9.1	Functions
9.2	Algebraic Operations on Functions
	<b>Definition 9.2</b> Given two functions $g:D_g \to \mathbb{R}$ and $f:D_f \to \mathbb{R}$ , we define their <b>composition</b> $f \circ g:D_{f \circ g} \to \mathbb{R}$ by $ (3) \qquad (f \circ g)(a) = f(g(a)),  a \in D_{f \circ g}; $
	$D_{f \circ g} = \{a \in \mathbb{R} : g \text{ is defined at } a \text{ and } f \text{ is defined at } g(a)\}$ .  Note that $f \circ g$ is read from right to left: first the mapping $g$ is performed, then the mapping $f$ ; it is this convention that makes (3) true.
	Two compositions interpreted geometrically by using the graph $G_f$ of $f(x)$ :  translation if $a > 0$ ,
	the graph of $f(x+a)$ is the graph $G_f$ moved to the <i>left a</i> units; the graph of $f(x-a)$ is the graph $G_f$ moved to the <i>right a</i> units; <b>change of scale</b> if $a>1$ ,
	the graph of $f(x/a)$ is the graph $G_f$ expanded horizontally by the factor $a$ ; the graph of $f(ax)$ is the graph $G_f$ compressed horizontally by $1/a$ .
9.3	Some Properties of Functions
	<b>Definition 9.3A</b> Let $f(x)$ be a function with domain $D$ . We say $f$ is
	increasing if $f(a) \le f(b)$ for all pairs $a < b$ in $D$ ; strictly increasing if $f(a) < f(b)$ for all pairs $a < b$ in $D$ ; decreasing if $f(a) \ge f(b)$ for all pairs $a < b$ in $D$ ;
	<b>strictly decreasing</b> if $f(a) > f(b)$ for all pairs $a < b$ in $D$ ; <b>monotone</b> if $f$ is either increasing in $D$ or decreasing in $D$ ; <b>strictly monotone</b> if $f$ is strictly increasing or strictly decreasing in $D$ .
	Definition 9.3B
	$f(x)$ is <b>even</b> if $f(-x) = f(x)$ for all $x \in D_f$ ; $f(x)$ is <b>odd</b> if $f(-x) = -f(x)$ for all $x \in D_f$ .
	For both definitions the domain $D_f$ of the function must be symmetric about the point 0 (i.e., $x \in D_f \Leftrightarrow \neg x \in D_f$ ), otherwise the equality makes no sense.  Geometrically, an even function is one whose graph is symmetric about the y-axis; an odd function is one whose graph is symmetric about the origin.
	<b>Definition 9.3C</b> We say $f(x)$ is <b>periodic</b> if there is a $c > 0$ such that $f(x+c) = f(x) \qquad \text{for all } x \in D_f.$ The number $c$ is called a <b>period</b> of $f$ ; the smallest such $c$ (if it exists) is called the <i>minimal period</i> of $f$ , or simply the <i>period</i> of $f$ .
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9,4	Inverse Functions
9,5	The Elementary Functions
	(a) the rational functions: those writable in the form $p(x)/q(x)$ , where $p(x)$ and $q(x)$ are polynomials;  (b) the basic trigonometric functions: $\cos x$ , $\sin x$ , $\tan x$ , their three recipro-
	cals, and the six inverses $\cos^{-1}x$ , $\sin^{-1}x$ ,;  (c) the exponential function $e^x$ and its inverse, $\ln x$ ;
	(d) the algebraic functions: those functions $y = y(x)$ which satisfy an equation of the form
	(12) $y^n + a_1(x)y^{n-1} + \ldots + a_n(x) = 0$
	- The elementary functions are then all functions that you can get from the four classes above by
	addition, multiplication, division, and composition of functions