1) a) i)  $\forall A \in S$ ,  $P(A) \geq 0$  (non-negativity)

 $-\nu$  ii) p(s)=1 (add up to 1) iii) A If A is are disjoints for all i's,  $p(P_i A_i) = \sum_{i=1}^{n} p(A_i)$ 

b) Central Limit Theorem:  $\sum_{i=1}^{n} X_i - np \xrightarrow{d} N(0,1)$ 

 $P(X \le x) = 1 - (1 - P)^{x} \ge \frac{1}{2}$ 

/n(1-p) × ≥/n=

 $X \ge \frac{I_n(\frac{1}{2})}{I_n(\frac{5}{2})} = 3.8$ 

정희철 201*631489*5

$$P(A=0) = P(A=0)$$

Let  $X \sim B(\binom{n}{2}, \frac{1}{365})$ . Then using the Poisson

Let  $X \sim B(\binom{n}{2}, \frac{1}{365})$ . Then using the Poisson paradigm,

 $\frac{1}{1} = e^{-\binom{N}{2}\frac{1}{365}}$ answer for #5

(6)  $f_{x}(x) = \int_{x}^{1} 8xy \, dy = 4xy^{2}|_{x} = 4x(1-x^{2}) = 4x-4x^{3}$ ,  $\theta < x < 1$  $f_{y}(y) = \int_{0}^{y} 8xy \, dx = 4x^{2}y \Big|_{0}^{y} = 4y(y^{2}) = 4y^{3}, 0 < y < 1$  Answers for #6 (ADD)

 $P(A) = \frac{\lambda^{x} e^{-\lambda}}{x!}$ , where x = 0 and  $\lambda = {n \choose 2} \frac{1}{265}$ 

 $M_X(t) = \int_0^\infty e^{tX} \cdot \frac{X^{\alpha-1}e^{-\frac{x}{B}}}{P(\alpha)B^{\alpha}} dX = \int_0^\infty \frac{X^{\alpha-1}e^{-\left(\frac{|B|}{1-Bt}\right)X}}{P(\alpha)B^{\alpha}} dX$  $=\int_{0}^{\infty} \frac{x^{\alpha-1} e^{-\left(\frac{b}{1-bt}\right)^{-1}} x}{\Gamma(\alpha) \beta^{\alpha}} \cdot \frac{\left(\frac{b}{1-bt}\right)^{\alpha}}{\left(\frac{b}{1-at}\right)^{\alpha}} dx$  $= \left(\frac{\beta}{1-\beta t}\right)^{\alpha} \cdot \frac{1}{\beta^{\alpha}} \int_{0}^{\infty} \frac{x^{\alpha-1} e^{-\left(\frac{\beta}{1-\beta t}\right)^{-1}} x}{T'(\alpha) \cdot \left(\frac{\beta}{1-\beta t}\right)^{\alpha}}$ 

=  $\left(\frac{1}{1-\beta+}\right)^{\alpha}$ , let  $\alpha < r$ ,  $\lambda = \frac{1}{\beta}$ 

 $= \left(\frac{1}{1-\frac{t}{r}}\right)^{\alpha} = \left(\frac{\lambda}{\lambda-t}\right)^{r}, r > 0, \lambda > 0, \lambda > t$ 

answer for #7

8) 
$$P(F_i E_i) = \sum_{i=1}^{N} P(E_i) - \sum_{i < i \ge 2}^{N-1} P(E_i, NE_{f_2}) + \sum_{i < i \ge 4}^{N-2} P(E_{i_1} NE_{i_2}, NE_{i_3}) + \cdots$$
using Indusion-Exclusion ReFormula,

$$P(\bigcap_{i=1}^{n} E_{i}) \leq P(\bigcap_{i=1}^{n} E_{i})$$
 for any positive sum of the Therefore, the terms of the expansion after  $\sum_{i=1}^{n} P(E_{i})$  is non-positive.

Therefore, the terms of the expansion after 
$$\sum_{i=1}^{n} p(E_i)$$
 is non-position  $P(\Sigma_i) = \sum_{i=1}^{n} p(E_i) - \sum_{i=1}^{n} p(E_i) + \cdots + (-1)^{n+1} \sum_{i=1}^{n} p(E_i) - \cdots \cap E_{i+1} + \cdots$ 

$$P(\bigcup_{i=1}^{n} E_{i}) = \sum_{i=1}^{n} P(E_{i}) - \sum_{i \neq i, j \neq 2}^{n} P(E_{i}, \bigcap_{i \neq j} E_{i, j}) + \dots + (-1)^{n+1} \sum_{i \neq j \neq k} P(E_{i}, \bigcap_{i \neq j} E_{i, j}) + \dots$$

$$P(i=|E_i|) = \frac{1}{2} P(E_i) - \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + (-1) + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12}) + \cdots + \frac{1}{4} \sum_{i \neq i} P(E_i, |I|E_{12$$

$$\leq \underset{i=1}{\geq} p(E_i)$$

$$\leq \mathcal{L}_{i}^{\mathcal{L}_{i}}(\mathcal{L}_{i})$$

$$\leq \underset{i}{\geq} P(E_i)$$