

# Energy Efficient Explosive Motion with Compliant Actuation Arrangements in Articulated Robots\*

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**Abstract**—This paper presents the motion optimization for a recently introduced asymmetric compliant actuator which provides energy efficient actuation for explosive motions such as jumping. Two actuation branches with significantly different stiffness and energy storage capacity properties driving a single joint make up the actuator design. An optimization problem is formulated to optimize the joint trajectories for energy efficient vertical jumping motions of a 2-DoF leg as proof-of-concept. Several configurations of the asymmetric compliant actuators have been investigated. Simulation studies of the optimized jumping motions demonstrate SOMETHING.

## I. INTRODUCTION

Introduction Citation [1]

## II. LEG DESIGN

### A. Compliant Actuation

Description actuation principle

### B. Configurations

SEA only, mono-articulated, bi-articulated

## III. DYNAMIC MODEL

### A. Forward Dynamics

$$\alpha + \beta = \chi \quad (1)$$

### B. Inverse Dynamics

more math

$$\alpha + \beta = \chi$$

## IV. DYNAMIC OPTIMISATION

Explain necessity problem downscaling

### A. Trajectory Parametrization

$$\alpha + \beta = \chi$$

### B. Pretension position

Explain relevance of pretension position to jumping and why it is added as an optimisation variable.

\*Supported by ???

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### C. Objective criteria

The objective function is comprised out of three criteria which reward the performance of the leg, penalize excessive torque needed to complete a movement and maintain the postural stability of the leg. A concrete minimization of the objective functions with these criteria is represented by:

$$\min_P J(P) = -c_1 \cdot J_{performane} + c_2 \cdot J_{torque} + c_3 \cdot J_{stability}$$

Here,  $c_1$ ,  $c_2$  and  $c_3$  denote scaling constants.

#### Performance

For the performance of the leg we distinguish two different objectives:

- 1) Jumping a maximum height, where the height is defined as the  $y$ -coordinate of the centre of mass of the leg with respect to the ground:

$$J_{performane} = y_{CoM}^2$$

- 2) Jumping to a certain height efficiently, where the  $y$ -coordinate of the centre of mass of the leg is bound to an equality constraint and the energy use is defined as the power used for the jump:

$$J_{performane} = -P^2$$

Here,  $P$  is defined as **define P**

#### Torque

The active torque  $\tau_a$  is to be bounded within the maximum and minimum deliverable torque  $[\underline{\tau}_a \bar{\tau}_a]$ . This is enforced by the penalty function:

$$J_{torque} = \sum_0^{t_f} (\underline{\tau}_a - \tau_a)^T (\underline{\tau}_a - \tau_a) + (\tau_a - \bar{\tau}_a)^T (\tau_a - \bar{\tau}_a)$$

Here,  $t_f$  denotes the last time segment of the motion.

#### Stability

To ensure postural stability a stability criterion is introduced. The leg posture is considered stable when the  $x$ -coordinate of the centre of mass of the leg is equal to its initial  $x$ -coordinate,  $x = 0$ , at the end of the motion. This is achieved with the minimization of:

$$J_{stability} = |x_{CoM}(t_f) - c_4|^2$$

Here,  $c_4$  is a constant.

#### D. Algorithm

The objective criteria described above require information concerning the kinematic and dynamic state of the leg. Both forward and inverse dynamic calculations are to be performed while the leg states are set by adjusting the earlier described  $B$ -spline joint trajectories. This dependence is managed by the optimisation algorithm. The algorithm in words yields:

- Provide initial guess trajectory
- Create control points
- ◇ Create trajectory with  $B$ -splines
- ◇ Check joint angles, continue if limits are not exceeded else, vary control points and repeat ◇ steps
- ◇ Run simulation of motion through forward dynamics
- ◇ Calculate active torques through inverse dynamics
- ◇ Evaluate objective function
- ◇ Exit if local minimum is reached, else vary control points and repeat ◇ steps

Textbox to insert figure

Fig. 1. Caption

#### V. RESULTS

Results, max height and energy cost for certain height.

The optimisation has been performed for the upward movement of the leg performing a jumping motion. The initial position of the leg yields a squatting posture and the optimisation is concluded when the upper segment of the leg, the trunk, reaches its highest point **add figure**.

TABLE I  
MAXIMUM JUMP HEIGHT FOR DIFFERENT CONFIGURATIONS

Configuration	Maximum jump height [m]
Only SEA	
Mono-articulated	
Bi-articulated	

#### VI. DISCUSSION

Comparison of actuation topologies.

#### VII. CONCLUSIONS

#### APPENDIX

Appendixes should appear before the acknowledgment.

#### ACKNOWLEDGMENT

The preferred spelling of the word acknowledgment in America is without an e after the g. Avoid the stilted expression, One of us (R. B. G.) thanks . . . Instead, try R. B. G. thanks. Put sponsor acknowledgments in the unnumbered footnote on the first page.

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