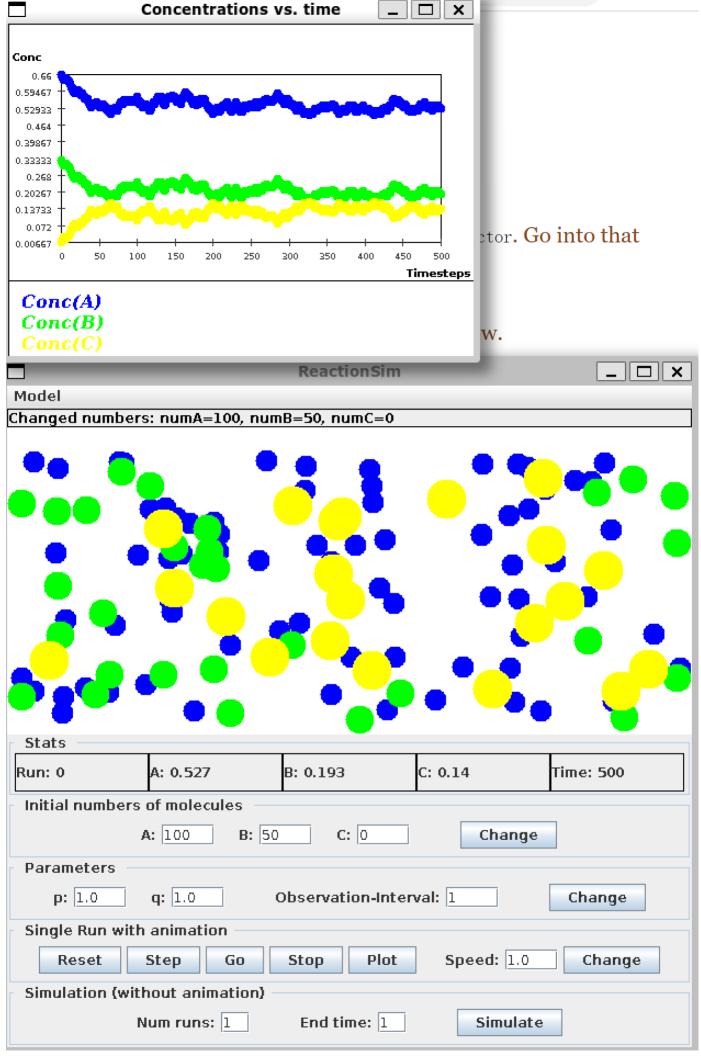
Exercise 1:



• Simulating 10000 particles seems to take three times than 100 particles to reach Time 100.

Exercise 2:

$$N_A = 10$$

$$N_B = 5$$

$$V_{total} = 10 + 5 = 15$$

$$E_A = rac{N_A}{V_{total}} = 0.67$$

$$E_B=rac{N_B}{V_{total}}=0.33$$

- Second reaction happed at time 1
- At time1:

$$\circ$$
 $N_A=8$

$$\circ$$
 $N_B=3$

$$\circ$$
 $N_C=2$

$$\circ V_{total} = 8 + 3 + 2 * 2 = 15$$

$$\circ E_A = \frac{8}{15}$$

•
$$E_B = \frac{3}{15}$$

$$\begin{array}{ccc} \circ & E_A = \frac{8}{15} \\ \circ & E_B = \frac{3}{15} \\ \circ & E_C = \frac{2}{15} \end{array}$$

Exercise 3:

- It settles after time 100, but small fluctuation still happening
- No they are still changing a little bit for there are in the state of dynamic balance
- $E_A \approx 0.55$
- $E_B \approx 0.25$
- $E_C \approx 0.13$

Exercise 4:

- uniform generate a random number between [0,1], if it's larger than the prob of A, then B will happen. or A will happen. So this functions well as appropriate probabilities
- It just use the distance to choose which pair of A,B particles to remove when generation a particle C

Exercise 5:

- I see that the concentration of C is higher than the non-spatial model, more fluctuation maybe caused by more randomness introduced by the spatial information.
- The curve become more smooth
- It become much more smooth
- In standard simulation, increasing num runs also make the curve smoother

Exercise 6:

55.667

Exercise 7:

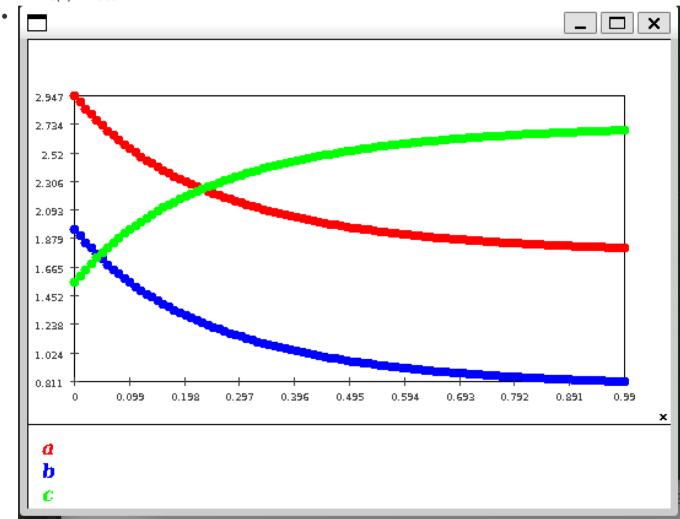
- the concentration is actually the distance between particles, so it works just fine using this setup
- closenessDistance is set for the spatial model. Doubling this parameter functions the same as doubling the concentration of particle A and B.

Exercise 8:

- A(0.01) = 2.947 B(0.01)=1.948 C(0.01) = 1.552
- A(0.02) = 2.898 B(0.02)=1.898 C(0.02) = 1.602
- A(0.03) = 2.851 B(0.03)=1.851 C(0.03) = 1.649

Exercise 9:

- final concentration
 - o A(1) = 1.811
 - o B(1) = 0.811
 - \circ C(1) = 2.689



Exercise 10:

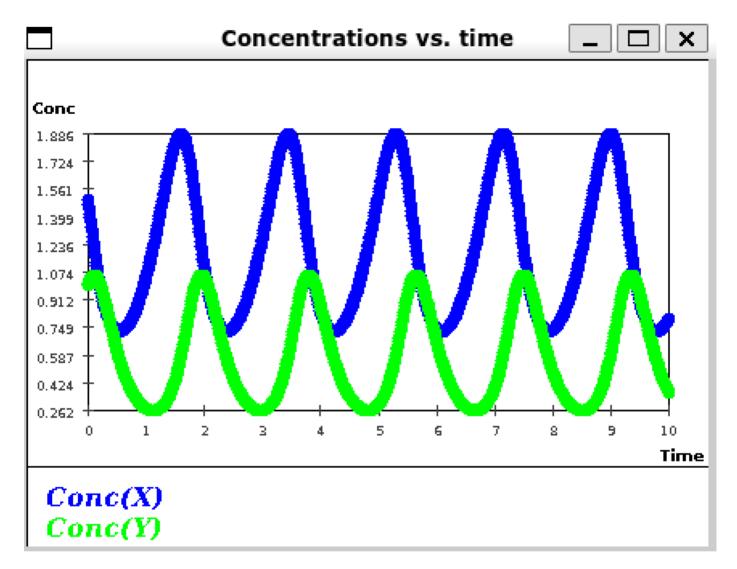
see ConcCalc2.java

The need for arithmetic operation is on the same level as the iterative one.

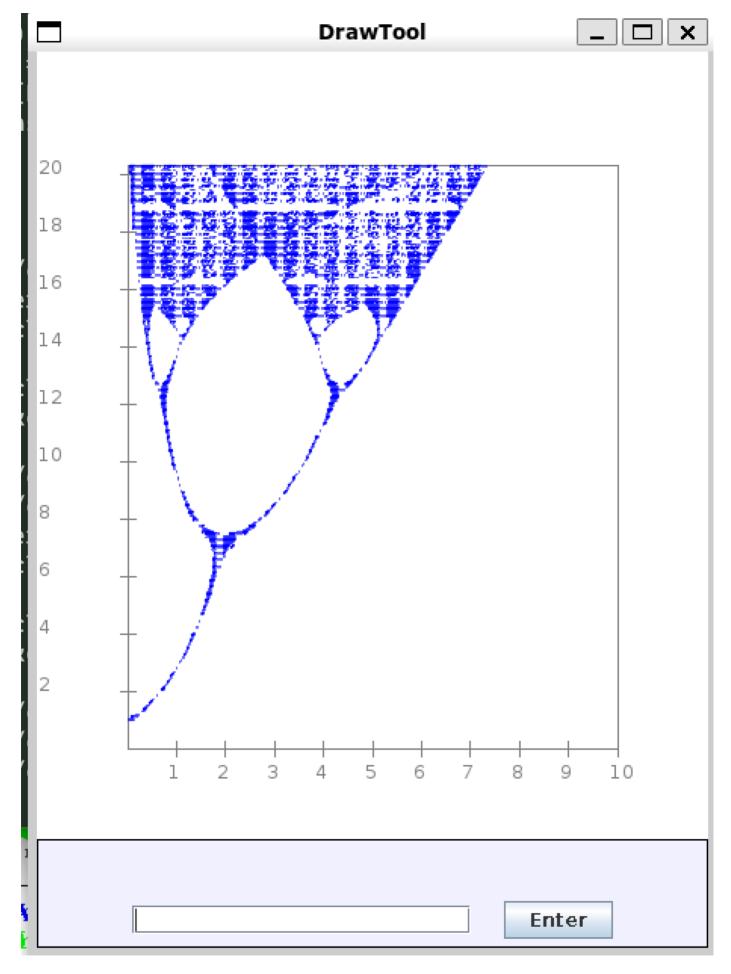
Exercise 11:

- Angular momentum makes ball goes a little east wards
- Coriolis force makes the ball goes a little south(AS it happens in the northern part of the earth)
- So it should be south-east

Exercise 12:



Exercise 13:



Exercise 14:

- TragetX = 10
- $\bullet \ \ M_{x}^{'}=vy=20$
- $\bullet \ \ M_{y}^{'}=MissileAY=3$

- Involved variables
 - TargetVx
 - o MissileVx
 - MissileAy

Exercise 15:

For a small Δt , $CC'=rac{1}{2}(AA'+BB')=rac{1}{2}R(w_L+w_R)\Delta t$

And if we want to sperate CC' into difference of x and y,

Then we can simply apply $\cos(\theta)CC'$ to get it's difference on x axis and apply $\sin(\theta)CC'$ to get it's difference on y axis. Then we get the differential equations same as above.

Exercise 16:

 $w_L R \Delta t$ is the distance difference on the circle. And L is the current radius(for the other wheel is not moving. So If we want the $\Delta \theta$ we can simply divide difference on the circle by radius.

Thus we get $\Delta heta = rac{w_L R \Delta t}{L}$

Exercise 17:

```
func simulate_next(x double,y double, t double, theta double, va double, vb double){
   //cal new x,new y, new theta based on old values
   new_x = x + 0.5*R*(va+vb)*cos(theta) * t;
   new_y = y + 0.5*R*(va+vb)*sin(theta) * t;
   new_theta = theta + (va-vb)*R/L*t;
   return new_x,new_y,new_theta;
}
```

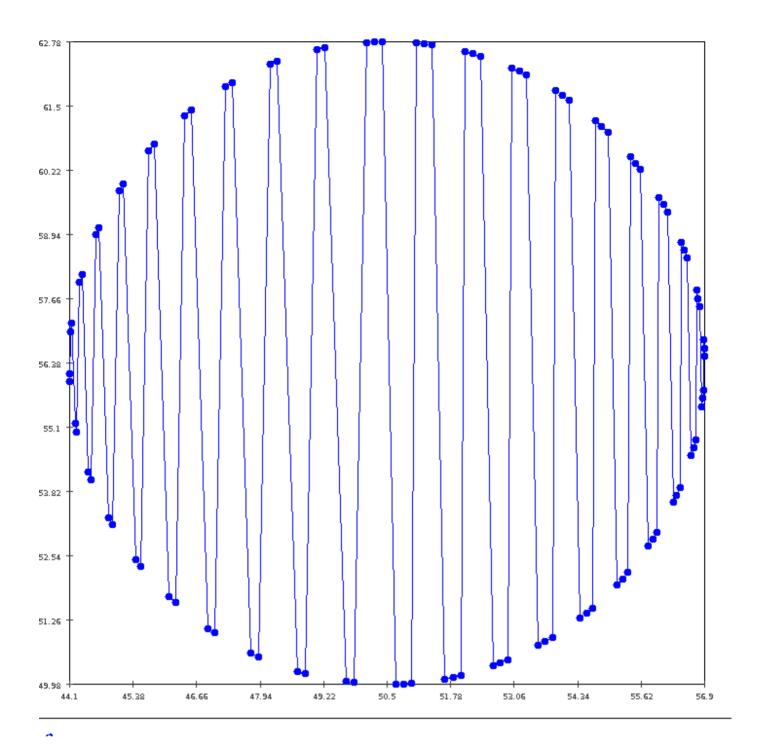
Exercise 18:

For accelerative version, We will need the equations for w_L and w_R For we don't know current angular speed if we just look at acceleration of these two wheels.

Exercise 19:

$$x'(t) = v \cos(\theta)$$
$$y'(t) = v \sin(\theta)$$
$$\theta'(t) = \phi$$

Implementation see SPTest.java, SimpleCarSimulator.java



Exercise 20:

Angular acceleration * Radius = linear acceleration

Exercise 21:

- angularAcc = (torque m*g*R) / (m*R*R + mw*R*R);
- No there isn't, any positive torque will cause the load to collide with the winch.

Exercise 22:

The load were frictionless so any positive torque will be able to pull the load.