

Substituting for λ , $\frac{10^{9} = +\frac{0.6931}{4.5 \times 10^{9}}}{5.5 \times 10^{9}}$ $\frac{1}{5.5 \times 10^{9}}$

```
(h) men of cork, radiis Ica, = IT (1×10<sup>-2</sup>) m²
    Force on coth F = p × Area = pT (1+10-2) N (p=pressure) 1
    Energy gamed by cork in 2 cm = F(2×10<sup>-2</sup>) = pT(1×10<sup>2</sup>) (2×10<sup>-2</sup>)
                                       $ (6.2)10-6J
                                        mgh = m=mas = 10 gms, h=6 m
                                     = 10×10-3(9.81)6
    Thus
                                  b = \frac{5.9 \times 10^{-1}}{6.2 \times 10^{-6}} = \frac{10^{5} P_{a}}{10^{5}}
     Accepte answers in range 104716 Pa.
     Alternative solutions acceptable – can use approx g=10.
(11) het w be the wedth of the tyre and t thickness left on road, Rraduis of tyre
    Removed volume = (5x10-3) 2TRW = 50,000x103x txW
                                       t = 2\pi (20 \times 10^{-2}) \times 10^{-10}
    Taking R=20 cm,
                                        t = 10 m
     Accept 10-9 > 10"m
    Alternative solutions acceptable
(1) Wong = mo2 = mgh (conservation of energy)
              v^2 = 2g (20 \times 10^{-2})  ( f = 20 \times 10^{-2} \text{m})
              v = 1.98 ms. (or Jo.4g)
(ii) Time to fall. 0.80 m, t, is given by
    Horzontal distance s = vt = 10:49 / 9 = 0.80 m
(iii) For a hole at height i above the floor, conservation of energy requires
                  = = mg (1-k)
    Twie, the fall distance hi given by
                           k = \frac{1}{2}gt^2 \quad \text{is} \quad t = \sqrt{\frac{2k}{g}}
    Hongental distance s, given by
                             S = v't' = \sqrt{\frac{2k}{g}} \sqrt{2g(1-k)}
    From (A)
    This gives an equation for k, k^2 - k + \frac{16}{100} = 0
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$$\frac{C_{1}M_{PON}M_{Eurth}}{R^{2}_{ME}} = \frac{Q^{2}}{(4172)}R_{ME}^{2}$$

$$Q^{2} = (4172)G(0.0123)M_{E}^{2}$$

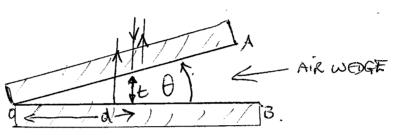
$$= 4\pi(8.854 \times 10^{12})(6.672 \times 10^{11})(0.0123)M_{E}^{2}$$

$$Q = 9.555 \times 10^{-12}M_{E}$$

Mass of electrons

 $M_Q = 9.555 \times 10^{-12} \frac{9.109 \times 10^{-31}}{1.602 \times 10^{-19}} M_E$ $M_Q = 5.43 \times 10^{-23} M_E$

 (ℓ)



- (i) hight reflected from two faces, OA and OB, upper and lower surfaces of air wedge to the phase change of IT at OB due to reflection at interface with lower to higher refractive index

 If thickness of wedge t at reflected region, destructe d from O, landstructive interference require $2t = (n+2) \lambda B$ (nultiger)

 Destructive interference $2t = n\lambda$ Pattern due to interference former suplem
- (ii) Now $t = d \tan \theta \approx d \theta$ Substituting into θ , $2d\theta = (n+i)\lambda$ for constructive functions of Separation Δd between constructive functions given by $2\Delta d\theta = \lambda$ is $\left[n+\frac{3}{2}-(n+2)J\right]$ $\Delta d = \frac{\lambda}{2\theta}$

Ad depends niversky on D; some morks for a qualitative answer

(III) For water refractive videx $\mu > 1$, path obsference becomes $2\mu d\theta$.

Growing $\Delta d = 1$ Fringe superation, $2\mu\theta$ Ad becomes smaller tham in air. Some marks for a qualitatively 1

correct answer. (4)

(m) Devieuse in p.e/= +
$$(0.20)g(0.16) = (+0.3139)$$

(ii) Energy $E = \frac{1}{2}k3c^2 = \frac{1}{2}k(0.16)^2$
At equilibrium $0.20g = k(0.16)$ or $k = \frac{1}{4}g$
Thus $E = \frac{1}{2}(\frac{0.20g}{0.16})(0.16)^2$
 $= 0.157 J = \frac{1}{2}(+V)$

(iv) Heat generated
$$V-E = \frac{1}{2}V$$

$$= 0.157J$$
(iv) Loss in p.e. = $\frac{1}{2}kL(0.24)^2 - (0.16)^2 J - (0.20)g(0.08)$

$$= \frac{1}{2}(\frac{5}{4}g)[(0.40)(0.08)J - 0.016g$$

$$= \frac{1}{2}(\frac{5}{4})g(0.032) - 0.016g$$

$$= 0.016g(\frac{5}{4}-1) = 0.016g(\frac{1}{4}) = 0.004g$$

$$= 39.2 \times 10^{-3} J$$

Gam in KE = 3:92×10⁻² J
(v)
$$T = 2\pi \int_{k}^{m} = 2\pi \int_{5/49}^{45} = 2\pi \int_{25q}^{4} = \frac{4\pi}{5} / \sqrt{g}$$

$$= 0.802 \le 1$$

(n) let n be the number of strokes; working volume of pump
$$V_1$$
 if each stroke produces a volume V_2 with required pressure p_2 , then for its stroke, $p_1V_1 = p_2V_{2i}$ $(V_2 = V_{2i})$ I hen n strokes will produce
$$np_1V_1 = p_2 \sum_i V_{2i} = p_2 V_2 \quad \text{where } V_2 \text{ total vol.}$$
(iving $n(q.0 \times 10^5)(1.0 \times 10^5) = (3.0 \times 10^5)(1.2 \times 10^{-3})$ of type I thus
$$\underline{n = 40}$$

In practice the expansion is not slow, so temperature does not remain constant. It is an achiabatic expansion in which heat generated 2 and does not escape; barrel becomes hot

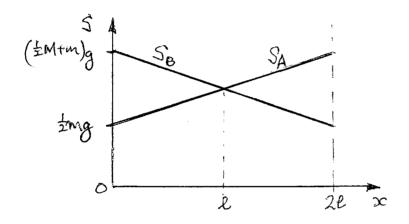
$$S_A + S_B = (M + m) g$$

Moments about A:

$$S_{B} = \left[\frac{1}{2m} + \left(1 - \frac{x}{2e}\right)M\right]g$$

$$S_A = (M+m)g - S_B$$

$$S_A = \left[\frac{1}{2m} + \left(\frac{2\pi}{2E}\right)M\right]g$$



[6]

SONTION TO Q2

[7]

(xi) the network is the same as in (i) with A and B reversed Consequently

i,=i4

 $\begin{bmatrix} 1 \end{bmatrix}$

[Using results in (1)

$$i_8 = i_1 = i_1 = i_4$$

 $i_9 = i_2 = i_{10} = i_3$]

(m) No change

[1]

(iv) In Figure 2.2. Total resistance of upper five resistors is
$$2R + \left(\frac{1}{R} + \frac{1}{2R}\right)^{7} = 2R + \frac{2}{3}R = \frac{8}{3}R$$

hower 5 resisters also $\frac{5}{3}R$.

Adding 2R in parallel with 3R which is in parallel with 3R

Total Resistance
$$R_{AB} = \left(\frac{3}{8} + \frac{3}{8} + \frac{1}{2}\right)R = \left(\frac{5}{4}\right)R$$

[[10]]

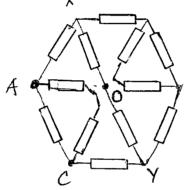
(b) Reversing the p.d. across A.C. requires, by symmetry,

$$i_1 = -i_{10}$$
 $i_5 = -i_7$
 $i_5 = -i_{12}$
 $i_2 = -i_{11}$

[17

Disconnect is and it at function O i, and ig at junction O This does not aller currents in the arms of network

We now have



Total resistance to right of XY =
$$2R + (\frac{1}{2}R + \frac{1}{R}) = \frac{8}{3}R$$

This is in parallel with resistance $2R$ along XY
Crising total resistance $(\frac{1}{2}R + \frac{3}{8}R)^{-1} = \frac{8}{7}R$

1

[1]

Now to night of XY: FR in series with 2R Total resistance FR FR is in parallel with 2R and R. (was to) Groung total resistance $R_{AC} = \left(\frac{7}{2}a + \frac{1}{2} + \frac{1}{1}\right)R$

[I][1]

KAC = 1 R

II 10 I

Wavelength of sound $\lambda = \frac{c_s + v}{f_o}$ Frequency ditected by observer $f = \frac{c_s + v}{\lambda} = \frac{c_s + v}{c_s / f_o}$

$$f = \frac{C+V}{C_S} f_0$$

(i)

(11) Source moving towards stationary observer, separation between successive crest, apparent wavelength,

 $\lambda = \frac{c_s}{f_0} - \frac{u}{f_0} =$

$$f = c_s / \left(\frac{c_u}{f_o}\right)$$

[2]

 $\begin{bmatrix} 1 \\ 2 \end{bmatrix}$

Velouty of senud relative to Ebserver

 $C_0 = C_S + V$

$$f = \frac{c_0}{\lambda} = \frac{c_{s+v}}{(c_{s-u})/f} = \frac{c_{s+v}}{c_{s-u}}f$$

S Source

Velocity component in direction of source is Veos O. This replaces 'v' m A. As O micreases the factor 'vioso' decreases, reducing the value of f in A. Once the observer has passed the closest

Q3

point to source, S, the sign of 'V' changes in (A), as he is moving away from the source, so f continues to decrease.

Correct explanation for approaching and receding from source.

Conrect EXPLANATION

(1) For small times approaching source

 $\oint = 210.4 = \left(\frac{c_s + V}{c_s}\right) \oint 0$

口了 from (A) (D)

For large time, receding from source

 $f = 181.6 = \left(\frac{C_s - V}{C_s}\right) f_0$

[i] from (A)

210.4 = <u>Cs+V</u> 181.6 Cs-V 0]

[3]

 $\frac{V}{C_s} = \frac{210.4 - 181.6}{240.4 + 181.6}$

 $V = 330 \left(\frac{28.8}{392} \right) = 24.26 \text{ m/s}^{-1}$

Substituting vinto D

f = 210.4 = 330 + 24.24 fo

 $f_0 = \frac{(210.4)(330)}{354.24} = 196.0 \text{ Hz}$

C17

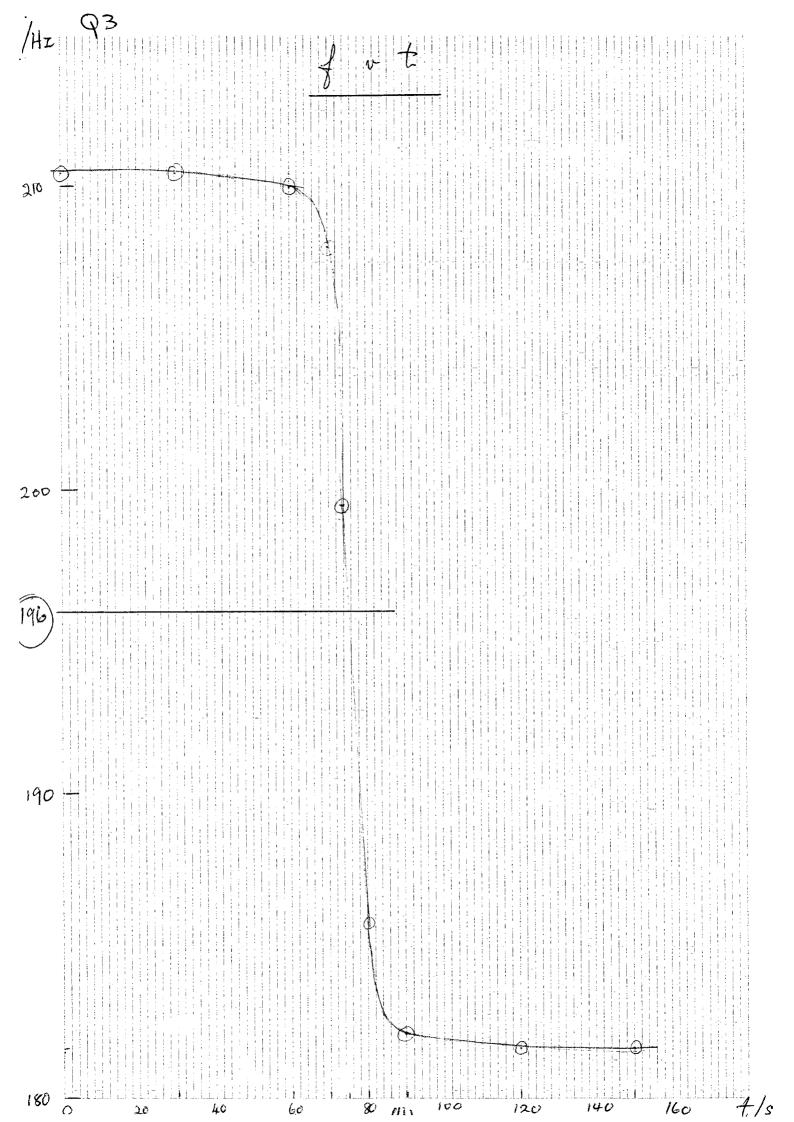
(iii) At the point of closest approach to source, time to, $v\cos\theta = 0$ is $\cos\theta = 0$ $\theta = 90^{\circ}$

f = fo = 196.0 Hz

From the graph at f = 196.0 $t_0 = 75.5 \pm 1.05$

[1+1]

[[127]



SOLUTION Q4

4 (i)

ha/mm	d/mm	d3/mm3.
,	,	,
290	1.22	1.816
162	1.01	1-030
41	0.64	0 . 262
1.3		

Theory correct for small he:

3 mg ho = Pd3.

Graph pusses through the origin

$$h_2 = \frac{P}{3mg} d^3$$
.

Table of rabues he against d³

Graph correctly flotted on a reasonable scale

making full use of graph paper

Strength line throughthe origin

Minor deviation from strength line for h= 290

[1]

(ii) Gradient $\frac{d^3}{k_2} = \frac{44350}{2080}$ mm² = $\frac{3mg}{p}$ = $(6.32 \pm 0.2)/0^{-3}$ in $\frac{2}{m^2}$ = $\frac{(6.32 \pm 0.2)/0^{-9}}{3mg}$ = $\frac{(1.85 \pm 0.05)}{3mg}$ $\frac{1}{3mg}$

$$\frac{P}{3mg} = \frac{k_2}{d^3}.$$

$$\frac{P}{2} = \frac{1}{2} + \frac{1}{2} = \frac{1}{2}$$
Henret occuracy

[1+1=2]

$$\frac{1}{2} m V^{2} = mgh$$

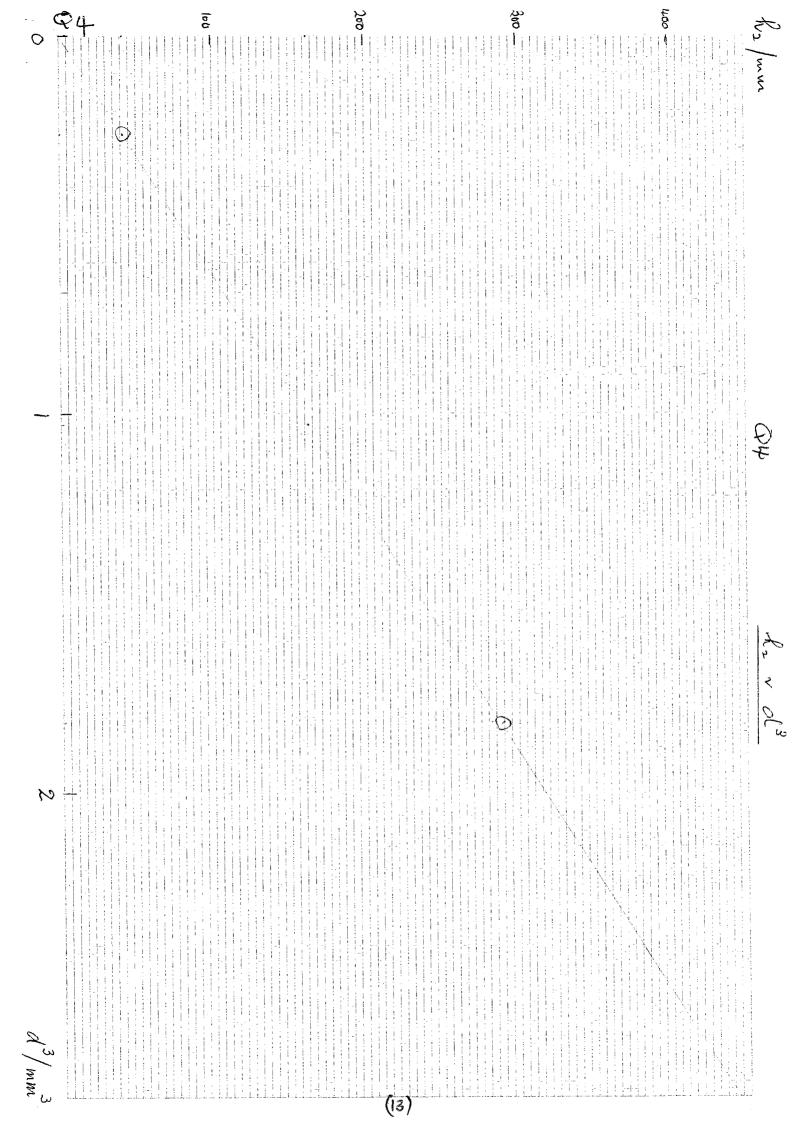
$$V^{2} = 2gh$$

$$V_{R} = \sqrt{2g} (h_{2})^{\frac{1}{2}}$$

$$V_{I} = \sqrt{2g} (h_{1})^{\frac{1}{2}}$$

$$\alpha = \left(\frac{h_{2}}{h_{1}}\right)^{\frac{1}{2}}$$

[3]



Sorotion

QH

ha/mm	hi/mm	(h2/h1) /2/mm=	(h,)2/mm2
290	1000	0.238	31.6
162	500	0.569	22-4
41	100	0.640	10.0
1.3	2.0	0.806	1041

Correct table of values Plot $(h_1/h_1)^{\frac{1}{2}}$ against $(h_1)^{\frac{1}{2}}$ Correct graph using major pertion of graph paper. Smooth curve through points	
(IV) The to fall 900 mm, to, given by $\frac{900}{1000} = \frac{1}{2}gto^{2} ie to = \sqrt{\frac{2}{g}}\sqrt{\frac{900}{1000}}$	[2]
Tune t, to rese to maximum height after first konne given by $h_2 = \frac{1}{2}gt_1^2 \text{if } t_1 = \sqrt{\frac{2}{g}} \int_{R_2}^{R_2}$ $2t_1 = 2\sqrt{\frac{2}{g}} \int_{R_2}^{R_2}$ (A)	[2
From α - (k_1) graph $(k_2)^{\frac{1}{2}} = 0.541$	
so require time	[]
$t_{0} + 2t_{1} = \sqrt{\frac{2}{9}} \sqrt{\frac{900}{1000}} \left[1 + 2(0.541) \right]$ $= 0.89 \pm 0.01 3$	[1]

(v) Heat, sommed, vibration, deformation of anvil (kelfmork for each mechanism up to max.2)

SONTION TO Q5

$$(i) \qquad V_1 = \frac{Q_1}{C_1}$$

$$\sqrt{2} = \frac{Q_2}{C_2}$$

$$(iii) E = V_1 + V_2 = Q_1 \left(\frac{1}{C_1} + \frac{1}{C_2} \right)$$

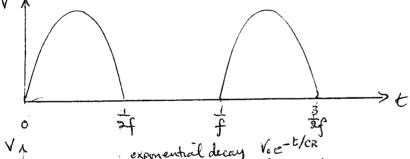
$$= \frac{Q_1}{C_1}$$

$$\frac{1}{C_1} = \frac{1}{C_1} + \frac{1}{C_2}$$

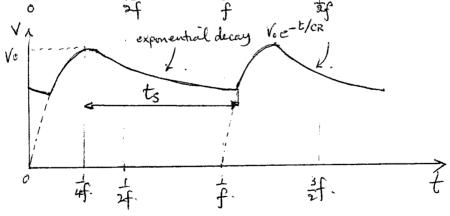
(iv) Energy
$$\mathcal{E} = \frac{1}{2} C E^2 = \frac{1}{2} \left(\frac{1}{C_1} + \frac{1}{C_2} \right) E^2$$

$$= \frac{1}{2} C \left(\frac{Q_1}{C_1} \right)^2$$

$$= \frac{1}{2} \frac{Q_1^2}{C_2}$$



$$\binom{1}{n}$$



Explanation -> [17

Exponential decay of voltage across capacitor when dide terminates current

$$t_s = -cR \ln (0.799049) = -(400 \times 10^6)(100) \ln (0.799049)$$

(17)

(V) ESTIMATES
$$V_{d} \simeq \frac{1}{2}(10+7.990) = 8.995$$

$$V_{a} \approx \frac{1}{2}(10-7.990) = 1.005$$
[1]
$$f_{a} = f = 100 \text{ Hz}$$

II i 3 II

(a) Eis the induced emf in volts due to a conductor cutting the magnetic flux field. It is equal to the rate of change of the flux lunkage, I, in unto of wehers per sec. The minus segn indicates that the induced current produce by the conductor culturg the magnetic field ereales à magnetic flux in the opposite direction to the external magnetic fluis; the arrent flows in such a derection as to oppose the change that is [3] toking place.

(b) (i)
$$E = \frac{(6 \times 10^5)(80)(720)10^3}{60 \times 60}$$

$$E = 0.96V$$

(iii)
$$E = \frac{(3 \times 10^{-5})(8)(720)10^3}{60 \times 60}$$
 [7]

(w) Honiz. wing compt.
$$E_{w} = \frac{(\sin 66)(90)(720)\times10^{3}(5\times10^{-5})}{60\times60}$$

$$E_{\omega} = 0.72 \text{ V}$$

Verhial component
$$E_V = \frac{(\cos 66)(8)(720) \times 10^3 (5 \times 10^{-5})(\cos 45)}{60 \times 60}$$
 $E_V = \frac{(\cos 66)(8)(720) \times 10^3 (5 \times 10^{-5})(\cos 45)}{60 \times 60}$

[[14]

Q6

(c) $V = \frac{1}{2}B\omega\left(\frac{L}{2}\right)^2 = \frac{1}{8}B\omega L^2$

[2]

(ii) ZERO

[1]

(iii) $\frac{1}{2}$ Bw $(L-xc)^2 - \frac{1}{2}x^2$ Bw

[1+1]

 $= \frac{1}{2} BwL(L-2x)$

LIJ

[[67]]

\$7 (a)

SOLUTION TO Q7

(i)

$$T = kR^{\alpha}$$

 $luT = \alpha luR + luk$

[1]

Plot lu Tagainst lu R gradient a, intercept link

PLANET	R/108km	lnR	T/days	luT
EARTH	1-49	0.3920	365	5.900
MARS	2.28	0.8242	687	6.532
TUPITER	7.78	2.0516	4333	8.37
URANUS	28.7	3.357	30690	10.33

TABLE OF VALUES [2]

CORRECT CORAPH

[2]

[1]

ACCURACY

171

(ii) When lin R = 0, lin T = link. i k = (T) R=0

From graph

luk = 5.4 ± 0.1

 $k = 221 \pm 25$ days /(108km) $^{3/2}$ [1]

In \$1 units

$$k = (221 \pm 25)_{24 \times 60 \times 60} / (10'')^{3/2} - 31^{2}$$

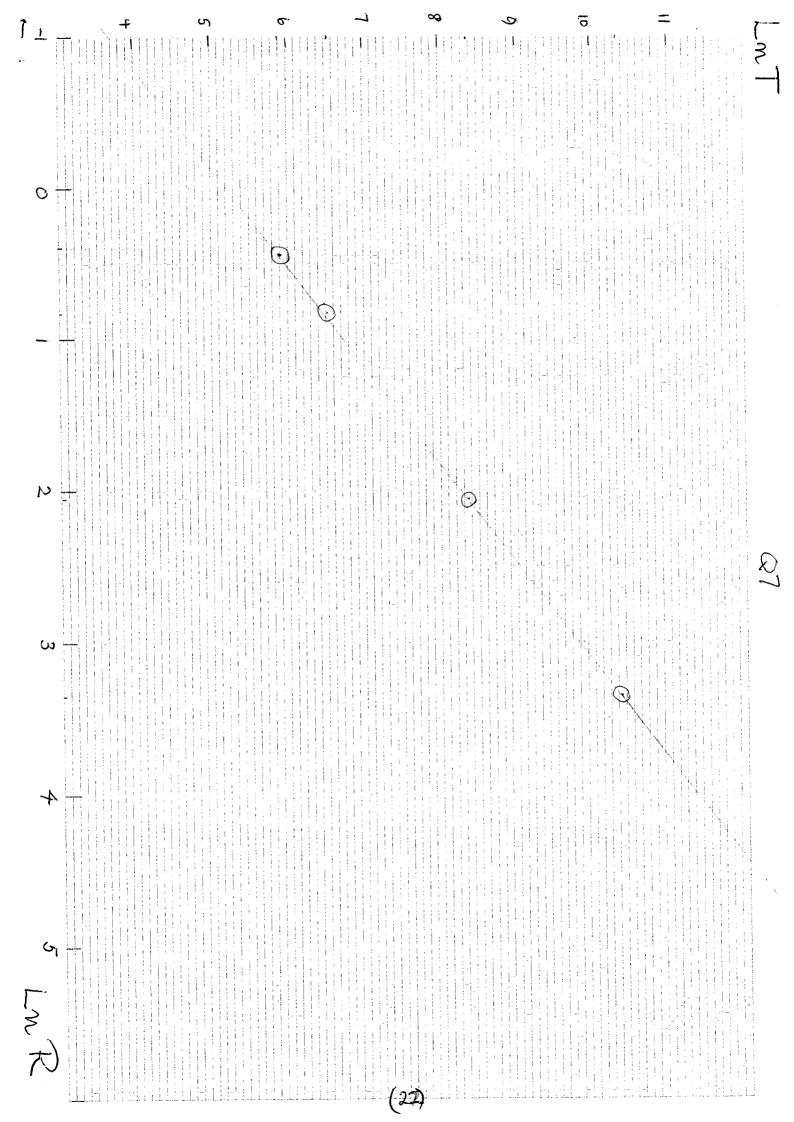
$$= (1.90 \pm .2) \sqrt{10} / \sqrt{0}$$

$$= (6.0 \pm 0.6) / \sqrt{0}$$
Sm Magnitude [1].

Dimensions [1]

$$= (1.70 \pm .2) / 10 / 0 = 312$$

[[10]]



(i) Equation for circular motion for planet of mass m ang. vel. w GM.m

$$mR\omega^{2} = \frac{GM_{SM}}{R^{2}}$$

$$R^{3} = GM_{S} \left(\frac{T}{2\pi}\right)^{2}$$

$$T^{2} = \frac{(2\pi)^{2}}{GM_{S}} R^{3}$$

$$T = 2\pi/\omega [1]$$

$$T = \frac{2\pi}{\sqrt{GM_s}} R^{3/2}$$

(11) Determination of Ms As points all le on a straight line to wiki accuracy of the graph, one can use any set of data to debermine Ms.

Mars Data Gives using
$$T^{2} = \frac{(2\pi)^{2}}{GM_{s}}R^{3}.$$

$$M_{s} = \frac{(2\pi)^{2}}{G}\frac{R^{3}}{T^{2}}$$

$$= \frac{(2\pi)^{2}(2.28 \times 10^{11})^{3}}{6.67 \times 10^{-11}(6.87 \times 24 \times 60 \times 60)^{2}}$$
[1]

$$M_s = (1.98 \pm 0.08) 10^{30} \text{kg}$$

[1]

Ail the other planets data give some result

from part (a) {[3] ALTERNATIVELY USING $K = \sqrt{GM_s} = 6.0 \times 10^{-10}$ GIVES SAME RESULT BUT LESS ACCURATE

(iii) Now
$$T_{Moon}^{2} = \frac{(3\pi)^{2}}{GM_{E}} R_{Moon}^{3}$$

$$T_{E}^{2} = \frac{(2\pi)^{2}}{GM_{S}} R_{E}^{3}$$
Thus
$$T_{Woon}^{2} = \frac{(2\pi)^{2}}{GM_{S}} R_{E}^{3}$$

$$T_{Woon}^{3} = \frac{(2\pi)^{2}}{GM_{S}} R_{E}^{3}$$

$$\frac{M_{s}}{M_{E}} = \left(\frac{R_{E}}{R_{Mocn}}\right) \left(\frac{T_{Moon}}{T_{E}}\right)$$

(23)

$$\frac{M_{5}}{M_{E}} = \left(\frac{1.49 \times 10^{8}}{3.8 \times 10^{5}}\right) \left(\frac{27.3}{365}\right)$$

$$= 3.4 \times 10^{5} \pm 0.2 \times 10^{5}.$$