

Statistical learning assignment 8- chapter 4

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7.

$$\begin{aligned} p_{yes}(x) &= \frac{\pi_{yes} \exp(-\frac{1}{2\sigma^2}(x-10)^2)}{\pi_{yes} \exp(-\frac{1}{2\sigma^2}(x-10)^2) + \pi_{no} \exp(-\frac{1}{2\sigma^2}x^2)} \\ &= \frac{0.8 \exp(-\frac{1}{72}(x-10)^2)}{0.8 \exp(-\frac{1}{72}(x-10)^2) + 0.2 \exp(-\frac{1}{72}x^2)} \end{aligned}$$

$$\Rightarrow p_{yes}(4) \approx 0.752$$

Approximately 75.2% that the company will issue a dividend.

8.

The training error rate is close to 0 if $K = 1$, and average error rate is 18%, that means error rate of 36% on the test data. So we prefer logistic regression.

9.

(a.)

$$\frac{P(X)}{1 - P(X)} = 0.37 \Rightarrow 1.37P(X) = 0.37, P(X) \approx 0.27$$

(b.)

$$\begin{aligned} P(X) &= 0.16 \\ odds &= \frac{P(X)}{1 - P(X)} = \frac{0.16}{0.84} \approx 0.19 \end{aligned}$$

12. (a)

```
> power=function()  
+ {  
+   result=2^3  
+   print(result)  
+ }  
> power()  
[1] 8
```

(b)

```
> power2=function(x,a)  
+ {  
+   result=x^a  
+   print(result)  
+ }  
> power2(3,8)  
[1] 6561
```

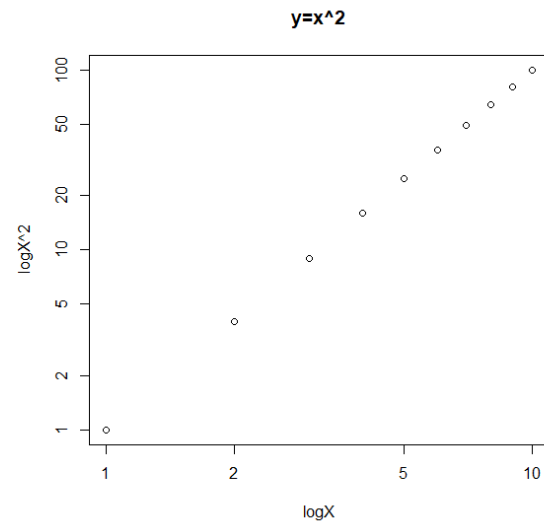
(c)

```
> power2(8,17)  
[1] 2.2518e+15
```

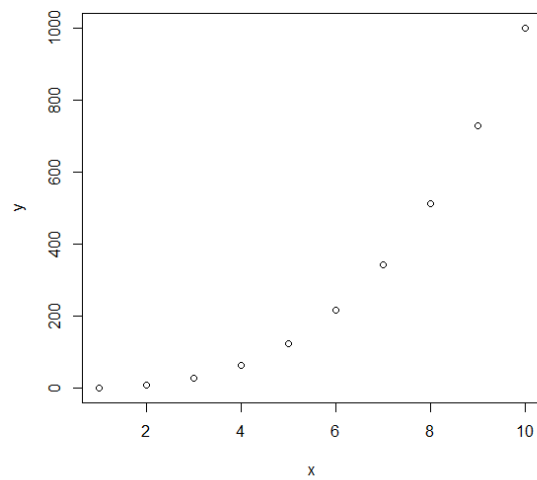
(d)

```
> power3=function(x,a)  
+ {  
+   result=x^a  
+   return(result)  
+ }
```

(e)



(f)



```
13. > #####logistic regression#####  
> {  
+ class=rep(0,nrow(Boston))  
+ class[which(crim>median(crim))]=1  
+ boston=data.frame(Boston,class)
```

```

+ attach(boston)
+ model=glm(class~.-crim,data=boston,family=binomial)
+ tr=boston[1:400,]#training set
+ te=boston[401:506,]#test set
+ tecr=te$class#real test
+ pro=predict(model,data.frame(te),type="response")
+ tepre=rep(0,nrow(te))
+ tepre[which(pro>0.5)]=1
+ mean(tepre!=tecr)#test error
+ }
[1] 0.04716981
> #####LDA#####
> {
+ LD=lda(class~.-crim,data=boston,family=binomial)
+ telda=predict(LD,data.frame(te))
+ mean(telda$class!=tecr)
+ }
[1] 0.0754717
> #####KNN#####
> {
+ kn=knn(tr,te,tr$class,k=1)
+ mean(kn!=tecr)
+ }
[1] 0.0754717
> {
+ kn=knn(tr,te,tr$class,k=10)
+ mean(kn!=tecr)
+ }
[1] 0.0754717
> {
+ kn=knn(tr,te,tr$class,k=100)
+ mean(kn!=tecr)
+ }
[1] 0.09433962

```

In this case we can find that the logistic regression is the best approach to predict, and the test error of LDA is equal to KNN when $K = 1, 10$.