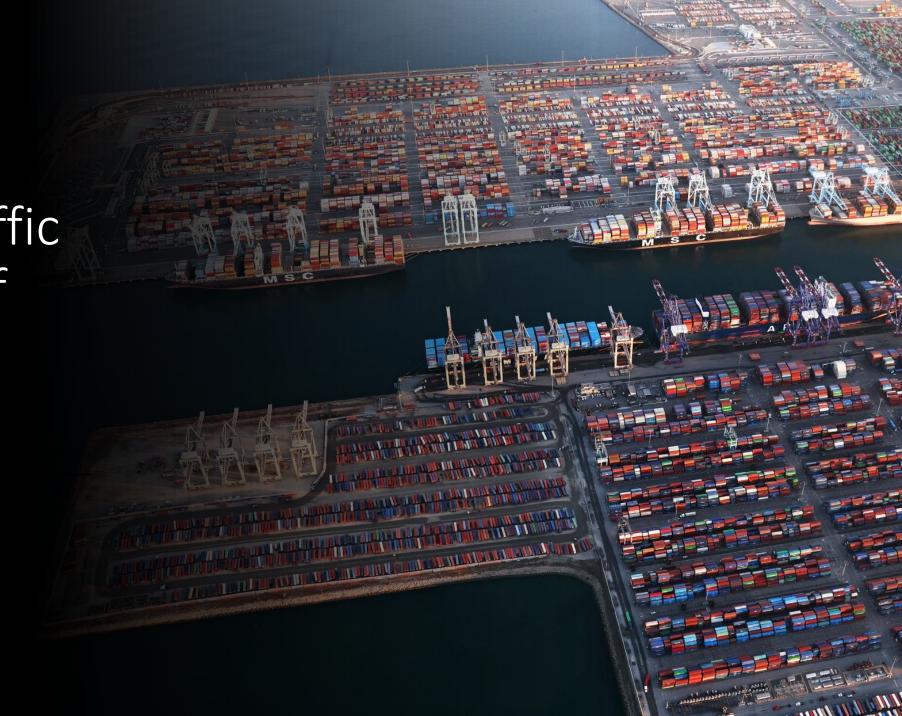
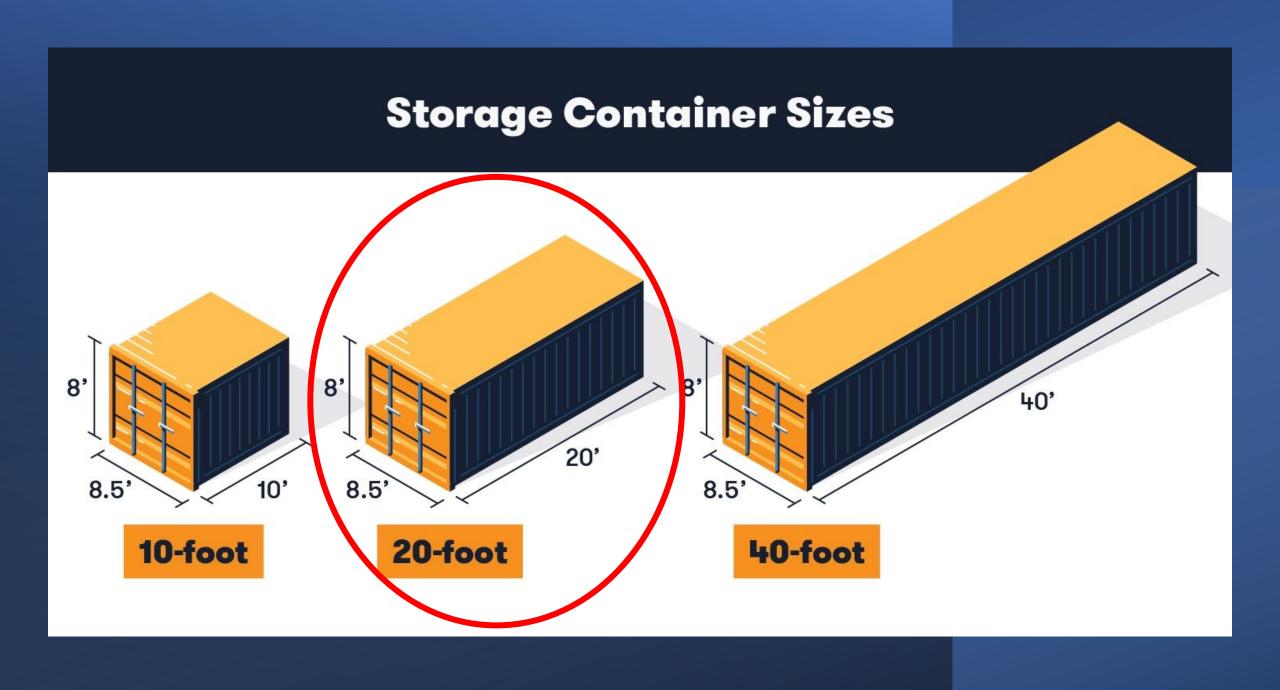
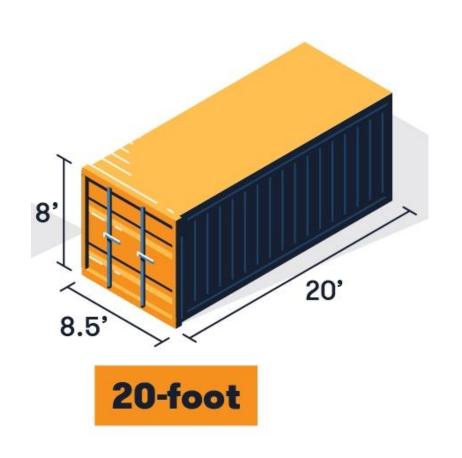
Forecasting
Container Traffic
for the Port of
Los Angeles

By: Jason Rogers and Daniel Schumacher

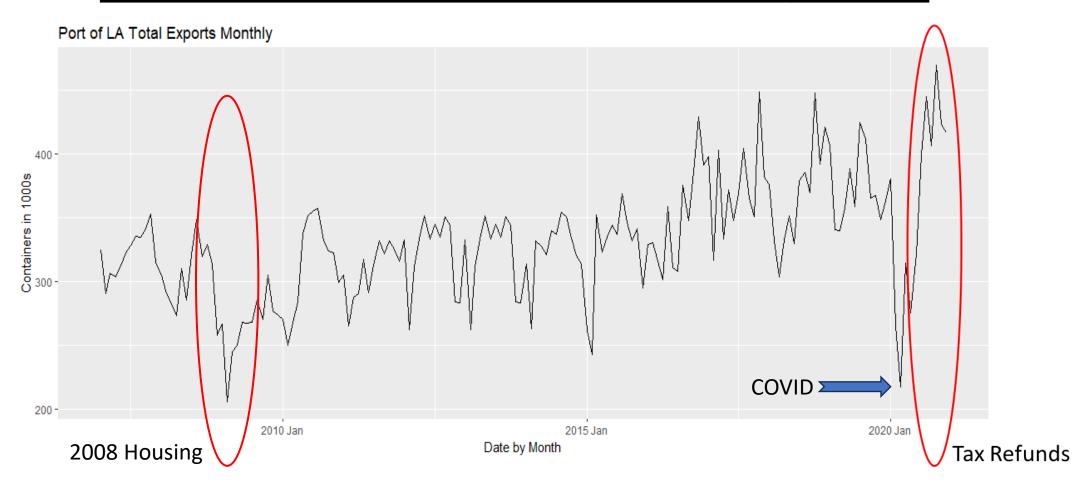






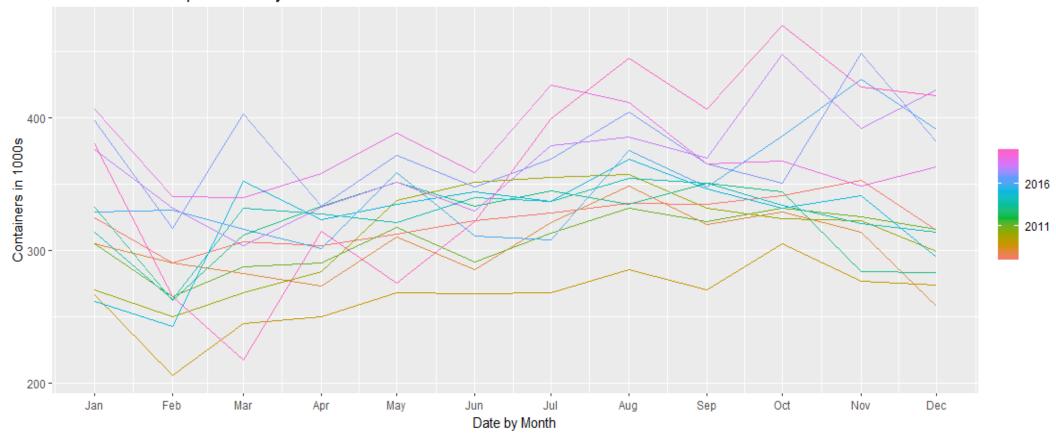
# Twenty Foot = Equivalent Units (TEUs)

# <u>Data Overview – Total Exports</u>

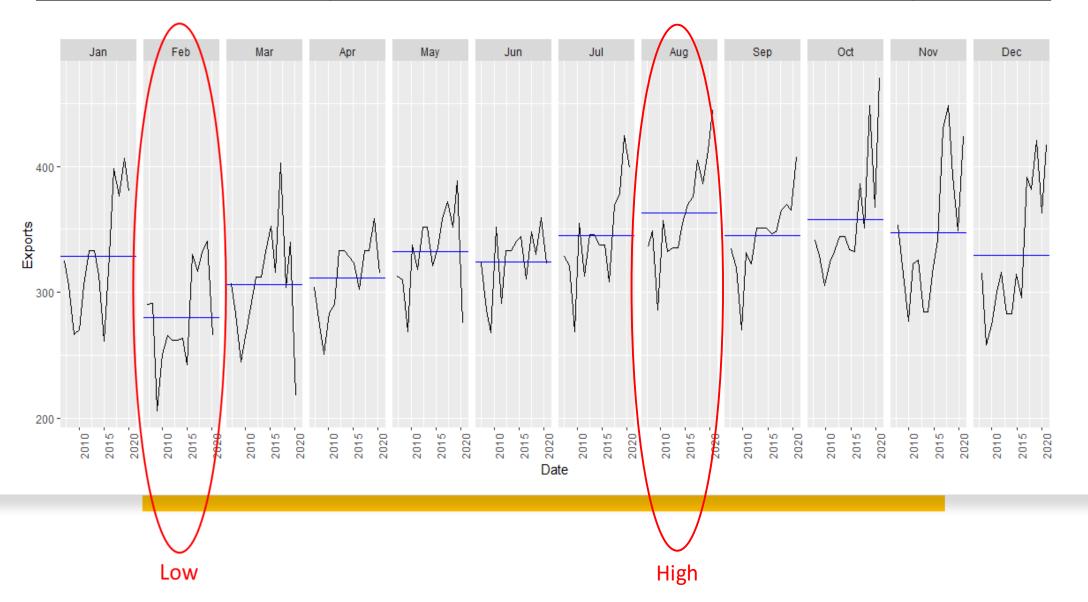


# <u>Seasonality Overview – Total Exports</u>

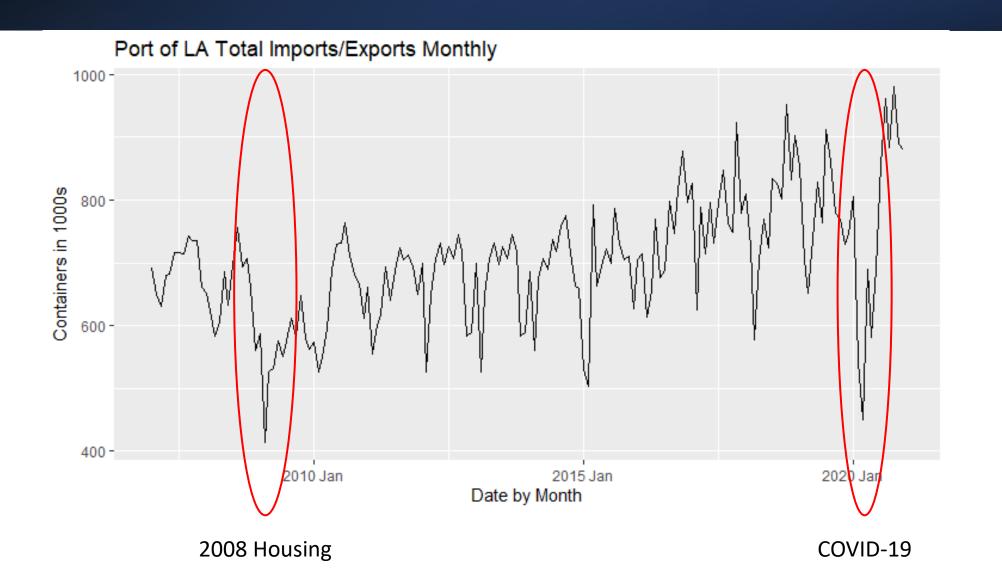




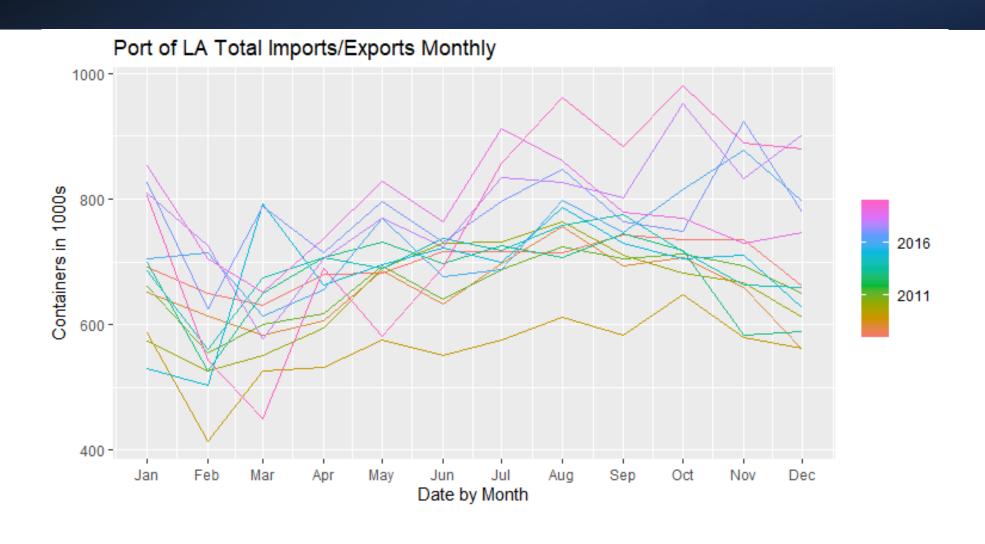
# <u>Seasonality Overview – Total Exports</u>



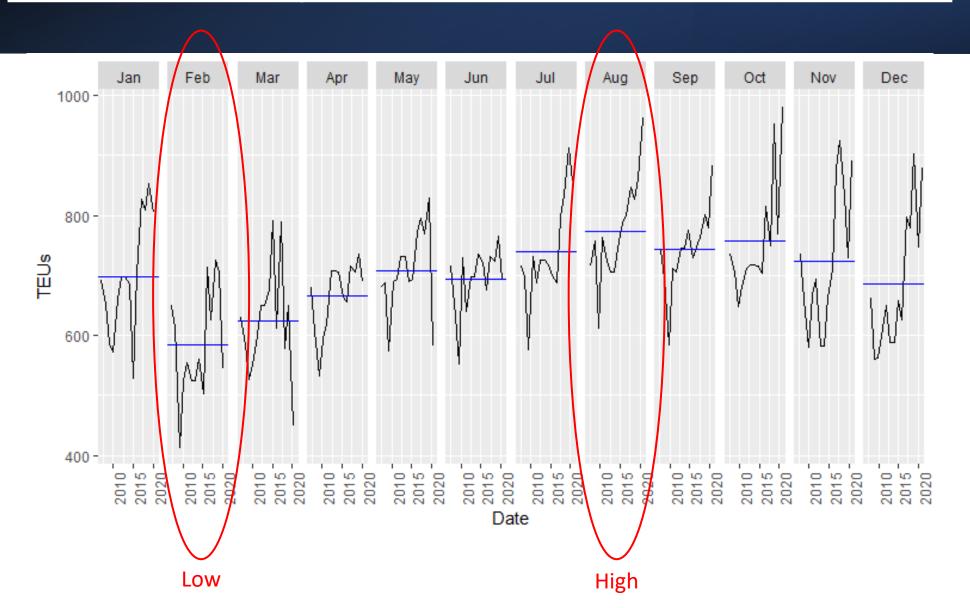
# Data Overview – Total TEUs



# Seasonality Overview — Total TEUs



## Seasonality Overview — Total TEUs



# Compare Linear Models

#### **Total Exports:**

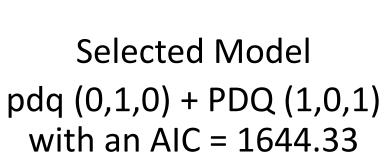
Linear Trend selected with residual standard error 32.85

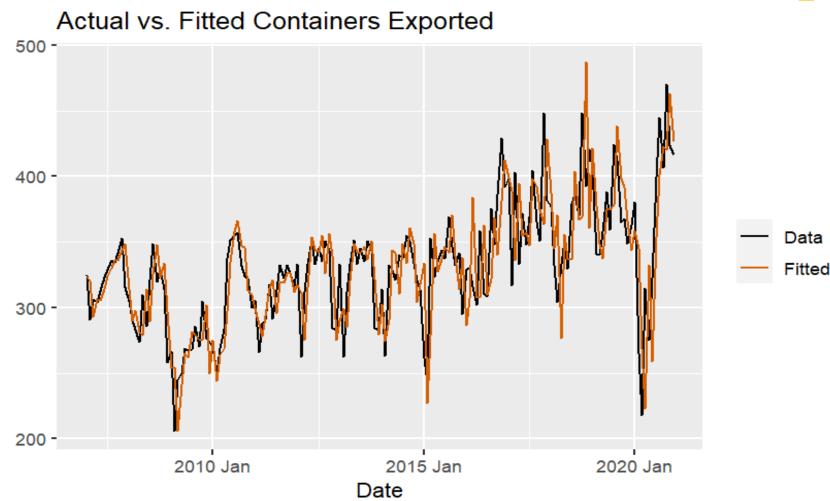
#### **Total TEUs:**

Quadratic Trend selected with residual standard error 69.11 v 71.09



## <u>ARIMA Fit – Total Exports</u>

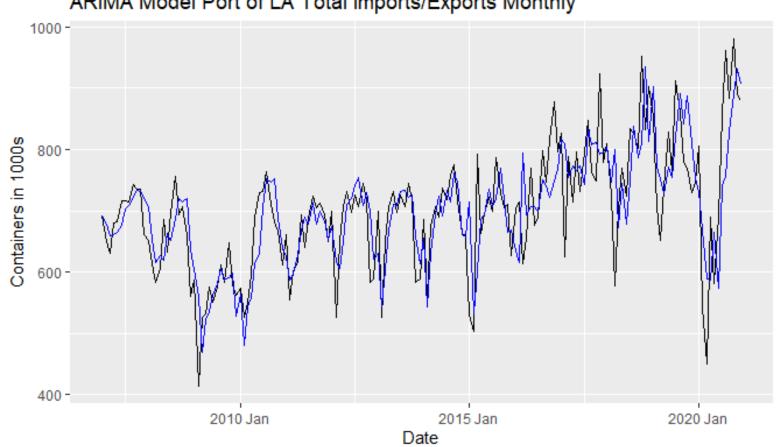




## ARIMA Fit – Total TEUs

#### ARIMA Model Port of LA Total Imports/Exports Monthly

Selected Model pdq (2,1,0) + PDQ (1,0,1) with an AIC = 1883.36



Series

Data

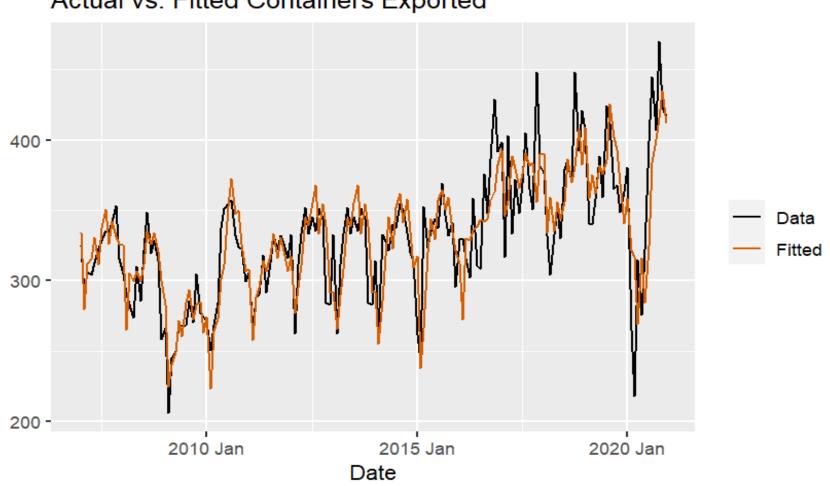
Fitted

## ETS Fit – Total Exports

Actual vs. Fitted Containers Exported

ETS model fits best with A, A, A or data that has constant trend with additive seasonality.

AIC = 2002.62

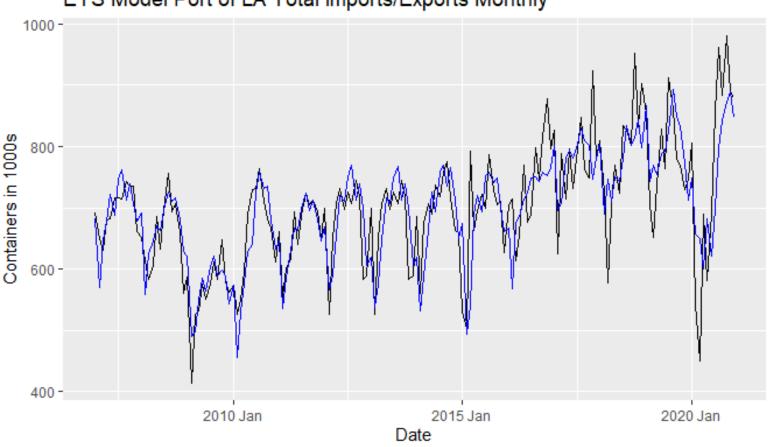


## ETS Fit – Total TEUs

ETS Model Port of LA Total Imports/Exports Monthly

ETS model fits with best with A, N, A or data that has constant trend with additive seasonality.

AIC = 2268.76



Series

Data

Fitted

## Comparing All Models



#### Best performing model was auto ETS

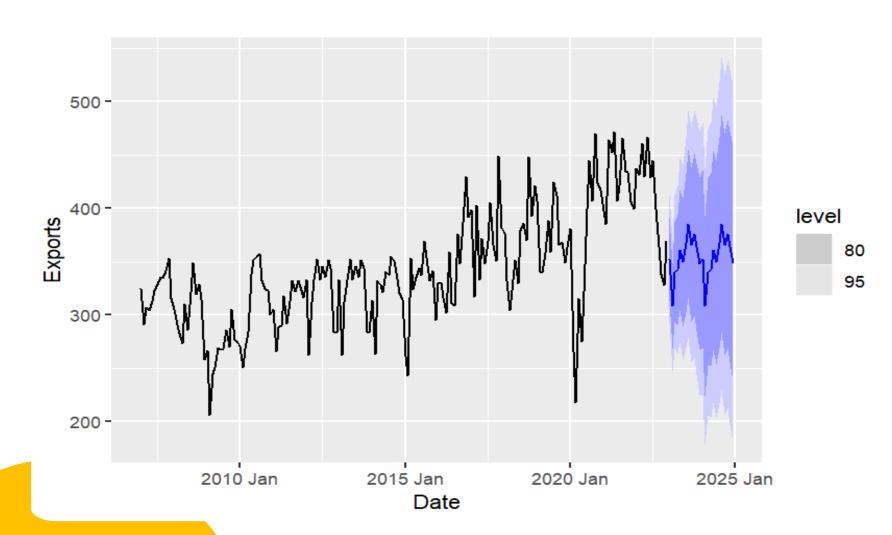
.model		ME	RMSE	MAE	MPE	MAPE	MASE	<b>RMSSE</b>
1 e	ts_auto	-0.437	47.2	37.6	-1.16	9.40	1.22	1.16
2 e	ts_manual1	-7.27	50.2	38.3	-2.86	9.75	1.25	1.23
3 C	ombination	3.89	53.0	41.7	-0.249	10.4	1.36	1.30
4 A	RIMA.auto	-10.3	60.9	44.3	-3.87	11.3	1.44	1.49
5 A	RIMA3.fit	e0.223	59.4	46.3	-1.25	11.5	1.50	1.45
6 t	rain.tb_lm	37.3	62.2	54.7	7.89	13.0	1.78	1.52

#### **Total TEUs:**

#### Best performing model was ETS A, N, A

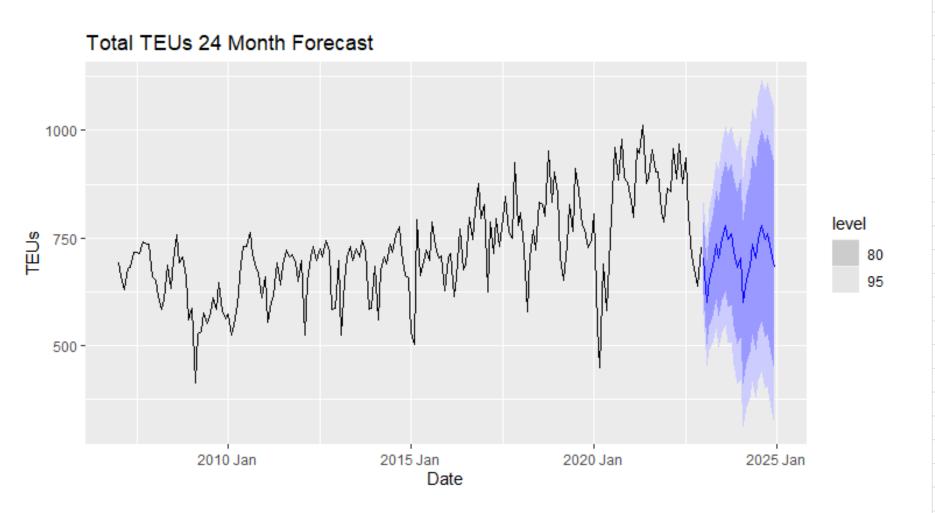
.model	ME	RMSE N	ИΑΕ	MPE	MAPE I	MASE RM	SSE
1 ETS_manual	-22.7	116	87.6	-4.17	11.1	1.35	1.34
2 ets_auto	-22.7	116	87.6	-4.17	' 11.1	1.35	1.34
3 ts_reg	3.49	125	95.6	-1.21	11.9	1.47	1.44
4 combination	-22.9	132	99.5	-4.39	12.5	1.53	1.53
5 arima_auto	-20.1	152	114.	-4.32	14.2	1.76	1.76
6 arima_manual	52.3	160	125.	-8.11	15.8	1.93	1.85

## Total Exports 24 Month Forecast



2023 Jan	252.27
2023 Feb	308.24
2023 Mar	340.00
2023 Apr	342.54
2023 May	360.65
2023 Jun	349.30
2023 Jul	367.55
2023 Aug	385.31
2023 Sep	365.83
2023 Oct	375.47
2023 Nov	363.90
2023 Dec	348.09
2024 Jan	352.27
2024 Feb	308.24
2024 Mar	340.00
2024 Apr	342.54
2024 May	360.65
2024 Jun	349.30
2024 Jul	367.55
2024 Aug	385.31
2024 Sep	365.83
2024 Oct	375.47
2024 Nov	363.90
2024 Dec	348.09

## Total TEUs 24 Month Forecast



2023 Jan	703.1859
2023 Feb	600.1623
2023 Mar	654.8572
2023 Apr	684.1826
2023 May	734.5271
2023 Jun	702.0776
2023 Jul	749.1346
2023 Aug	778.7497
2023 Sep	746.2127
2023 Oct	758.8937
2023 Nov	718.5186
2023 Dec	681.6405
2024 Jan	703.1859
2024 Feb	600.1623
2024 Mar	654.8572
2024 Apr	684.1826
2024 May	734.5271
2024 Jun	702.0776
2024 Jul	749.1346
2024 Aug	778.7497
2024 Sep	746.2127
2024 Oct	758.8937
2024 Nov	718.5186
2024 Dec	681.6405

# Questions



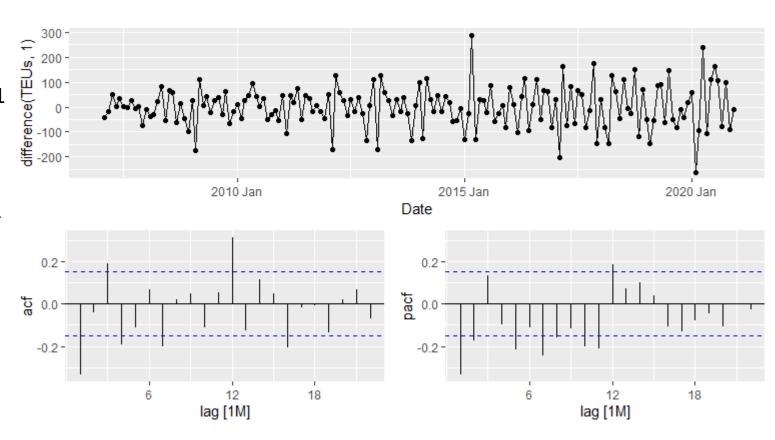
## Appendix A: ARIMA Fit – Total Exports

#### **Plotting ACF and PACF**

Testing for P = 1 due to significant value at PACF = 1 pdq (0,1,0) + PDQ (1,0,0) AIC = 1932.34

Testing for Q = 1 due to significant value at ACF = 1 pdq (0,1,0) + PDQ (0,0,1) AIC = 1942.94

Testing for Both P = 1 and Q = 1pdq (0,1,0) + PDQ (1,0,1)AIC = 1925.03



## **UPDATE**

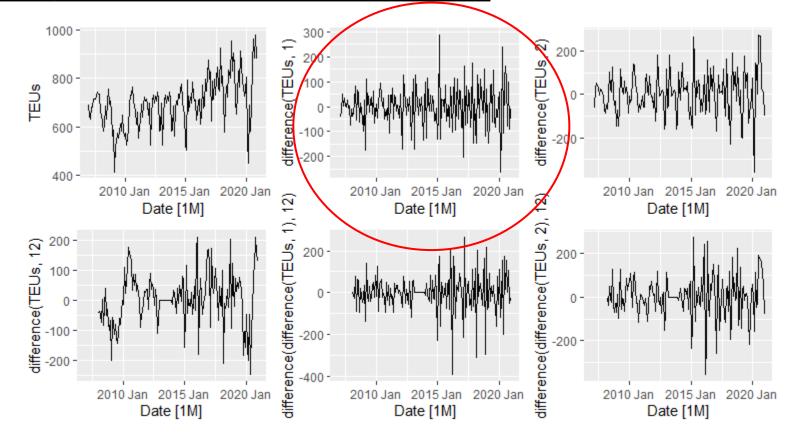
## Appendix B: ARIMA Fit – Total TEUs

#### Test for d and D:

Do we need to remove any seasonal trend? (D) TEUs.train %>% features(TEUs, unitroot\_nsdiffs) # Do not test for seasonal (lag 12) difference due to the results being 0, D=0

Do we also need to remove any non-seasonal trend? (d) TEUs.train %>% features(TEUs, unitroot\_ndiffs)

The number 12 due to monthly data for 1 LAG, d = 1.



Graphing the differences confirms d/D test, the circled graph appears to be the smoothest plot

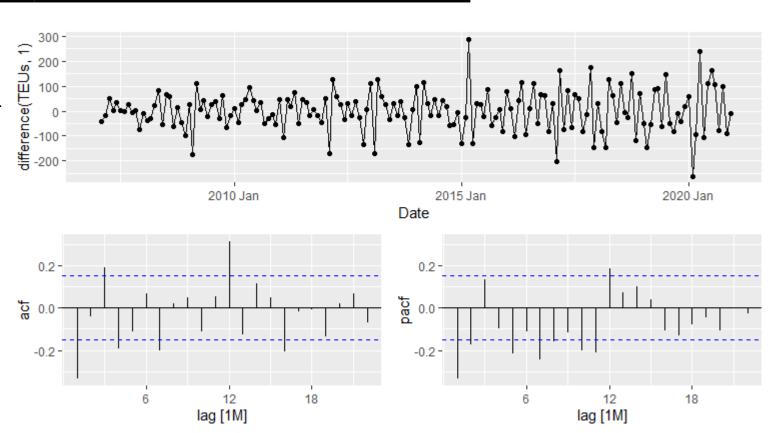
### Appendix B: ARIMA Fit – Total TEUs

#### **Plotting ACF and PACF**

Testing for P = 1 due to significant value at PACF = 1 pdq (0,1,0) + PDQ (1,0,0) AIC = 1932.34

Testing for Q = 1 due to significant value at ACF = 1 pdq (0,1,0) + PDQ (0,0,1)AIC = 1942.94

> Testing for Both P = 1 and Q = 1 pdq (0,1,0) + PDQ (1,0,1)AIC = 1925.03



### Appendix B: ARIMA Fit – Total TEUs

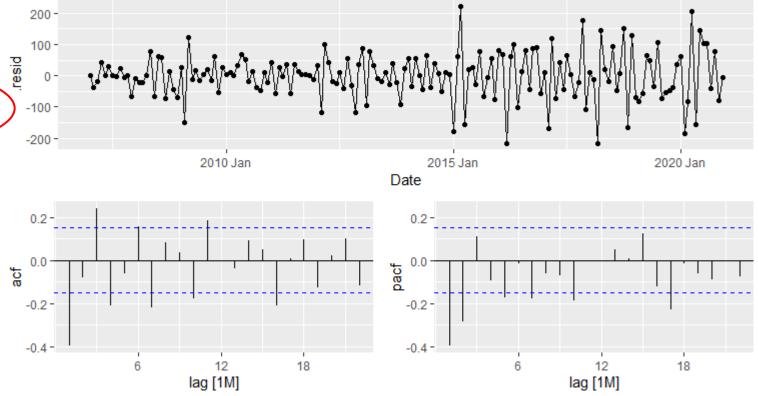
#### **Checking for remaining residuals**

Residuals continue to appear at ACF 1 and PACF 2

Testing for p = 2 due to significant value at PACF = 2 pdq (2,1,0) + PDQ (1,0,1) AIC = 1883.36

Testing for q = 1 due to significant value at ACF = 1 pdq (0,1,1) + PDQ (1,0,1) AIC = 1885.67

Testing for Both p = 2 and q = 1pdq (2,1,1) + PDQ (1,0,1)AIC = 1883.56



No Remaining Residuals after running p=2

## <u>Appendix B: ETS Fit – Total TEUs</u>

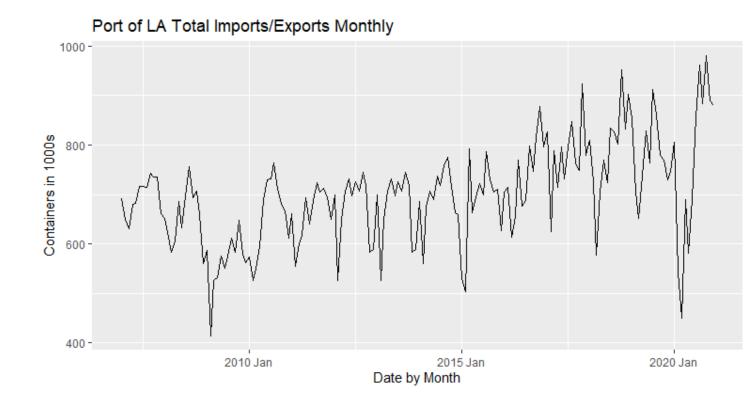
#### **Testing ETS models:**

Selected A, A, A to test first to determine if there was upward linear trend with additive seasonality AIC = 2272.346

Selected A, M, A second to test for upward exponential trend with additive seasonality AIC = 2272.471

Last Selected A, N, A to determine if there was a constant trend with additive seasonality

AIC = 2268.760



```
##Jason Rogers 669 Final Project##
##load libraries##
library(tsibble)
##
## Attaching package: 'tsibble'
## The following objects are masked from 'package:base':
##
##
       intersect, setdiff, union
library(dplyr)
## Warning: package 'dplyr' was built under R version 4.2.3
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
       filter, lag
## The following objects are masked from 'package:base':
##
##
       intersect, setdiff, setequal, union
library(fpp3)
## Warning: package 'fpp3' was built under R version 4.2.3
## — Attaching packages —
                                                                       - fpp3 0.5 --
## √ tibble
                 3.2.1

√ tsibbledata 0.4.1

## √ tidyr
                 1.3.0

√ feasts
                                          0.3.0
## ✓ lubridate 1.8.0
                           √ fable
                                          0.3.2
## √ ggplot2
                 3.4.3

√ fabletools 0.3.2

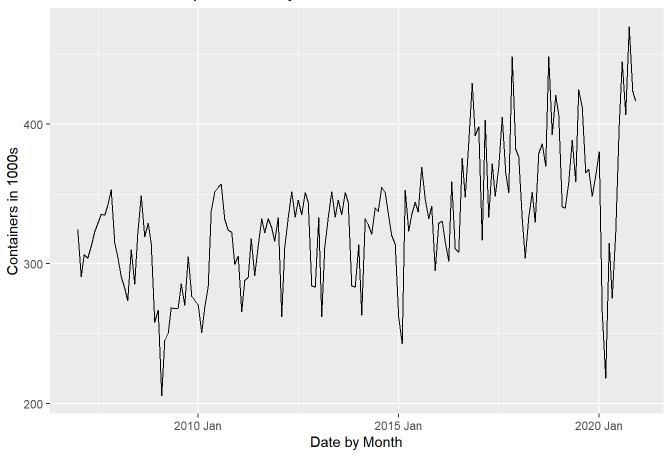
## Warning: package 'tibble' was built under R version 4.2.3
## Warning: package 'tidyr' was built under R version 4.2.3
```

## Warning: package 'ggplot2' was built under R version 4.2.3

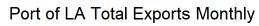
```
##set directory##
setwd("C:/Users/roger/OneDrive/Desktop/SCMA 669 Merrick")
##Load dataset##
exports.df <- read.csv("Containers Port of Los Angeles Exports.csv", header = TRUE)
exports.df <- exports.df %>%
  select(Date, Exports)
View(exports.df)
##format Date column and make Month##
exports.tb <- exports.df %>%
 mutate(Month = as.Date(Date, "%m/%d/%Y")) %>%
 mutate(Date = yearmonth(Month))
##set index and create tsibble##
exports.tb <- exports.tb %>%
  as_tsibble(index = Date)
##partition the data for training##
train.tb <- exports.tb %>%
 filter(year(Date) <= 2020)
##Visualize your training data##
```

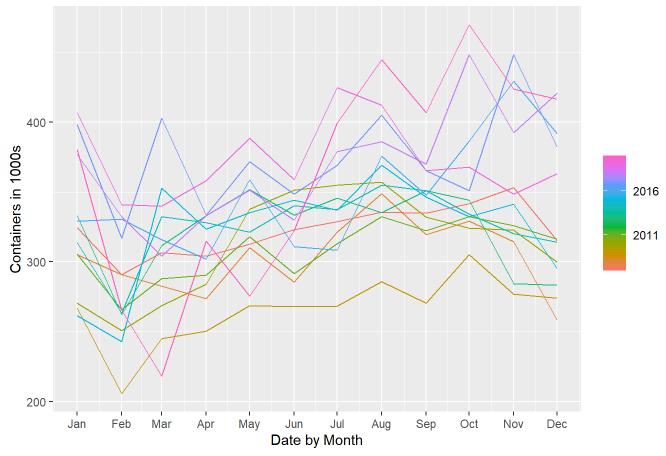
```
# Create a time series plot.
train.tb %>% autoplot(Exports) +
  ylab("Containers in 1000s") +
  xlab("Date by Month") +
  ggtitle("Port of LA Total Exports Monthly")
```

#### Port of LA Total Exports Monthly

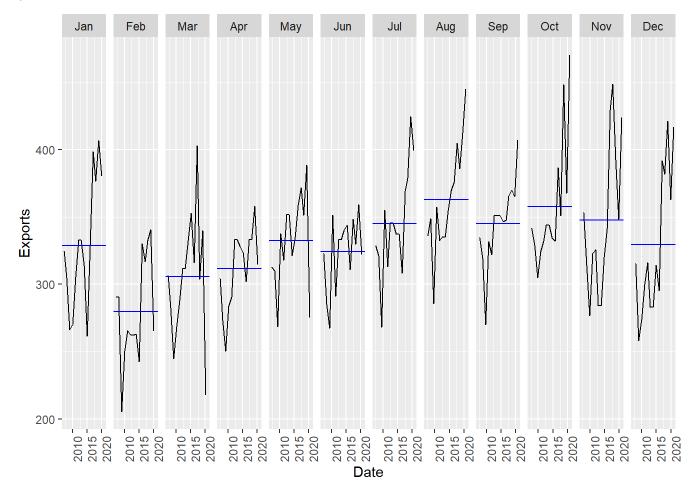


```
# Create a seasonal plot.
train.tb %>% gg_season(Exports, period = "year") +
  ylab("Containers in 1000s") +
  xlab("Date by Month") +
  ggtitle("Port of LA Total Exports Monthly")
```





# Create a sub-series plot.
train.tb %>% gg\_subseries(Exports)



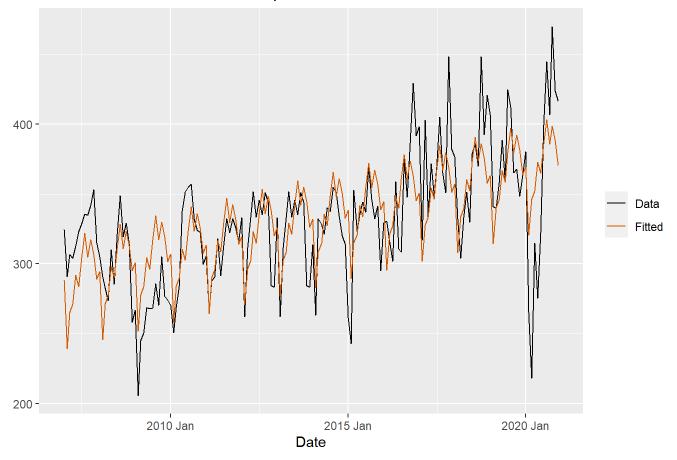
##There is a slight upward linear trend with seasonality that is additive. The trend has more ex planatory power than the seasonality. The graph also shows how exports were impacted during COVI D, both 2008 and 2020 break from the trend and dip heavily.##

```
##Fit a regression model to the training data with appropriate trend and seasonality##

train.tb_lm <- train.tb %>%
  model(TSLM(Exports ~ trend() + season()))%>%
  report()
```

```
## Series: Exports
## Model: TSLM
##
## Residuals:
##
        Min
                                               Max
                   1Q
                         Median
                                      3Q
## -128.3113 -17.5576
                         0.1169
                                           79.1221
                                19.8077
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
                              9.7077 29.643 < 2e-16 ***
## (Intercept)
                 287.7620
## trend()
                   0.5203
                              0.0524
                                     9.929 < 2e-16 ***
## season()year2 -49.4339
                            12.4180 -3.981 0.000105 ***
## season()year3 -24.2170
                            12.4184 -1.950 0.052969 .
## season()year4 -18.8959
                            12.4189 -1.522 0.130161
## season()year5
                  1.3516
                            12.4197 0.109 0.913480
## season()year6
                 -7.1972
                            12.4207 -0.579 0.563126
## season()year7
                 13.1325
                            12.4219 1.057 0.292061
## season()year8
                  30.1480
                            12.4233
                                      2.427 0.016383 *
## season()year9
                  12.1834
                            12.4250 0.981 0.328340
## season()year10 24.2597
                            12.4269
                                      1.952 0.052716 .
                             12.4290
## season()year11 13.3978
                                      1.078 0.282730
## season()year12 -5.0846
                            12.4313 -0.409 0.683090
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 32.85 on 155 degrees of freedom
## Multiple R-squared: 0.5336, Adjusted R-squared: 0.4975
## F-statistic: 14.78 on 12 and 155 DF, p-value: < 2.22e-16
```

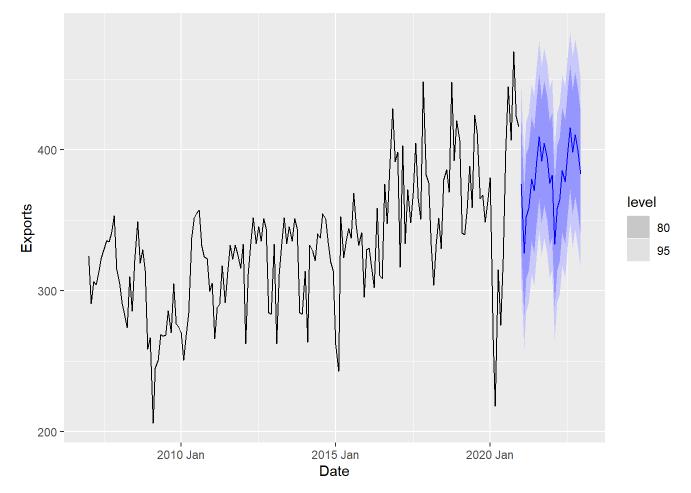
#### Actual vs. Fitted Containers Exported



```
##Forecasting 24 months##

fc_train.tb_lm <- train.tb_lm %>%
  forecast(h = 24)

fc_train.tb_lm %>%
  autoplot(train.tb)
```



```
accuracy(fc_train.tb_lm, exports.tb)
```

```
##Mape 13##

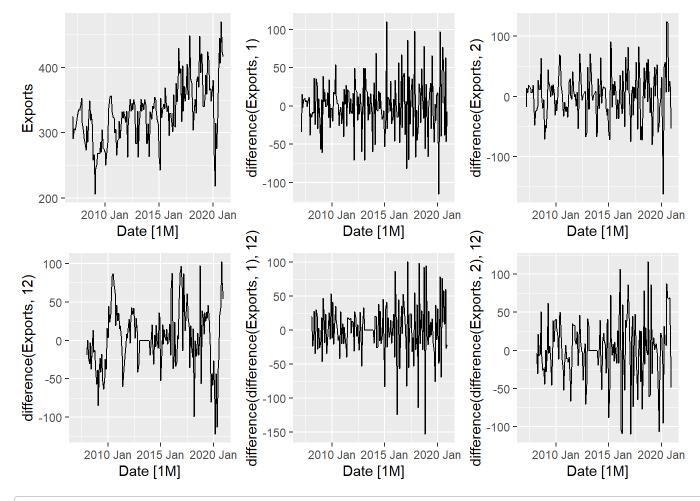
##Fit an ARIMA model##

##remove any seasonal trend? (D)##

train.tb %>% features(Exports, unitroot_nsdiffs)
```

```
## # A tibble: 1 × 1
## nsdiffs
## <int>
## 1 0
```

```
##We do seasonal (lag 12) difference due to the results being 0. D=0##
##remove any non-seasonal trend? (d)##
train.tb %>% features(Exports, unitroot_ndiffs)
## # A tibble: 1 × 1
     ndiffs
##
##
      <int>
## 1
          1
##The number 12 due to monthly data for 1 LAG, d = 1.##
library(gridExtra)
##
## Attaching package: 'gridExtra'
## The following object is masked from 'package:dplyr':
##
##
       combine
grid.arrange(train.tb %>% autoplot(Exports),
             train.tb %>% autoplot(difference(Exports, 1)),
             train.tb %>% autoplot(difference(Exports, 2)),
             train.tb %>% autoplot(difference(Exports, 12)),
             train.tb %>% autoplot(difference(difference(Exports, 1), 12)),
             train.tb %>% autoplot(difference(difference(Exports, 2), 12)),
             ncol = 3, nrow = 2)
## Warning: Removed 1 row containing missing values (`geom_line()`).
## Warning: Removed 2 rows containing missing values (`geom_line()`).
## Warning: Removed 12 rows containing missing values (`geom_line()`).
## Warning: Removed 13 rows containing missing values (`geom_line()`).
## Warning: Removed 14 rows containing missing values (`geom_line()`).
```

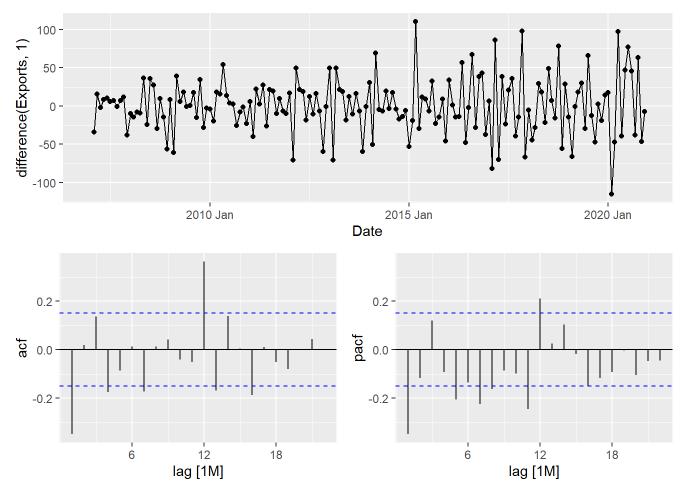


##ACF and PACF##

train.tb %>% gg\_tsdisplay(difference(Exports, 1), plot\_type='partial')

## Warning: Removed 1 row containing missing values (`geom\_line()`).

## Warning: Removed 1 rows containing missing values (`geom\_point()`).



```
# Graph shows spikes at AR1, AR5 and AR7 without a solid pattern forming in ACF. # There is a spike at AR12 to consider ##Let's try d=1, D=0, p=0, P=1## ARIMA1.fit <- train.tb %>% model(ARIMA(Exports \sim pdq(0,1,0) + PDQ(1,0,0))) report(ARIMA1.fit)
```

```
## Series: Exports
## Model: ARIMA(0,1,0)(1,0,0)[12]
##
  Coefficients:
##
##
           sar1
         0.4253
##
##
  s.e.
         0.0750
## sigma^2 estimated as 1100: log likelihood=-822.44
## AIC=1648.88
                 AICc=1648.95
                                BIC=1655.11
```

```
##AIC 1648.88##

ARIMA2.fit <- train.tb %>% model(ARIMA(Exports ~ 1 + pdq(0,1,0) + PDQ(0,0,1)))
report(ARIMA2.fit)
```

```
## Series: Exports
## Model: ARIMA(0,1,0)(0,0,1)[12] w/ drift
##
## Coefficients:
##
           sma1 constant
         0.2630
##
                   0.6303
## s.e. 0.0625
                   3.3146
##
## sigma^2 estimated as 1199: log likelihood=-828.34
## AIC=1662.67
                AICc=1662.82
                                BIC=1672.02
```

```
##AIC 1662.67##

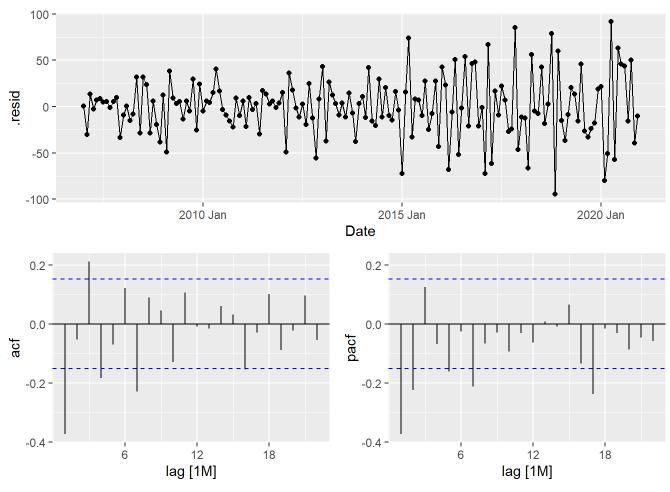
ARIMA3.fit <- train.tb %>% model(ARIMA(Exports ~ 1 + pdq(0,1,0) + PDQ(1,0,1)))
report(ARIMA3.fit)
```

```
## Series: Exports
## Model: ARIMA(0,1,0)(1,0,1)[12] w/ drift
##
## Coefficients:
##
           sar1
                    sma1 constant
##
         0.7894 -0.4505
                            0.0915
## s.e. 0.1070
                0.1632
                            1.1449
##
## sigma^2 estimated as 1049: log likelihood=-818.17
## AIC=1644.33
                AICc=1644.58
                               BIC=1656.81
```

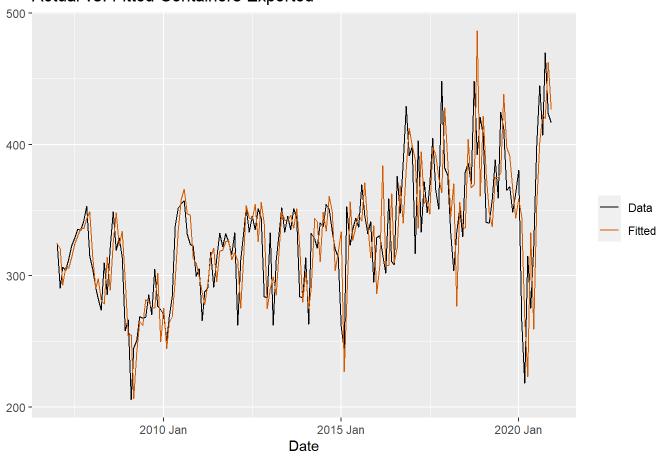
```
##AIC 1644.33, this has the Lowest mape##

##Residuals##

augment(ARIMA3.fit) %>% gg_tsdisplay(.resid, plot_type='partial')
```

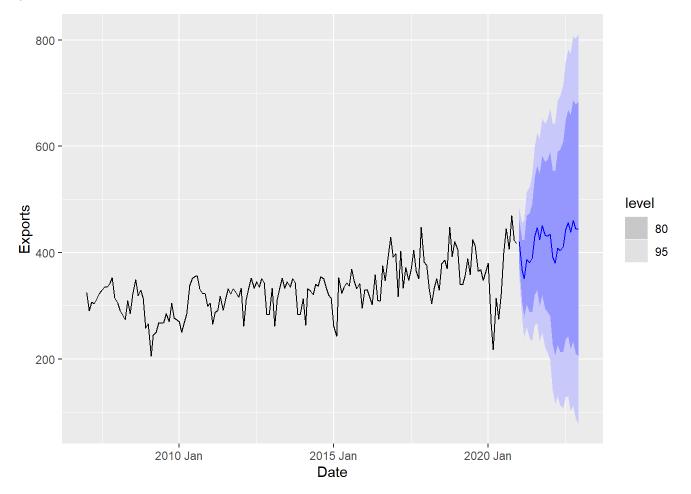






fc\_ARIMA3.fit <- ARIMA3.fit %>%
 forecast(h = 24)

fc\_ARIMA3.fit %>%
 autoplot(train.tb)



```
accuracy(fc_ARIMA3.fit, exports.tb)
```

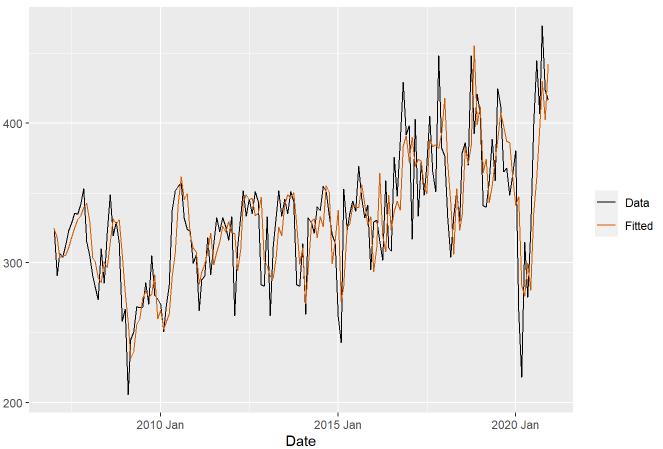
```
##Mape 11.5##

##auto.arima()##

ARIMA.auto <- train.tb %>% model(ARIMA(Exports))
report(ARIMA.auto)
```

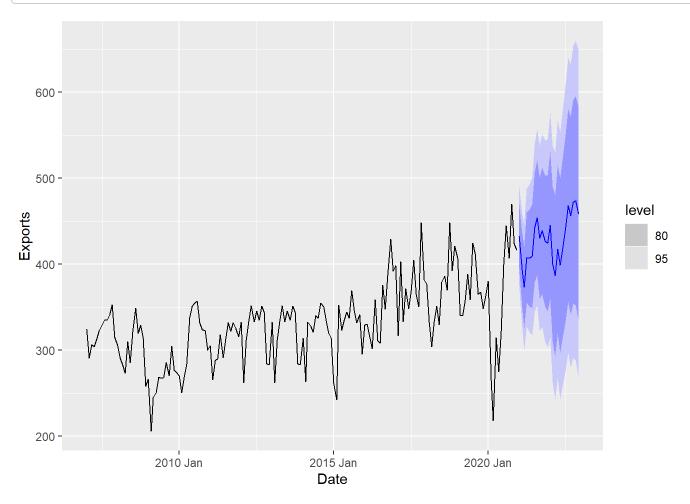
```
## Series: Exports
## Model: ARIMA(0,1,1)(0,0,2)[12]
##
## Coefficients:
##
                    sma1
                            sma2
             ma1
##
         -0.4391 0.2986 0.4526
                 0.0793 0.0850
##
          0.0759
##
## sigma^2 estimated as 854.8: log likelihood=-802.26
## AIC=1612.52
                 AICc=1612.77
                                BIC=1624.99
```

### Actual vs. Fitted Containers Exported



```
fc_ARIMA.auto <- ARIMA.auto %>%
  forecast(h = 24)

fc_ARIMA.auto %>%
  autoplot(train.tb)
```



#### accuracy(fc\_ARIMA.auto, exports.tb)

```
##Mape 11.3##
```

##exponential smoothing model##

##The ETS model I would first try would be a model with an additive linear trend with seasonalit y##

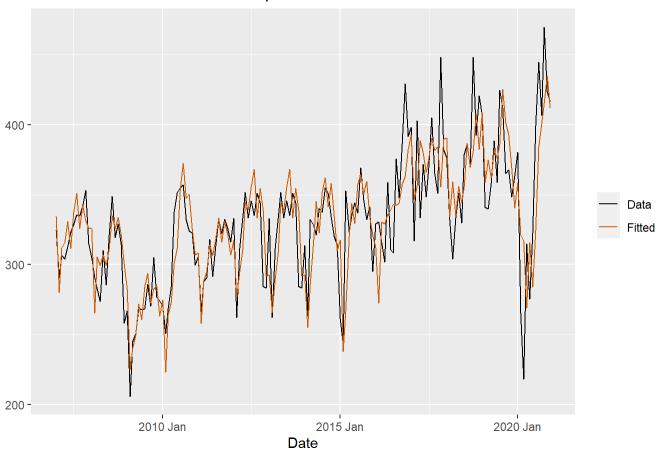
ets\_manual1 <- train.tb %>% model(ETS(Exports ~ error("A") + trend("A") + season("A")))
report(ets\_manual1)

```
## Series: Exports
## Model: ETS(A,A,A)
##
     Smoothing parameters:
##
       alpha = 0.5482453
##
       beta = 0.0001000069
##
       gamma = 0.0001100631
##
##
     Initial states:
##
        1[0]
                  b[0]
                            s[0]
                                    s[-1] s[-2]
                                                     s[-3]
                                                              s[-4]
                                                                        s[-5]
##
    332.9468 0.5518572 -4.040492 13.54669 24.187 13.42605 30.61627 12.91895
##
                 s[-7]
                           s[-8]
                                      s[-9]
                                               s[-10]
                                                         s[-11]
##
    -6.102845 3.922654 -17.30098 -23.21312 -48.79914 0.8389554
##
##
     sigma^2: 807.623
##
##
        AIC
                AICc
                          BIC
## 2002.620 2006.700 2055.727
```

```
##AIC 2002.62
ets_manual2 <- train.tb %>% model(ETS(Exports ~ error("A") + trend("A") + season("M")))
report(ets_manual2)
```

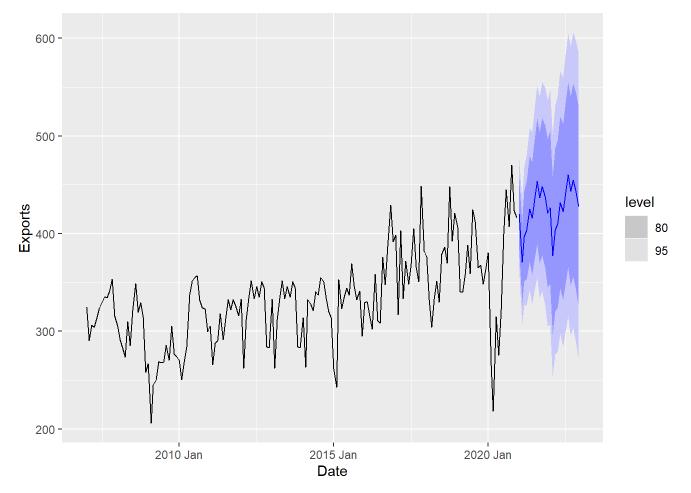
```
## Series: Exports
## Model: ETS(A,A,M)
##
     Smoothing parameters:
##
       alpha = 0.4474613
       beta = 0.0001000051
##
##
       gamma = 0.1698272
##
##
     Initial states:
##
        1[0]
                  b[0]
                            s[0]
                                    s[-1]
                                            s[-2]
                                                      s[-3]
                                                               s[-4]
                                                                        s[-5]
##
    331.6285 0.5417158 0.9611465 1.011077 1.04821 1.037531 1.055291 1.062521
##
                s[-7]
                          s[-8]
                                    s[-9]
                                              s[-10]
                                                        s[-11]
##
    1.016476 1.041335 0.9808745 0.9844664 0.8599736 0.9410976
##
##
     sigma^2: 910.8587
##
##
        AIC
                AICc
                          BIC
## 2022.829 2026.909 2075.936
```

## Actual vs. Fitted Containers Exported



```
fc_ets_manual1 <- ets_manual1 %>%
  forecast(h = 24)

fc_ets_manual1 %>%
  autoplot(train.tb)
```



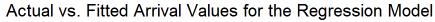
```
accuracy(fc_ets_manual1, exports.tb)
```

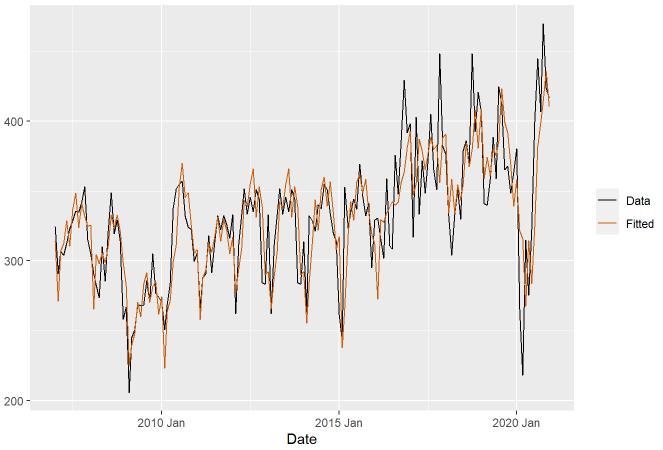
```
##Mape 9.75##

##Auto ETS##

ets_auto <- train.tb %>% model(ETS(Exports))
report(ets_auto)
```

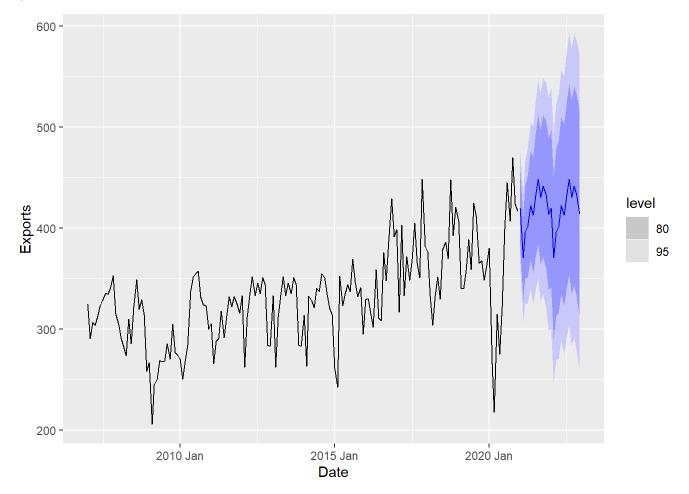
```
## Series: Exports
## Model: ETS(A,N,A)
##
     Smoothing parameters:
##
       alpha = 0.550009
##
       gamma = 0.0001000379
##
    Initial states:
##
##
       1[0]
                 s[0]
                         s[-1]
                                  s[-2]
                                         s[-3]
                                                    s[-4]
                                                             s[-5]
                                                                        s[-6]
##
   313.051 -4.749498 13.93889 23.21871 12.14124 29.94124 13.66059 -5.491295
##
                                    s[-10]
                 s[-8]
                           s[-9]
                                             s[-11]
   3.895073 -17.10702 -22.65474 -47.82946 1.036267
##
##
##
    sigma^2: 799.458
##
##
        AIC
                AICc
                          BIC
## 1999.109 2002.267 2045.968
```





```
fc_ets_auto <- ets_auto %>%
  forecast(h = 24)

fc_ets_auto %>%
  autoplot(train.tb)
```

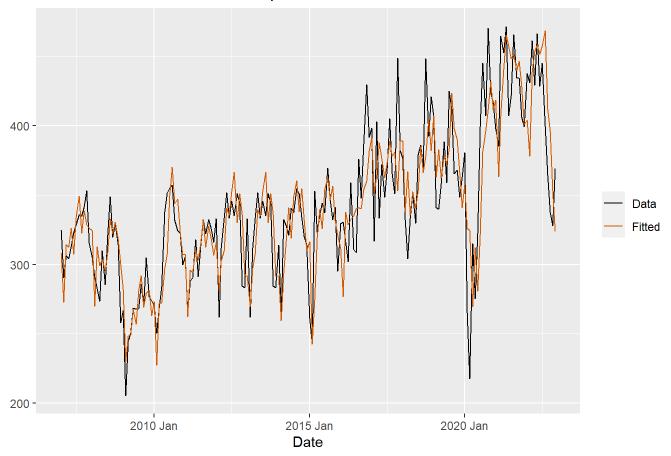


#### accuracy(fc\_ets\_auto, exports.tb)

```
##Mape 9.40##
##Ensemble##
##Predictive accuracy of your five models in cross-validation##
all.models.fit <- train.tb %>%
  model(train.tb_lm = TSLM(Exports ~ trend() + season()),
        ARIMA3.fit = ARIMA(Exports \sim 1 + pdq(0,1,0) + PDQ(1,0,1)),
        ARIMA.auto = ARIMA(Exports),
        ets_manual1 = ETS(Exports ~ error("A") + trend("A") + season("A")),
        ets_auto = ETS(Exports),
        combination = combination_model(ARIMA(Exports \sim 1 + pdq(0,1,0) + PDQ(1,0,1)),
                                        ARIMA(Exports),
                                        TSLM(Exports ~ trend() + season()),
                                        ETS(Exports ~ error("A") + trend("A") + season("A")),
                                        ETS(Exports),
                                         cmbn_args = list(weights = "equal")))
all.models.pred <- all.models.fit %>% forecast(h = 24)
all.models.pred %>% accuracy(exports.tb) %>% arrange(MAPE, decreasing = TRUE)
```

```
## # A tibble: 6 × 10
##
     .model
                .type
                          ME RMSE
                                    MAE
                                           MPE MAPE MASE RMSSE ACF1
##
    <chr>>
                <chr>
                       <dbl> <
## 1 ets auto
               Test
                      -0.437 47.2 37.6 -1.16
                                                9.40 1.22 1.16 0.757
                      -7.27
                              50.2 38.3 -2.86 9.75 1.25 1.23 0.777
## 2 ets_manual1 Test
## 3 combination Test
                       3.89
                              53.0 41.7 -0.249 10.4 1.36 1.30 0.753
## 4 ARIMA.auto Test -10.3
                              60.9 44.3 -3.87 11.3 1.44 1.49 0.704
## 5 ARIMA3.fit Test
                       0.223 59.4 46.3 -1.25 11.5
                                                     1.50 1.45 0.723
## 6 train.tb_lm Test
                      37.3
                              62.2 54.7 7.89 13.0 1.78 1.52 0.776
```

# Actual vs. Fitted Containers Exported



```
fc_ets_auto_full <- ets_auto_full %>%
  forecast(h = 24)

fc_ets_auto_full %>%
  autoplot(exports.tb)
```

