

Energy Efficient Explosive Motion with Compliant Actuation Arrangements in Articulated Robots*

Roel Djajadiningrat¹ and Wesley Roozing²

Abstract—This paper presents the motion optimization for a recently introduced asymmetric compliant actuator which provides energy efficient actuation for explosive motions such as jumping. Two actuation branches with significantly different stiffness and energy storage capacity properties driving a single joint make up the actuator design. An optimization problem is formulated to optimize the joint trajectories for energy efficient vertical jumping motions of a 2-DoF leg as proof-of-concept. Several configurations of the asymmetric compliant actuators have been investigated. Simulation studies of the optimized jumping motions demonstrate SOMETHING.

I. INTRODUCTION

Introduction Citation [1]

II. LEG DESIGN

A. Compliant Actuation

Description actuation principle

B. Configurations

SEA only, mono-articulated, bi-articulated

III. DYNAMIC MODEL

A. Forward Dynamics

$$\alpha + \beta = \chi \quad (1)$$

B. Inverse Dynamics

more math

$$\alpha + \beta = \chi$$

IV. DYNAMIC OPTIMISATION

Explain necessity problem downscaling

A. Trajectory Parametrization

$$\alpha + \beta = \chi$$

B. Pretension position

Explain relevance of pretension position to jumping and why it is added as an optimisation variable.

*Supported by ???

¹ Roel Djajadiningrat is a M.Sc student at the Department of Mechanical Engineering, TU Delft and a visiting student at Istituto Italiano di Tecnologia; r.djajadiningrat@student.tudelft.nl

² Wesley Roozing is with the Department of Advanced Robotics, (Fondazione) Istituto Italiano di Tecnologia, via Morego, 30, 16163 Genova, Italy. wesley.roozing@iit.it

C. Objective criteria

The objective function is comprised out of three criteria which reward the performance of the leg, penalize excessive torque needed to complete a movement and maintain the postural stability of the leg. A concrete minimization of the objective functions with these criteria is represented by:

$$\min_P J(P) = -c_1 \cdot J_{performane} + c_2 \cdot J_{torque} + c_3 \cdot J_{stability}$$

Here, c_1 , c_2 and c_3 denote scaling constants.

1) *Performance*: For the performance of the leg we distinguish two different objectives:

- 1) Jumping a maximum height, where the height is defined as the y -coordinate of the centre of mass of the leg with respect to the ground:

$$J_{performane} = y_{CoM}^2$$

- 2) Jumping to a certain height efficiently, where the maximum y -coordinate reached by the centre of mass of the leg is bound to an equality constraint and the energy use is defined as the power used for the jump:

$$J_{performane} = -P^2$$

Here, P is defined as **define P**

- 2) *Torque*: The active torque τ_a is to be bounded within the maximum and minimum deliverable torque $[\underline{\tau}_a \bar{\tau}_a]$. This is enforced by means of a penalty function:

$$J_{torque} = \sum_0^{t_f} (\underline{\tau}_a - \tau_a)^T (\underline{\tau}_a - \tau_a) + (\tau_a - \bar{\tau}_a)^T (\tau_a - \bar{\tau}_a)$$

Here, t_f denotes the last time segment of the motion.

- 3) *Stability*: To ensure postural stability a stability criterion is introduced. The leg posture is considered stable when the x -coordinate of the centre of mass of the leg is equal to its initial x -coordinate, $x = 0$, at the end of the motion. This is achieved with the minimization of:

$$J_{stability} = |x_{CoM}(t_f) - c_4|^2$$

Here, c_4 is a constant.

D. Algorithm

The objective criteria described above require information concerning the kinematic and dynamic state of the leg. Both forward and inverse dynamic calculations are to be performed while the leg states are set by adjusting the earlier described B -spline joint trajectories. This dependence is managed by the optimisation algorithm. The algorithm in words yields:

- Provide initial guess trajectory
- Create control points
- ◊ Create trajectory with B -splines
- ◊ Check joint angles, continue if limits are not exceeded else, vary control points and repeat ◊ steps
- ◊ Run simulation of motion through forward dynamics
- ◊ Calculate active torques through inverse dynamics
- ◊ Evaluate objective function
- ◊ Exit if local minimum is reached, else vary control points and repeat ◊ steps

Textbox to insert figure

Fig. 1. Caption

V. RESULTS

Results, max height and energy cost for certain height.

The optimisation has been performed for the upward movement of the leg performing a jumping motion. The initial position of the leg yields a squatting posture and the optimisation is concluded when the centre of mass reaches its highest point **add figure of motion sequence**.

TABLE I

MAXIMUM JUMP HEIGHT FOR DIFFERENT CONFIGURATIONS

Configuration	Maximum jump height [m]
Only SEA	
Mono-articulated	
Bi-articulated	

TABLE II

MINIMUM ENERGY USE FOR DIFFERENT CONFIGURATIONS

Configuration	Minimum energy use [J]
Only SEA	
Mono-articulated	
Bi-articulated	

VI. DISCUSSION

Comparison of actuation topologies.

VII. CONCLUSIONS

APPENDIX

Appendices should appear before the acknowledgment.

ACKNOWLEDGMENT

The preferred spelling of the word acknowledgment in America is without an e after the g. Avoid the stilted expression, One of us (R. B. G.) thanks . . . Instead, try R. B. G. thanks. Put sponsor acknowledgments in the unnumbered footnote on the first page.

REFERENCES

- [1] G. O. Young, Synthetic structure of industrial plastics (Book style with paper title and editor), in *Plastics*, 2nd ed. vol. 3, J. Peters, Ed. New York: McGraw-Hill, 1964, pp. 1564.
- [2] W.-K. Chen, *Linear Networks and Systems* (Book style). Belmont, CA: Wadsworth, 1993, pp. 123135.
- [3] H. Poor, *An Introduction to Signal Detection and Estimation*. New York: Springer-Verlag, 1985, ch. 4.
- [4] B. Smith, *An approach to graphs of linear forms* (Unpublished work style), unpublished.
- [5] E. H. Miller, A note on reflector arrays (Periodical styleAccepted for publication), *IEEE Trans. Antennas Propagat.*, to be published.
- [6] J. Wang, *Fundamentals of erbium-doped fiber amplifiers arrays* (Periodical styleSubmitted for publication), *IEEE J. Quantum Electron.*, submitted for publication.
- [7] C. J. Kaufman, Rocky Mountain Research Lab., Boulder, CO, private communication, May 1995.
- [8] Y. Yorozu, M. Hirano, K. Oka, and Y. Tagawa, Electron spectroscopy studies on magneto-optical media and plastic substrate interfaces(Translation Journals style), *IEEE Transl. J. Magn.Jpn.*, vol. 2, Aug. 1987, pp. 740741 [Dig. 9th Annu. Conf. Magnetics Japan, 1982, p. 301].
- [9] M. Young, *The Techincal Writers Handbook*. Mill Valley, CA: University Science, 1989.
- [10] J. U. Duncombe, *Infrared navigationPart I: An assessment of feasibility* (Periodical style), *IEEE Trans. Electron Devices*, vol. ED-11, pp. 3439, Jan. 1959.
- [11] S. Chen, B. Mulgrew, and P. M. Grant, A clustering technique for digital communications channel equalization using radial basis function networks, *IEEE Trans. Neural Networks*, vol. 4, pp. 570578, July 1993.
- [12] R. W. Lucky, Automatic equalization for digital communication, *Bell Syst. Tech. J.*, vol. 44, no. 4, pp. 547588, Apr. 1965.
- [13] S. P. Bingulac, On the compatibility of adaptive controllers (Published Conference Proceedings style), in *Proc. 4th Annu. Allerton Conf. Circuits and Systems Theory*, New York, 1994, pp. 816.
- [14] G. R. Faulhaber, Design of service systems with priority reservation, in *Conf. Rec. 1995 IEEE Int. Conf. Communications*, pp. 38.
- [15] W. D. Doyle, Magnetization reversal in films with biaxial anisotropy, in *1987 Proc. INTERMAG Conf.*, pp. 2.2-12.2-6.
- [16] G. W. Juette and L. E. Zeffanella, Radio noise currents n short sections on bundle conductors (Presented Conference Paper style), presented at the IEEE Summer power Meeting, Dallas, TX, June 2227, 1990, Paper 90 SM 690-0 PWRs.
- [17] J. G. Kreifeldt, An analysis of surface-detected EMG as an amplitude-modulated noise, presented at the 1989 Int. Conf. Medicine and Biological Engineering, Chicago, IL.
- [18] J. Williams, *Narrow-band analyzer* (Thesis or Dissertation style), Ph.D. dissertation, Dept. Elect. Eng., Harvard Univ., Cambridge, MA, 1993.
- [19] N. Kawasaki, Parametric study of thermal and chemical nonequilibrium nozzle flow, M.S. thesis, Dept. Electron. Eng., Osaka Univ., Osaka, Japan, 1993.
- [20] J. P. Wilkinson, *Nonlinear resonant circuit devices* (Patent style), U.S. Patent 3 624 12, July 16, 1990.