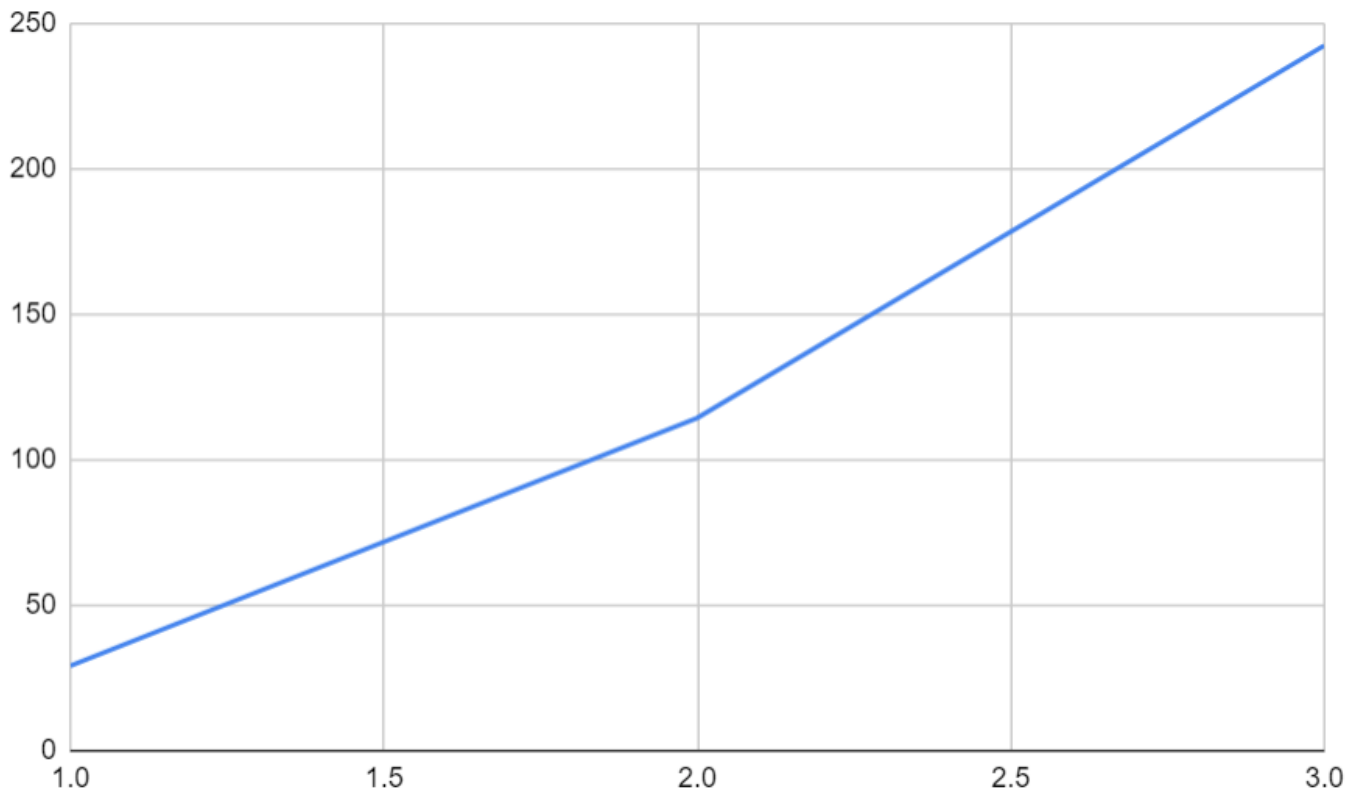


## Exercise 1:

1 second 29.22

2 second 114.43

3 second 242.55



- velocity around 40 between 1 and 2 second
- velocity around 65 between 2 and 3 second
- How do these graphs change if you double the mass?
  - Shouldn't change
- How do these graphs change if you double the angle?
  - The angle in the graph should also double.

## Exercise 2:

Distance increases exponentially with time.

## Exercise 3:

The derivative increases linearly with time.

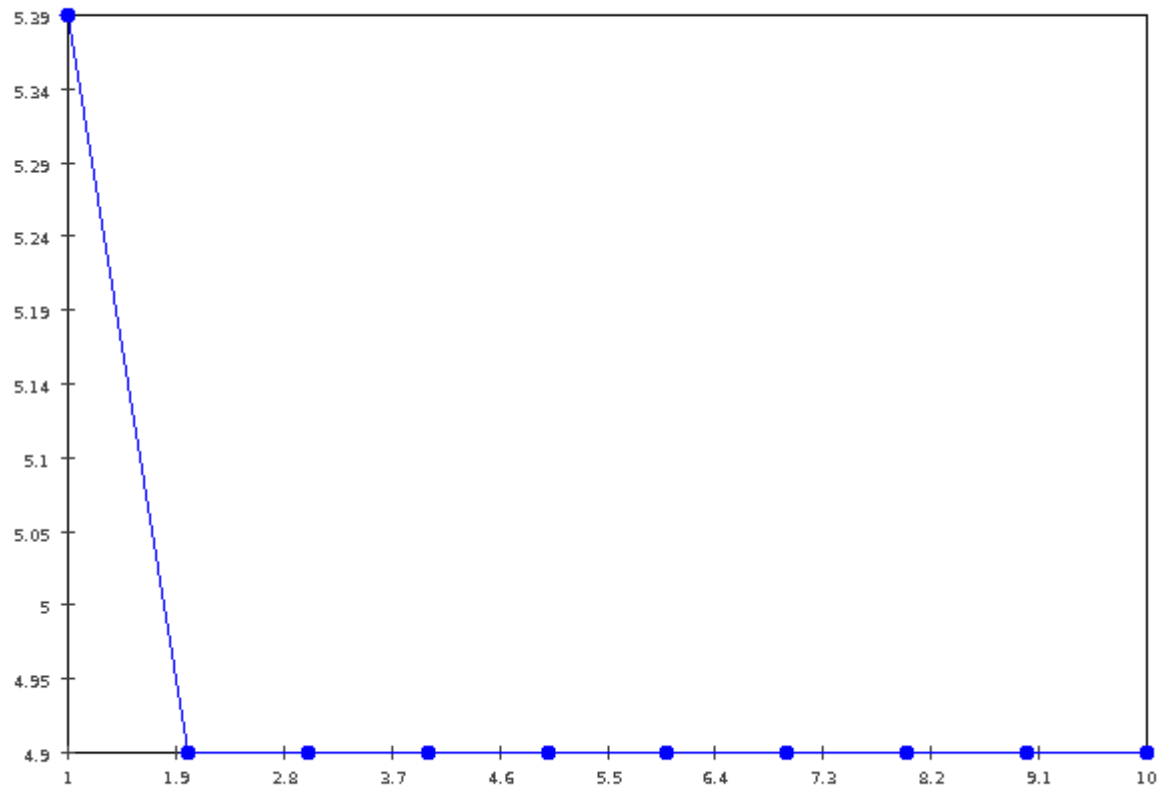
Using 0.0001 gets a very similar result as using 0.01 as time delta.

## Exercise 4:

The rate-of-change stay the same at  $x=1, x=2, x=3$ . And doesn't change as well when changing  $\Delta t$  from 0.1 to 0.01

## Exercise 5:

The slope should be  $y = 4.9x$



*velocity*

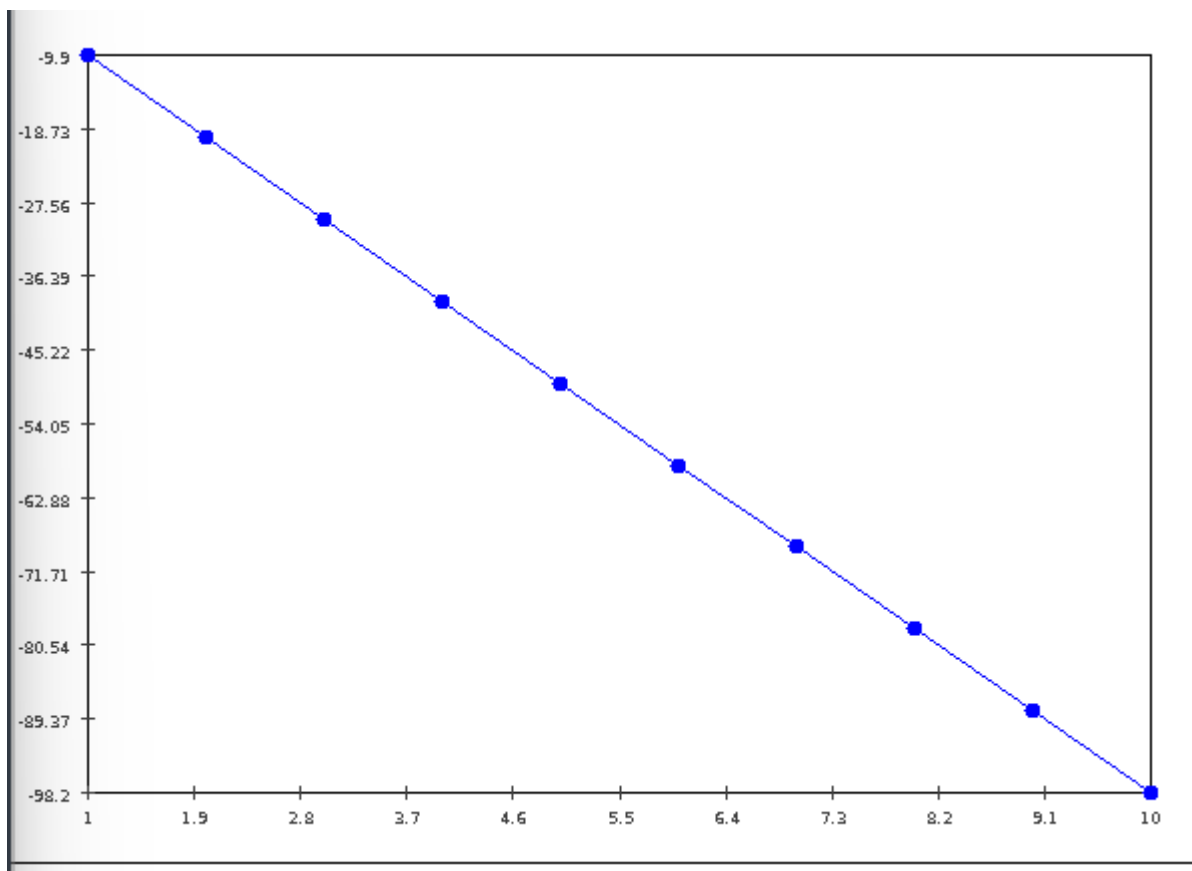
The derivative of  $v$  is at 4.9

## Exercise 6:

- Acceleration is not affected by mass
- Acceleration is increasing as the angle increases
- We can form a formula that takes all related variables and describe the status of the object with these variables.

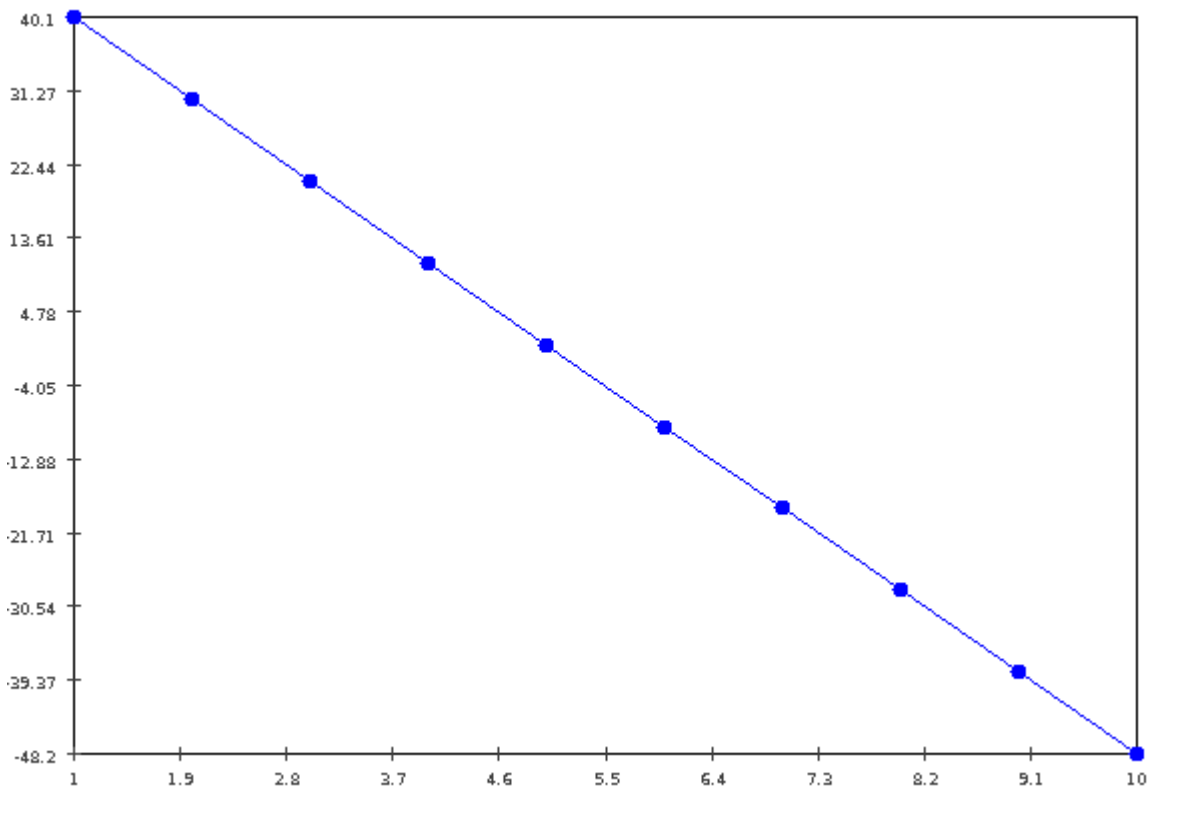
## Exercise 7:

see `BallDropSimulatorExample.java`



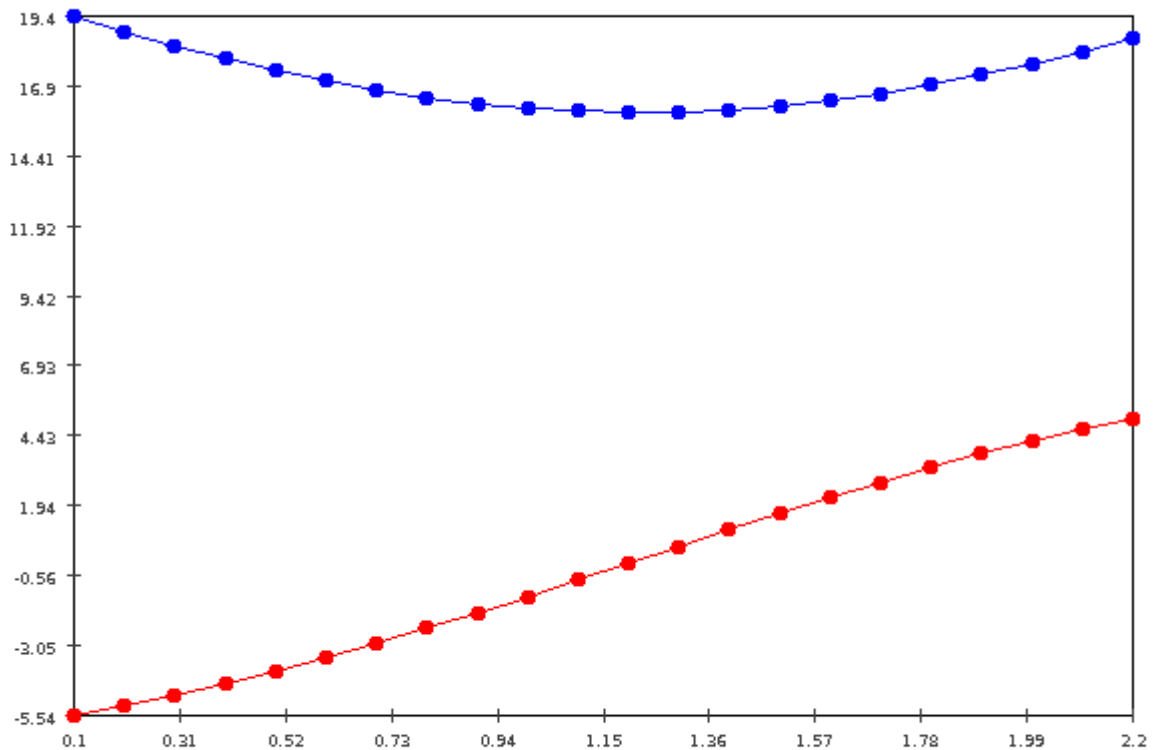
- $\text{slope} = (-98.2 - 9.9)/9 = -9.81$
- I think I can use some substitution to get the velocity of an object falling from certain altitude. Like dropping balls from a certain height and measure the height of splash when the object hits water.
- Clock tech isn't advanced enough to give a small enough  $\Delta T$ .

## Exercise 8:



The change of speed is constant in all scenarios above.

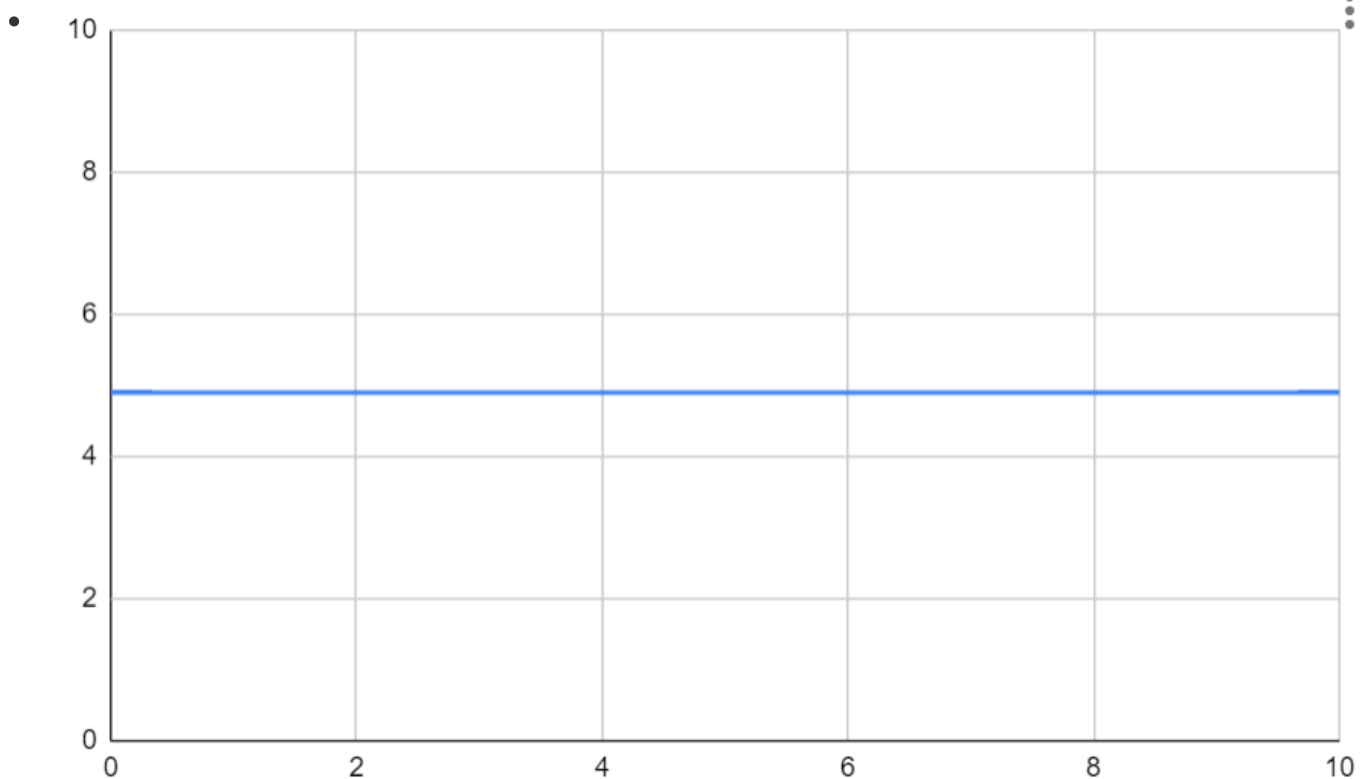
## Exercise 9:



*vel*  
*distance*

- The velocity is constantly increasing from negative to positive.
- Angle=70 makes change of velocity sharper.

## Exercise 10:



- - $v(0.1) = a * 0.1 = 0.49$
  - $v(0.2) = a * 0.2 = 0.98$

- $v(0.3) = a * 0.3 = 1.47$
- $v(0.4) = a * 0.4 = 1.96$
- $v(0.5) = a * 0.5 = 2.45$
- initial speed is 0 and acc is 4.9, for half a second the speed should be 2.45
- The line is the constant acceleration and it's the slope of the increment of velocity.
  - $v(t)=at$

## Exercise 11:

- velocity is re-calculated each time the `computeFinalVelocity` is called. It can be reused in the while loop which will reduce the computational complexity from  $O(n^2)$  to  $O(n)$
- Increasing the interval size will cause the approximate speed to be higher than it should be at a certain moment in this example.

## Exercise 12:

I will setup different test scenarios and compare their error to the real final distances. The one with smaller error should be better.

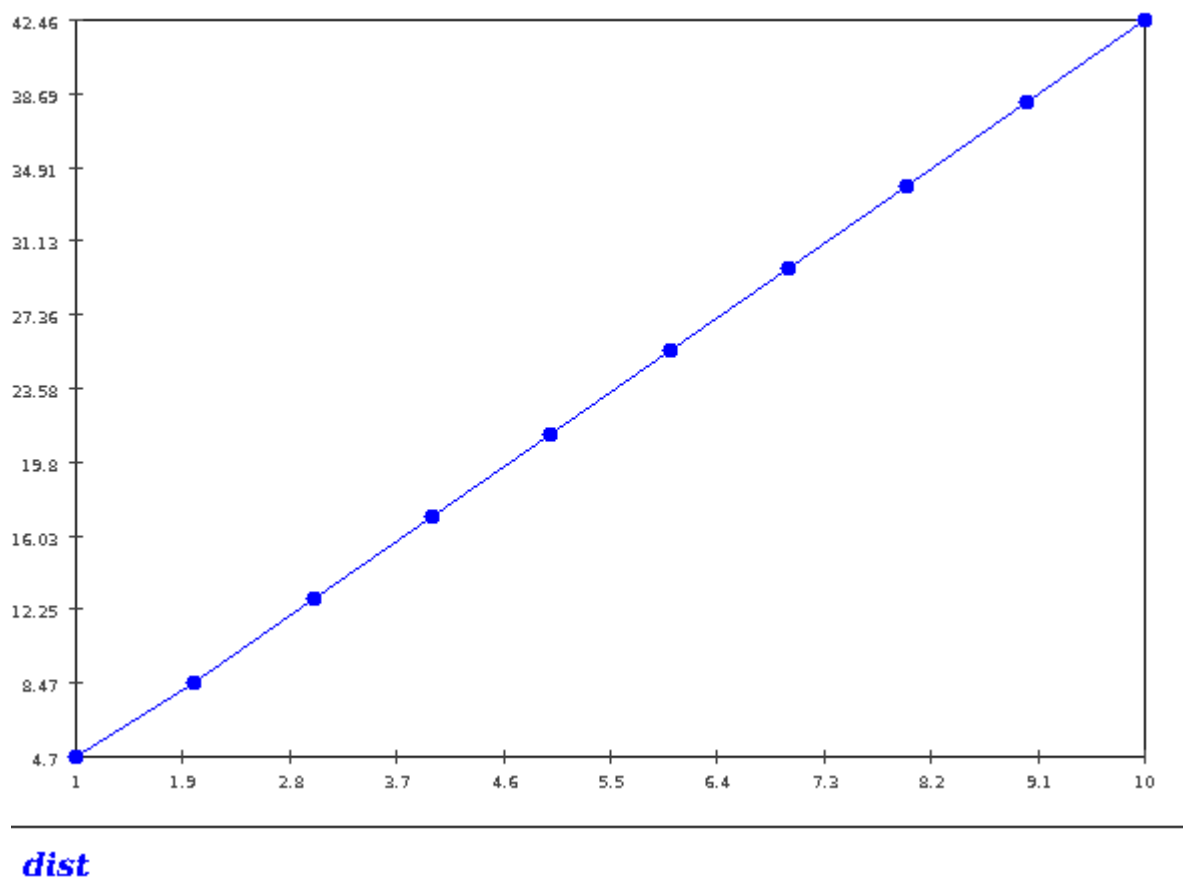
## Exercise 13:

- Should be Euler-Cromer, for velocity is updated first.
- No, acceleration is only relevant to `angleRadians`

## Exercise 14:

Yes, it should, for the slope if constant. And the objects' shadow should also follow the "universal law"

## Exercise 15:



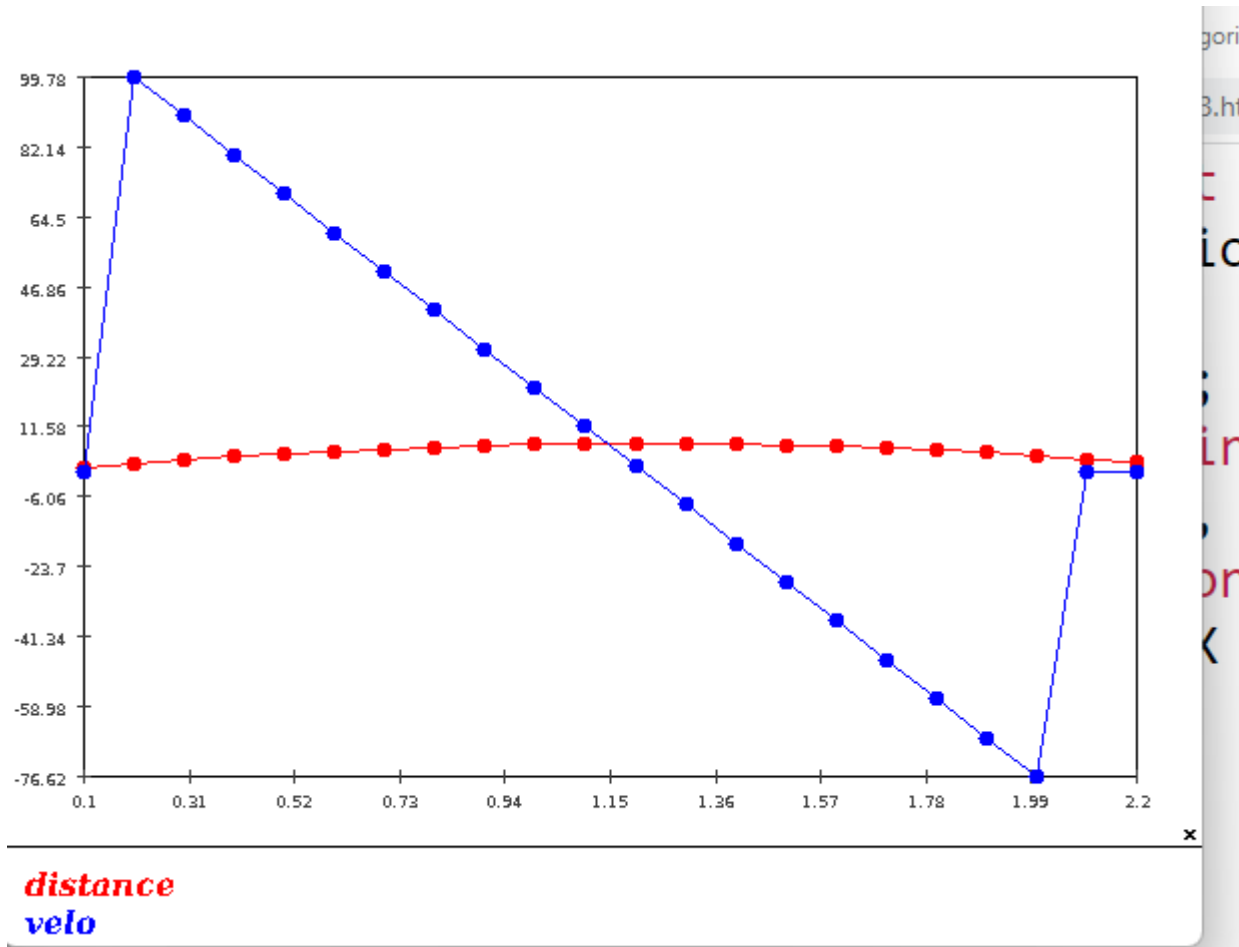
The velocity of x-axis shadow is also increasing constantly.

## Exercise 16:

The distance plot has a fixed slope, which means it's velocity should be constant.

The plot for velocity is indeed constant.

## Exercise 17:



Yes, they both satisfy our universal law.

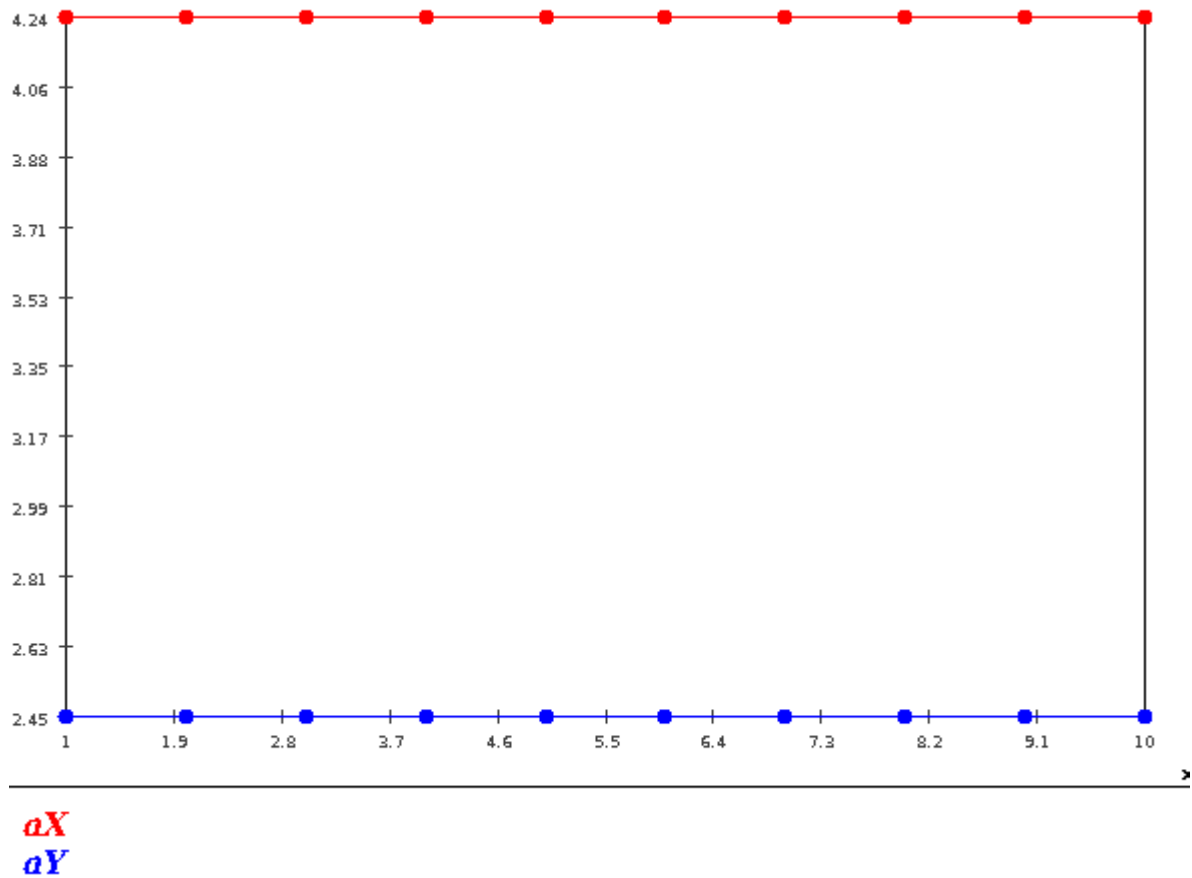
## Exercise 18:

- $d(t) = \frac{x(t)}{\cos(\theta)}$
- $\theta = \arctan \frac{x(t)}{y(t)}$
- So with these equations, it's easy to show that the previous two statements are true and equivalent.

## Exercise 19:

The distance is calculated with current point(x,y) and the next point(nextX,nextY). So we need nextX and nextY for the information of next point.

## Exercise 20:



We can see that  $aX$  and  $aY$  are all constants.

## Exercise 21:

Acceleration on x-axis is not yet addressed.

## Exercise 22:

The acceleration in the x-direction should be caused by the slope and  $g$  together.

the  $g$  has a effect on the x-direction so it's not simply  $g$ .

## Exercise 23:

it will take around 2000 loops to get the result.

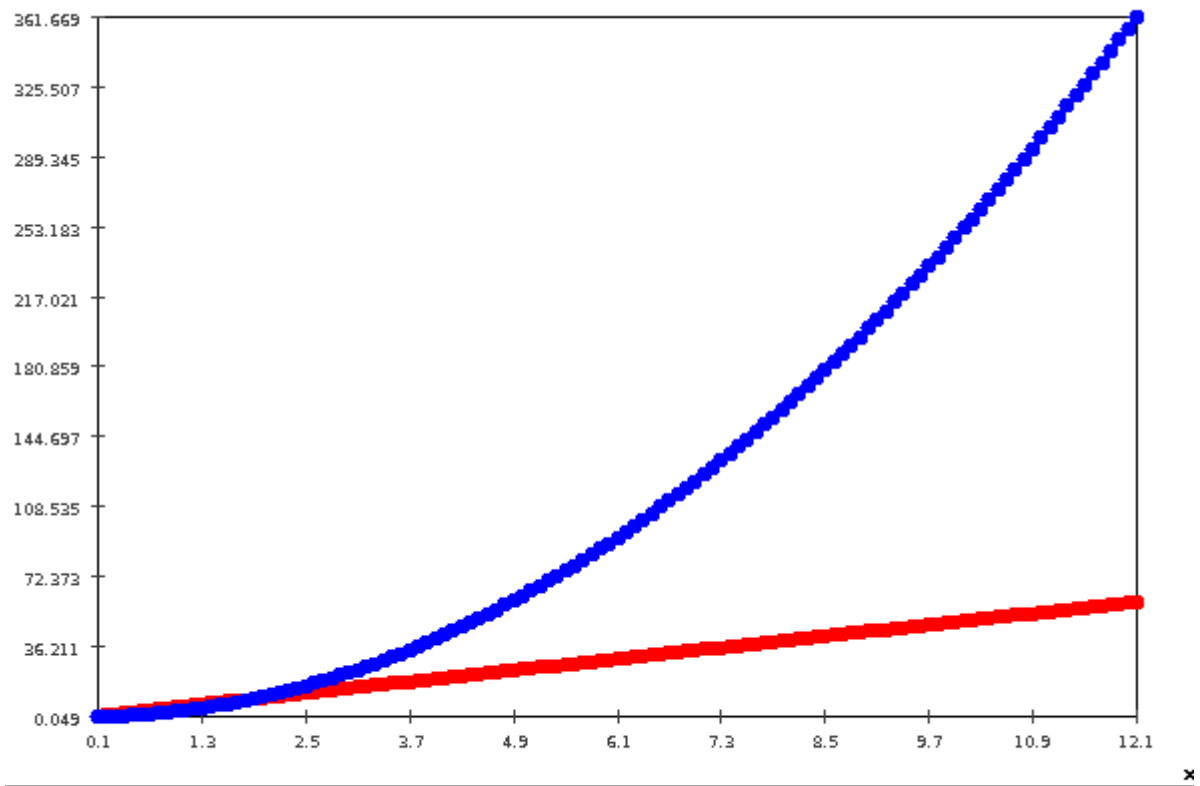
We can use binary search on finding the height to make it much more efficient.

## Exercise 24:

Height required: 250.0 time required 7.143000000000072

code see `BallDropSimulatorExercise2.java`

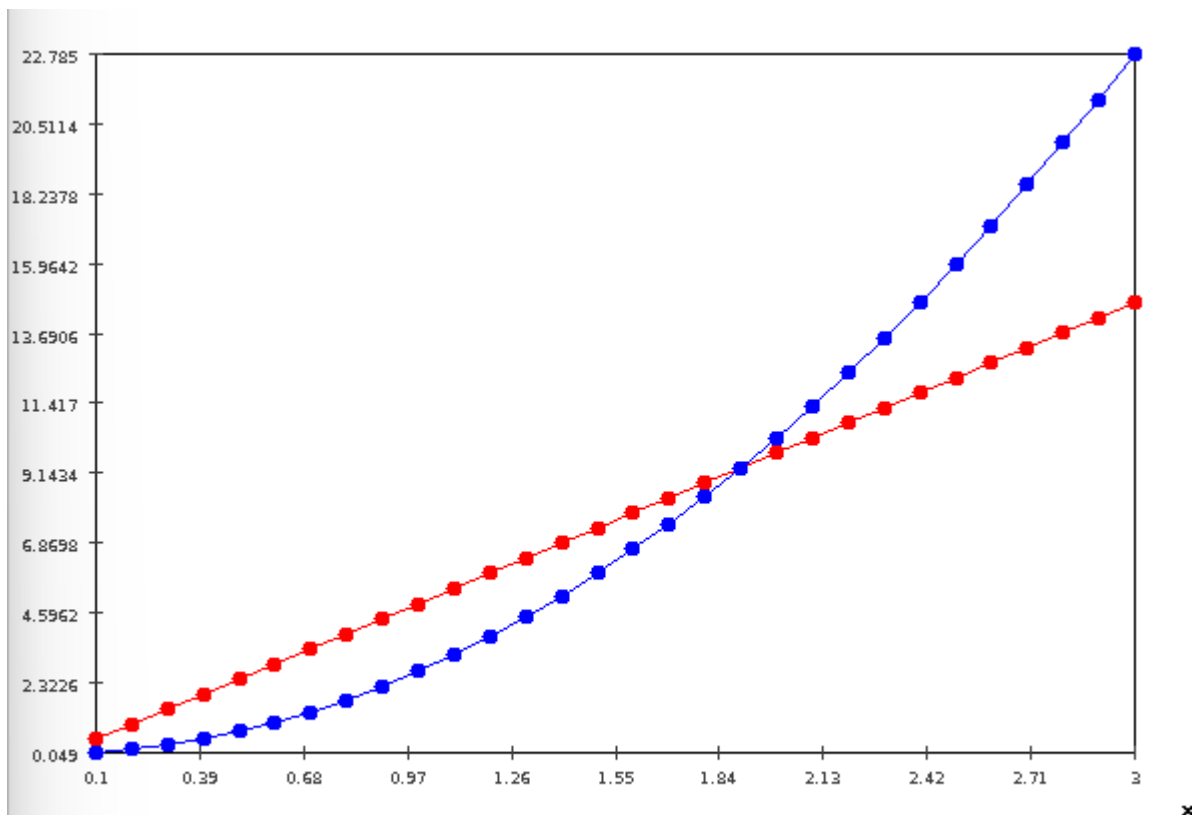
## Exercise 37:



**Velocity**  
**Distance**

## Exercise 38:

see `MovingObjectBasic.java`



**Velocity**  
**Distance**



### Exercise 39:

The size of all rectangle are  $0.1 \times 4.9 = 0.49$

### Exercise 40:

See `MovingObjectIntegration.java`

