

Show that the Hotelling  $T^2$  test only works when  $n > p$ .

Hint: One solution is to represent  $S$  using the  $n \times p$  data matrix  $\mathbf{Y}$  and the  $n \times p$  sample mean matrix  $\bar{\mathbf{Y}}$  (What should  $\bar{\mathbf{Y}}$  be?) Also note that  $\text{rank}(\mathbf{A}^T \mathbf{A}) = \text{rank}(\mathbf{A})$ .