

## Exercise 1:

- After 7430000 departures: avgWait=5.530658049364452 avgSystemTime=7.0307692633769765
- The customer just choose a random queue
- After 9211000 departures: avgWait=1.9952709836764186 avgSystemTime=3.4667403493575204

phase transition

5, 8-11, 13-14, 19, 23, 25-29, 31-34, 40, 44, 46, 48.

$$C_k^n = \frac{n!}{(n-k)!k!}$$

## Exercise 5:

- $\Pr[X \leq 2] = 0.784$
- $\Pr[X \leq 3] = 1$
- $\Pr[X \leq 0] = 0.064$
- $\Pr[X \leq 1] = 0.352$
- $\Pr[X=0] = (1-p)^3$
- $\Pr[X=1] = C_3^2 (1-p)^2 * p$
- $\Pr[X=2] = C_3^2 (1-p) * p^2$
- $\Pr[X=3] = p^3$

## Exercise 8:

$$\Pr = (1-p-p*(1-p))*p = 0.096$$

$$\Pr[1\text{st h appears on 3rd flip}] = 0.095991$$

## Exercise 9:

$\Pr[X=3]$  for  $p = 0.6$  will be higher

$$\Pr[X=3] = (1-p)^2 * p$$

$$\Pr = 0.096 \text{ for } p = 0.6$$

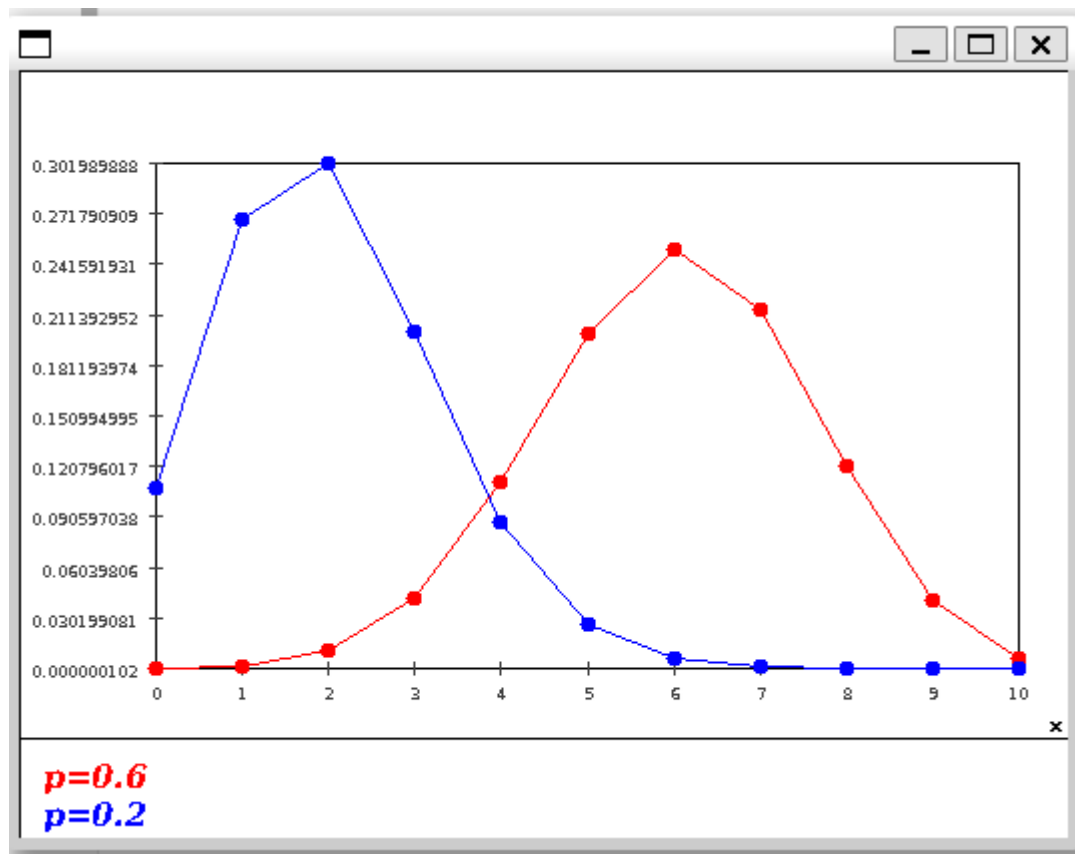
$$\Pr = 0.032 \text{ for } p = 0.8$$

## Exercise 10:

$$\Pr[X > k] = (1-p)^k$$

## Exercise 11:

$$\Pr[X=3] = 0.042467328000000006$$



Pr[3 H in 10 flips]=0.042469

### Exercise 13:

$$\sum \frac{\gamma^k}{k!} = e^\gamma$$

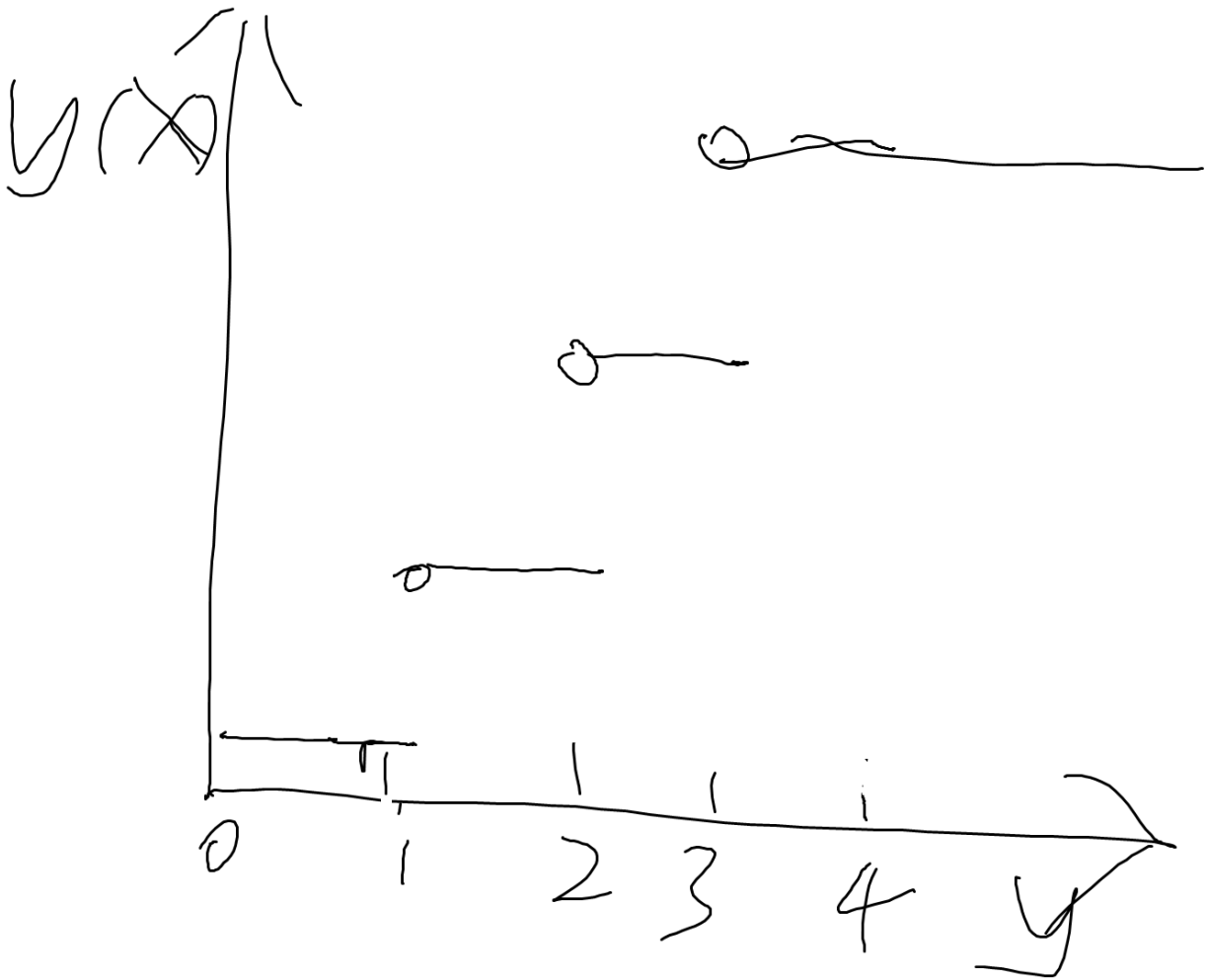
$$e^\gamma * e^{-\gamma} = 1$$

### Exercise 14:

Prob: 0.1813

This value is very approx to the  $P[X=3]$  in Poisson (2)

### Exercise 19:

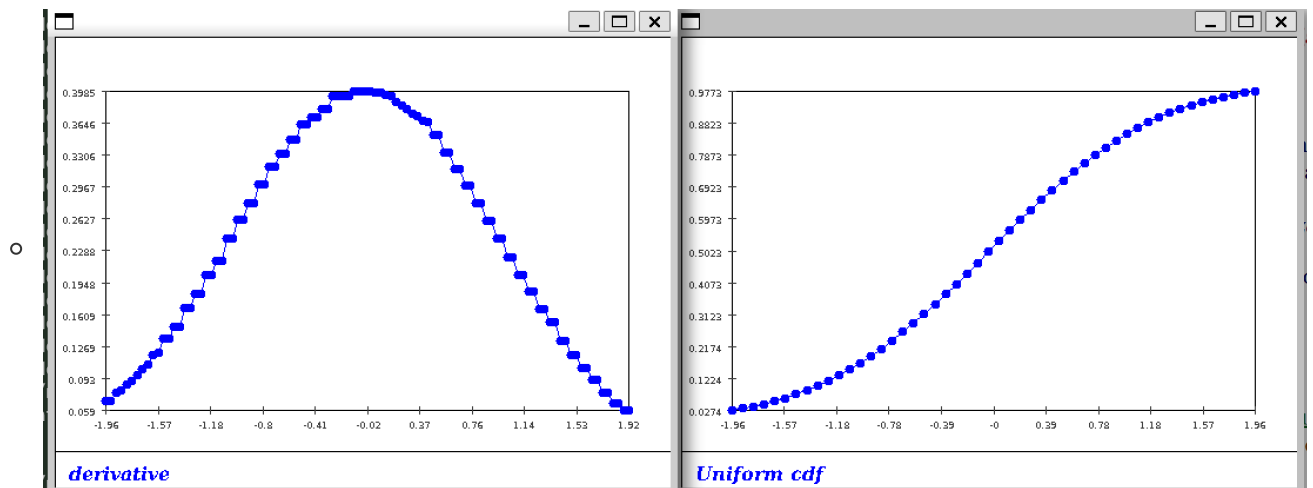


## Exercise 25

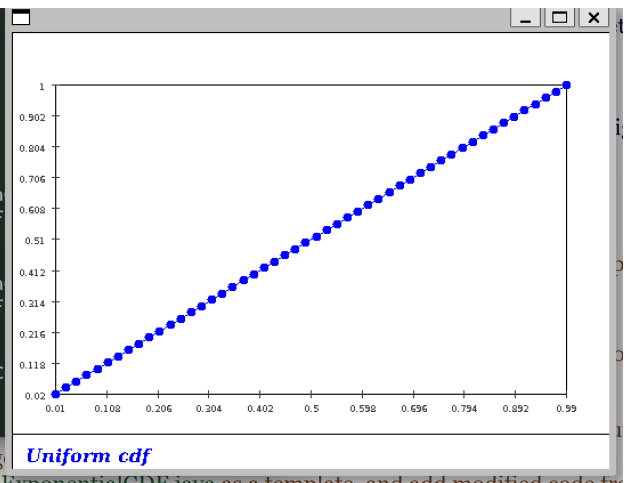
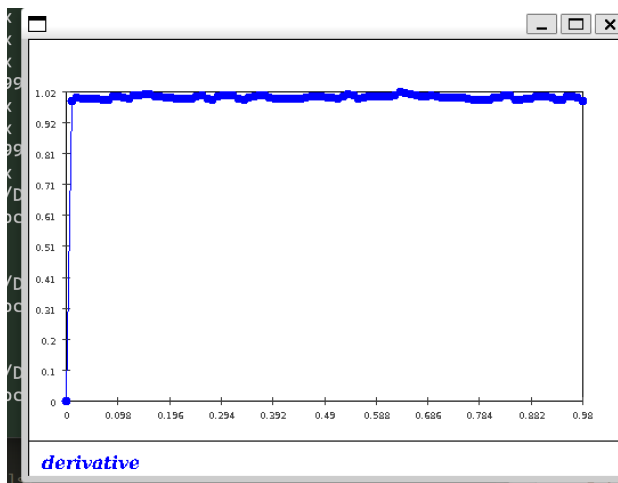
- 1  $\Pr[0 < X \leq 2] : 0.462294$
- 2  $\Pr[X > 0] : 0.462294$

## Exercise 26

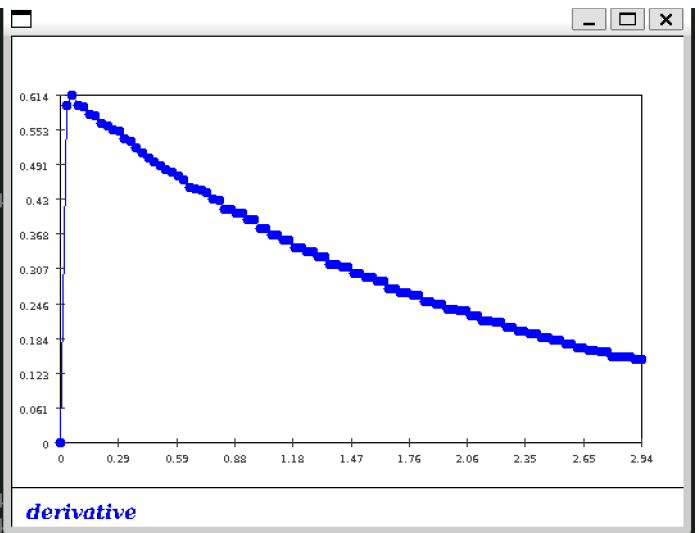
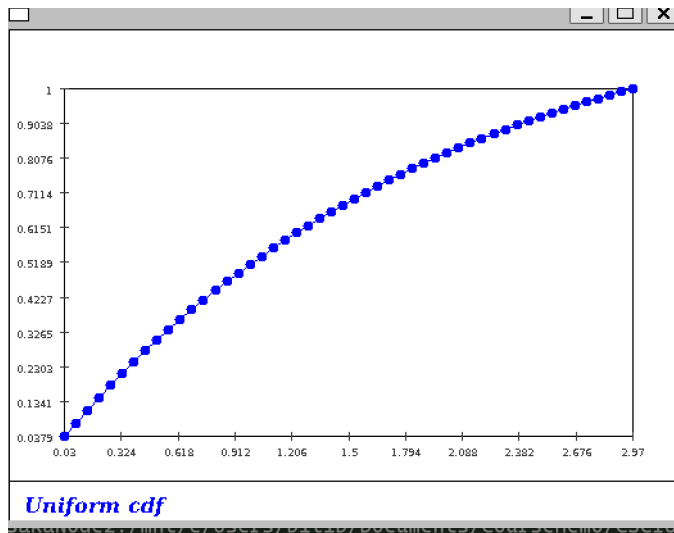
- Gaussian



- Uniform



## Exercise 27



## Exercise 28:

$$E[X] = 1.8$$

$$\text{For } \Pr[H]=0.5, E[X] = 1.5$$

## Exercise 29:

The calculation is exactly the same as in the 3-coin-flip example above

## Exercise 31:

Becomes the probability of k heads

## Exercise 32:

$$E = 1.8000819999999997$$

result is accurate comparing to the earlier results

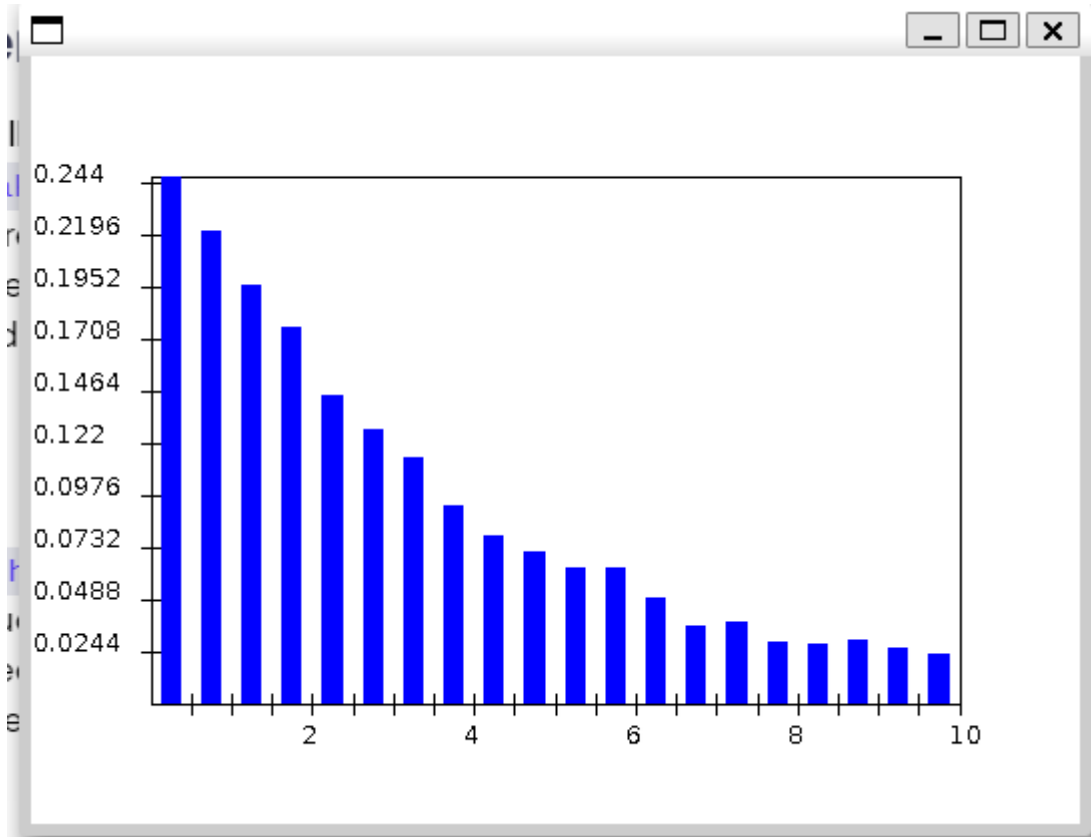
## Exercise 33:

$$E = 10.00$$

**Exercise 34:**

See java files, the accuracy doesn't improve much when using more intervals in expectation computation.

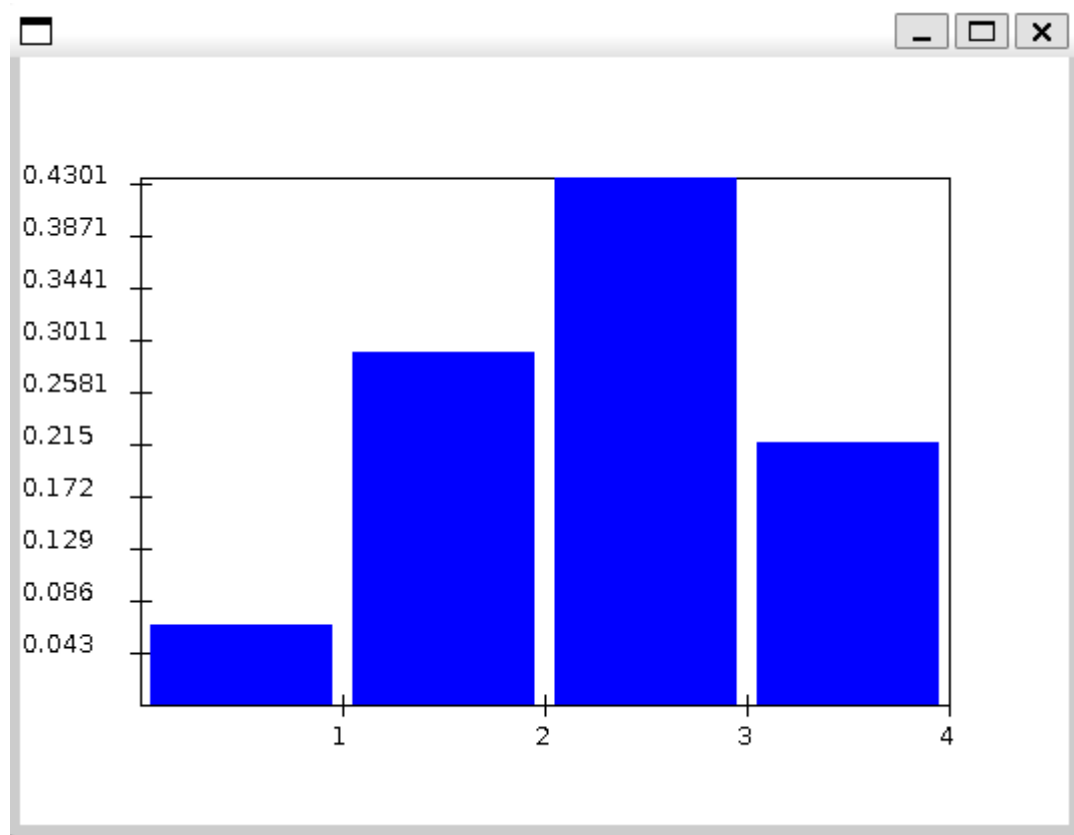
**Exercise 40:**



**Exercise 44:**

$$F^{-1}(y) = \frac{\log(\frac{y}{\gamma})}{-\gamma}$$

**Exercise 46:**



### Exercise 48:

