm', 1.0: 'atrial_fibril
sns.pairplot(data, hue='label', plot_kws={'s': 4})

plot_features(features[i_train], targets[i_train])

```



Question 2

Would it be possible to discriminate between the two classes with these features and a linear classifier?

Answer: No. Although the main mode of the mean and std distribution of each class are clearly separated, there is a significant overlap between the distributions. There is no hyperplane that can entirely separate the two set of points.

To classify atrial fibrillation and normal rhythm, we define three models: a multi-layer perceptron (MLP), a convolutional neural network (CNN), and a recurrent neural network (RNN).

Make sure you understand the differences between these models.

```
In [6]: class MlpModel(torch.nn.Module):

    def __init__(self, input_size, output_size, n_hidden_layers=1, n_units=128):
        super().__init__()
        self.input_size = input_size
        self.output_size = output_size
        self.n_hidden_layers = n_hidden_layers
        self.n_units = n_units
        self.layers = self._build_layers()

    def _build_layers(self):
        sizes = [self.input_size]
        sizes.extend(itertools.repeat(self.n_units, self.n_hidden_layers))
        layers = []
```

```

        for i in range(self.n_hidden_layers):
            layers.append(torch.nn.Linear(sizes[i], sizes[i + 1]))
            layers.append(torch.nn.ReLU())
        layers.append(torch.nn.Linear(sizes[-1], self.output_size))
        return torch.nn.Sequential(*layers)

    def forward(self, x):
        return self.layers(x)

class CnnModel(torch.nn.Module):

    def __init__(self,
                  input_size,
                  output_size,
                  n_layers=3,
                  n_initial_channels=8,
                  kernel_size=3):
        super().__init__()
        self.input_size = input_size
        self.output_size = output_size
        self.n_layers = n_layers
        self.n_initial_channels = n_initial_channels
        self.kernel_size = kernel_size
        self.layers = self._build_layers()

    def _build_layers(self):
        layers = []

        # Build convolutional layers. Each layer is composed of a convolution,
        # a ReLU activation, and max pooling (except for the last convolutional
        # layer that uses global average pooling).
        n_output_channels = 1
        for i in range(self.n_layers):
            n_input_channels = n_output_channels
            n_output_channels = self.n_initial_channels * 2 ** i
            layers.append(torch.nn.Conv1d(
                in_channels=n_input_channels,
                out_channels=n_output_channels,
                kernel_size=self.kernel_size,
                padding='same',
            ))
            layers.append(torch.nn.ReLU())
            if i < self.n_layers - 1:
                layers.append(torch.nn.MaxPool1d(kernel_size=2))
            else:
                layers.append(torch.nn.AdaptiveAvgPool1d(1))
        layers.append(torch.nn.Flatten())

        # Build output layer.
        layers.append(torch.nn.Linear(
            in_features=self.n_initial_channels * 2 ** (self.n_layers - 1),
            out_features=self.output_size,
        ))

        return torch.nn.Sequential(*layers)

    def forward(self, x):
        x = x.view(x.shape[0], 1, x.shape[1])
        return self.layers(x)

```

```

class RnnModel(torch.nn.Module):

    def __init__(self, input_size, output_size, hidden_size=64):
        super().__init__()
        self.input_size = input_size
        self.output_size = output_size
        self.hidden_size = hidden_size
        self.recurrent_layer = torch.nn.GRU(
            input_size=1,
            hidden_size=self.hidden_size,
            num_layers=1,
            batch_first=False,
        )
        self.output_layer = torch.nn.Linear(self.hidden_size, self.output_size)

    def forward(self, x):
        x = x.transpose(0, 1)[..., None]
        y, h = self.recurrent_layer(x)
        return self.output_layer(y[-1])

```

We also define a class to manage different models and a few functions to train and evaluate models.

```

In [7]: class Classifier(pl.LightningModule):

    def __init__(self, config):
        super().__init__()
        self.save_hyperparameters()
        self.config = config
        self.model = self._build_model()
        self.example_input_array = torch.zeros((1, self.model.input_size))

    def _build_model(self):
        name = self.config['model']['name']
        config = self.config['model'].get('config', {})
        if name == 'mlp':
            return MlpModel(**config)
        elif name == 'cnn':
            return CnnModel(**config)
        elif name == 'rnn':
            return RnnModel(**config)
        else:
            raise ValueError(f'unknown model: {name!r}')

    def configure_optimizers(self):
        name = self.config['optimizer']['name']
        config = self.config['optimizer'].get('config', {})
        if name == 'sgd':
            return torch.optim.SGD(self.parameters(), **config)
        elif name == 'adam':
            return torch.optim.Adam(self.parameters(), **config)
        else:
            raise ValueError(f'unknown optimizer: {name!r}')

    def forward(self, x):
        return self.model(x)

```

```

def training_step(self, batch, batch_idx):
    return self._run_step(batch, 'train')

def validation_step(self, batch, batch_idx):
    self._run_step(batch, 'val')

def test_step(self, batch, batch_idx):
    self._run_step(batch, 'test')

def predict_step(self, batch, batch_idx, dataloader_idx=0):
    x, y = batch
    return self.model(x)

def _run_step(self, batch, subset):
    x, y = batch
    logits = self.model(x)
    loss = torch.nn.functional.binary_cross_entropy_with_logits(logits, y)
    acc = ((logits > 0.0).float() == y).float().mean()
    self.log_dict({f'{subset}_loss': loss, f'{subset}_acc': acc},
                  on_step=False, on_epoch=True, prog_bar=True)
    return loss

def build_loader(*tensors, batch_size=100, shuffle=False, n_workers=0):
    dataset = torch.utils.data.TensorDataset(*map(torch.Tensor, tensors))
    return torch.utils.data.DataLoader(
        dataset=dataset,
        batch_size=batch_size,
        shuffle=shuffle,
        num_workers=n_workers,
    )

def train_model(name, config, x, y, i_train, i_val, n_epochs=10, batch_size=100):
    train_loader = build_loader(x[i_train], y[i_train], batch_size=batch_size, shuffle=True)
    val_loader = build_loader(x[i_val], y[i_val], batch_size=batch_size, shuffle=False)
    classifier = Classifier(config)
    print(pl.utilities.model_summary.ModelSummary(classifier, max_depth=-1))

    with warnings.catch_warnings():
        warnings.simplefilter('ignore')
        trainer = pl.Trainer(
            default_root_dir=LOG_DIRECTORY,
            logger=pl.loggers.TensorBoardLogger(LOG_DIRECTORY, name),
            enable_model_summary=False,
            max_epochs=n_epochs,
        )
        trainer.fit(classifier, train_loader, val_loader)

    return classifier

def compute_metrics(targets, predictions, threshold=0.5):
    targets = np.ravel(targets) > threshold
    predictions = np.ravel(predictions) > threshold
    c = sklearn.metrics.confusion_matrix(targets, predictions)
    tp = c[1, 1]
    tn = c[0, 0]
    fp = c[0, 1]
    fn = c[1, 0]
    return {

```



```

        'count': c.sum(),
        'acc': (tp + tn) / (tp + tn + fp + fn),
        'tpr': tp / (tp + fn),
        'tnr': tn / (tn + fp),
        'ppv': tp / (tp + fp),
        'npv': tn / (tn + fn),
        'f1': 2 * tp / (2 * tp + fp + fn),
    }

def evaluate_model(model, x, y, i_train, i_val, i_test, batch_size=100):
    loader = build_loader(x, y, batch_size=batch_size)

    with warnings.catch_warnings():
        warnings.simplefilter('ignore')
        trainer = pl.Trainer(
            default_root_dir=LOG_DIRECTORY,
            logger=False,
            enable_progress_bar=False,
            enable_model_summary=False,
        )
        z = trainer.predict(model, loader)
    z = np.vstack([u.numpy() for u in z])
    z = scipy.special.expit(z) # Convert logits to probabilities.

    metrics = []
    for subset, indices in (('train', i_train), ('val', i_val), ('test', i_test)):
        metrics.append({
            'subset': subset,
            **compute_metrics(y[indices], z[indices]),
        })

    return pd.DataFrame(metrics)

```

The final step before training and evaluating models is to define the configurations of the different models.

We will train the following models:

- Features as inputs (input size = 2):
 - Logistic regression
 - Multi-layer perceptron
 - Dense layer (output size = 128)
 - ReLU activation
 - Dense layer (output size = 128)
 - ReLU activation
 - Dense layer (output size = 1)
- Interbeat intervals as inputs (input_size = 32):
 - Logistic regression
 - Multi-layer perceptron
 - Dense layer (output size = 128)
 - ReLU activation
 - Dense layer (output size = 128)
 - ReLU activation

- Dense layer (output size = 1)
- Convolutional neural network
 - Convolutional layer (kernel size = 3, output size = 32, output channels = 8)
 - ReLU activation
 - Max pooling (output size = 16, output channels = 8)
 - Convolutional layer (kernel size = 3, output size = 16, output channels = 16)
 - ReLU activation
 - Max pooling (output size = 8, output channels = 16)
 - Convolutional layer (kernel size = 3, output size = 8, output channels = 32)
 - ReLU activation
 - Global average pooling (output size = 32)
 - Dense layer (output size = 1)
- Recurrent neural network
 - GRU layer (output size = 64)
 - Dense layer (output size = 1)

```
In [8]: n_epochs = 40
batch_size = 200

configs = {
    'features_logistic': {
        'model': {
            'name': 'mlp',
            'config': {
                'input_size': features.shape[1],
                'output_size': targets.shape[1],
                'n_hidden_layers': 0, # A multi-layer perceptron without hidden
            },
        },
        'optimizer': {
            'name': 'adam',
            'config': {'lr': 0.01},
        },
    },
    'features_mlp': {
        'model': {
            'name': 'mlp',
            'config': {
                'input_size': features.shape[1],
                'output_size': targets.shape[1],
                'n_hidden_layers': 2,
                'n_units': 128,
            },
        },
        'optimizer': {
            'name': 'adam',
            'config': {'lr': 0.001},
        },
    },
    'logistic': {
        'model': {
            'name': 'mlp',
            'config': {
```

```

        'input_size': intervals.shape[1],
        'output_size': targets.shape[1],
        'n_hidden_layers': 0, # A multi-layer perceptron without hidden
    },
},
'optimizer': {
    'name': 'adam',
    'config': {'lr': 0.001},
},
},
'mlp': {
    'model': {
        'name': 'mlp',
        'config': {
            'input_size': intervals.shape[1],
            'output_size': targets.shape[1],
            'n_hidden_layers': 2,
            'n_units': 128,
        },
    },
    'optimizer': {
        'name': 'adam',
        'config': {'lr': 0.001},
    },
},
'cnn': {
    'model': {
        'name': 'cnn',
        'config': {
            'input_size': intervals.shape[1],
            'output_size': targets.shape[1],
            'n_layers': 3,
            'n_initial_channels': 8,
            'kernel_size': 3,
        },
    },
    'optimizer': {
        'name': 'adam',
        'config': {'lr': 0.001},
    },
},
'rnn': {
    'model': {
        'name': 'rnn',
        'config': {
            'input_size': intervals.shape[1],
            'output_size': targets.shape[1],
            'hidden_size': 64,
        },
    },
    'optimizer': {
        'name': 'adam',
        'config': {'lr': 0.001},
    },
},
}

```

To visualize the loss and accuracy during training, we start TensorBoard.

If you prefer to view TensorBoard in a separate window, you can open <http://localhost:6006/> in your web browser.

```
In [9]: %reload_ext tensorboard
%tensorboard --logdir ../logs/af_classification --port 6006
```

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Nom	Taille	Date de modification
\$Recycle.Bin/		23/11/2023 20:06:09
AppData/		09/12/2023 12:20:38
Config.Msi/		22/11/2024 19:32:34
DATA/		23/11/2023 21:31:22
Dokumente und Einstellungen/		23/11/2023 17:25:38
gurobi1003/		24/05/2024 19:45:05
hp/		02/09/2023 15:07:32
Kairos/		09/12/2023 12:21:05
OneDriveTemp/		13/05/2024 09:21:25
PerfLogs/		07/05/2022 07:24:50
Program Files/		12/12/2024 09:39:35
Program Files (x86)/		03/10/2024 15:05:28
ProgramData/		22/11/2024 19:32:39
Programme/		23/11/2023 17:25:38
Recovery/		23/11/2023 19:49:01
System Volume Information/		09/12/2024 19:44:33
System.sav/		03/09/2023 02:01:15
Users/		23/11/2023 20:57:48
Windows/		13/11/2024 03:36:39
DumpStack.log.tmp	12.0 kB	22/11/2024 19:32:37
hiberfil.sys	6.3 GB	12/12/2024 09:38:15
install.log	1015 kB	09/12/2023 12:21:15
pagefile.sys	31.0 GB	09/12/2024 20:19:31
Rapport-batterie.html	83.5 kB	02/12/2024 11:32:23
swapfile.sys	16.0 MB	22/11/2024 19:32:37

Finally, we train the different models. It will take a few minutes.

```
In [10]: models = {}
for name, config in configs.items():
    print(f'Training {name!r} model')
```

```
x = features if name.startswith('features') else intervals
y = targets
models[name] = train_model(name, config, x, y, i_train, i_val, n_epochs, bat
print('\n\n') # Add blank lines to separate models in the output.
```

Training 'features_logistic' model

	Name	Type	Params	Mode	In sizes	Out sizes
--	------	------	--------	------	----------	-----------

0	model	MlpModel	3	train	[1, 2]	[1, 1]
1	model.layers	Sequential	3	train	[1, 2]	[1, 1]
2	model.layers.0	Linear	3	train	[1, 2]	[1, 1]

3 Trainable params

0 Non-trainable params

3 Total params

0.000 Total estimated model params size (MB)

3 Modules in train mode

0 Modules in eval mode

Sanity Checking: | 0/? [00:00<?, ?it/s]

Training: | 0/? [00:00<?, ?it/s]

Validation: | 0/? [00:00<?, ?it/s]

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Validation: | 0/? [00:00<?, ?it/s]

Validation: | 0/? [00:00<?, ?it/s]

Training 'features_mlp' model

	Name	Type	Params	Mode	In sizes	Out sizes
0	model	MlpModel	17.0 K	train	[1, 2]	[1, 1]
1	model.layers	Sequential	17.0 K	train	[1, 2]	[1, 1]
2	model.layers.0	Linear	384	train	[1, 2]	[1, 128]
3	model.layers.1	ReLU	0	train	[1, 128]	[1, 128]
4	model.layers.2	Linear	16.5 K	train	[1, 128]	[1, 128]
5	model.layers.3	ReLU	0	train	[1, 128]	[1, 128]
6	model.layers.4	Linear	129	train	[1, 128]	[1, 1]

17.0 K Trainable params

0 Non-trainable params

17.0 K Total params

0.068 Total estimated model params size (MB)

7 Modules in train mode

0 Modules in eval mode

Sanity Checking: | 0/? [00:00<?, ?it/s]

Training: | 0/? [00:00<?, ?it/s]

Validation: | 0/? [00:00<?, ?it/s]

Validation: | 0/? [00:00<?, ?it/s]

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Training 'logistic' model

	Name	Type	Params	Mode	In sizes	Out sizes
0	model	MlpModel	33	train	[1, 32]	[1, 1]
1	model.layers	Sequential	33	train	[1, 32]	[1, 1]
2	model.layers.0	Linear	33	train	[1, 32]	[1, 1]

```
33      Trainable params
0       Non-trainable params
33      Total params
0.000   Total estimated model params size (MB)
3       Modules in train mode
0       Modules in eval mode
```

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Sanity Checking: |           | 0/? [00:00<?, ?it/s]
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Training: |           | 0/? [00:00<?, ?it/s]
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Training 'mlp' model

	Name	Type	Params	Mode	In sizes	Out sizes
0	model	MlpModel	20.9 K	train	[1, 32]	[1, 1]
1	model.layers	Sequential	20.9 K	train	[1, 32]	[1, 1]
2	model.layers.0	Linear	4.2 K	train	[1, 32]	[1, 128]
3	model.layers.1	ReLU	0	train	[1, 128]	[1, 128]
4	model.layers.2	Linear	16.5 K	train	[1, 128]	[1, 128]
5	model.layers.3	ReLU	0	train	[1, 128]	[1, 128]
6	model.layers.4	Linear	129	train	[1, 128]	[1, 1]

20.9 K Trainable params

0 Non-trainable params

20.9 K Total params

0.083 Total estimated model params size (MB)

7 Modules in train mode

0 Modules in eval mode

Sanity Checking: | 0/? [00:00<?, ?it/s]

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Training 'cnn' model

	Name	Type	Params	Mode	In sizes	Out sizes

0	model	CnnModel	2.0 K	train	[1, 32]	[1, 1]
1	model.layers	Sequential	2.0 K	train	[1, 1, 32]	[1, 1]
2	model.layers.0	Conv1d	32	train	[1, 1, 32]	[1, 8, 32]
3	model.layers.1	ReLU	0	train	[1, 8, 32]	[1, 8, 32]
4	model.layers.2	MaxPool1d	0	train	[1, 8, 32]	[1, 8, 16]
5	model.layers.3	Conv1d	400	train	[1, 8, 16]	[1, 16, 16]
6	model.layers.4	ReLU	0	train	[1, 16, 16]	[1, 16, 16]
7	model.layers.5	MaxPool1d	0	train	[1, 16, 16]	[1, 16, 8]
8	model.layers.6	Conv1d	1.6 K	train	[1, 16, 8]	[1, 32, 8]
9	model.layers.7	ReLU	0	train	[1, 32, 8]	[1, 32, 8]
10	model.layers.8	AdaptiveAvgPool1d	0	train	[1, 32, 8]	[1, 32, 1]
11	model.layers.9	Flatten	0	train	[1, 32, 1]	[1, 32]
12	model.layers.10	Linear	33	train	[1, 32]	[1, 1]

 2.0 K Trainable params
 0 Non-trainable params
 2.0 K Total params
 0.008 Total estimated model params size (MB)
 13 Modules in train mode
 0 Modules in eval mode
 Sanity Checking: | | 0/? [00:00<?, ?it/s]
 Training: | | 0/? [00:00<?, ?it/s]
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[illegible]

Training 'rnn' model

	Name	Type	Params	Mode	In sizes	Out sizes
0	model	RnnModel	12.9 K	train	[1, 32]	[1, 1]
1	model.recurrent_layer	GRU	12.9 K	train	[32, 1, 1]	[[32, 1, 64], [1, 1, 64]]
2	model.output_layer	Linear	65	train	[1, 64]	[1, 1]

[illegible]

```

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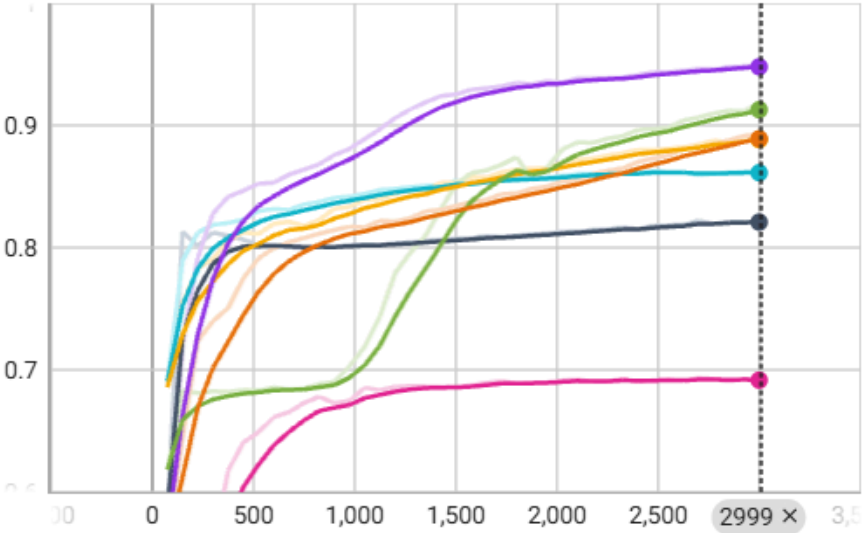
Question 3

Based on the model summaries printed above and the metrics shown in TensorBoard, answer the following questions:

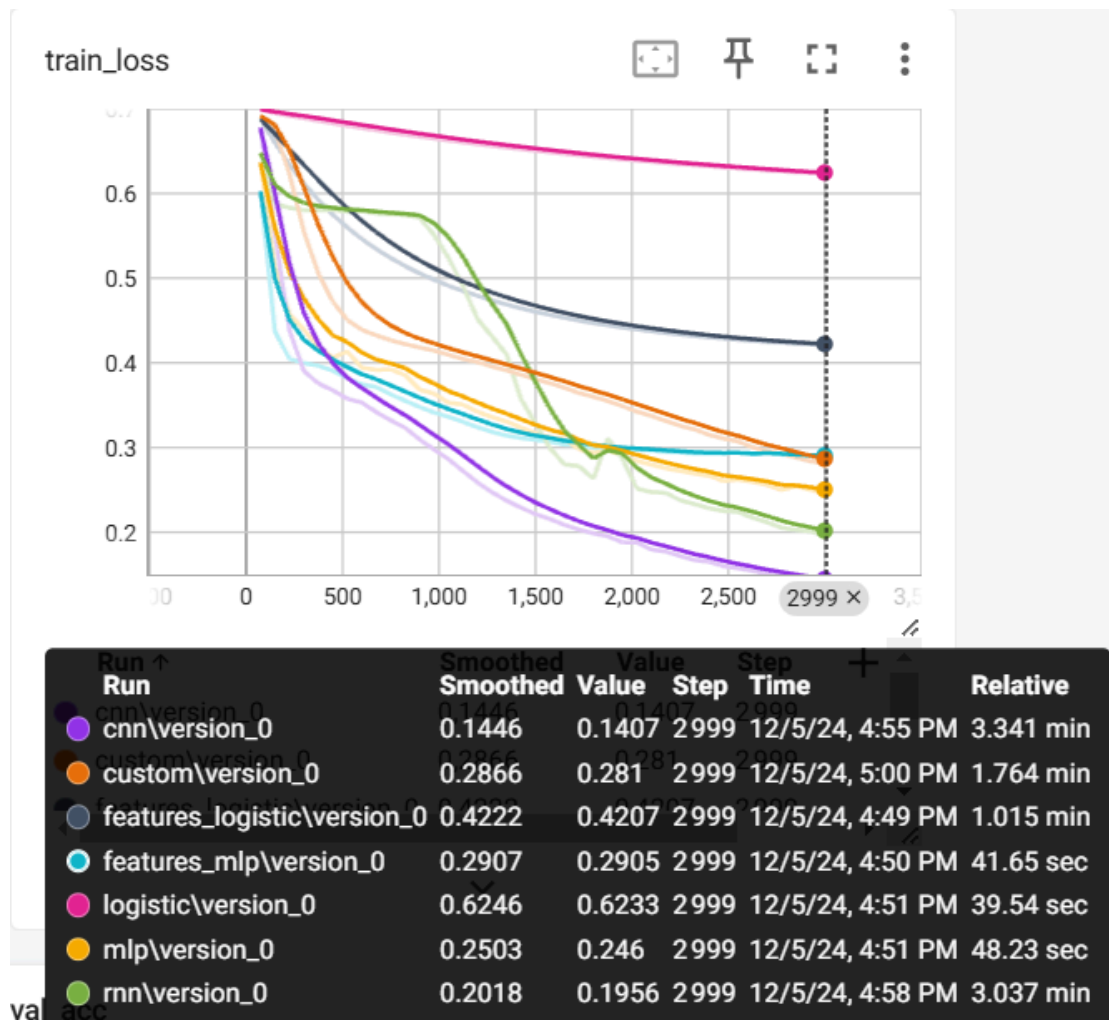
1. After training is finished, you can see the number of parameters for each model.
Why is the number of parameters for the CNN model much lower than for the MLP model?
2. What can you about the loss and accuracy of the different models on the training and validation subsets? Do some model overfit?
3. Why does the logistic regression that takes features as inputs performs much better than the logistic regression that takes raw interbeat intervals as inputs?
4. Are there models that would benefit from training for more epochs?

Train Accuracy

Run	Smoothed Value	Step	Time	Relative
● cnn\version_0	0.9479	0.9491	2999	12/5/24, 4:55 PM 3.341 min
● custom\version_0	0.889	0.8927	2999	12/5/24, 5:00 PM 1.764 min
● features_logistic\version_0	0.8209	0.8215	2999	12/5/24, 4:49 PM 1.015 min
● features_mlp\version_0	0.8613	0.8613	2999	12/5/24, 4:50 PM 41.65 sec
● logistic\version_0	0.6916	0.6908	2999	12/5/24, 4:51 PM 39.54 sec
● mlp\version_0	0.8884	0.8908	2999	12/5/24, 4:51 PM 48.23 sec
● rnn\version_0	0.9128	0.9179	2999	12/5/24, 4:58 PM 3.037 min

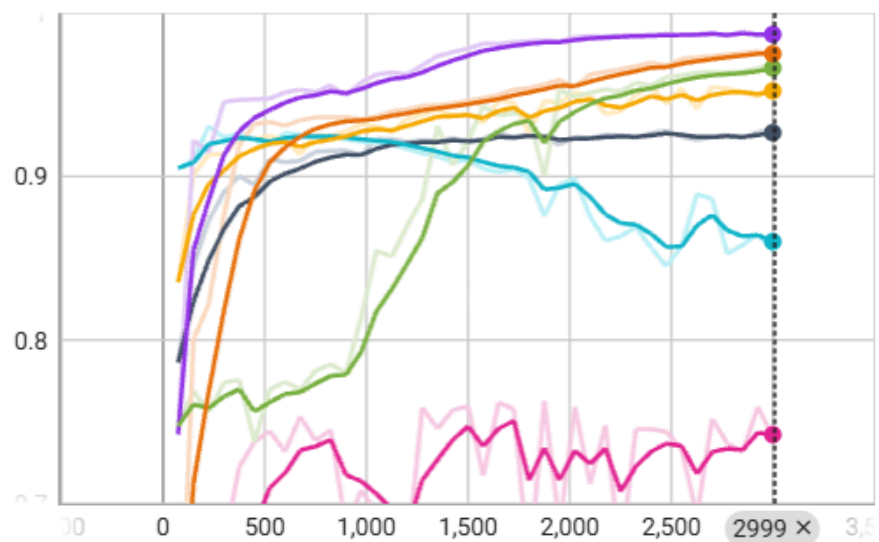


Train Loss



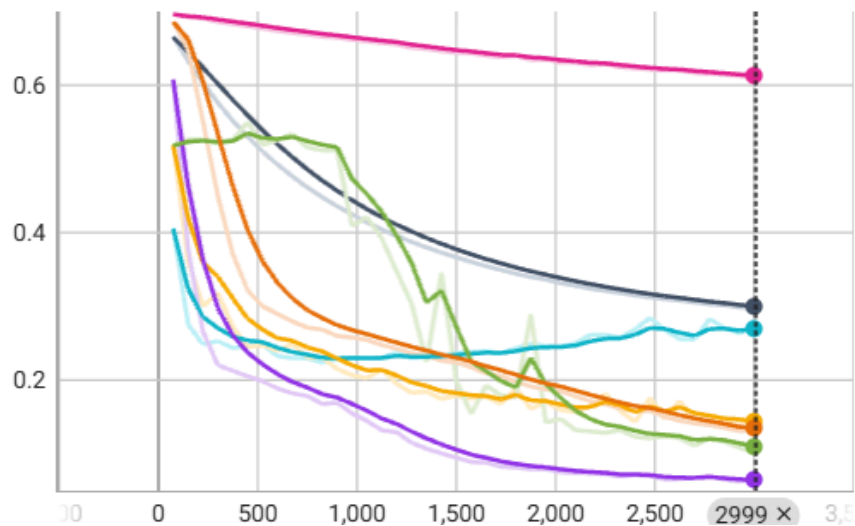
Validation Accuracy

Run	Smoothed Value	Value	Step	Time	Relative
cnn\version_0	0.9869	0.9869	2999	12/5/24, 4:55 PM	3.341 min
custom\version_0	0.975	0.975	2999	12/5/24, 5:00 PM	1.764 min
features_logistic\version_0	0.9268	0.9289	2999	12/5/24, 4:49 PM	1.015 min
features_mlp\version_0	0.8602	0.8544	2999	12/5/24, 4:50 PM	41.66 sec
logistic\version_0	0.7422	0.7405	2999	12/5/24, 4:51 PM	39.55 sec
mlp\version_0	0.9523	0.9553	2999	12/5/24, 4:51 PM	48.23 sec
rnn\version_0	0.9663	0.9692	2999	12/5/24, 4:58 PM	3.037 min



Validation Loss

Run	Smoothed Value	Step	Time	Relative
● cnn\version_0	0.06527	0.06503	2 999	12/5/24, 4:55 PM 3.341 min
● custom\version_0	0.1351	0.1328	2 999	12/5/24, 5:00 PM 1.764 min
○ features_logistic\version_0	0.2999	0.2967	2 999	12/5/24, 4:49 PM 1.015 min
● features_mlp\version_0	0.2698	0.2736	2 999	12/5/24, 4:50 PM 41.66 sec
● logistic\version_0	0.6132	0.6111	2 999	12/5/24, 4:51 PM 39.55 sec
● mlp\version_0	0.144	0.1397	2 999	12/5/24, 4:51 PM 48.23 sec
● rnn\version_0	0.1097	0.1026	2 999	12/5/24, 4:58 PM 3.037 min



Answer:

1. A convolution is a special case of a linear transformation. While a linear layer is defined by the $m \times n$ coefficients of the associated matrix, where m and n are the output and input dimensions respectively, a convolutional layer is defined by its kernel, which is much smaller than the input and output dimensions. This allows the CNN model to have less parameters in total despite having more layers, as each layer has much less parameters.
2. All models show a validation accuracy higher than their training accuracy, suggesting that they are not overfitting. The exception is the features_MLP because the Validation Loss is increasing at later epochs, indicating overfitting. Overall the best model is the CNN model and the worst is the Logistic one. The CNN and RNN are able to capture the temporal dependencies between subsequent data samples thanks to their architectures.
3. The logistic model cannot learn non-linear features such as the variance, which we have seen to be significantly different between atrial fibrillation and normal fibrillation. Hence, the model performs much better when these features are used as inputs.
4. Training more epochs will only benefit models that have not yet reached a plateau in their loss curves. The CNN reaches a plateau in its validation loss and the `features_mlp` clearly has an increasing validation loss at later epochs. Therefore, those models will not benefit from additional epochs. We guess that the MLP and RNN will continue improving with further training.

Now that all models are trained we can evaluate them on the subsets for training, validation, and testing. For each model, we compute the following metrics:

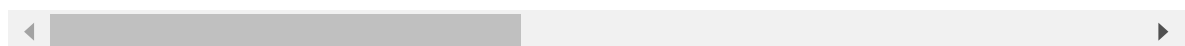
- Accuracy (ACC)
- True positive rate (TPR)
- True negative rate (TNR)
- Positive predictive value (PPV)
- Negative predictive value (NPV)
- F1 score (F1)

You can find more information about these metrics on [Wikipedia](#).

```
In [11]: metrics = []
for name, model in models.items():
    x = features if name.startswith('features') else intervals
    y = targets
    df = evaluate_model(model, x, y, i_train, i_val, i_test, batch_size=batch_size)
    df.insert(0, 'model', name)
    metrics.append(df)
metrics = pd.concat(metrics, axis=0, ignore_index=True)
metrics = metrics.set_index(['model', 'subset'])
index = metrics.index.get_level_values(0).unique()
columns = pd.MultiIndex.from_product([metrics.columns, metrics.index.get_level_values(1).unique()])
metrics = metrics.unstack().reindex(index=index, columns=columns)
IPython.display.display(metrics)
```

model	count				acc				
	subset	train	val	test	train	val	test	train	val
features_logistic		15000	4964	5100	0.823400	0.928888	0.917647	0.875139	0.989227
features_mlp		15000	4964	5100	0.860467	0.854351	0.889804	0.921297	0.851866
logistic		15000	4964	5100	0.691333	0.740532	0.653922	0.726519	0.724509
mlp		15000	4964	5100	0.887733	0.955278	0.933922	0.955699	0.973836
cnn		15000	4964	5100	0.948400	0.986906	0.969216	0.958050	0.982301
rnn		15000	4964	5100	0.920200	0.969178	0.950588	0.939611	0.969604

6 rows × 21 columns



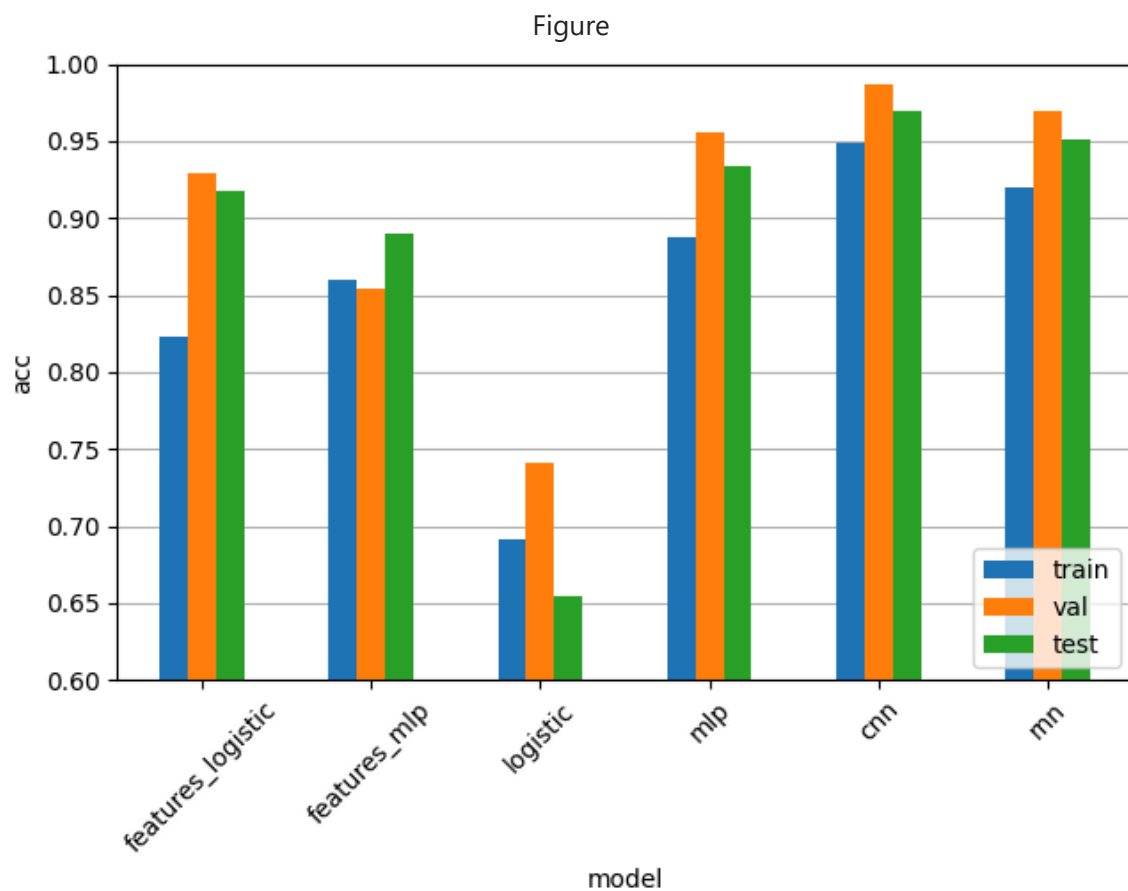
We can also plot the different metrics.

```
In [12]: def plot_metrics(data):
for metric in data.columns.get_level_values(0).unique():
    if metric == 'count':
        continue
    df = data[metric]
    plt.figure(constrained_layout=True)
    plt.gca().set_axisbelow(True)
    df.plot(kind='bar', ylabel=metric, ax=plt.gca())
```

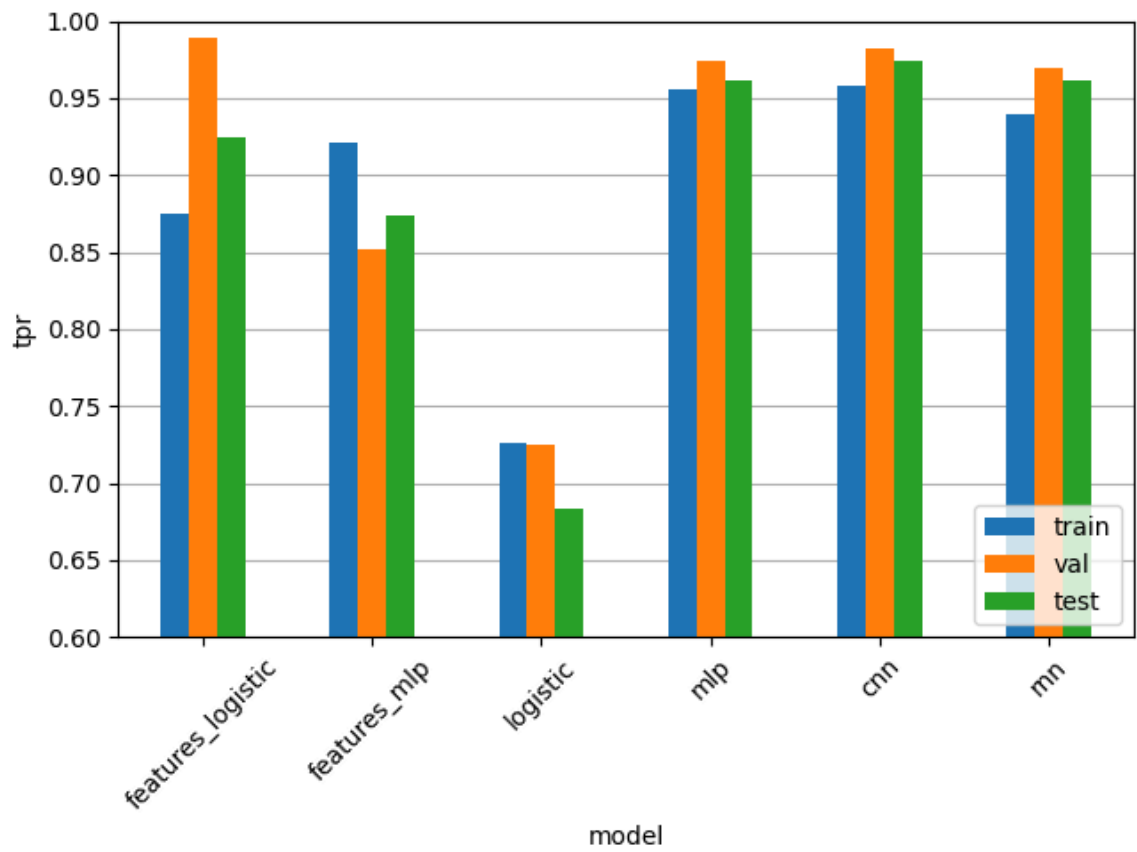


```
plt.grid(axis='y')
plt.ylim(0.6, 1.0)
plt.legend(loc='lower right')
plt.gca().xaxis.set_tick_params(rotation=45)

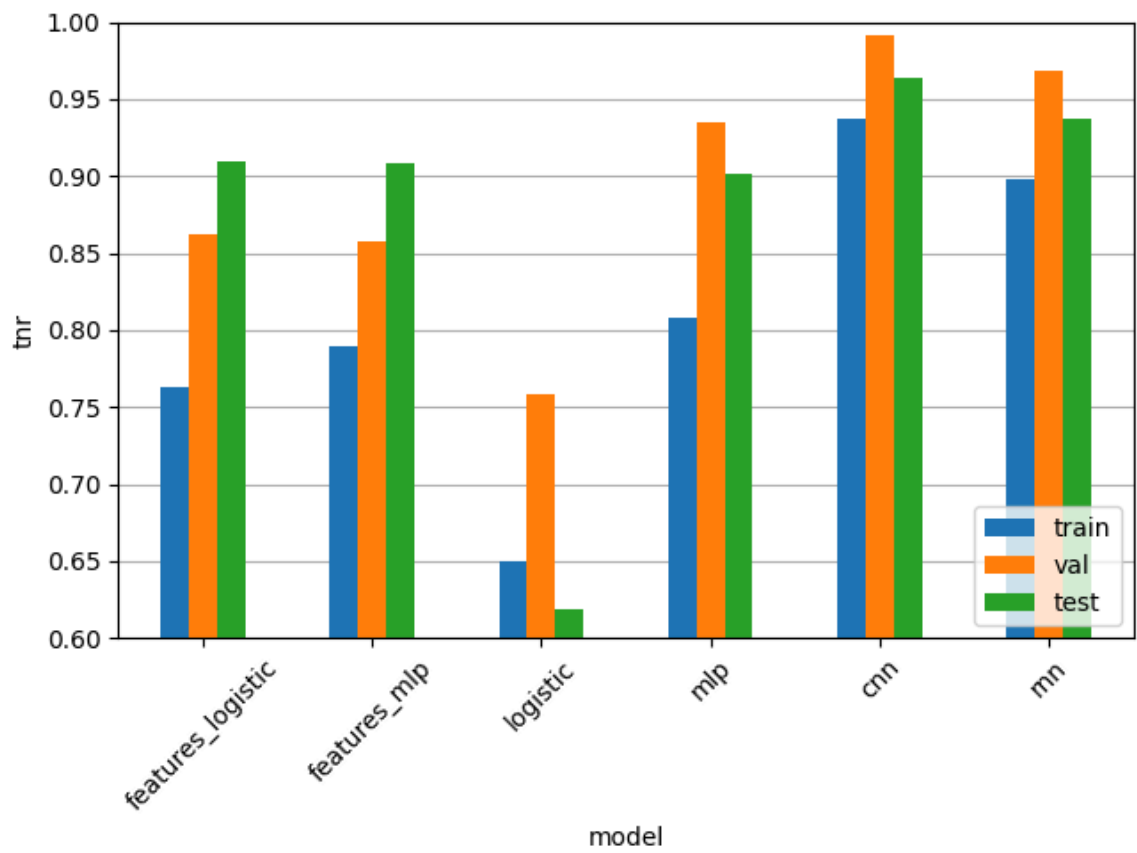
plot_metrics(metrics)
```



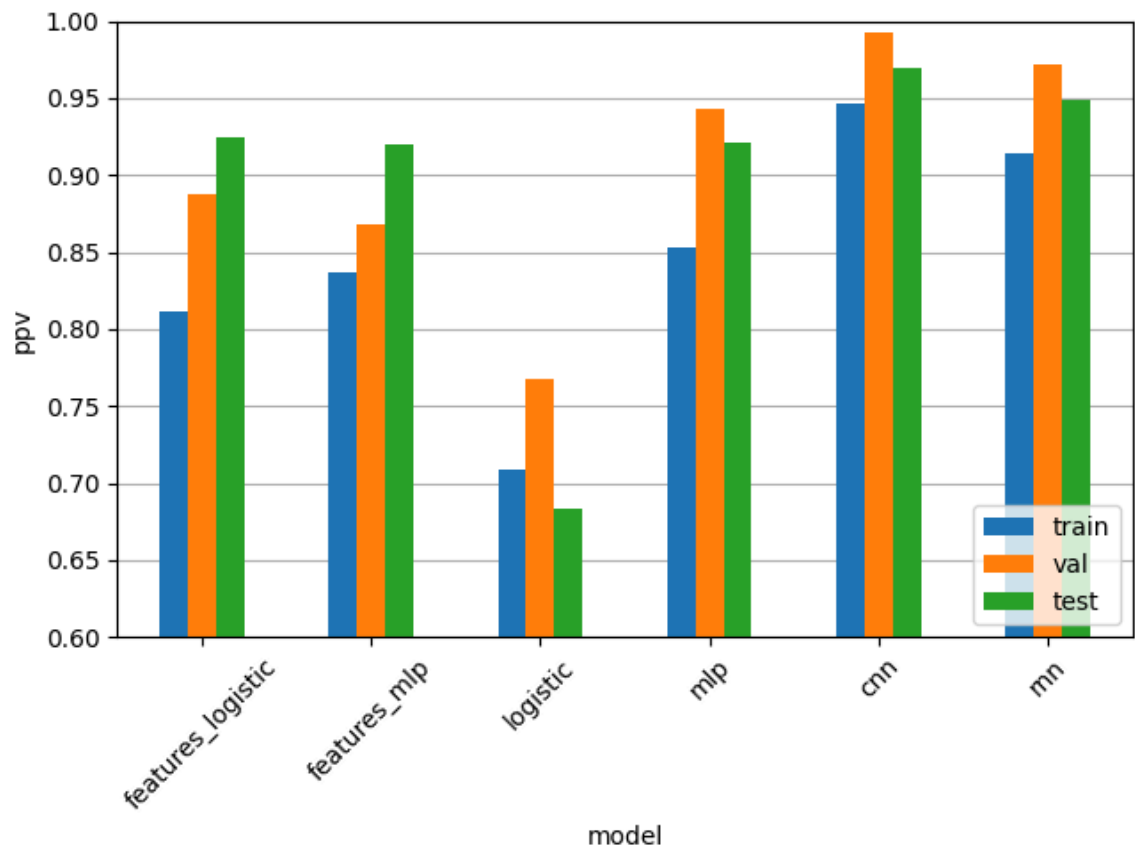
Figure



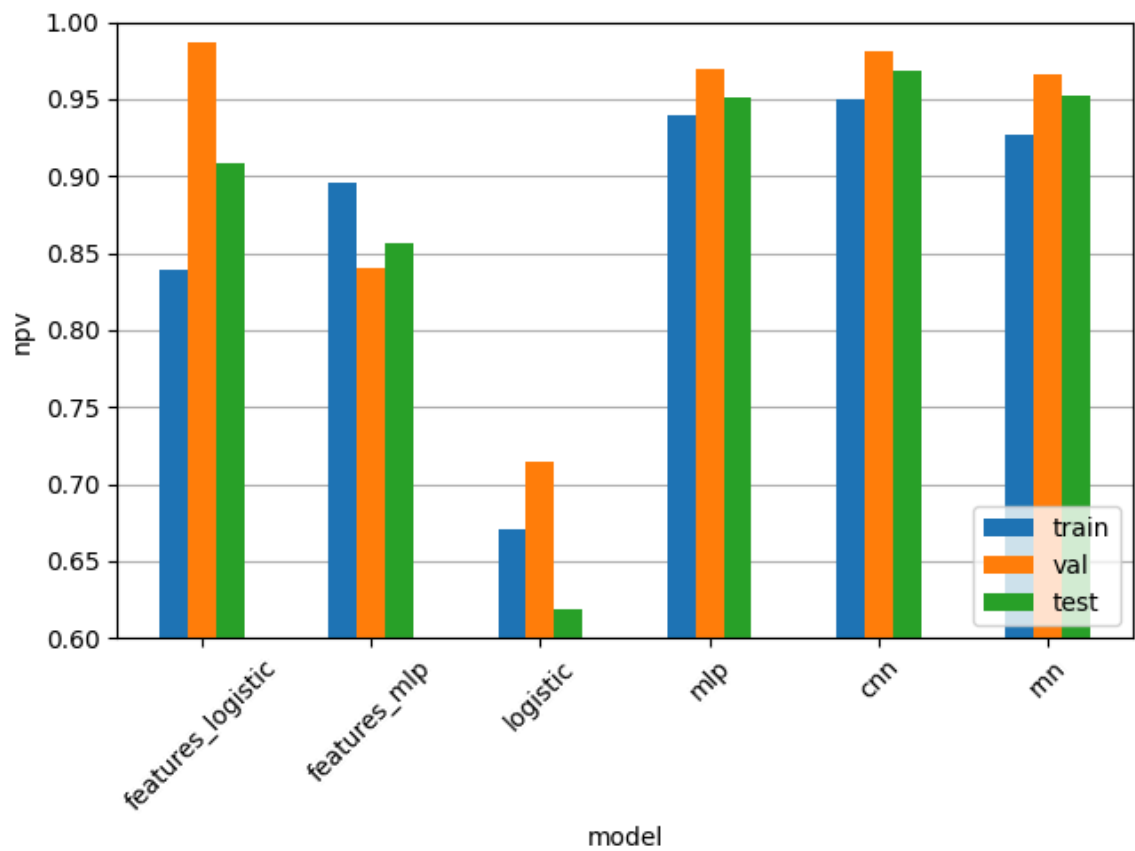
Figure

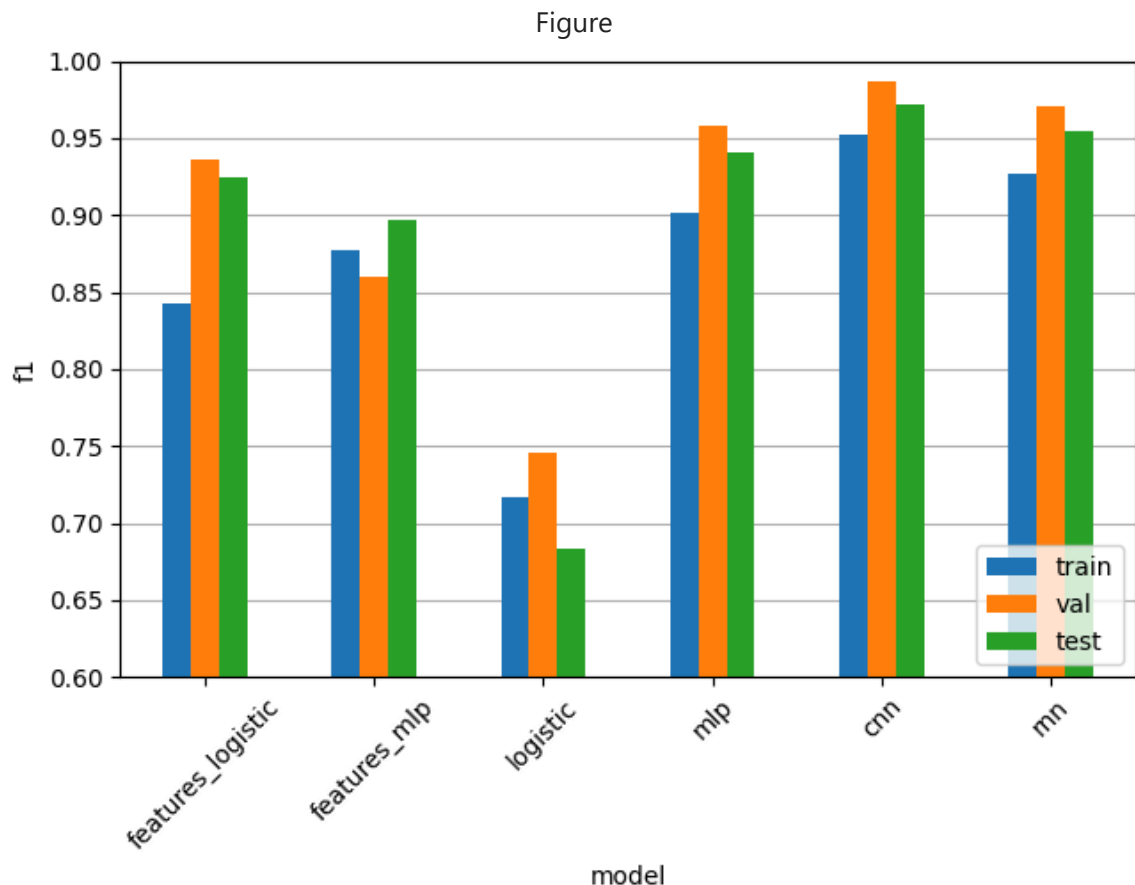


Figure



Figure





Question 4

Based on the performance metrics shown above, answer the following questions:

1. Which are the best models?
2. What can you say about the models using features as inputs?
3. Bonus question: do you think it is *honest* to compare several models based on metrics computed on the test set in order to select the best one ?

Answer:

1. From the F1-score, the CNN is the best model. The RNN, MLP and features_logistic are all slightly worse, but still significantly better than features_mlp and logistic .
2. features_logistic is tremendously better than the logistic model. However, the MLP performs worse when using features as inputs. This may be because the MLP can learn better features from the raw data, thanks to its architecture.
3. It would be better to do so using metrics computed on the validation set. Indeed, the test set should only be used as an indicator of the model's performance when presented with data it has never seen before.

Question 5

Train and evaluate a model with a custom configuration. Can you obtain better performance than the previous models?

```
In [13]: # Customize the model configuration below.
custom_config_name = 'custom'
custom_config = {
    'model': {
        'name': 'cnn',
        'config': {
            'input_size': intervals.shape[1],
            'output_size': targets.shape[1],
            'n_layers': 3,
            'n_initial_channels': 16,
            'kernel_size': 5,
        },
    },
    'optimizer': {
        'name': 'adam',
        'config': {'lr': 0.0001},
    },
}

custom_model = train_model(custom_config_name, custom_config, intervals, targets)
custom_metrics = evaluate_model(custom_model, intervals, targets, i_train, i_val)
IPython.display.display(custom_metrics)
```

	Name	Type	Params	Mode	In sizes	Out sizes

0	model	CnnModel	13.1 K	train	[1, 32]	[1, 1]
1	model.layers	Sequential	13.1 K	train	[1, 1, 32]	[1, 1]
2	model.layers.0	Conv1d	96	train	[1, 1, 32]	[1, 16, 32]
3	model.layers.1	ReLU	0	train	[1, 16, 32]	[1, 16, 32]
4	model.layers.2	MaxPool1d	0	train	[1, 16, 32]	[1, 16, 16]
5	model.layers.3	Conv1d	2.6 K	train	[1, 16, 16]	[1, 32, 16]
6	model.layers.4	ReLU	0	train	[1, 32, 16]	[1, 32, 16]
7	model.layers.5	MaxPool1d	0	train	[1, 32, 16]	[1, 32, 8]
8	model.layers.6	Conv1d	10.3 K	train	[1, 32, 8]	[1, 64, 8]
9	model.layers.7	ReLU	0	train	[1, 64, 8]	[1, 64, 8]
10	model.layers.8	AdaptiveAvgPool1d	0	train	[1, 64, 8]	[1, 64, 1]
11	model.layers.9	Flatten	0	train	[1, 64, 1]	[1, 64]
12	model.layers.10	Linear	65	train	[1, 64]	[1, 1]

13.1 K	Trainable params					
0	Non-trainable params					
13.1 K	Total params					
0.052	Total estimated model params size (MB)					
13	Modules in train mode					
0	Modules in eval mode					
Sanity Checking:			0/? [00:00<?, ?it/s]			
Training:			0/? [00:00<?, ?it/s]			
Validation:			0/? [00:00<?, ?it/s]			

[illegible]

	subset	count	acc	tpr	tnr	ppv	npv	f1
0	train	15000	0.896400	0.899641	0.892615	0.907276	0.883927	0.903442
1	val	4964	0.975020	0.963063	0.988161	0.988937	0.960543	0.975828
2	test	5100	0.950392	0.946576	0.954998	0.962099	0.936757	0.954274

Yes. We obtain better performance (accuracy) by adding an additional layer.