

A Syntax of V^-

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We present a grammar of V^- :

$\langle \text{program} \rangle$	$::= \{ \langle \text{def} \rangle \}$
$\langle \text{def} \rangle$	$::= \text{val } \langle \text{name} \rangle \langle \text{exp} \rangle$ $\langle \text{exp} \rangle$
$\langle \text{name} \rangle$	$::=$ any token that is not an <i>int-lit</i> , does not contain whitespace, and is not a $\langle \text{value-constructor-name} \rangle$ or a reserved word. $\langle \text{value-constructor-name} \rangle ::=$ $\text{cons} \mid \langle \text{exp} \rangle ::= \langle \text{integer-literal} \rangle$ $\langle \text{name} \rangle$ $\langle \text{name} \rangle$ $\langle \text{guarded-if} \rangle$ $\langle \text{lambda} \rangle$
$\langle \text{integer-literal} \rangle$	$::=$ token composed only of digits, possibly prefixed with a + or -.
$\langle \text{lambda} \rangle$	$::= \lambda \{ \langle \text{name} \rangle \}. \langle \text{exp} \rangle$
$\langle \text{guarded-if} \rangle$	$::= \text{if } [\langle \text{guarded-exp} \rangle \{ [] \langle \text{guarded-exp} \rangle \}] \text{ fi}$
$\langle \text{guarded-exp} \rangle$	$::= \langle \text{exp} \rangle$ $\text{E } \{ \langle \text{logical-var} \rangle \}. \langle \text{guarded-exp} \rangle$ $\langle \text{exp} \rangle ; \langle \text{guarded-exp} \rangle$ $\langle \text{logical-var} \rangle = \langle \text{exp} \rangle ; \langle \text{guarded-exp} \rangle$ $\langle \text{exp} \rangle = \langle \text{exp} \rangle ; \langle \text{guarded-exp} \rangle$ $\langle \text{guarded-exp} \rangle \mid \langle \text{guarded-exp} \rangle$ $\text{one}(\{ \langle \text{guarded-exp} \rangle \})$ $\text{all}(\{ \langle \text{guarded-exp} \rangle \})$
$\langle \text{logical-var} \rangle$	$::=$ a fresh name (cannot be lam- or E-bound in this scope).

Add patterns, value constructors (application), choice, one, all.

1 Forms of Judgement for V^- :

Metavariables:

v, v' : value

eq : equation

$?t$: a temporarily-stuck equation

fail : failure

$\rho, \hat{\rho}$: environment: $\text{name} \rightarrow \mathcal{V}_\perp$

\mathcal{T} : Context of all temporarily stuck equations

e : An expression

ge : A guarded expression

Forms of judgement on equations:

$$\langle \rho, eq \rangle \mapsto \hat{\rho} \text{ (EQUATIONSUCCESS)}$$

$$\langle \rho, eq \rangle \mapsto ?t \text{ (EQUATIONTEMPSTUCK)}$$

$$\langle \rho, eq \rangle \mapsto \mathbf{fail} \text{ (EQUATIONFAIL)}$$

Forms of judgement on expressions:

$$\langle \rho, e \rangle \Downarrow v \text{ (EVALSUCC)}$$

$$\langle \rho, e \rangle \Downarrow \mathbf{fail} \text{ (EVALFAIL)}$$

$$\langle \rho, \mathcal{T}, ge \rangle \Downarrow v \text{ (EVALGESUCC)}$$

$$\langle \rho, \mathcal{T}, ge \rangle \Downarrow \mathbf{fail} \text{ (EVALGEFAIL)}$$

$$\langle \rho, ?t; \mathcal{T} \rangle \mapsto \langle \hat{\rho}, \mathcal{T} \rangle \text{ (CTXTORHO)}$$

In english:

An equation is either solved to produce bindings that extend an environment, gets temporarily stuck, or fails.

An expression either evaluates to produce a value or fails.

Other important guidelines (where do we put these?):

$$\rho \subseteq \rho'$$

$$\text{when } \text{dom } \rho \subseteq \text{dom } \rho'$$

$$\text{and } \forall x \in \text{dom } \rho : \rho(x) \subseteq \rho'(x)$$

When $\langle \rho, e \rangle \mapsto \rho'$, then $\rho \subseteq \rho'$.

2 Rules (Big-step Operational Semantics) for V^- :

$$\text{(GE-CTX-STUCK)} \frac{\langle \rho, eq \rangle \mapsto ?t \quad \langle \rho, ?t; \mathcal{T} \rangle \mapsto \langle \hat{\rho}, \mathcal{T} \rangle \quad \langle \rho, \mathcal{T}, ge \rangle \Downarrow v}{\langle \rho, eq; \mathcal{T}, ge \rangle \Downarrow v}$$

$$\text{(GE-CTX-STUCK)} \frac{\frac{\langle \rho, eq \rangle \mapsto ?t}{\langle \rho, ?t; \mathcal{T} \rangle \mapsto \langle \hat{\rho}, \mathcal{T} \rangle} \quad \langle \rho, \mathcal{T}, ge \rangle \Downarrow v}{\langle \rho, eq; \mathcal{T}, ge \rangle \Downarrow v}$$

Which of the above two do you prefer?

$$\text{(GE-CTX-STUCK)} \frac{\langle \rho, eq \rangle \mapsto ?t \quad \langle \rho, ?t; \mathcal{T} \rangle \mapsto \langle \hat{\rho}, \mathcal{T} \rangle \quad \langle \rho, \mathcal{T}, ge \rangle \Downarrow v}{\langle \rho, eq; \mathcal{T}, ge \rangle \Downarrow v}$$

$$\text{(GE-EQ-STUCK)} \frac{\langle \rho, eq; \mathcal{T}, ge \rangle \Downarrow v}{\langle \rho, \mathcal{T}, eq; ge \rangle \Downarrow v}$$