

$$1) a) SS_T = SS_{trt} + SS_E$$

$$\sum_{i=1}^a \sum_{j=1}^n (y_{ij} - \bar{y}_{..})^2 = n \sum_{i=1}^a (\bar{y}_{i.} - \bar{y}_{..})^2 + \sum_{i=1}^a \sum_{j=1}^n (y_{ij} - \hat{y}_{ij})^2$$

$$\bar{y}_{..} = \frac{3.25 + 0.75}{2} = 2$$

$$SS_T = 92$$

$$SS_{trt} = 25$$

$$SS_E = 67$$

Sources of Variations	Sums of Squares	degrees of freedom	Mean Squares	F ₀
Diet (A, B)	SS _{trt} = 25	a - 1 = 1	MS _{trt} = 25	$\frac{MS_{trt}}{MS_E} = \frac{25}{4.786} = 5.224$
Weight Loss (pounds)	SS _E = 67	N - a = 14	MS _E = 4.786	
Total	SS _T = 92	N - 1 = 15	MS _T = 29.786	

H₀: $\mu_1 = \mu_2$, μ_i is the average weight loss in the ith group.

H_a: $\mu_1 \neq \mu_2$

∴ Given the fact that $F_{0.05, 1, 14} = 4.46$, we can reject the null hypothesis. There appears to be difference in weight loss depending on the diet.

b)

$$SS_T = SS_{trt} + SS_{block} + SS_E$$

$$SS_T = 92$$

$$SS_{trt} = 25$$

$$SS_{block} = 25$$

$$SS_E = 42$$

Sources of Variations	Sums of Squares	degrees of freedom	Mean Squares	F ₀
Diet (A, B)	SS _{trt} = 25	a - 1 = 1	MS _{trt} = 25	$\frac{MS_{trt}}{MS_E} = \frac{25}{6} = 4.167$
Sex	SS _{block} = 25	b - 1 = 1	MS _{block} = 3.571	
Weight Loss (pounds)	SS _E = 42	(a-1)(b-1) = 1	MS _E = 6	
Total	SS _T = 92	N - 1 = 15	MS _T = 34.571	

H₀: $\mu_{male} = \mu_{female}$

H_a: $\mu_{male} \neq \mu_{female}$

∴ Given the critical value $F_{0.05, 1, 1} = 5.59$, we cannot reject the null hypothesis. There appears to be no difference in the average weight loss between male and female

c) The first student's report is better because the p-value of Dief in the second student's report is over 1, which makes the report unreliable since a p-value can never exceed 1.

$$2) \quad MS_A = \sum_{i=1}^4 (\bar{y}_{i..} - \bar{y}_{...})^2$$

$$MS_B =$$

$$3) \quad a) \quad \sum_{i=1}^a \tau_i = 0, \quad \sum_{j=1}^b \beta_j = 0, \quad \varepsilon_{ij} \sim NID(0, \sigma^2) \\ \sim iid, \sigma_\tau^2 \quad \sim iid, \sigma_\beta^2$$

1. Each block contains the same number of units

2. Each treatment occur the same number of times in total

3. Each pair of treatments occurs together the same number of times in total

$$b) \quad H_0: \tau_i = 0$$

$$H_a: \tau_i \neq 0$$

$$4) \quad a) \quad \mu - 50.2 = 69.8 - \mu \quad \text{because } 50.2 \text{ and } 69.8 \text{ are } 95\% \text{ confidence interval.}$$

$$\Rightarrow \mu = 60$$

$$\Rightarrow \text{The length } |\mu - 50.2| = |69.8 - \mu| = t_{0.025, 9n-1} \sqrt{\frac{MS_E}{9n}} = 9.8$$

$$\sigma_\tau^2 = \frac{E(MS_{\tau+\tau}) - E(MS_E)}{n}$$

$$\sigma^2 = E(MS_E)$$

$$\begin{aligned}
 b) \quad E(\bar{Y}_{..}) &= E\left(\frac{1}{gn} \sum_{i=1}^g \sum_{j=1}^n Y_{ij}\right) = \frac{1}{gn} E\left(\sum_{i=1}^g \sum_{j=1}^n \mu + \tau_i + \varepsilon_{ij}\right), \text{ since } \sum_{i=1}^g \tau_i = \sum_{i=1}^g \sum_{j=1}^n \varepsilon_{ij} = 0 \\
 &= \frac{1}{gn} (gn\mu) \\
 &= \mu = 60
 \end{aligned}$$

$$\begin{aligned}
 \text{Var}(\bar{Y}_{..}) &= \text{Var}\left(\frac{1}{gn} \sum_{i=1}^g \sum_{j=1}^n \mu + \tau_i + \varepsilon_{ij}\right) \\
 &= \frac{1}{gn} (n\sigma_\tau^2 + \sigma^2) \\
 &= \frac{1}{gn} [E(MS_{\tau\tau}) - E(MS_E) + E(MS_E)] \\
 &= \frac{1}{gn} E(MS_{\tau\tau})
 \end{aligned}$$