

Declarative Semantics Definition

Term Rewriting

Guido Wachsmuth

Assessment

last lecture

Assessment

last lecture

What are the plagues of non-declarative syntax definitions?

Assessment

last lecture

What are the plagues of non-declarative syntax definitions?

- grammar classes

Assessment

last lecture

What are the plagues of non-declarative syntax definitions?

- grammar classes
- disambiguation

Assessment

last lecture

What are the plagues of non-declarative syntax definitions?

- grammar classes
- disambiguation
- lexical syntax

Assessment

last lecture

What are the plagues of non-declarative syntax definitions?

- grammar classes
- disambiguation
- lexical syntax
- tree construction

Assessment

last lecture

What are the plagues of non-declarative syntax definitions?

- grammar classes
- disambiguation
- lexical syntax
- tree construction
- evolution

Assessment

last lecture

What are the plagues of non-declarative syntax definitions?

- grammar classes
- disambiguation
- lexical syntax
- tree construction
- evolution
- composition

Assessment

last lecture

What are the plagues of non-declarative syntax definitions?

- grammar classes
- disambiguation
- lexical syntax
- tree construction
- evolution
- composition
- restriction to parsers

Overview today's lecture

manual implementation

- static analysis & error checking
- code generation
- semantic editor services

domain-specific language

- Stratego
- transform ASTs
- working on ATerms
- declarative style

I

overview

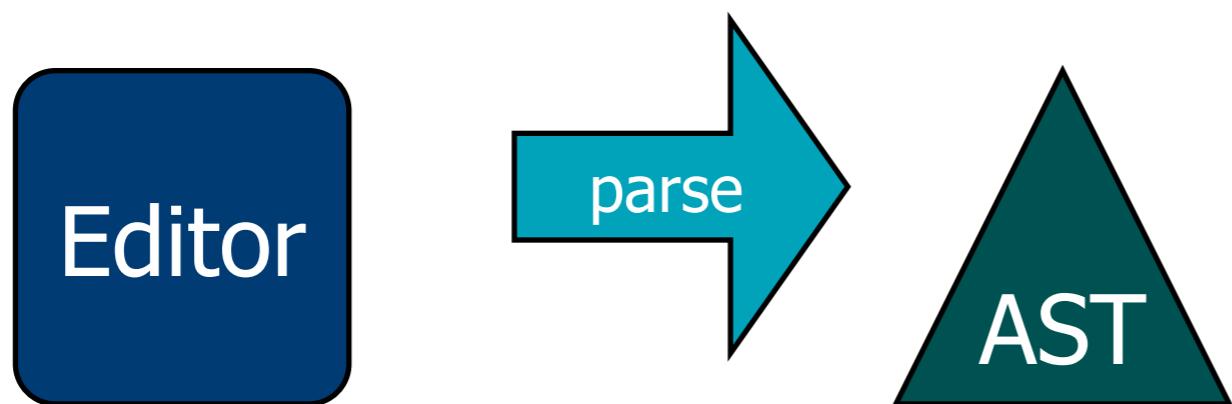
Modern Compilers in IDEs

architecture

Editor

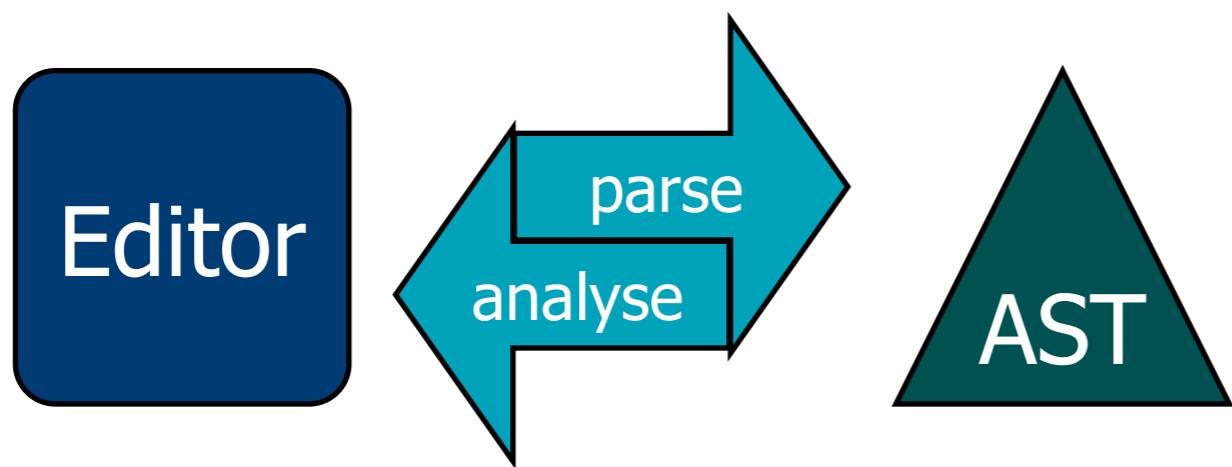
Modern Compilers in IDEs

architecture



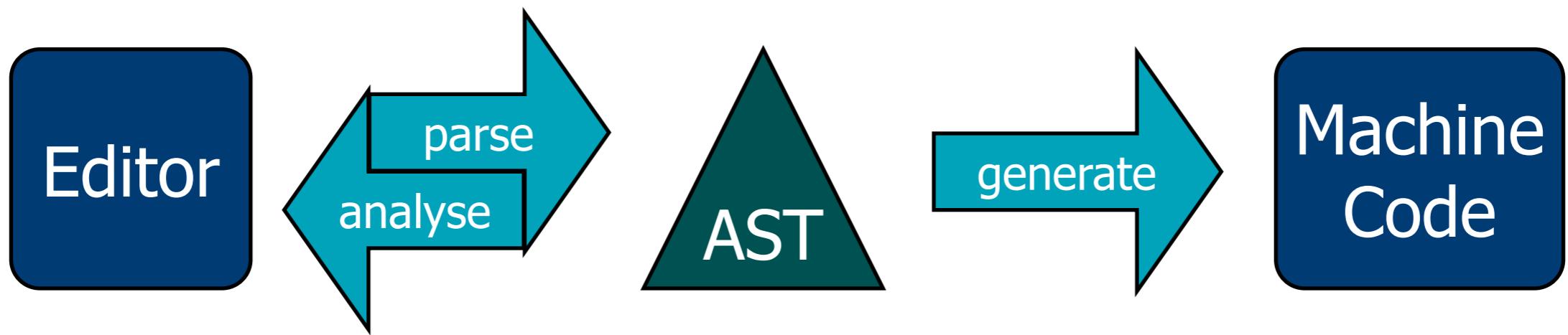
Modern Compilers in IDEs

architecture



Modern Compilers in IDEs

architecture



Recap: Compiler Construction strategies

Recap: Compiler Construction strategies

manual implementation

- general-purpose language, particular implementation techniques
- domain-specific language, domain = language processing

Recap: Compiler Construction strategies

manual implementation

- general-purpose language, particular implementation techniques
- domain-specific language, domain = language processing

generation + generation

- input: language definition
- output: implementation in general-purpose language

Recap: Compiler Construction strategies

manual implementation

- general-purpose language, particular implementation techniques
- domain-specific language, domain = language processing

generation + generation

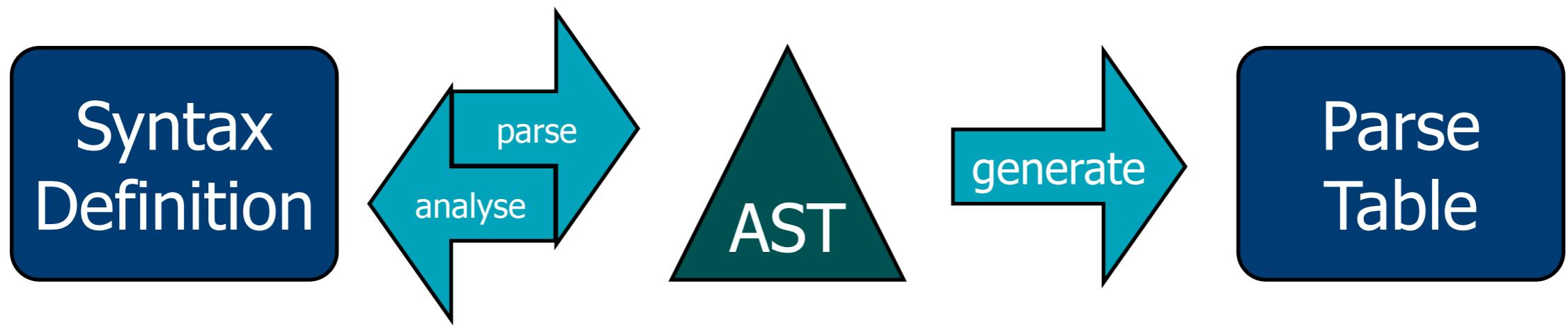
- input: language definition
- output: implementation in general-purpose language

generation + interpretation

- virtual machine for language processing
- input: language definition
- output: “machine code”

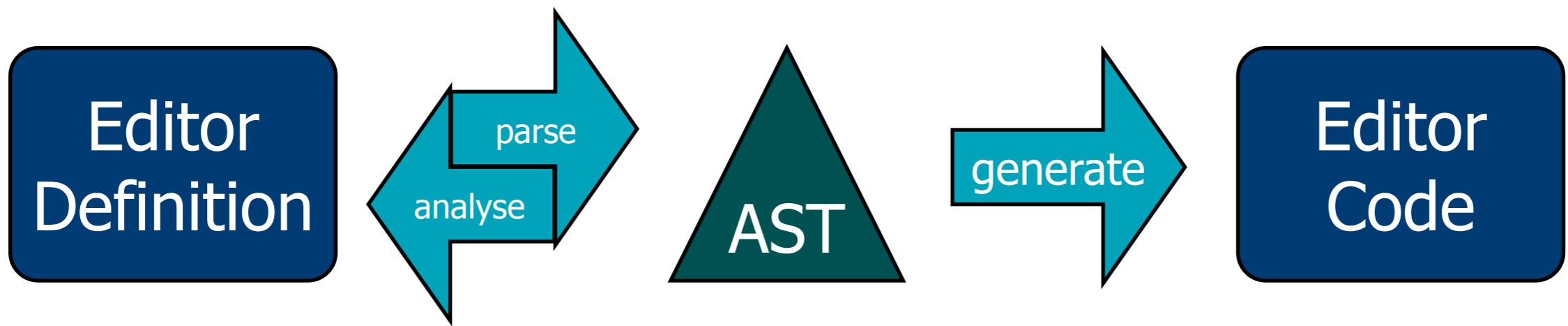
Spoofax Language Workbench

generation + interpretation



Spoofax Language Workbench

generation + generation



Spoofax Language Workbench

manual implementation

Stratego

- declarative DSL
- domain: program transformation
- means to manipulate ASTs
- working on ATerms
- compiles to C or Java

Stratego in Spooftax

- static analysis & error checking
- code generation
- semantic editor services



Stratego concepts

signatures

rewrite rules

- transform term to term
- left-hand side
 - pattern matching & variable binding
- right-hand side
 - pattern instantiation & variable substitution

rewrite strategies

- algorithm for applying rewrite rules



Stratego example

module desugar

imports

include/Tiger
operators

strategies

desugar-all = innermost(desugar)

rules

desugar: IfThen(e1, e2) -> IfThenElse(e1, e2, NoVal())

II

signatures

Signatures

context-free syntax

```
"-" Exp      -> Exp {cons("Uminus")}  
Exp "+" Exp -> Exp {cons("Plus")}  
Exp "-" Exp -> Exp {cons("Minus")}  
Exp "*" Exp -> Exp {cons("Times")}  
Exp "/" Exp -> Exp {cons("Divide")}  
  
Exp "=" Exp -> Exp {cons("Eq")}  
Exp "<>" Exp -> Exp {cons("Neq")}  
Exp ">" Exp -> Exp {cons("Gt")}  
Exp "<" Exp -> Exp {cons("Lt")}  
Exp ">=" Exp -> Exp {cons("Geq")}  
Exp "<=" Exp -> Exp {cons("Leq")}  
  
Exp "&" Exp -> Exp {cons("And")}  
Exp "!" Exp -> Exp {cons("Or")}
```

signature

constructors

```
Uminus : Exp      -> Exp  
Plus   : Exp * Exp -> Exp  
Minus  : Exp * Exp -> Exp  
Times  : Exp * Exp -> Exp  
Divide : Exp * Exp -> Exp  
  
Eq     : Exp * Exp -> Exp  
Neq   : Exp * Exp -> Exp  
Gt    : Exp * Exp -> Exp  
Lt    : Exp * Exp -> Exp  
Geq   : Exp * Exp -> Exp  
Leq   : Exp * Exp -> Exp  
  
And   : Exp * Exp -> Exp  
Or    : Exp * Exp -> Exp
```

ATerms in Stratego signature

signature

constructors

Constructor	:	Cons	->	Term
Application	:	Cons * List(Term)	->	Term
List	:	List(Term)	->	Term
Tuple	:	List(Term)	->	Term

signature

constructors

Nil	:	->	List(a)	
Cons	:	a * List(a)	->	List(a)
Conc	:	List(a) * List(a)	->	List(a)

III

rewrite rules

Desugaring

```
if x then  
  printint(x)
```

```
if x then  
  printint(x)  
else  
  ()
```

Desugaring

```
if x then  
    printint(x)
```

```
if x then  
    printint(x)  
else  
    ()
```

```
IfThen(  
    Var("x")  
, Call(  
        "printint"  
, [Var("x")])  
)  
)
```

```
IfThenElse(  
    Var("x")  
, Call(  
        "printint"  
, [Var("x")])  
)  
, NoVal()  
)
```

Desugaring

```
if x then  
    printint(x)
```

```
if x then  
    printint(x)  
else  
    ()
```

```
IfThen(  
    Var("x")  
, Call(  
        "printint"  
, [Var("x")])  
)  
)
```

```
IfThenElse(  
    Var("x")  
, Call(  
        "printint"  
, [Var("x")])  
)  
, NoVal())  
)
```

```
desugar: IfThen(e1, e2) -> IfThenElse(e1, e2, NoVal())
```

Desugaring

```
if x then  
  printint(x)
```

```
if x then  
  printint(x)  
else  
  ()
```

```
IfThen(  
  Var("x")  
, Call(  
    "printint"  
, [Var("x")])  
)  
)
```

pattern matching

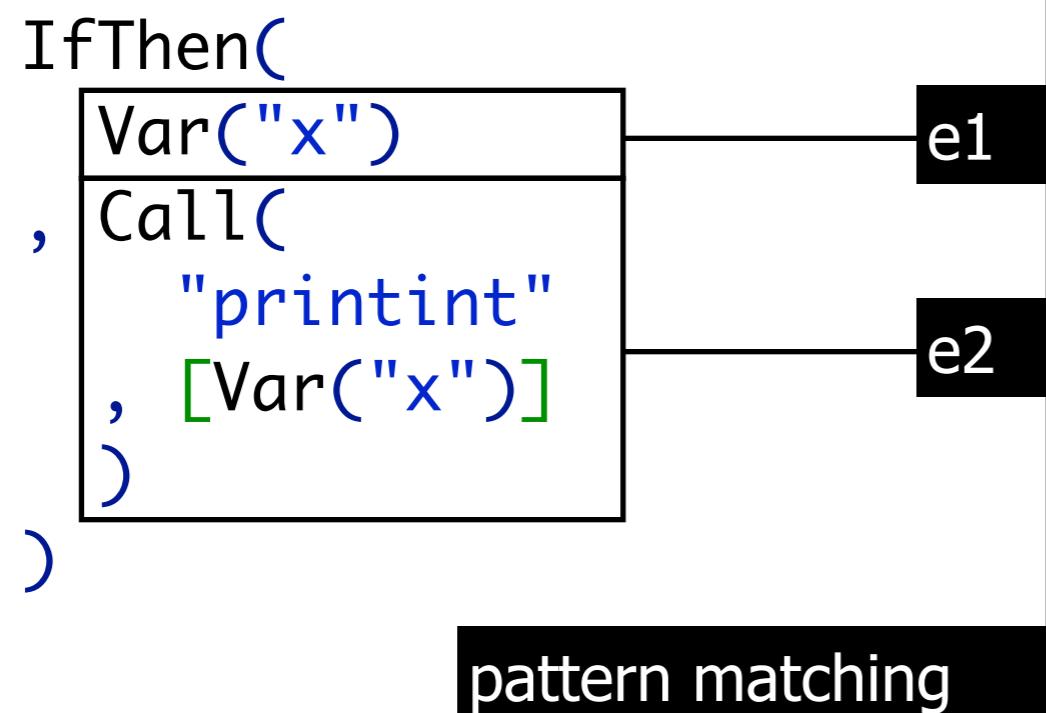
```
IfThenElse(  
  Var("x")  
, Call(  
    "printint"  
, [Var("x")])  
)  
, NoVal()  
)
```

```
desugar: IfThen(e1, e2) -> IfThenElse(e1, e2, NoVal())
```

Desugaring

```
if x then  
  printint(x)
```

```
if x then  
  printint(x)  
else  
  ()
```



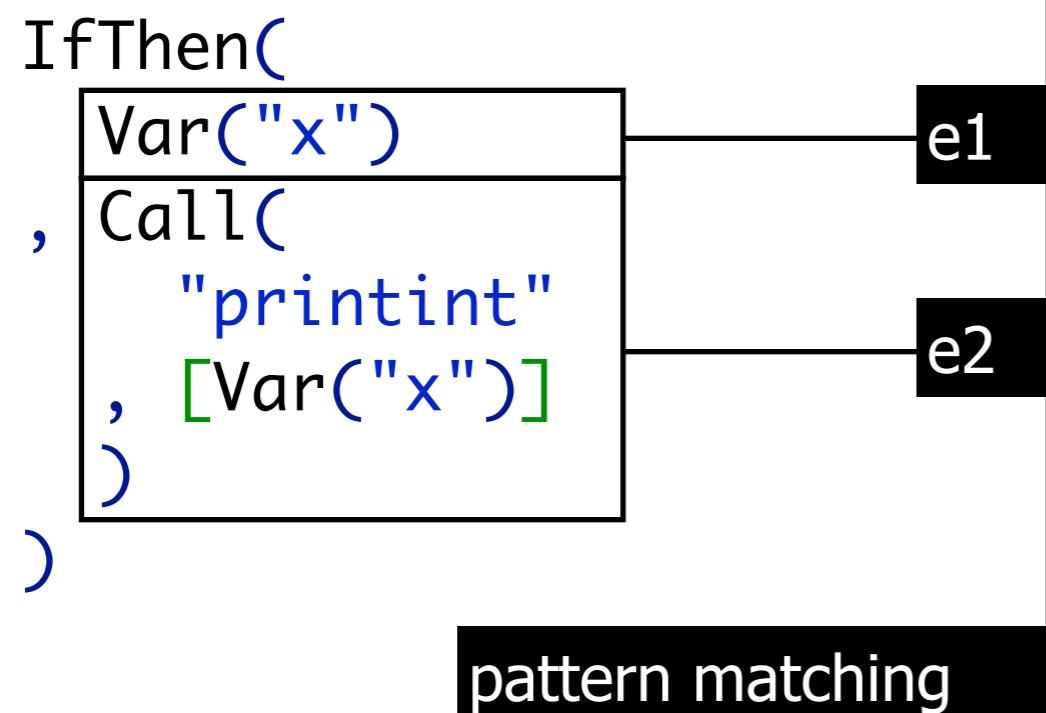
```
IfThenElse(  
  Var("x")  
, Call(  
    "printint"  
, [Var("x")])  
, NoVal())  
)
```

```
desugar: IfThen(e1, e2) -> IfThenElse(e1, e2, NoVal())
```

Desugaring

```
if x then  
  printint(x)
```

```
if x then  
  printint(x)  
else  
  ()
```



IfThenElse(

```
  Var("x")  
, Call(  
  "printint"  
, [Var("x")])  
)  
, NoVal()  
)
```

pattern instantiation

```
desugar: IfThen(e1, e2) -> IfThenElse(e1, e2, NoVal())
```

Desugaring

```
if x then  
  printint(x)
```

```
if x then  
  printint(x)  
else  
  ()
```

IfThen(

```
  Var("x")  
, Call(  
    "printint"  
, [Var("x")])  
)
```

e1

e2

pattern matching

IfThenElse(

```
  Var("x")  
, Call(  
    "printint"  
, [Var("x")])  
, NoVal()  
)
```

pattern instantiation

```
desugar: IfThen(e1, e2) -> IfThenElse(e1, e2, NoVal())
```

More Desugaring

```
desugar: Uminus(e)      -> Bop(MINUS(), Int("0"), e)
```

```
desugar: Plus(e1, e2)   -> Bop(PLUS(), e1, e2)
desugar: Minus(e1, e2)  -> Bop(MINUS(), e1, e2)
desugar: Times(e1, e2)  -> Bop(MUL(), e1, e2)
desugar: Divide(e1, e2) -> Bop(DIV(), e1, e2)
```

```
desugar: Eq(e1, e2)     -> Rop(EQ(), e1, e2)
desugar: Neq(e1, e2)    -> Rop(NE(), e1, e2)
desugar: Leq(e1, e2)    -> Rop(LE(), e1, e2)
desugar: Lt(e1, e2)     -> Rop(LT(), e1, e2)
desugar: Geq(e1, e2)    -> Rop(LE(), e2, e1)
desugar: Gt(e1, e2)     -> Rop(LT(), e2, e1)
```

```
desugar: And(e1, e2)   -> IfThenElse(e1, e2, Int("0"))
desugar: Or(e1, e2)     -> IfThenElse(e1, Int("1"), e2)
```

signature constructors

```
PLUS: BinOp
MINUS: BinOp
MUL: BinOp
DIV: BinOp
```

```
EQ: RelOp
NE: RelOp
LE: RelOp
LT: RelOp
```

```
Bop: BinOp * Expr * Expr -> Expr
Rop: RelOp * Expr * Expr -> Expr
```

Constant Folding

```
x := 21 + 21 + x
```

```
x := 42 + x
```

Constant Folding

```
x := 21 + 21 + x
```

```
x := 42 + x
```

```
Assign(  
    Var("x")  
, Plus(  
        Plus(  
            Int("21")  
, Int("21"))  
, Var("x"))  
)
```

```
Assign(  
    Var("x")  
, Plus(  
        Int("42")  
, Var("x"))  
)
```

Constant Folding

```
x := 21 + 21 + x
```

```
x := 42 + x
```

```
Assign(  
    Var("x")  
, Plus(  
        Plus(  
            Int("21")  
, Int("21"))  
, Var("x"))  
)
```

```
Assign(  
    Var("x")  
, Plus(  
        Int("42")  
, Var("x"))  
)
```

```
eval: Bop(PLUS(), Int(i1), Int(i2)) -> Int(i3)  
      where <addS> (i1, i2) => i3
```

More Constant Folding

```
eval: Bop(PLUS(), Int(i1), Int(i2)) -> Int(<addS> (i1, i2))

eval: Bop(MINUS(), Int(i1), Int(i2)) -> Int(<subtS> (i1, i2))

eval: Bop(MUL(), Int(i1), Int(i2)) -> Int(<mulS> (i1, i2))

eval: Bop(DIV(), Int(i1), Int(i2)) -> Int(<divS> (i1, i2))

eval: Rop(EQ(), Int(i), Int(i)) -> Int("1")
eval: Rop(EQ(), Int(i1), Int(i2)) -> Int("0") where not( <eq> (i1, i2) )

eval: Rop(NE(), Int(i), Int(i)) -> Int("0")
eval: Rop(NE(), Int(i1), Int(i2)) -> Int("1") where not( <eq> (i1, i2) )

eval: Rop(LT(), Int(i1), Int(i2)) -> Int("1") where <ltS> (i1, i2)
eval: Rop(LT(), Int(i1), Int(i2)) -> Int("0") where not( <ltS> (i1, i2) )

eval: Rop(LE(), Int(i1), Int(i2)) -> Int("1") where <leqS> (i1, i2)
eval: Rop(LE(), Int(i1), Int(i2)) -> Int("0") where not( <leqS> (i1, i2))
```

Rewrite Rules

parameters

$f(x,y|a,b)$: lhs \rightarrow rhs

- strategy or rule parameters x, y
- term parameters a, b
- no matching

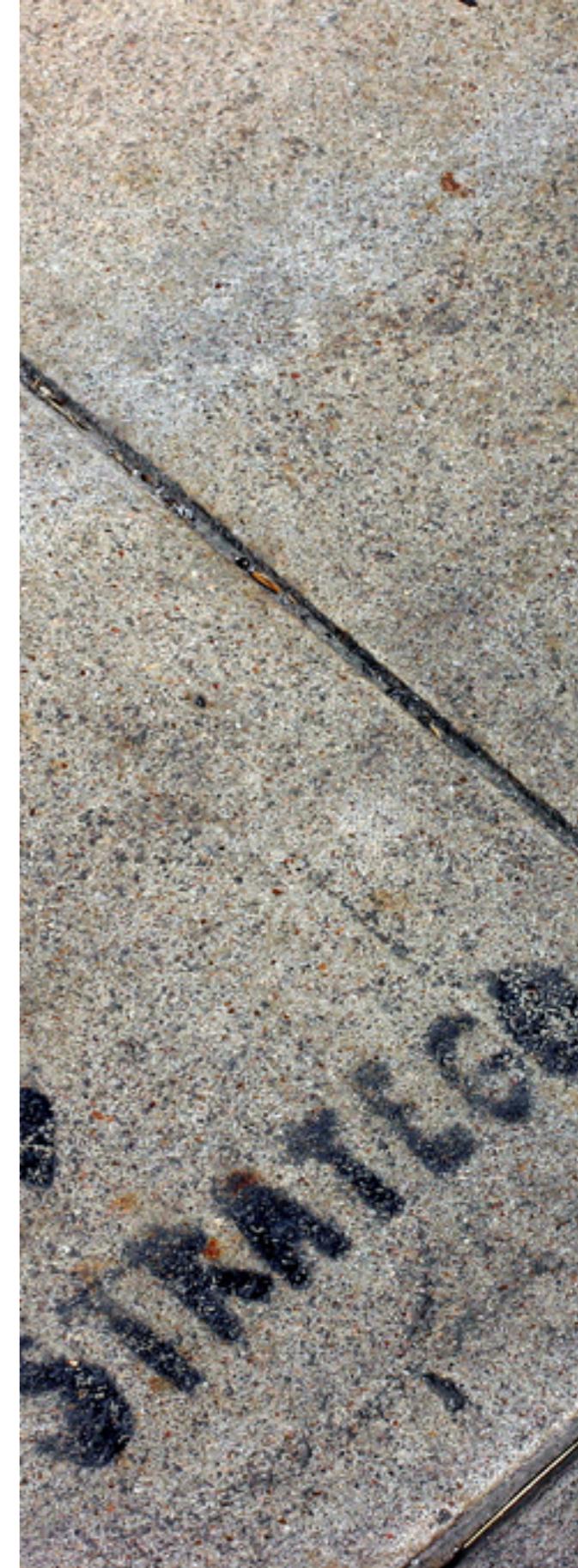
$f(|a,b)$: lhs \rightarrow rhs

- optional strategy parameters

$f(x,y)$: lhs \rightarrow rhs

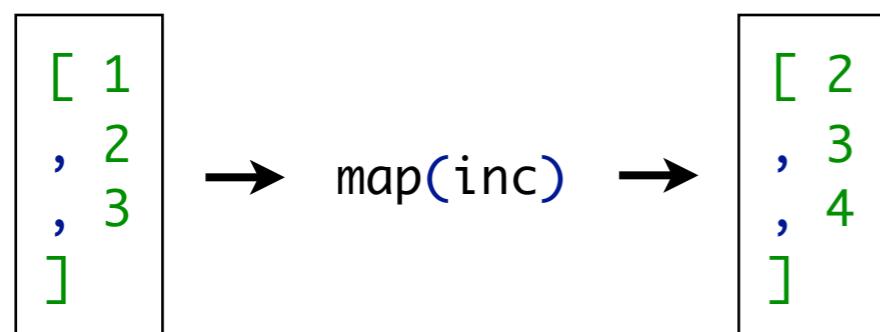
- optional term parameters

f : lhs \rightarrow rhs



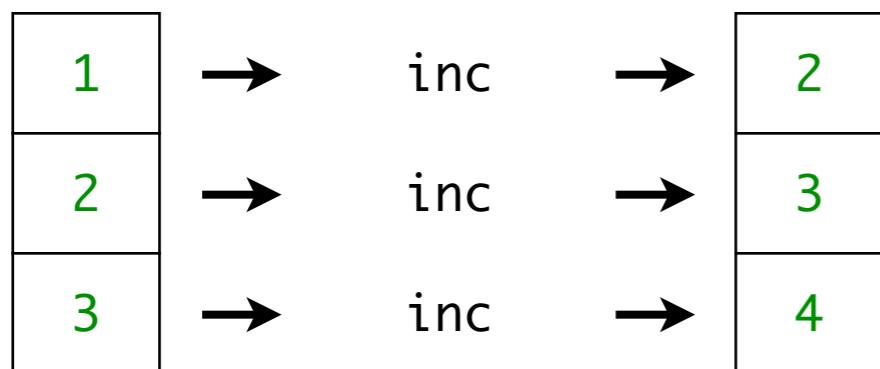
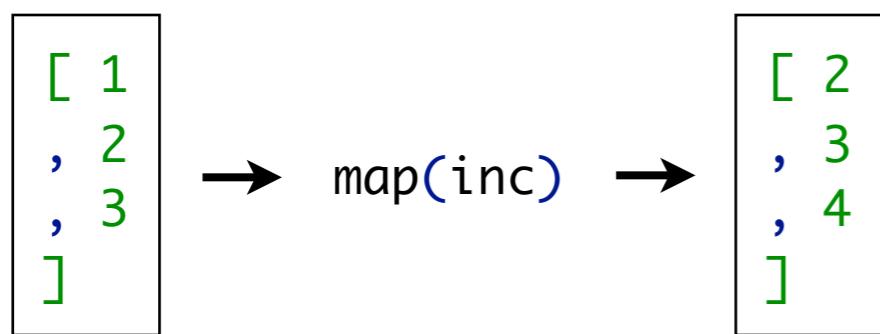
Rules with Parameters

example: map



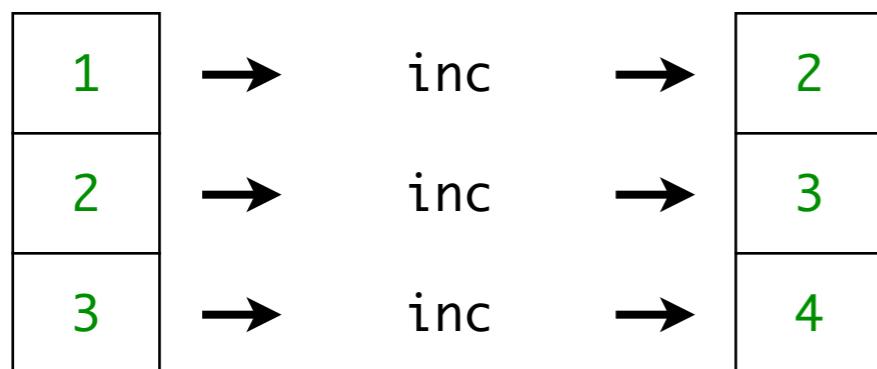
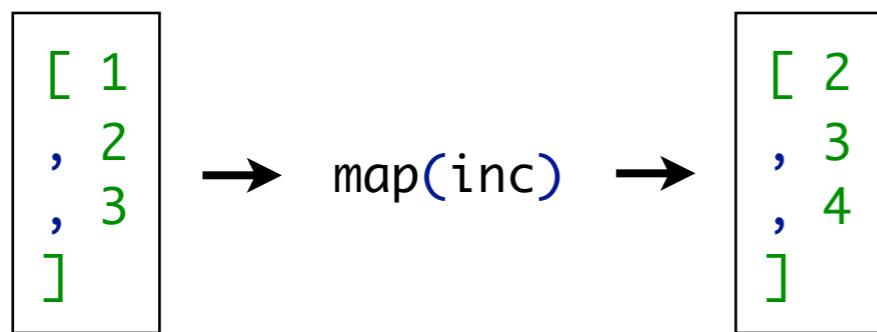
Rules with Parameters

example: map



Rules with Parameters

example: map

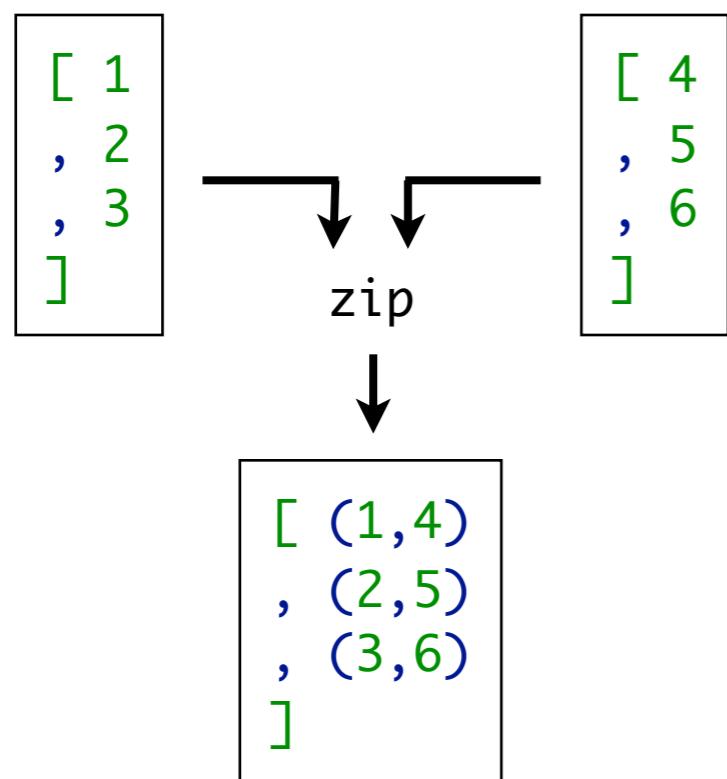


`map(s): [] -> []`
`map(s): [x|xs] -> [<s> x | <map(s)> xs]`



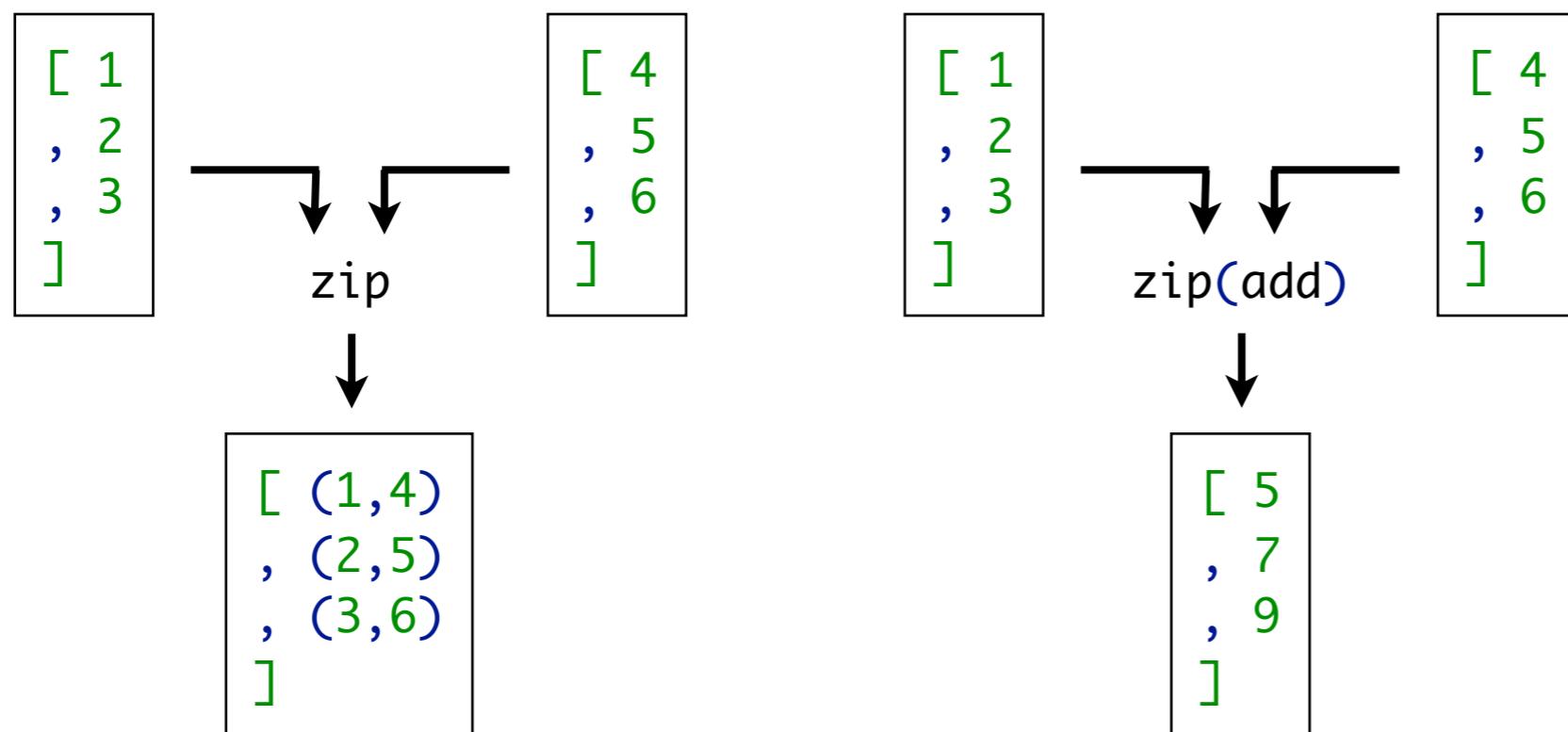
Rules with Parameters

example: zip



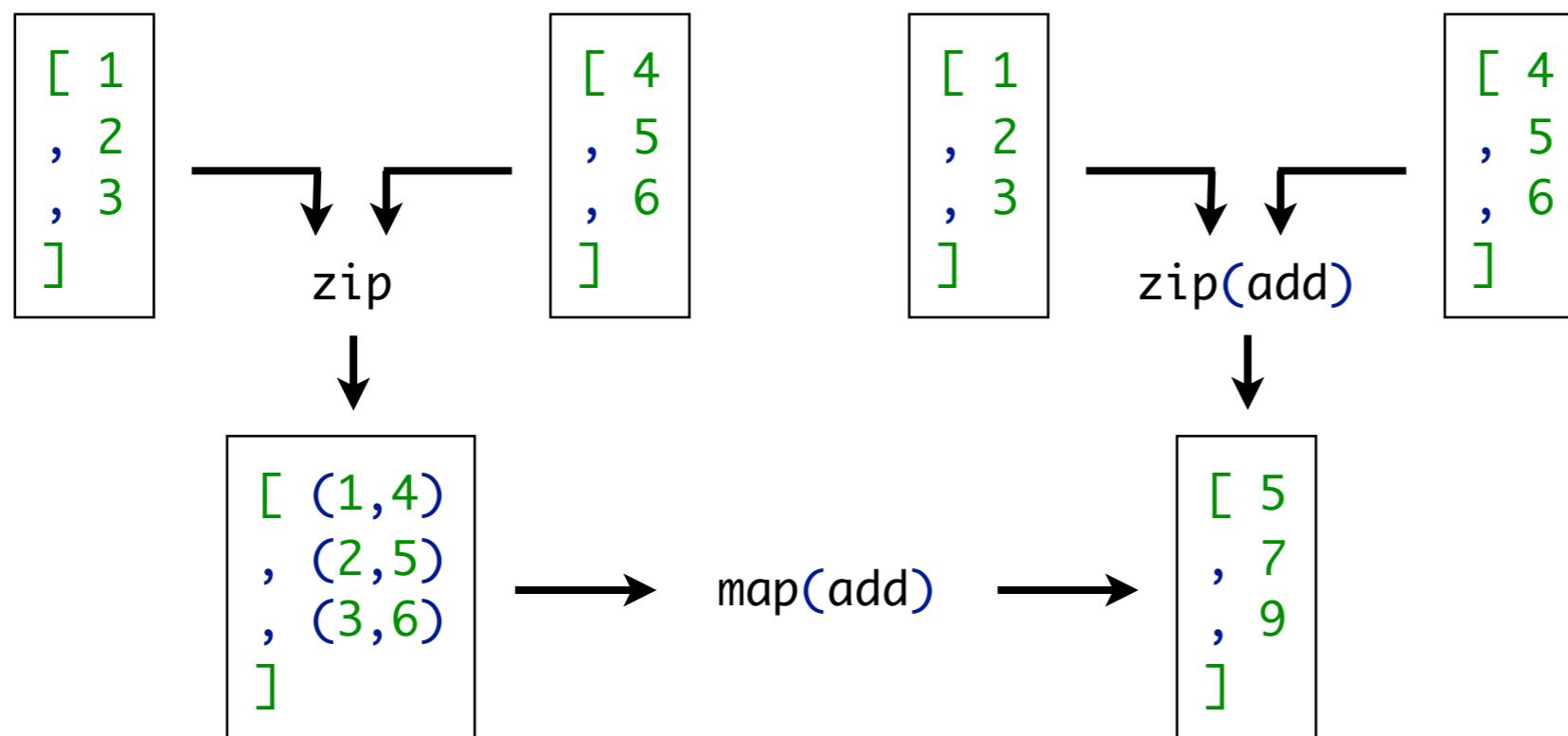
Rules with Parameters

example: zip



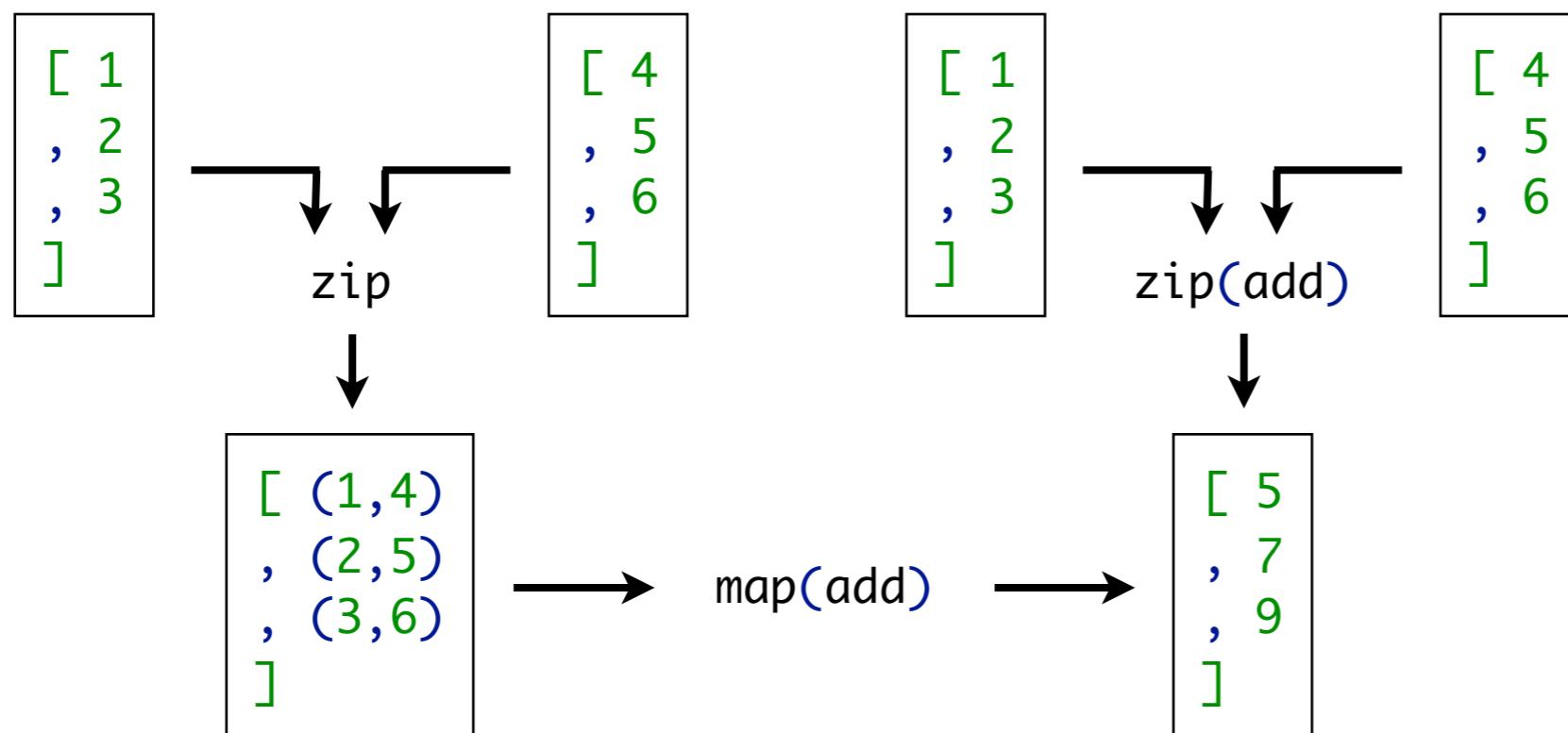
Rules with Parameters

example: zip



Rules with Parameters

example: zip



`zip(s): ([] , []) → []`

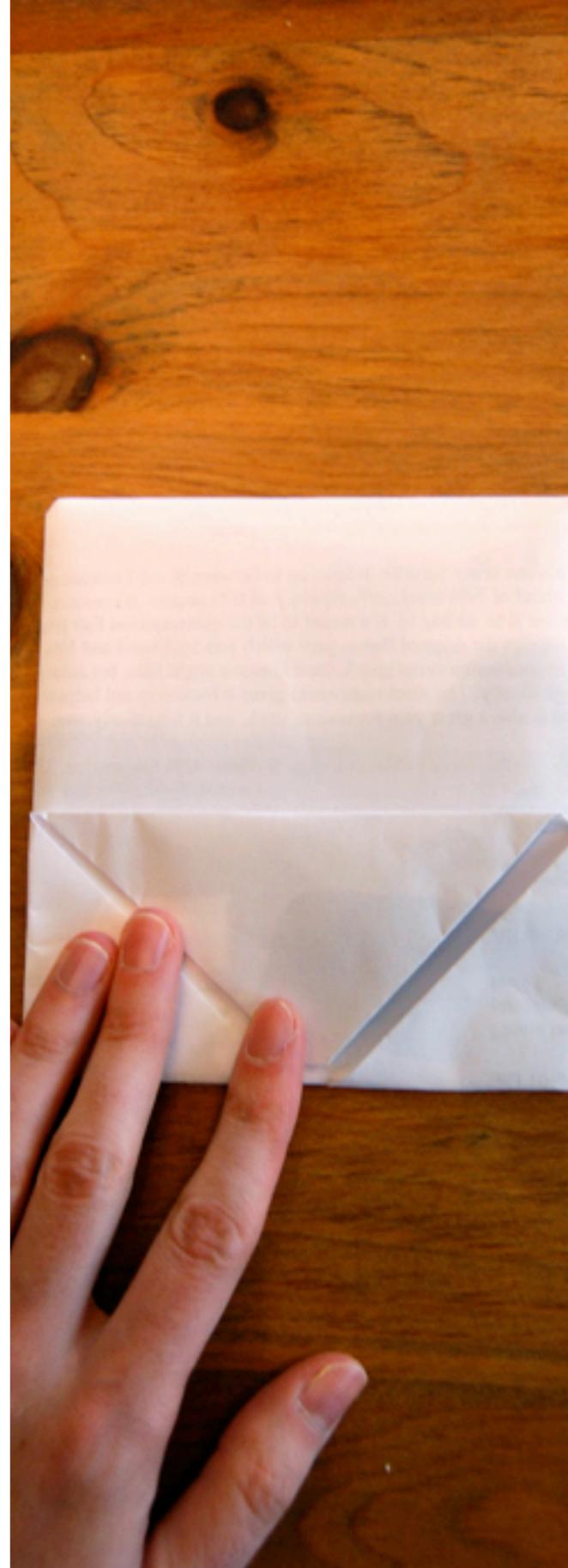
`zip(s): ([x|xs] , [y|ys]) → [<s> (x,y) | <zip(s)> (xs,ys)]`

`zip = zip(id)`

Rules with Parameters

example: fold

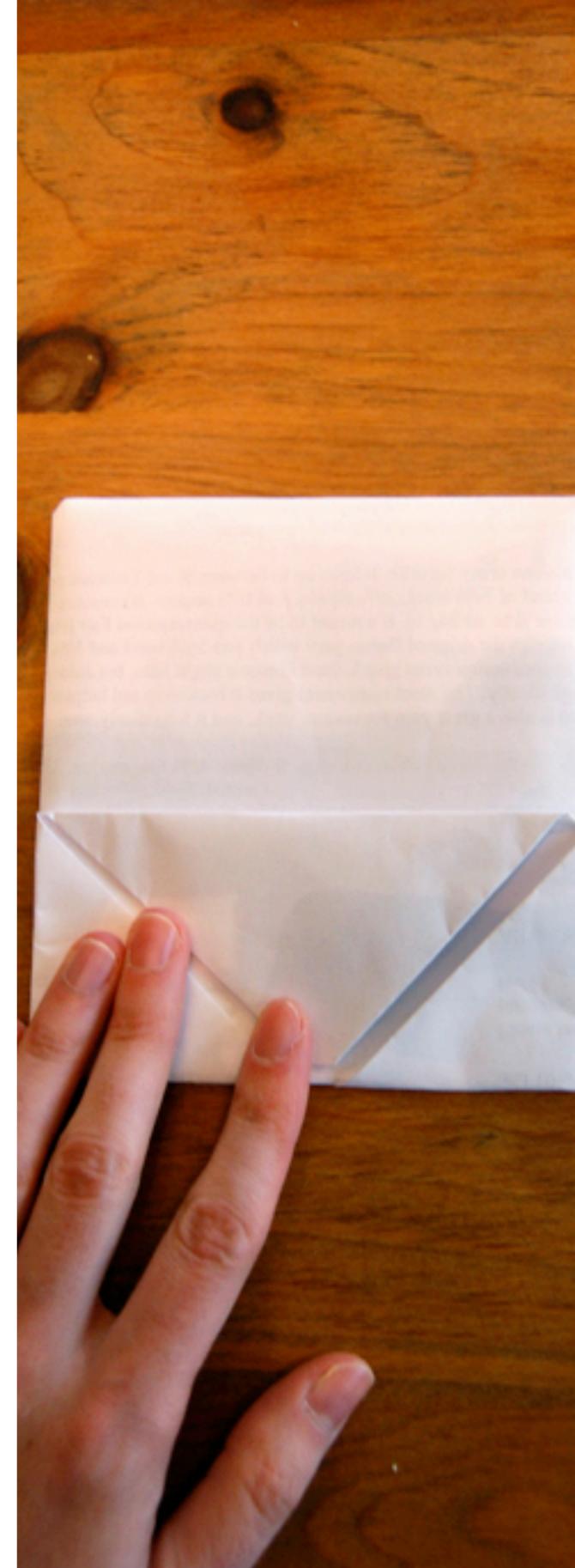
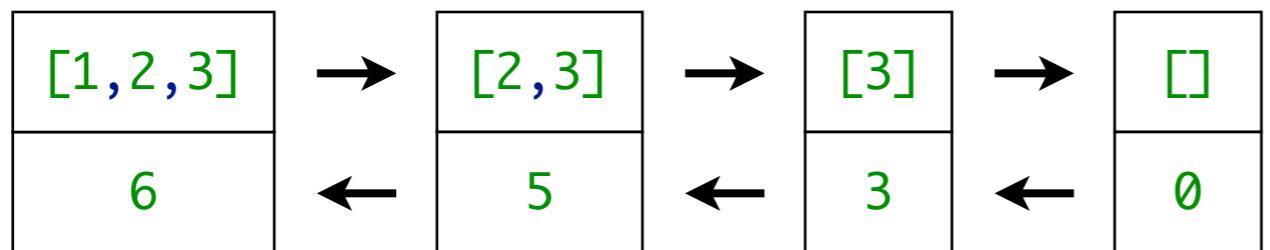
```
[1,2,3] → foldr(!0,add) → 6
```



Rules with Parameters

example: fold

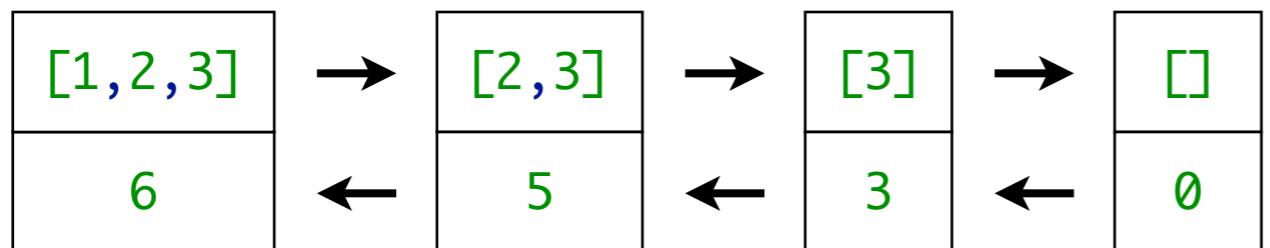
$[1,2,3] \rightarrow \text{foldr}(!0, \text{add}) \rightarrow 6$



Rules with Parameters

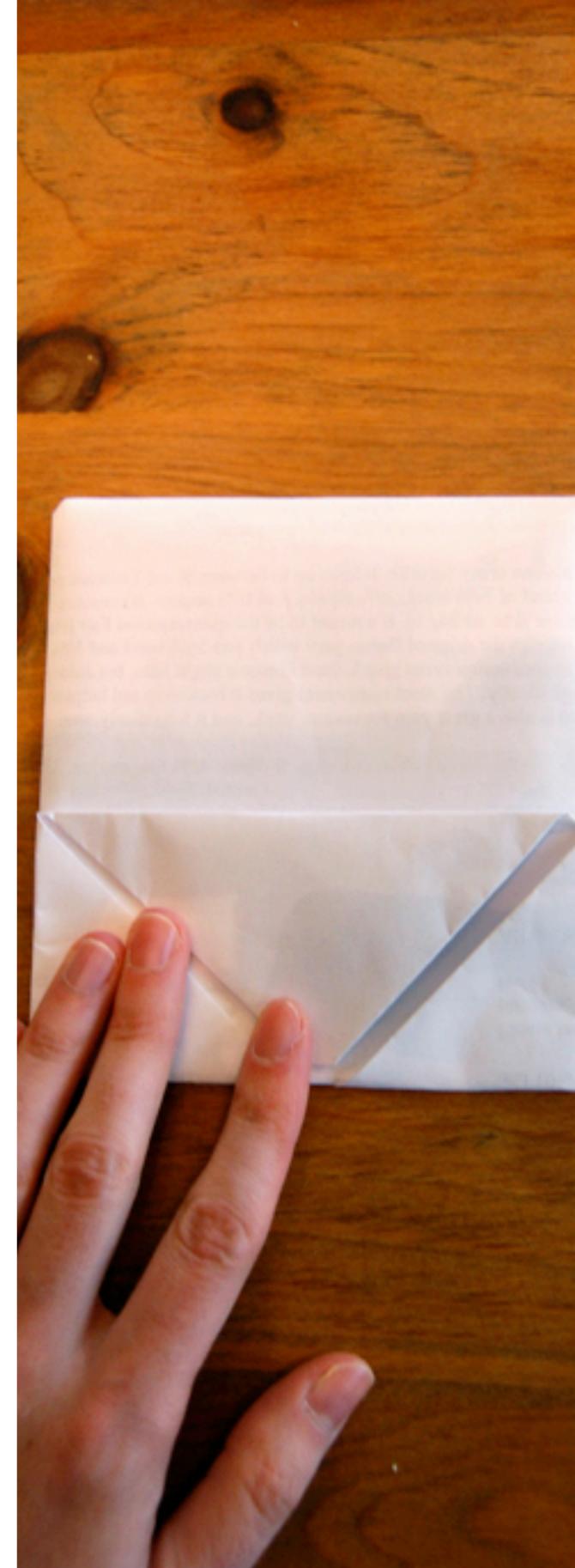
example: fold

$$\boxed{[1,2,3]} \rightarrow \text{foldr}(!0, \text{add}) \rightarrow \boxed{6}$$



`foldr(s1,s2): [] -> <s1>`

`foldr(s1,s2): [x|xs] -> <s2> (x,<foldr(s1,s2)> xs)`



Rules with Parameters

example: inverse

$$\boxed{[1, 2, 3]} \rightarrow \text{inverse}(\boxed{1}) \rightarrow \boxed{[3, 2, 1]}$$



Rules with Parameters

example: inverse

$$\boxed{[1, 2, 3]} \rightarrow \text{inverse}(\square) \rightarrow \boxed{[3, 2, 1]}$$

$$\begin{array}{c} \boxed{[1, 2, 3]} \\ \hline \square \end{array} \rightarrow \begin{array}{c} \boxed{[2, 3]} \\ \hline [1] \end{array} \rightarrow \begin{array}{c} \boxed{[3]} \\ \hline [2, 1] \end{array} \rightarrow \begin{array}{c} \square \\ \hline \end{array} \rightarrow \boxed{[3, 2, 1]}$$



Rules with Parameters

example: inverse

$$\boxed{[1,2,3]} \rightarrow \text{inverse}(\boxed{\square}) \rightarrow \boxed{[3,2,1]}$$

$$\begin{array}{c} \boxed{[1,2,3]} \\ \hline \boxed{\square} \end{array} \rightarrow \begin{array}{c} \boxed{[2,3]} \\ \hline \boxed{[1]} \end{array} \rightarrow \begin{array}{c} \boxed{[3]} \\ \hline \boxed{[2,1]} \end{array} \rightarrow \begin{array}{c} \boxed{\square} \\ \hline \boxed{[3,2,1]} \end{array}$$

`inverse(λ is): $\square \rightarrow \text{is}$`

`inverse(λ is): $[x|xs] \rightarrow \langle \text{inverse}(\lambda[x|is]) \rangle xs$`



coffee break



IV

rewrite strategies

Transformation Definitions rules and strategies

rewrite rules

- term to term
- left-hand side matching
- right-hand side instantiation
- conditional
- partial transformation

rewrite strategies

- rule selection
- algorithm
- composition of transformations



Stratego example

module desugar

imports

include/Tiger
operators

strategies

desugar-all = innermost(desugar)

rules

desugar: IfThen(e1, e2) -> IfThenElse(e1, e2, NoVal())

Stratego example

module eval

imports

include/Tiger
operators
desugar

strategies

eval-all = innermost(desugar + eval)

rules

eval: Bop(PLUS(), Int(i1), Int(i2)) -> Int(i3)
where <addS> (i1, i2) => i3

Strategy Combinators

identity

id

Strategy Combinators

identity

`id`

failure

`fail`

Strategy Combinators

identity

`id`

failure

`fail`

sequential composition

`s1 ; s2`

Strategy Combinators

identity

`id`

failure

`fail`

sequential composition

`s1 ; s2`

deterministic choice

`s1 <+ s2`

Strategy Combinators

identity

`id`

failure

`fail`

sequential composition

`s1 ; s2`

deterministic choice

`s1 <+ s2`

non-deterministic choice

`s1 + s2`

Strategy Combinators

identity

`id`

failure

`fail`

sequential composition

`s1 ; s2`

deterministic choice

`s1 <+ s2`

non-deterministic choice

`s1 + s2`

guarded choice

`s1 < s2 + s3`

Strategy Combinators

variables

pattern matching

?t

Strategy Combinators

variables

pattern matching

?t

pattern instantiation

!t

Strategy Combinators

variables

pattern matching

?t

pattern instantiation

!t

strategy application

`<s> t ≡ !t ; s`

Strategy Combinators

variables

pattern matching

?t

pattern instantiation

!t

strategy application

$\langle s \rangle \ t \equiv !t ; s$

result matching

$s \Rightarrow t \equiv s ; ?t$

$\langle s \rangle \ t1 \Rightarrow t2$

$t2 := \langle s \rangle \ t1$

Strategy Combinators

variables

pattern matching

?t

pattern instantiation

!t

strategy application

$\langle s \rangle \ t \equiv !t ; s$

result matching

$s \Rightarrow t \equiv s ; ?t$

$\langle s \rangle \ t1 \Rightarrow t2$

$t2 := \langle s \rangle \ t1$

variable scope

$\{x, y : s\}$

Strategy Combinators

rules and strategies

named rewrite rule

```
l: t1 -> t2 where s ≡ l = ?t1 ; s ; !t2
```

Strategy Combinators

rules and strategies

named rewrite rule

```
l: t1 -> t2 where s ≡ l = ?t1 ; s ; !t2
```

unscoped rewrite rule

```
(t1 -> t2 where s) ≡ ?t1 ; s ; !t2
```

Strategy Combinators

rules and strategies

named rewrite rule

$$l : t1 \rightarrow t2 \text{ where } s \equiv l = ?t1 ; s ; !t2$$

unscoped rewrite rule

$$(t1 \rightarrow t2 \text{ where } s) \equiv ?t1 ; s ; !t2$$

strategy definition

$$f(x,y|a,b) = s$$

Strategy Combinators

examples

```
try(s) = s <+ id
```

```
repeat(s) = try(s ; repeat(s))
```

Strategy Combinators

examples

```
try(s) = s <+ id
```

```
repeat(s) = try(s ; repeat(s))
```

```
topdown(s) = s ; all(topdown(s))
```

Strategy Combinators

examples

```
try(s) = s <+ id
```

```
repeat(s) = try(s ; repeat(s))
```

```
topdown(s) = s ; all(topdown(s))
```

```
alltd(s) = s <+ all(alltd(s))
```

Strategy Combinators

examples

```
try(s) = s <+ id
```

```
repeat(s) = try(s ; repeat(s))
```

```
topdown(s) = s ; all(topdown(s))
```

```
alltd(s) = s <+ all(alltd(s))
```

```
bottomup(s) = all(bottomup(s)) ; s
```

```
innermost(s) = bottomup(try(s ; innermost(s)))
```

```
oncetd(s) = s <+ one(oncetd(s))
```

```
contains(lt) = oncetd(?t)
```

Strategy Combinators

examples

```
try(s) = s <+ id
```

```
repeat(s) = try(s ; repeat(s))
```

```
topdown(s) = s ; all(topdown(s))
```

```
alltd(s) = s <+ all(alltd(s))
```

```
bottomup(s) = all(bottomup(s)) ; s
```

```
innermost(s) = bottomup(try(s ; innermost(s)))
```

```
oncetd(s) = s <+ one(oncetd(s))
```

```
contains(lt) = oncetd(?t)
```

Strategy Combinators

examples

```
try(s) = s <+ id
```

```
repeat(s) = try(s ; repeat(s))
```

```
topdown(s) = s ; all(topdown(s))
```

```
alltd(s) = s <+ all(alltd(s))
```

```
bottomup(s) = all(bottomup(s)) ; s
```

```
innermost(s) = bottomup(try(s ; innermost(s)))
```

```
oncetd(s) = s <+ one(oncetd(s))
```

```
contains(lt) = oncetd(?t)
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Strategy Combinators

examples

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Strategy Combinators

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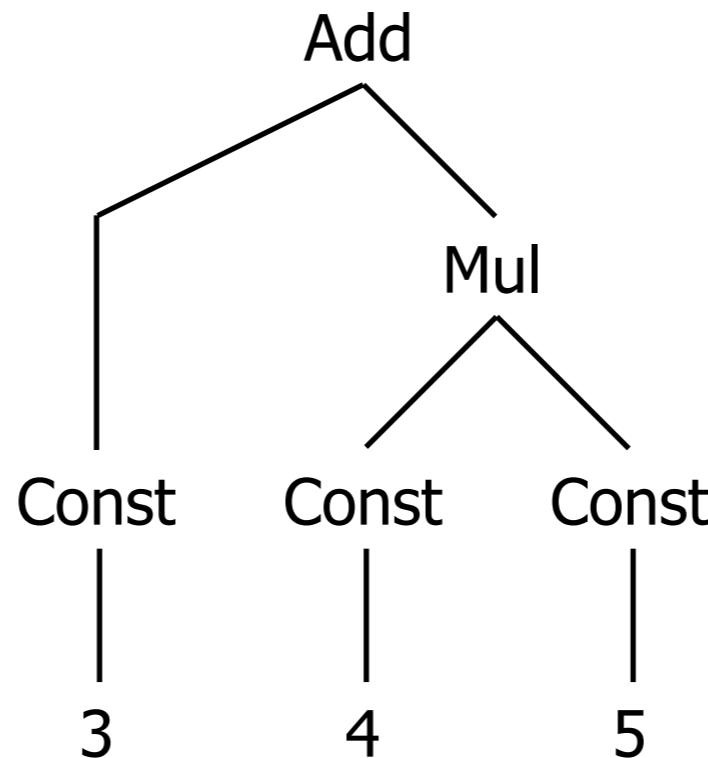
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contains(lt) = oncetd(?t)
```

Stratego example

```
switch: Add(e1, e2) -> Add(e2, e1)
switch: Mul(e1, e2) -> Mul(e2, e1)
```

```
topdown(s) = s ; all(topdown(s))
```

```
topdown(switch)
```

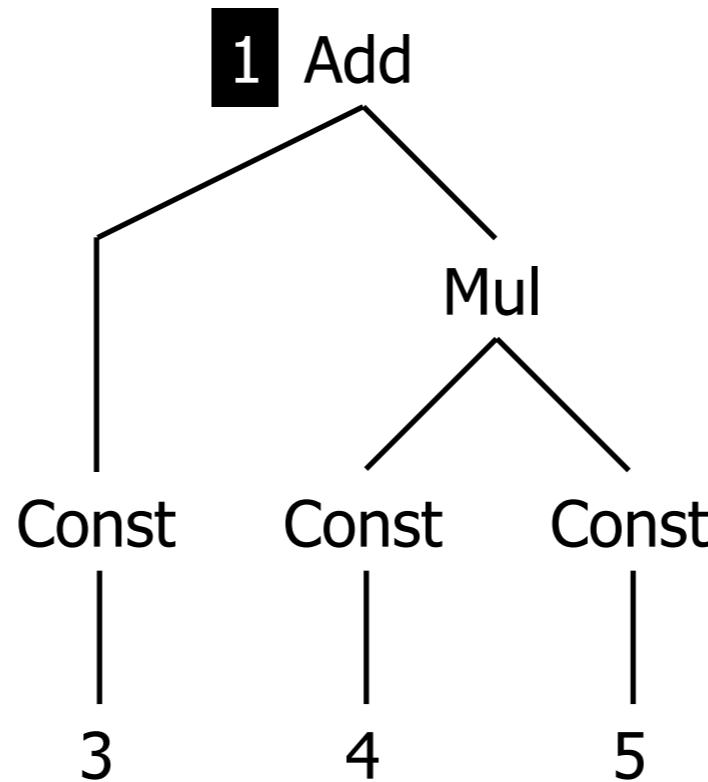


Stratego example

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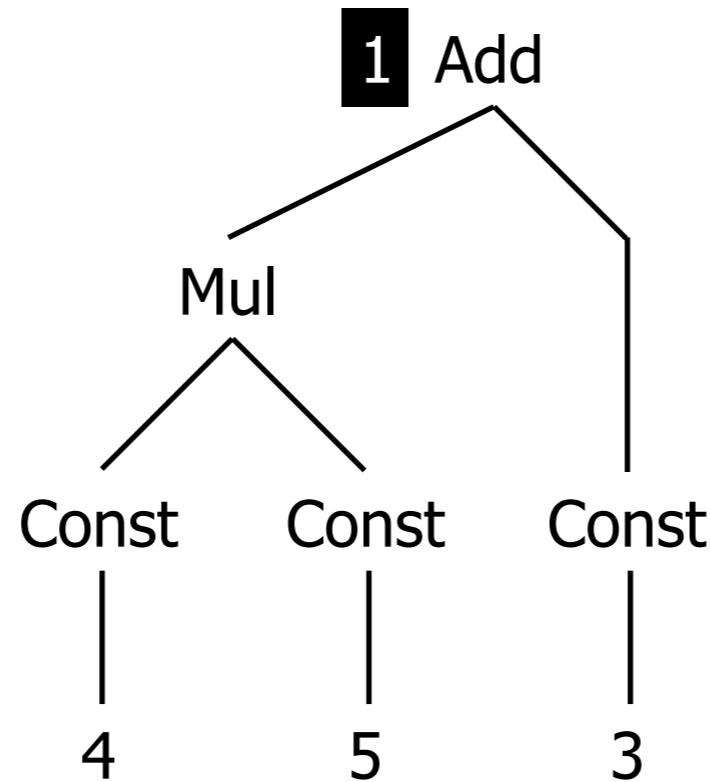


Stratego example

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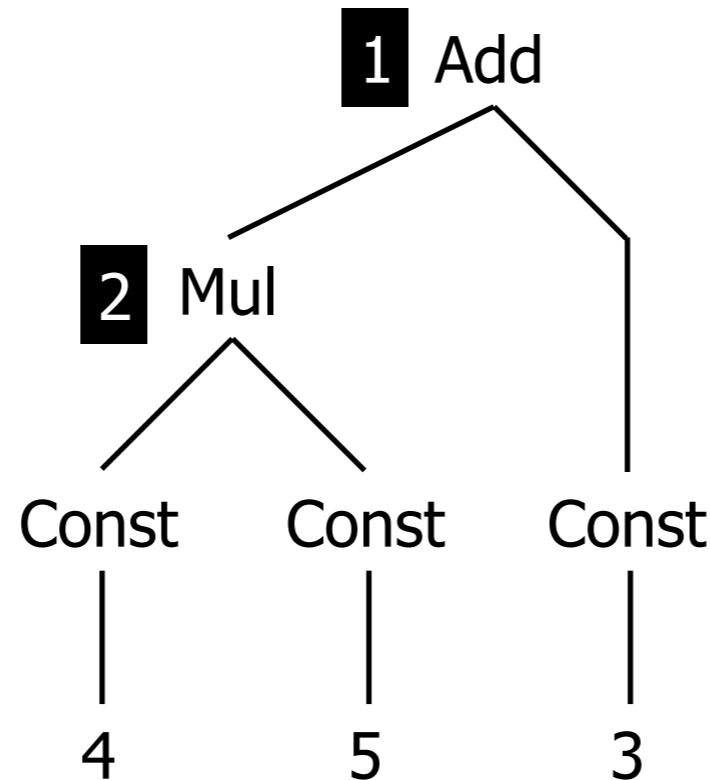


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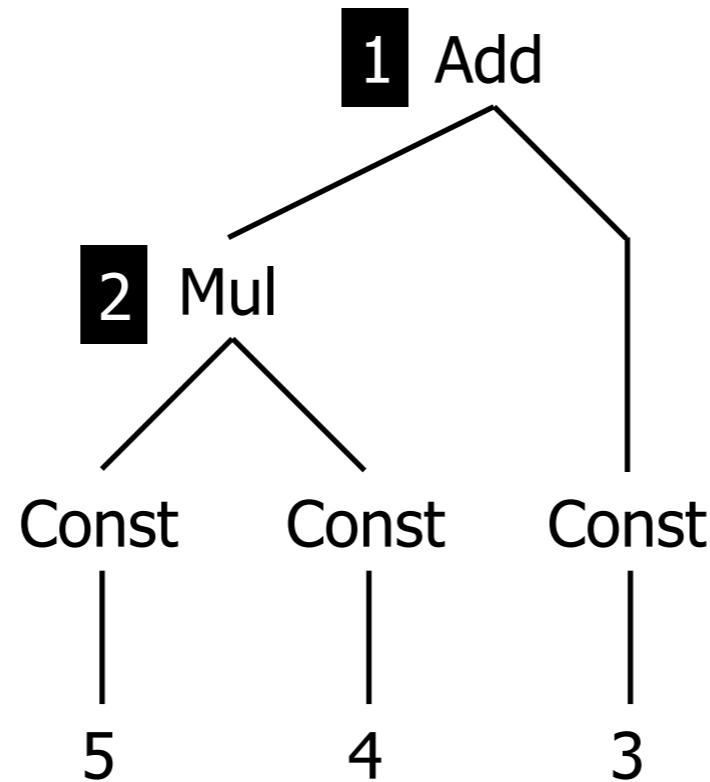


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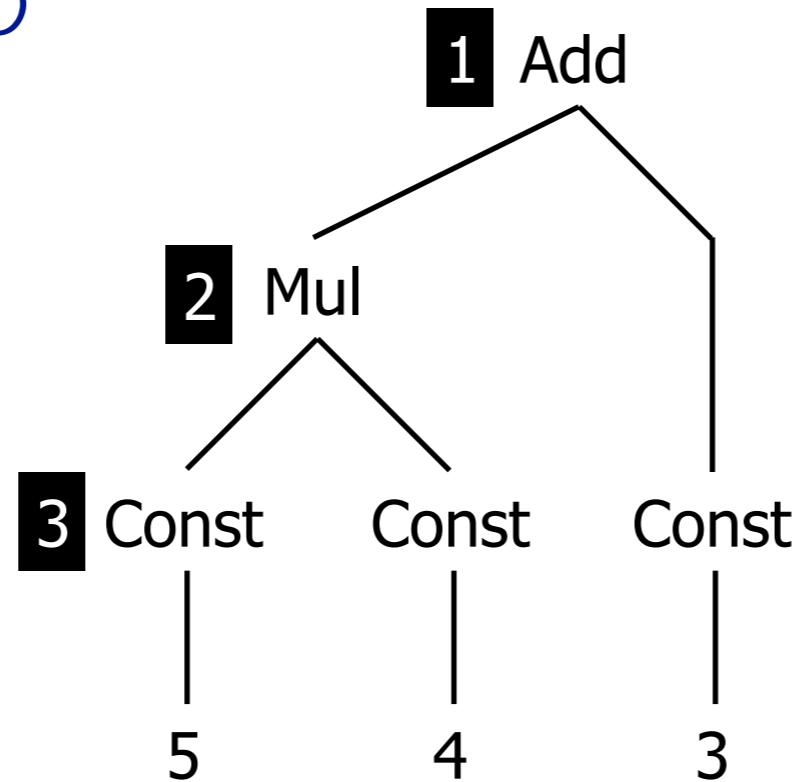


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topdown(switch)
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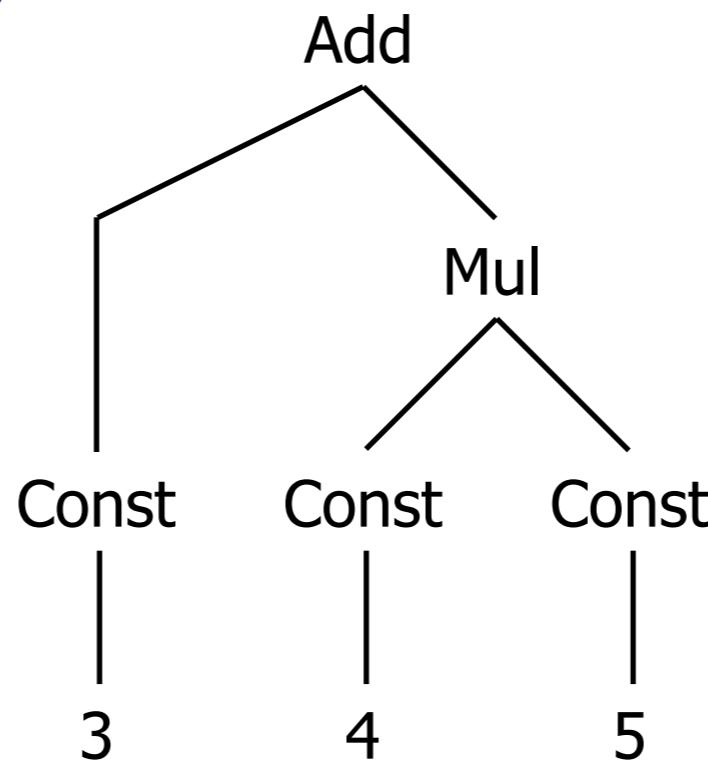


Stratego example

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```
topdown(try(switch))
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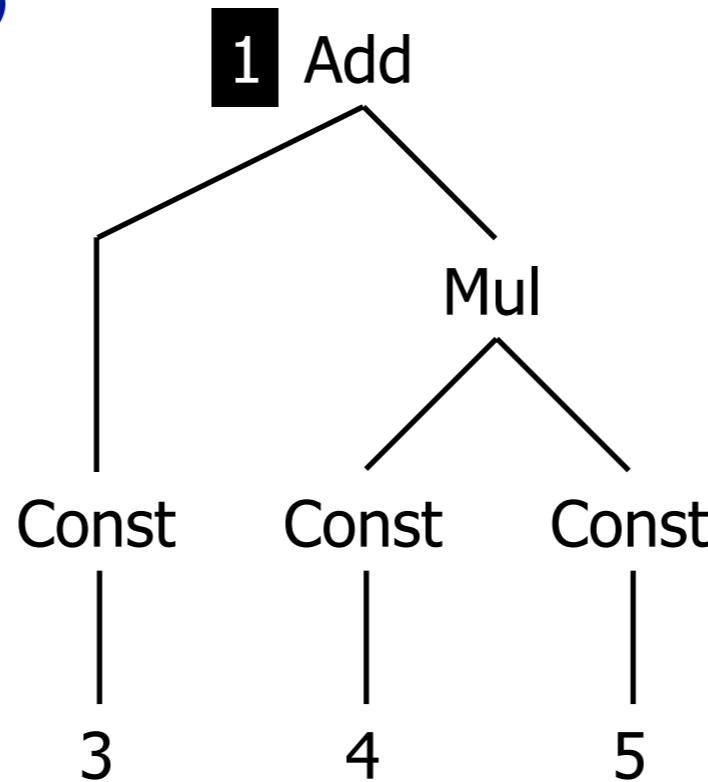


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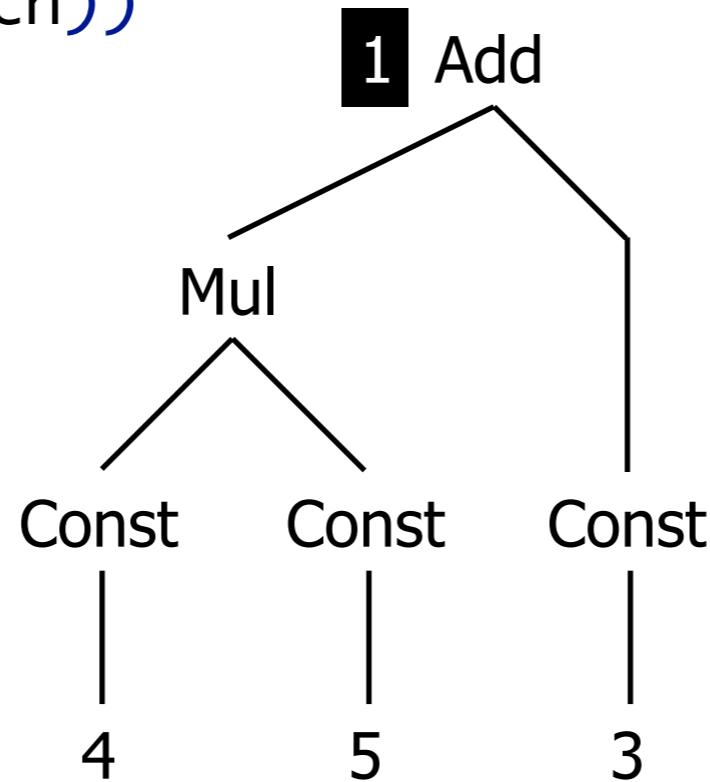


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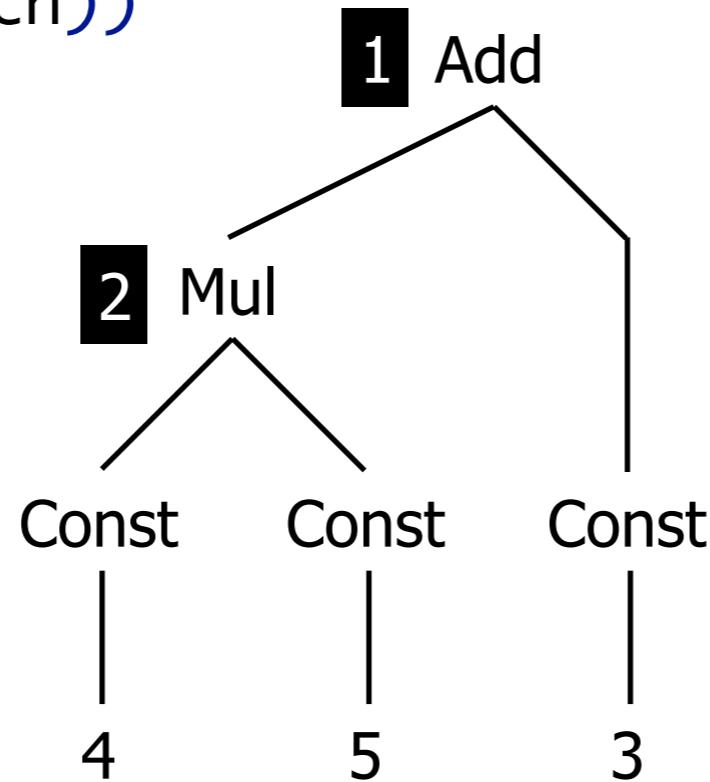


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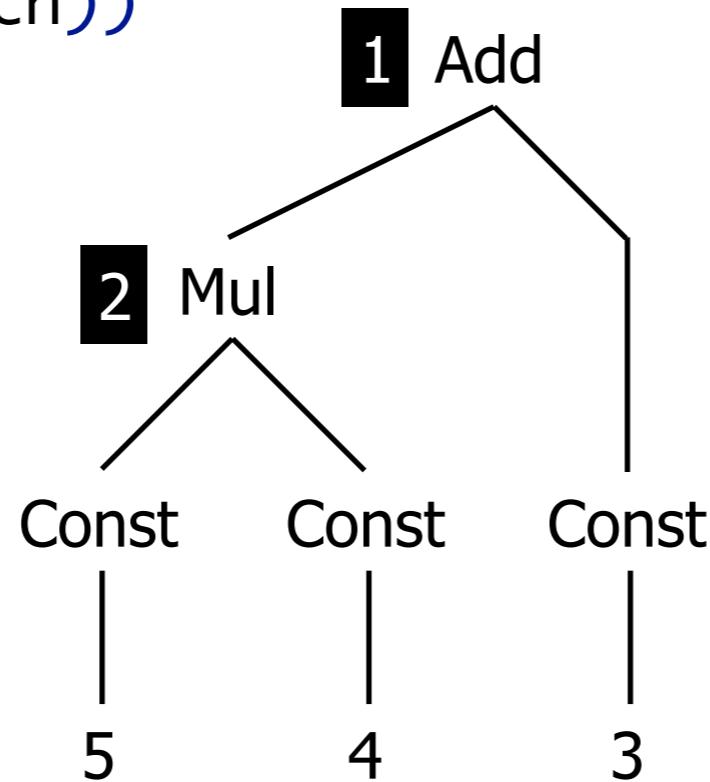


Stratego example

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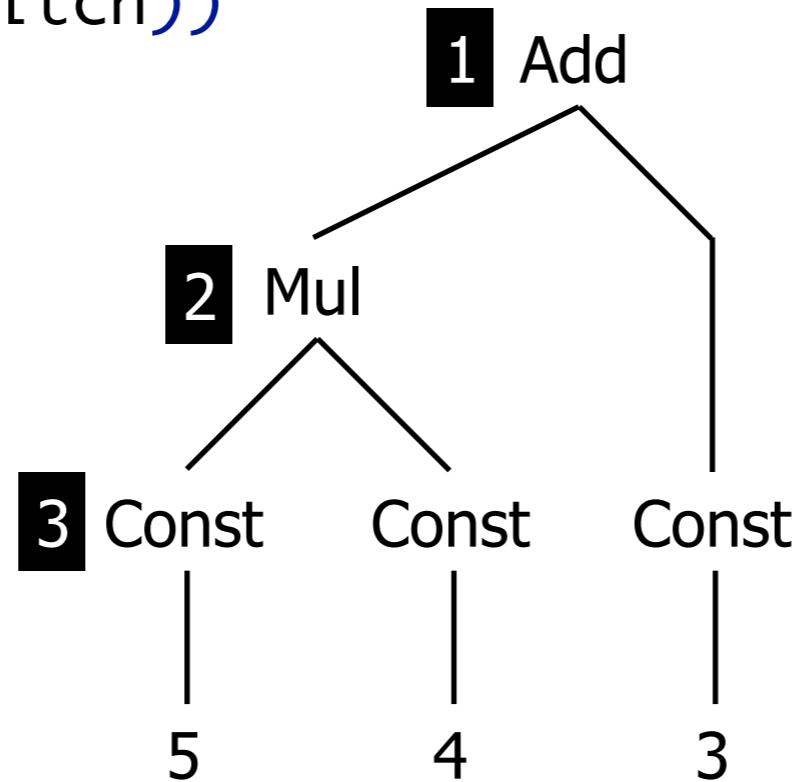


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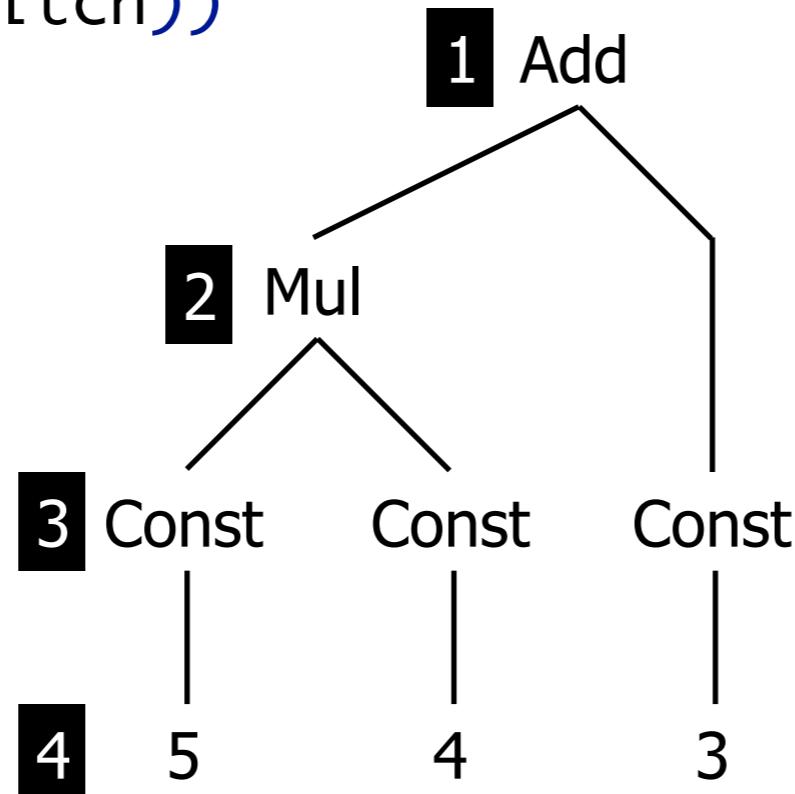


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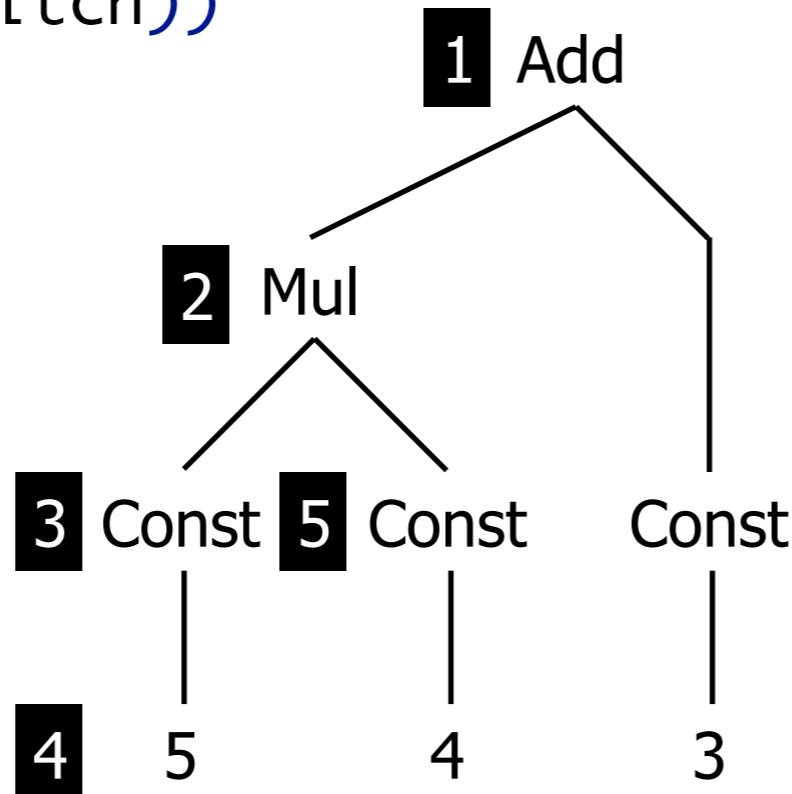


Stratego example

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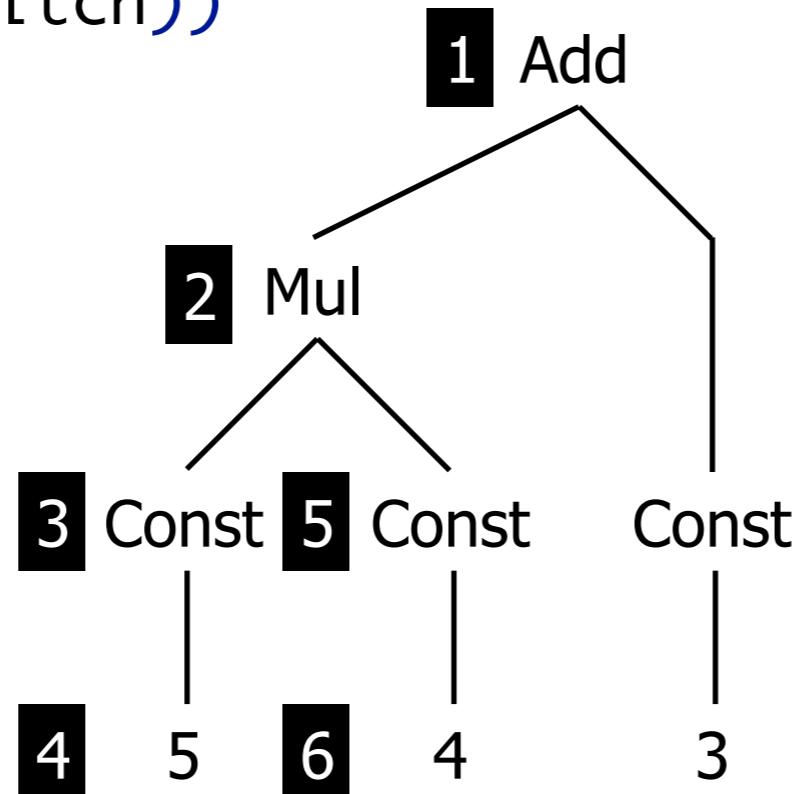


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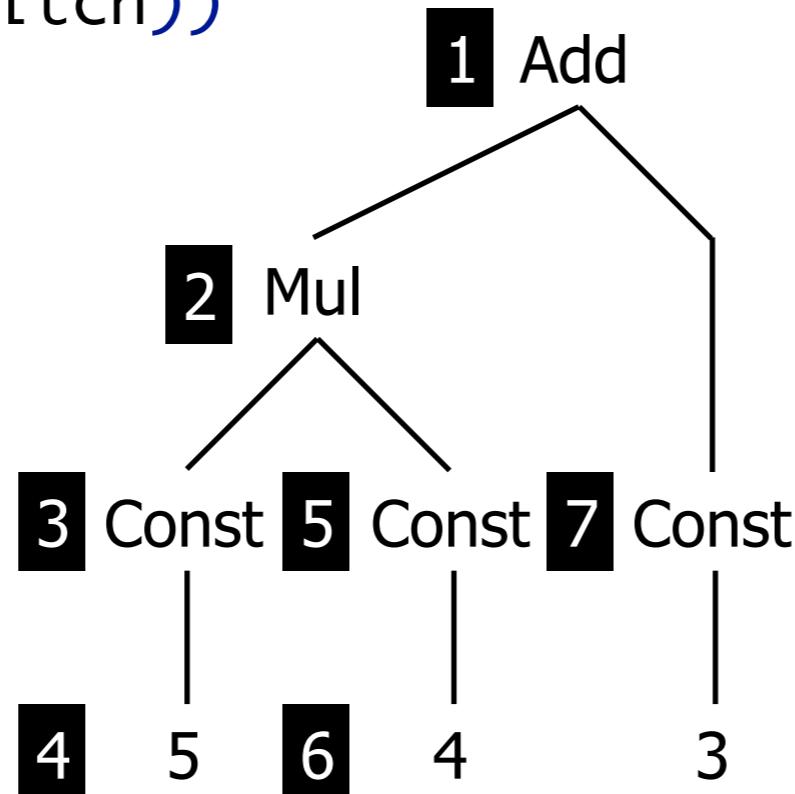


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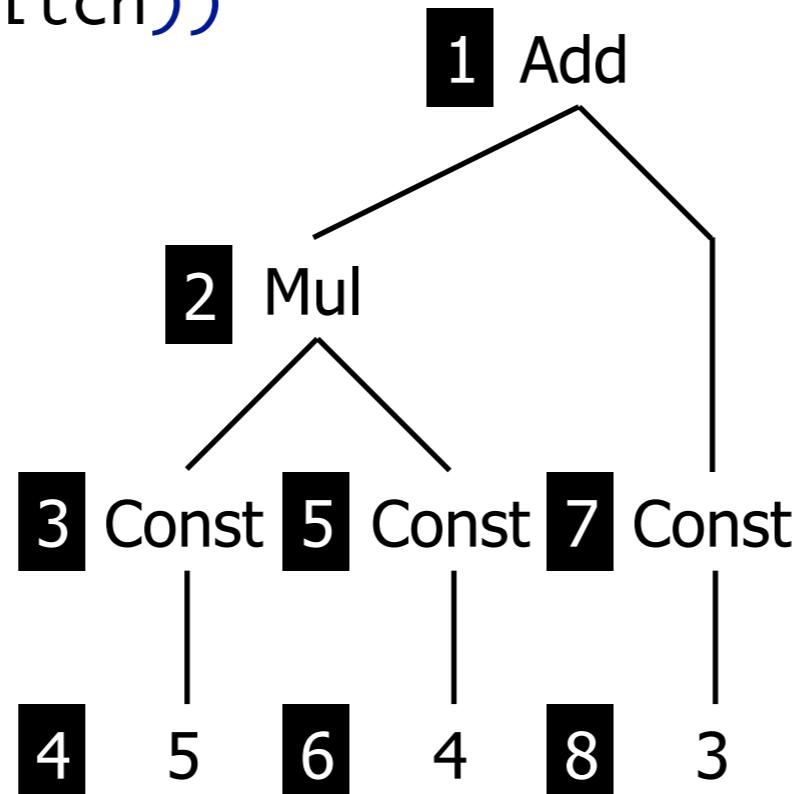


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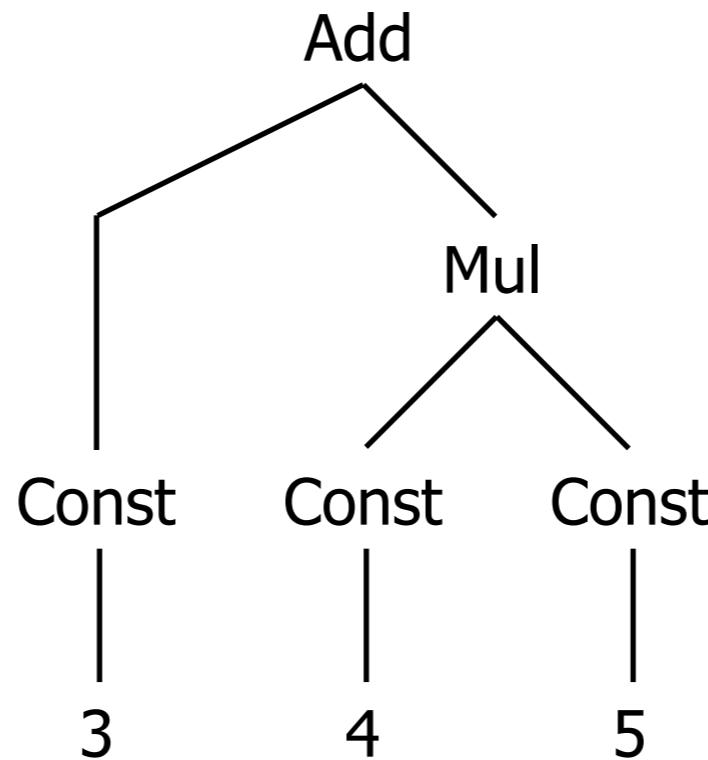


Stratego example

```
switch: Add(e1, e2) -> Add(e2, e1)
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```
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```

```
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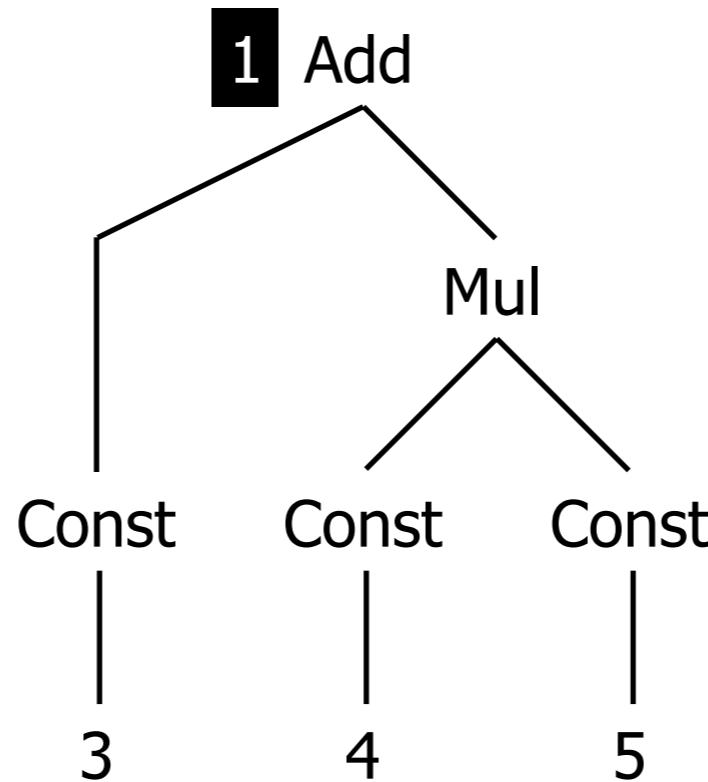


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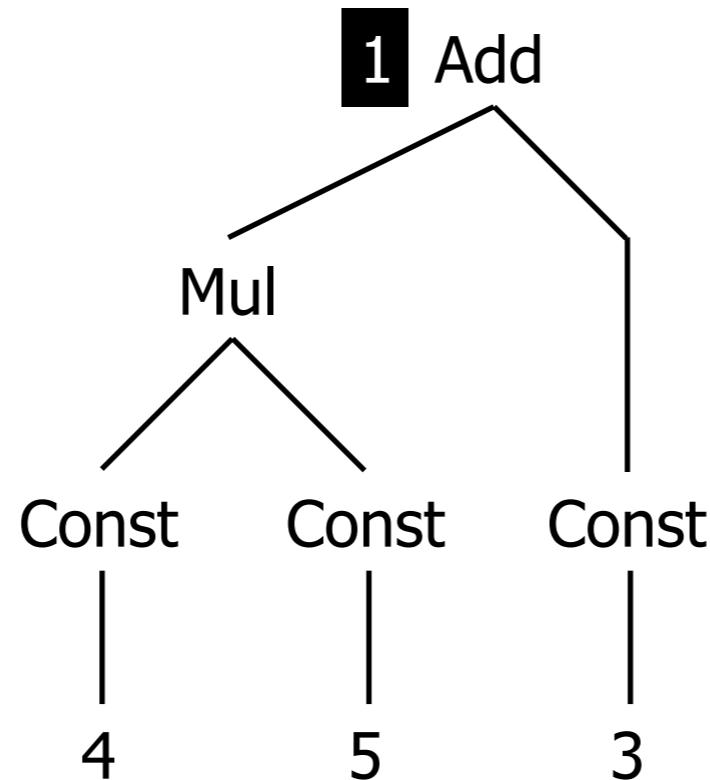


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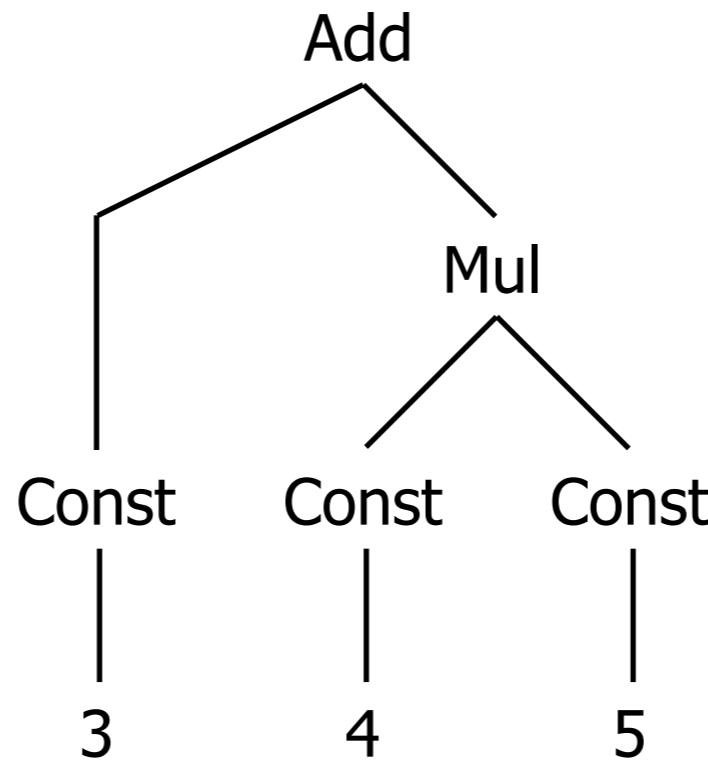


Stratego example

switch: $\text{Mul}(e_1, e_2) \rightarrow \text{Mul}(e_2, e_1)$

$\text{alltd}(s) = s \leftarrow \text{all}(\text{alltd}(s))$

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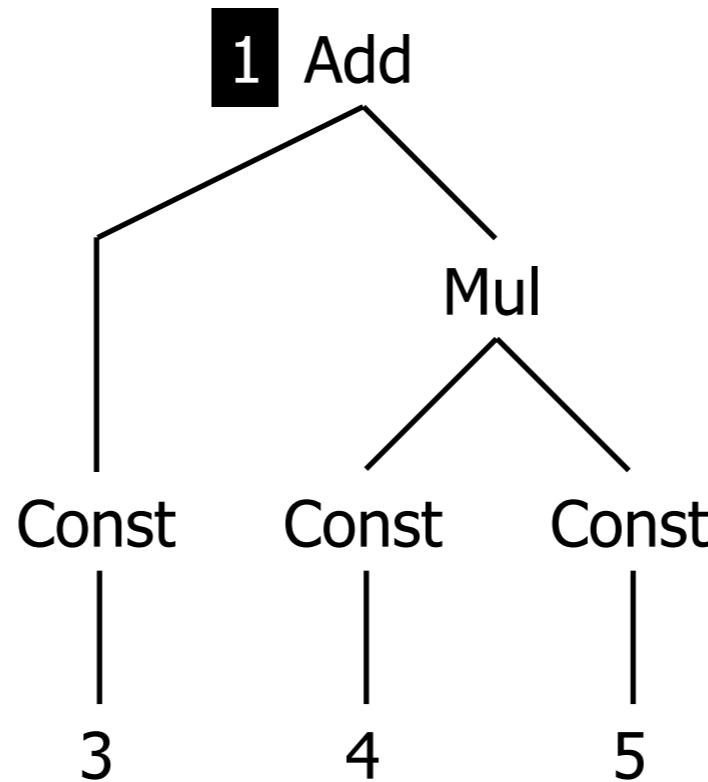


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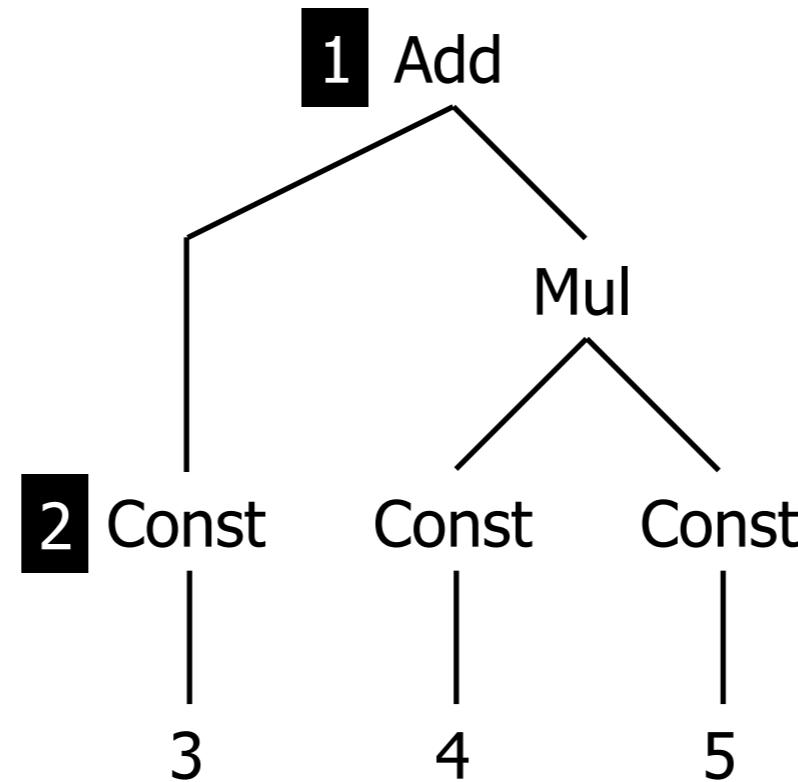


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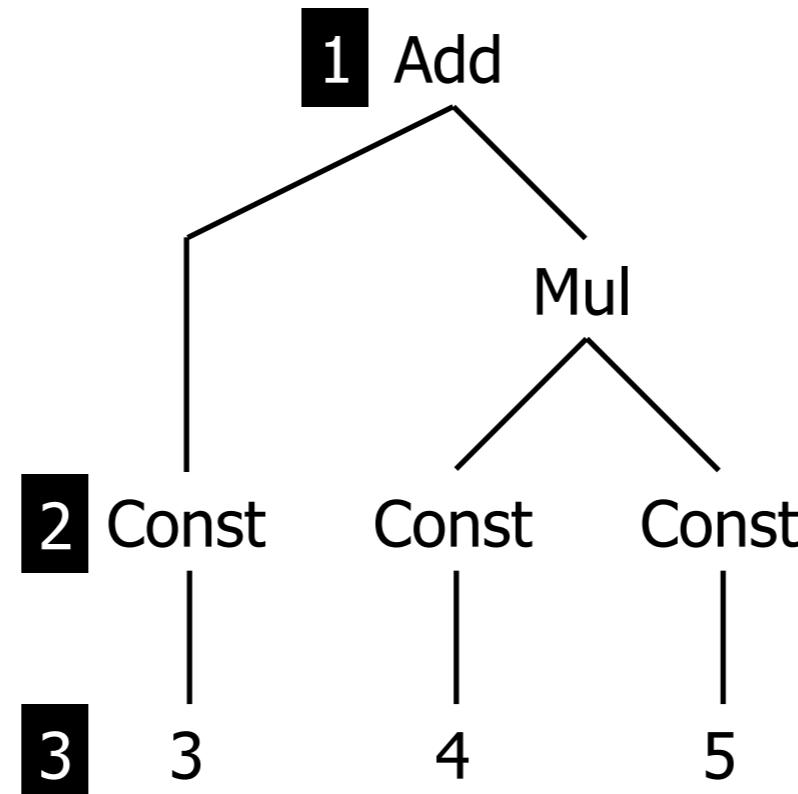


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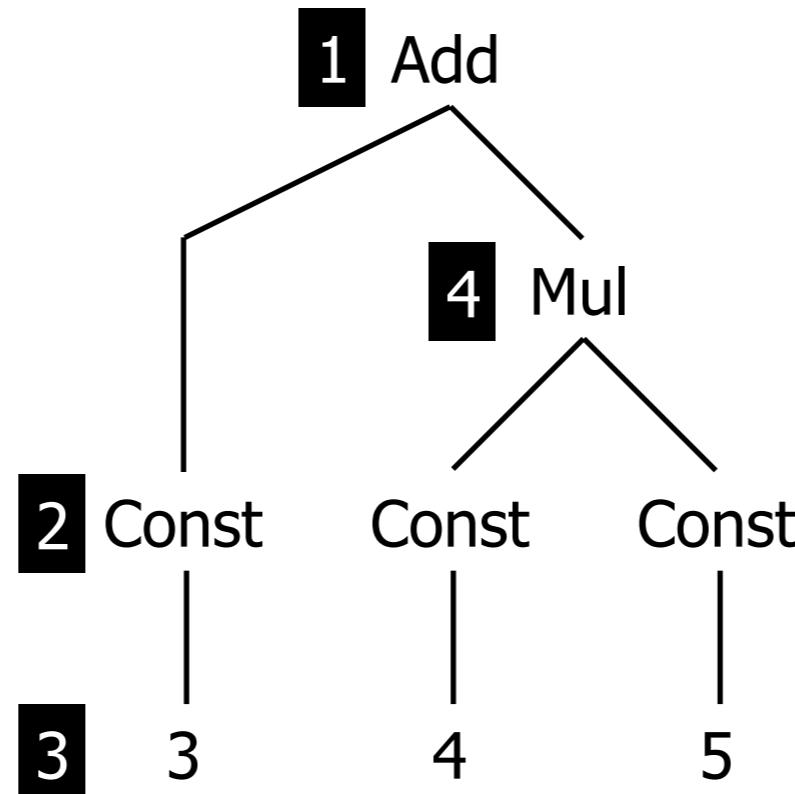


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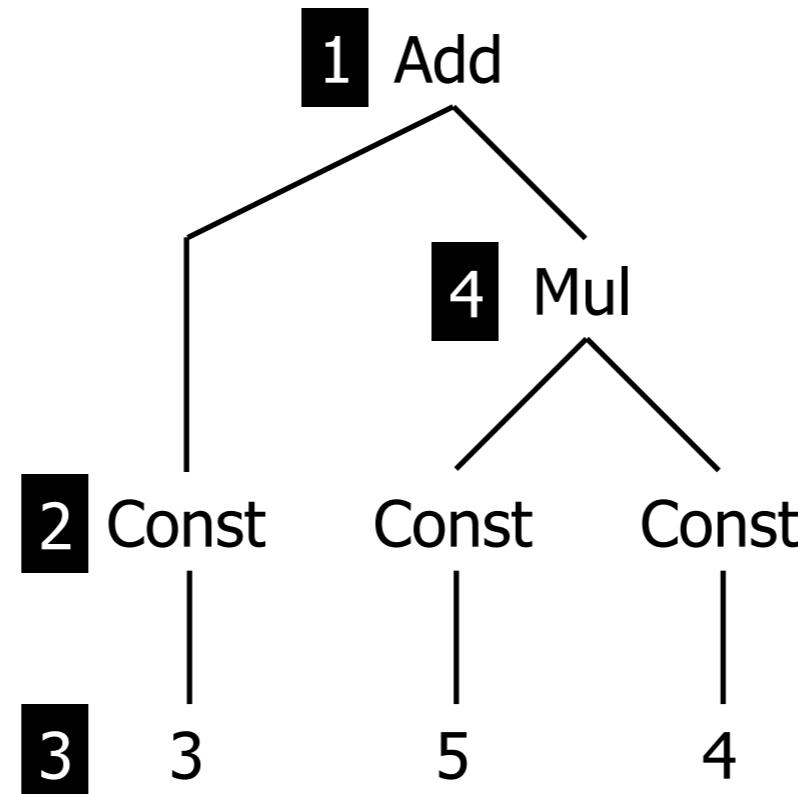


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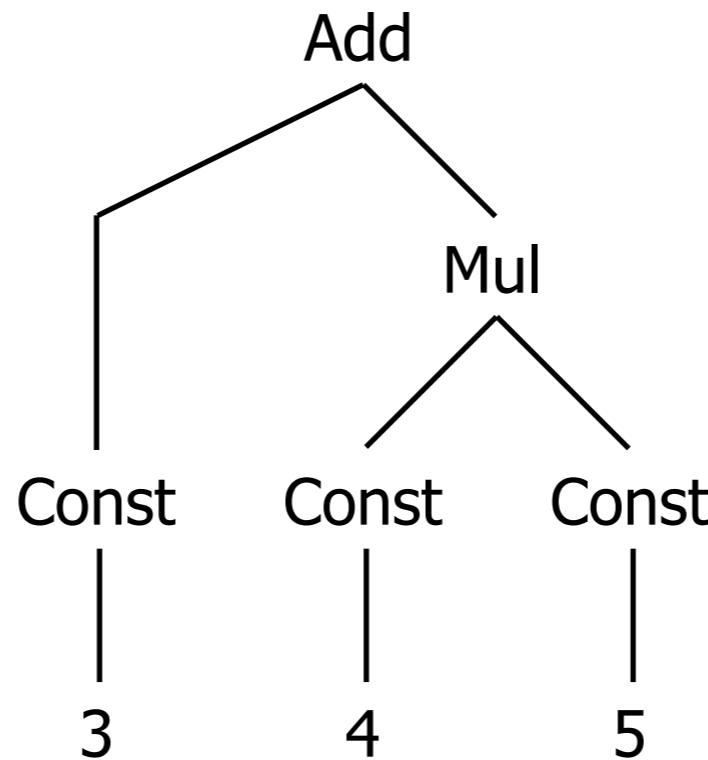


Stratego example

```
switch: Add(e1, e2) -> Add(e2, e1)
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```
bottomup(s) = all(bottomup(s)) ; s
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bottomup(switch)
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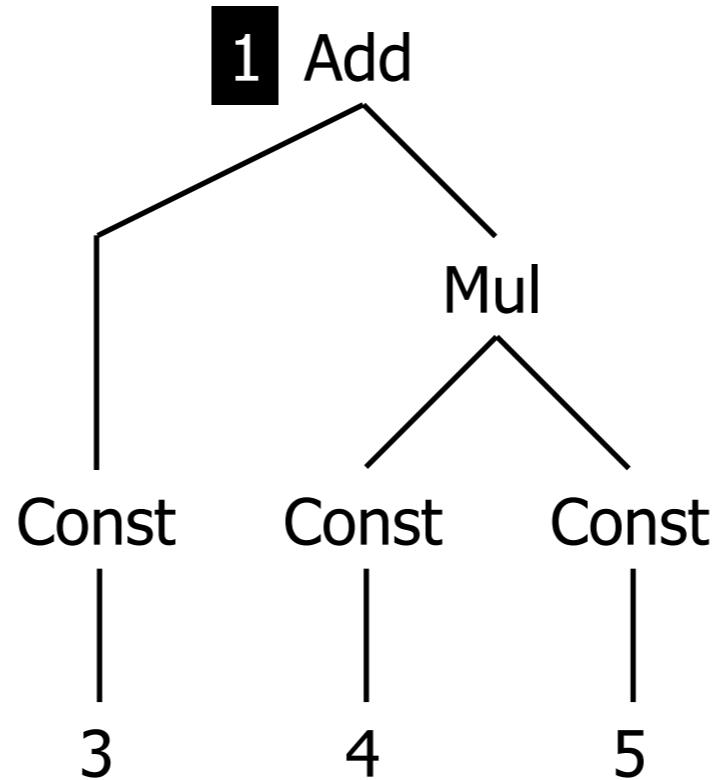


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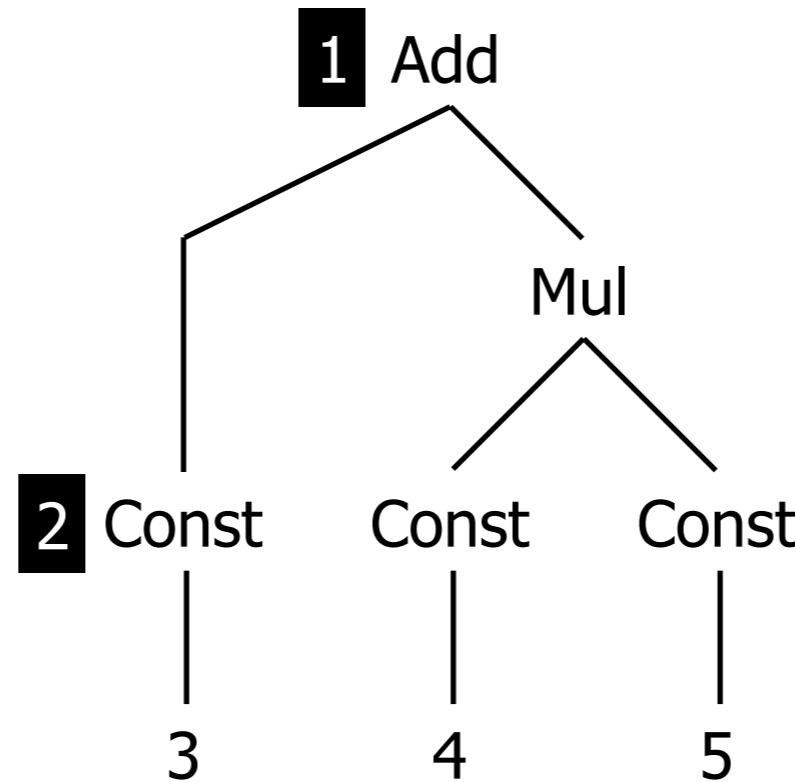


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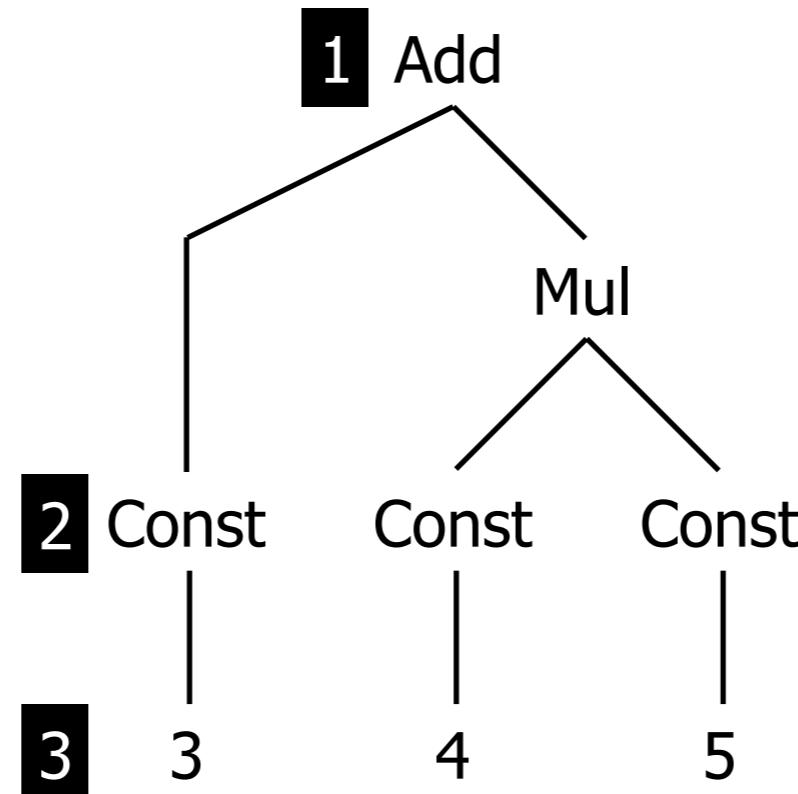


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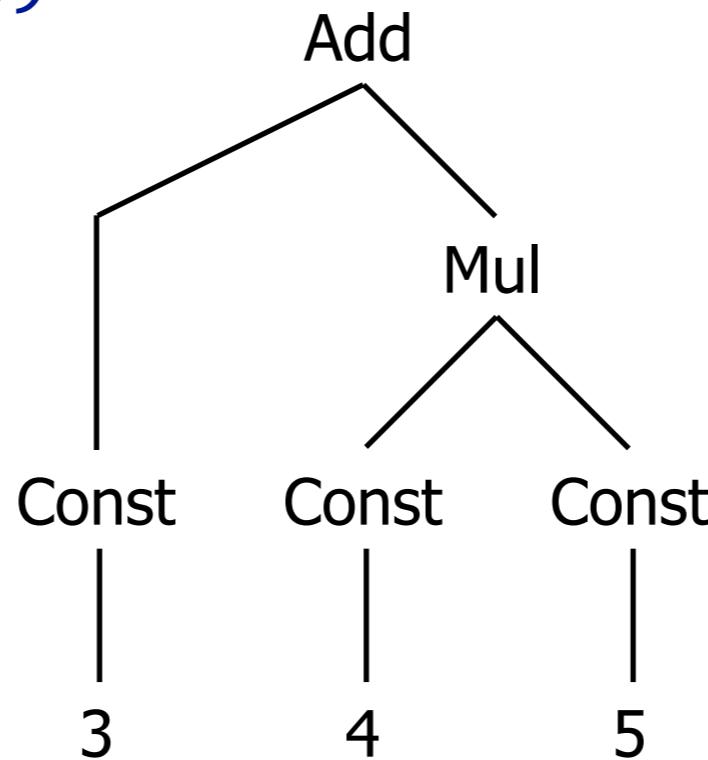


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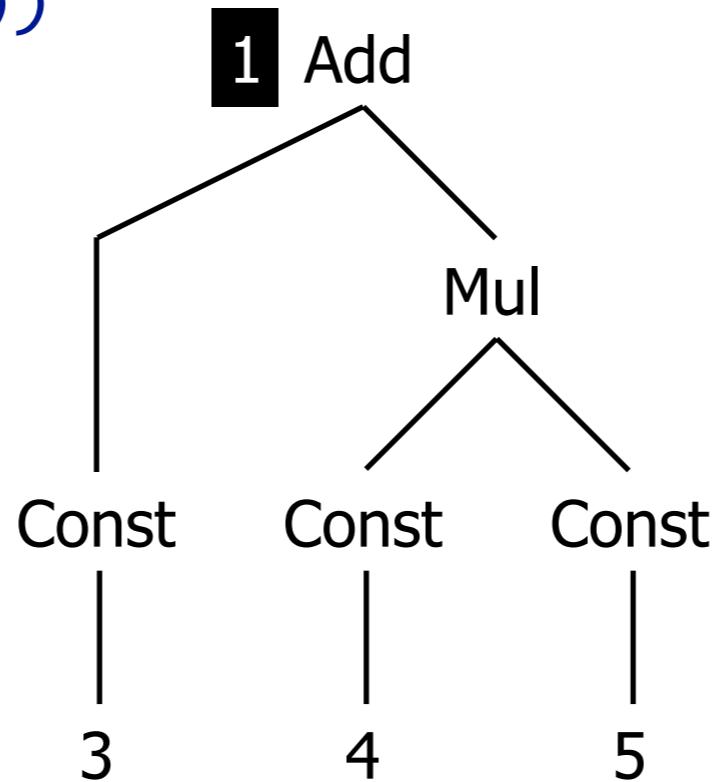


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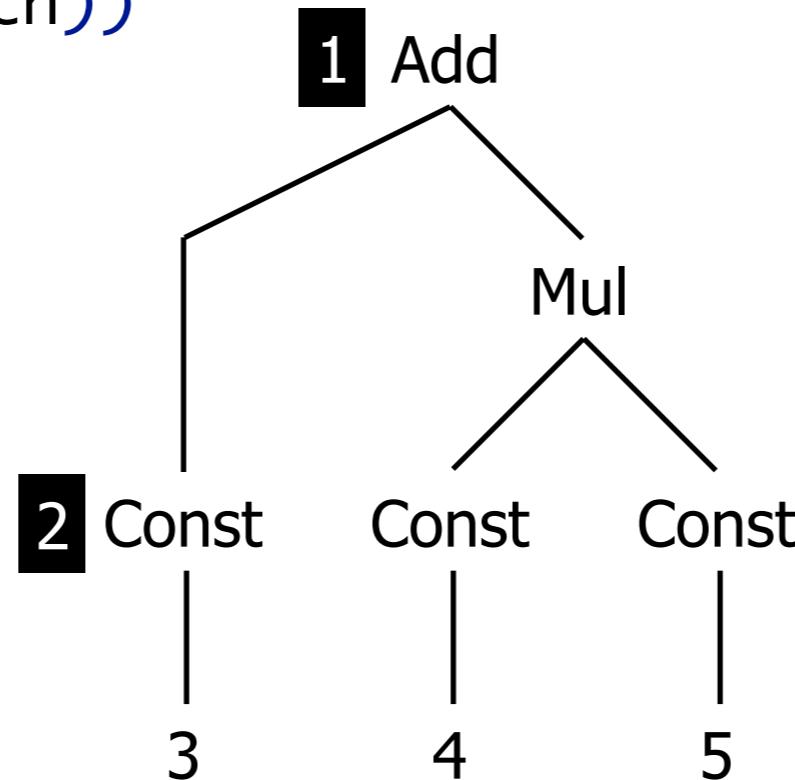


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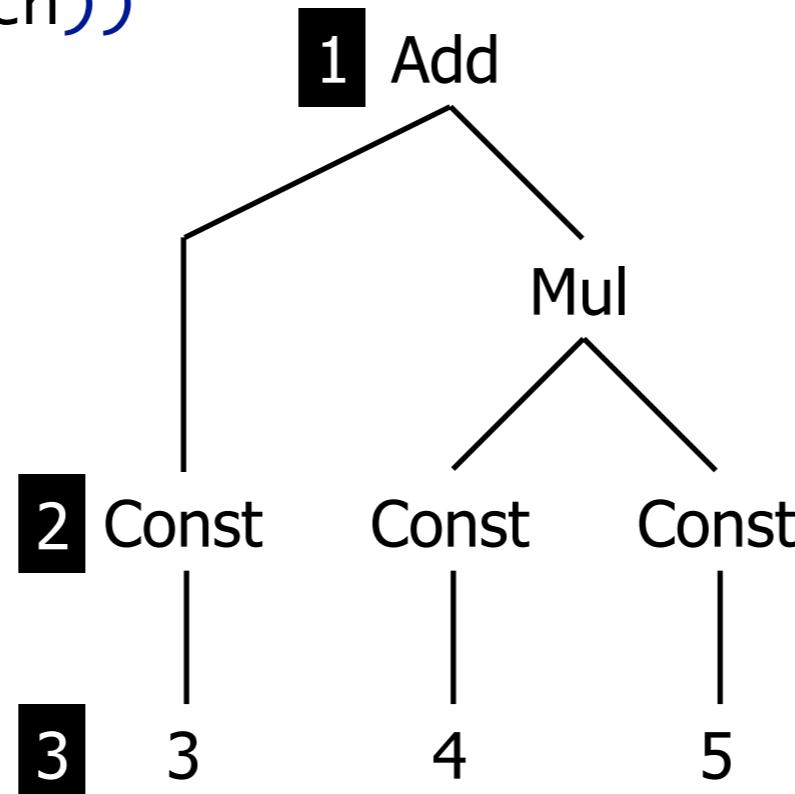


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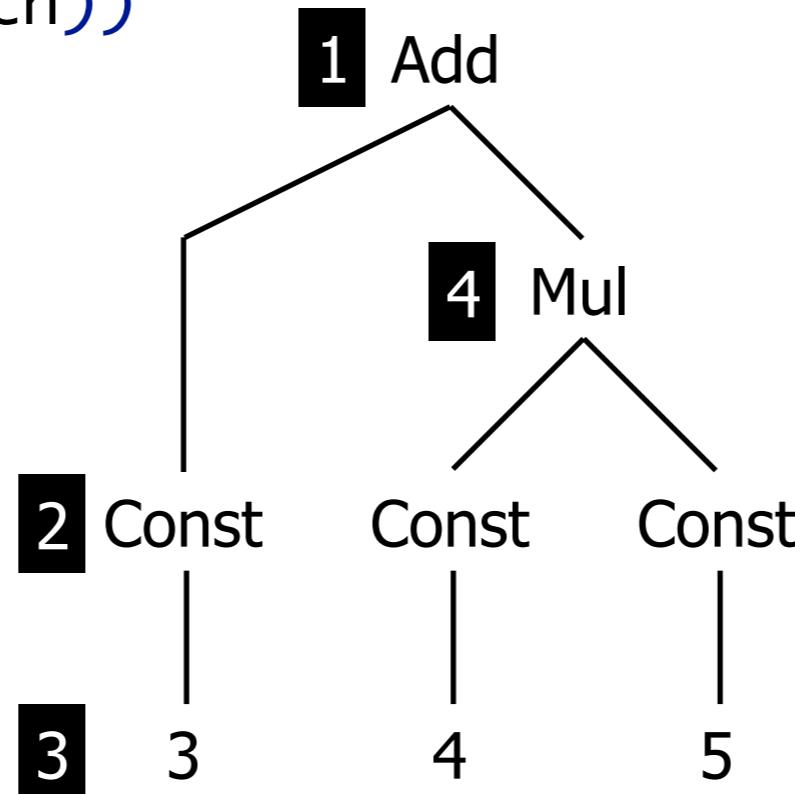


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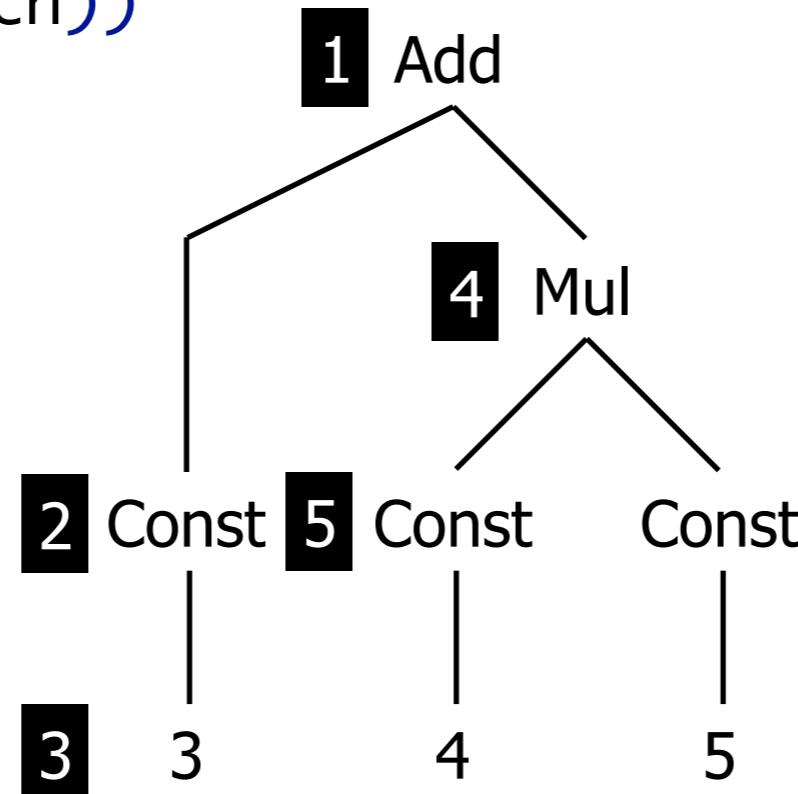


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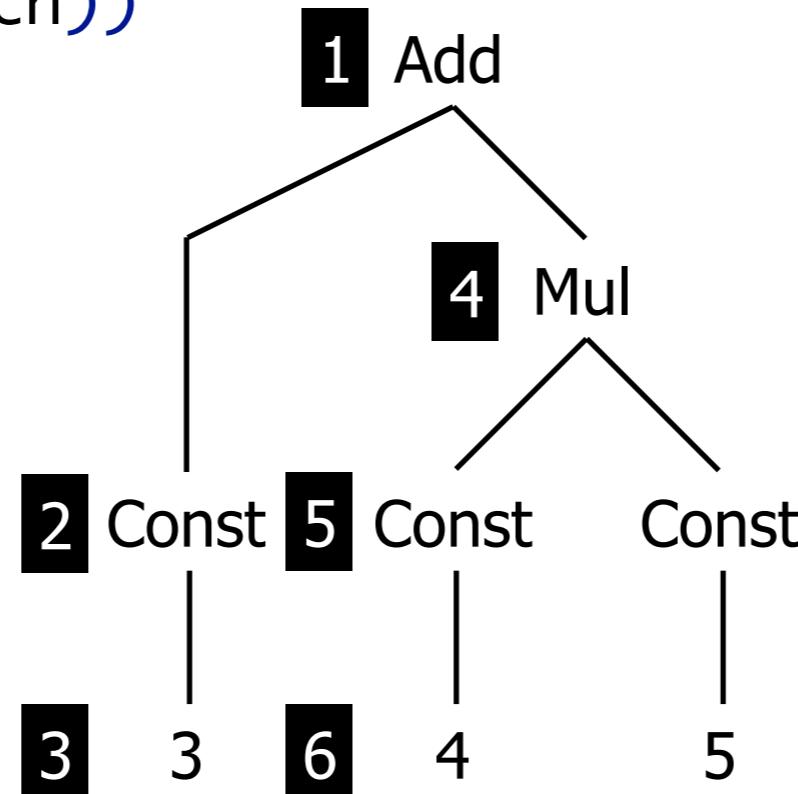


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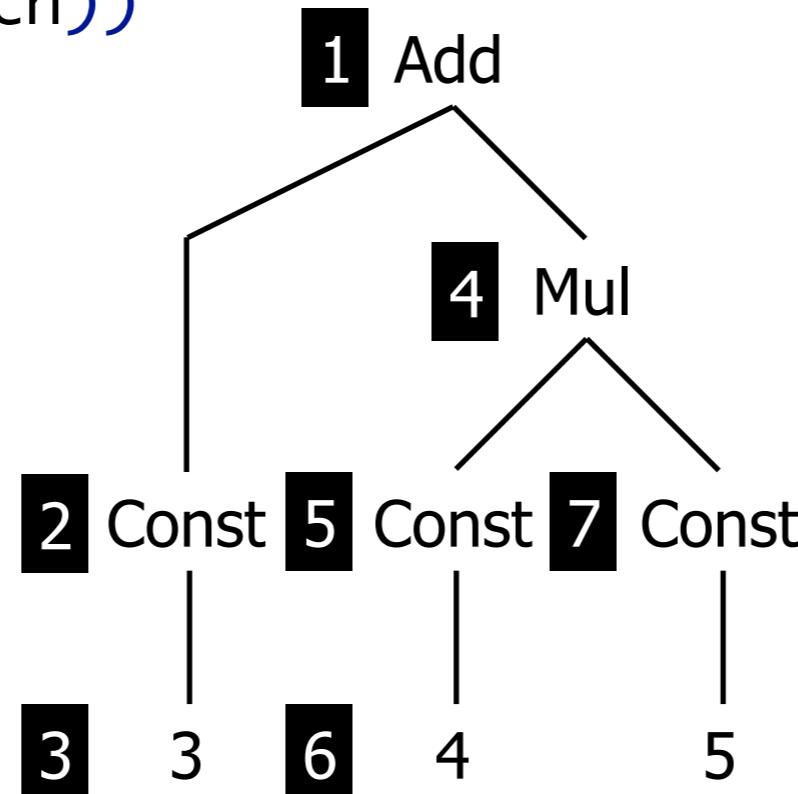


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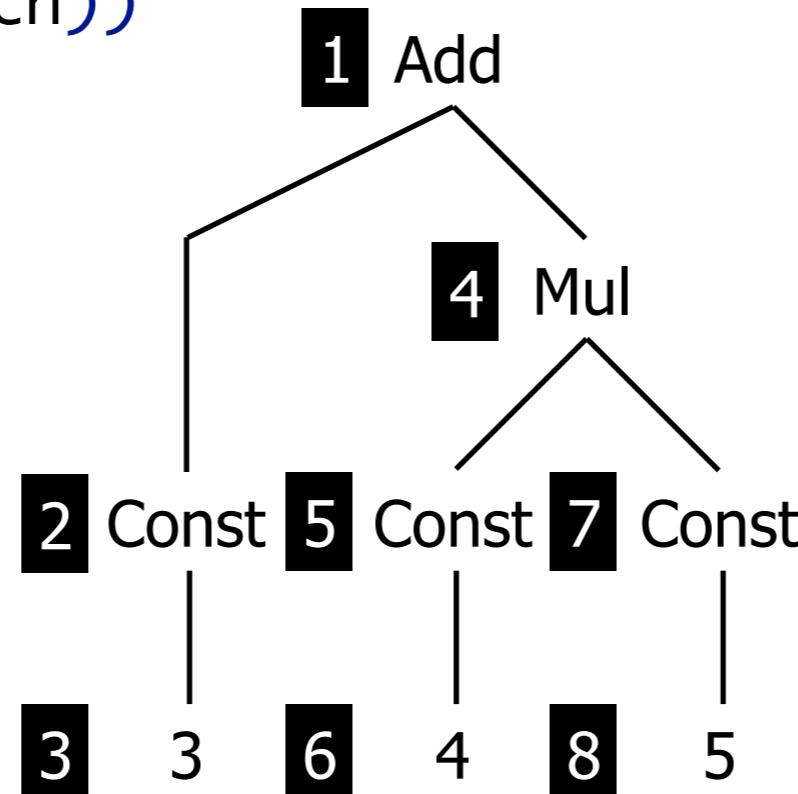


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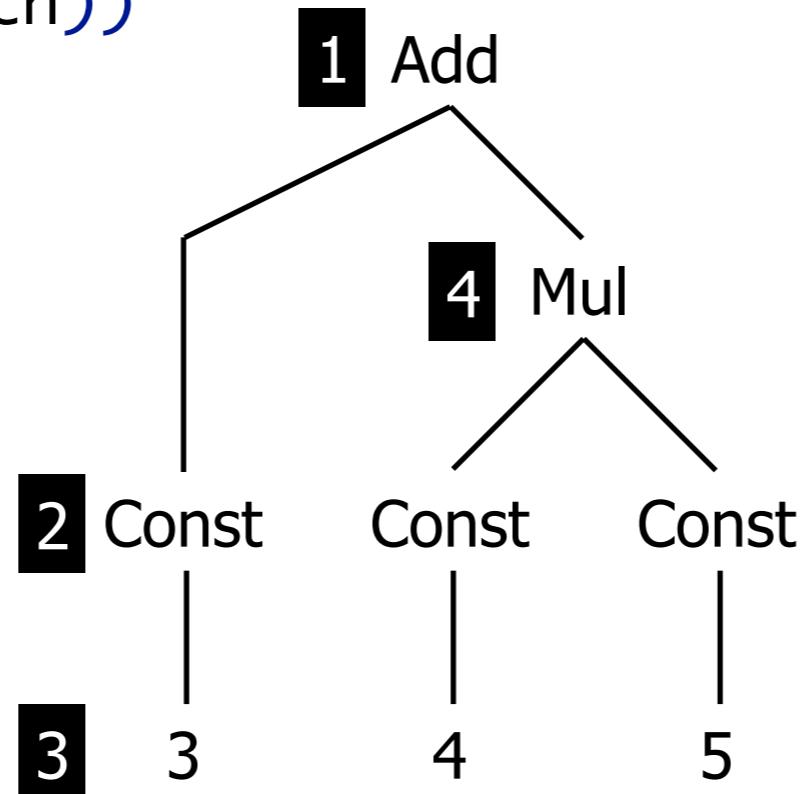


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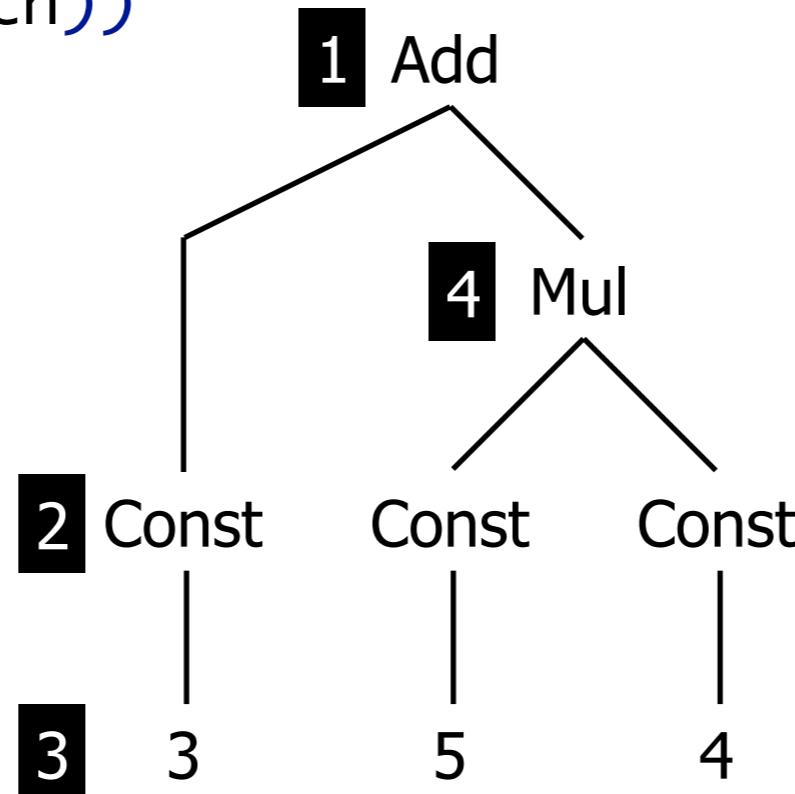


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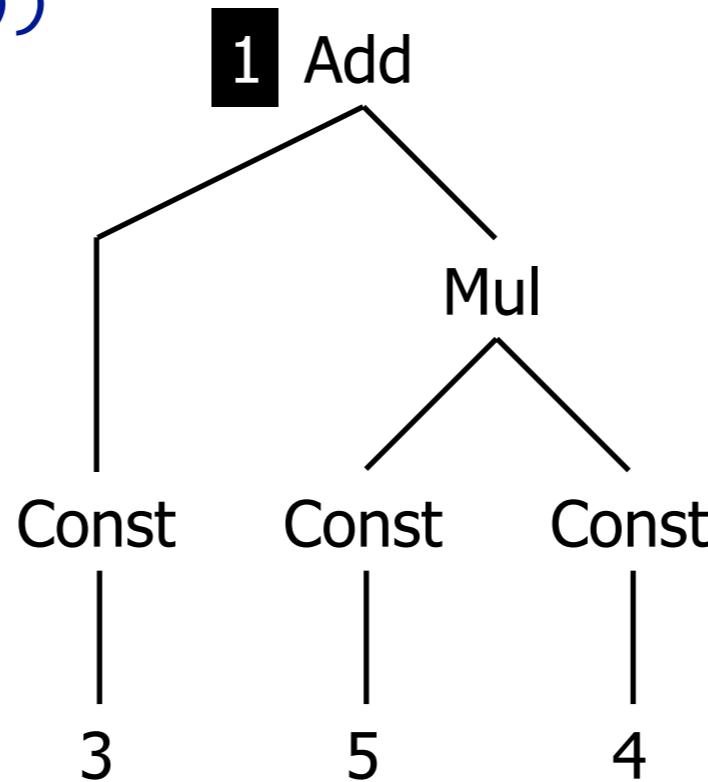


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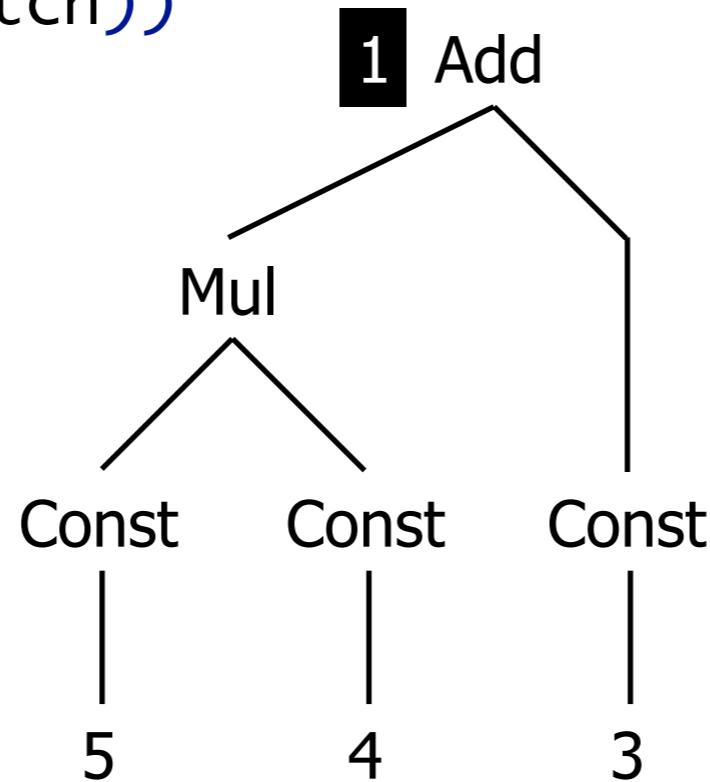


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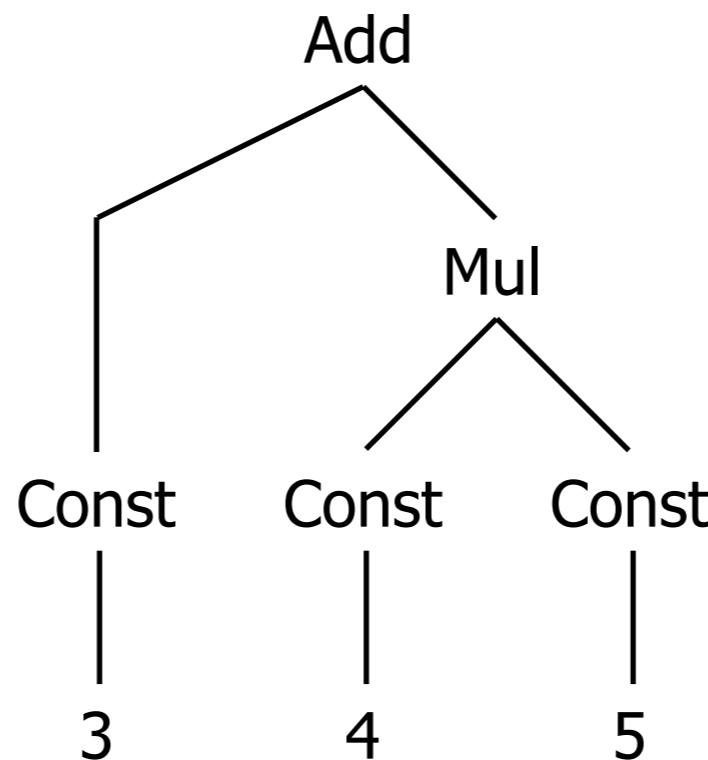
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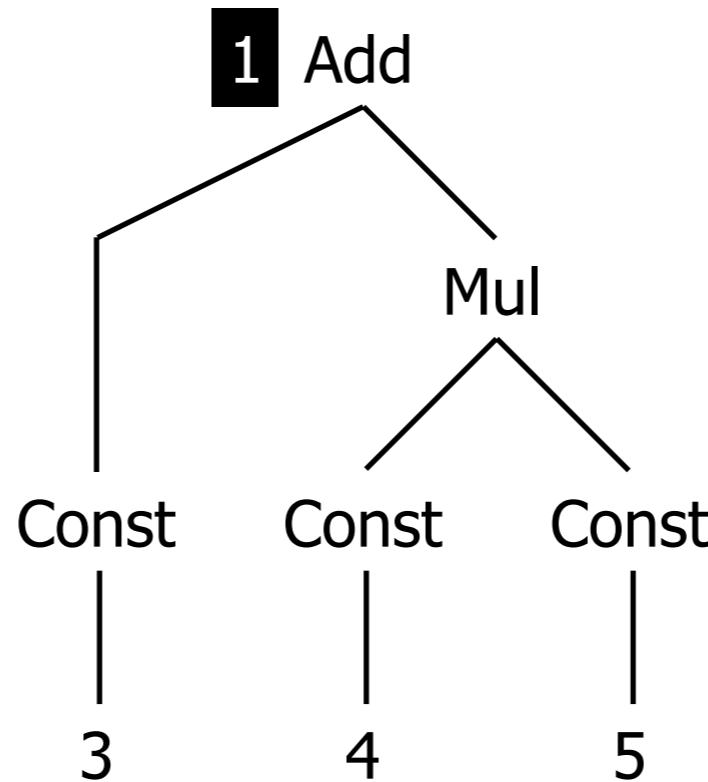
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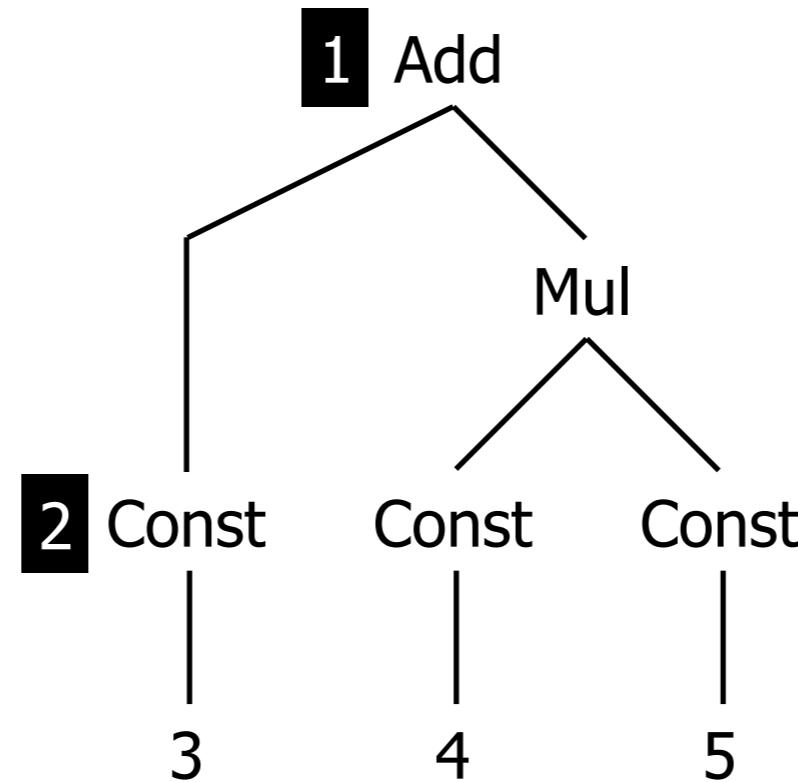
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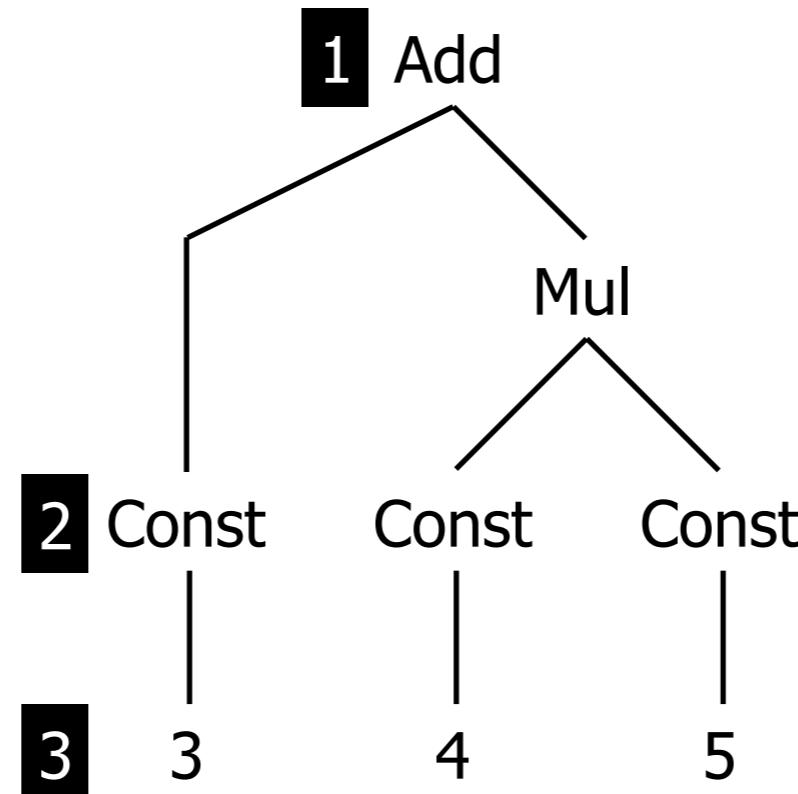
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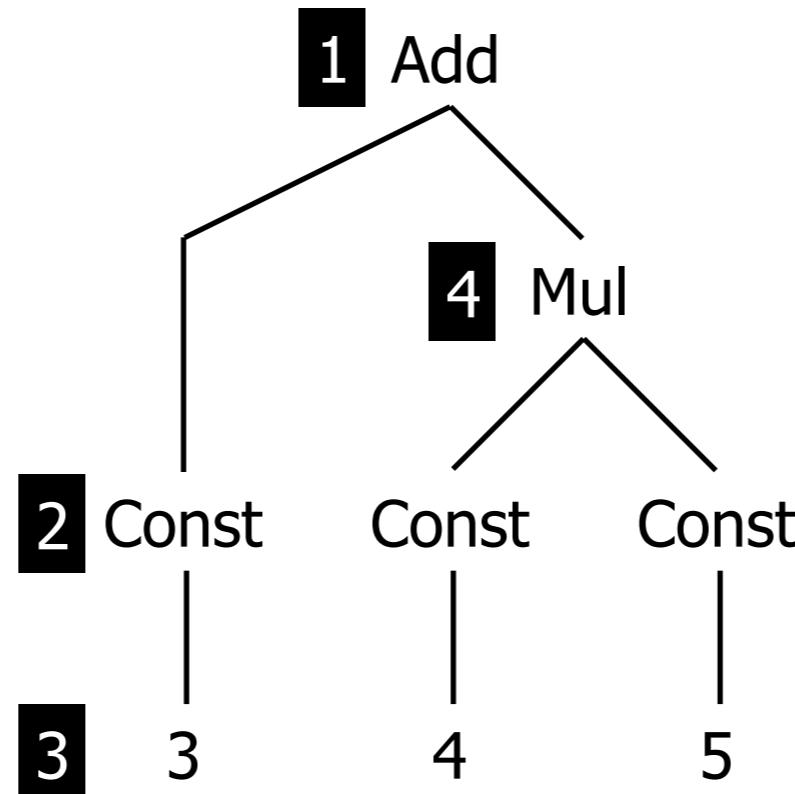
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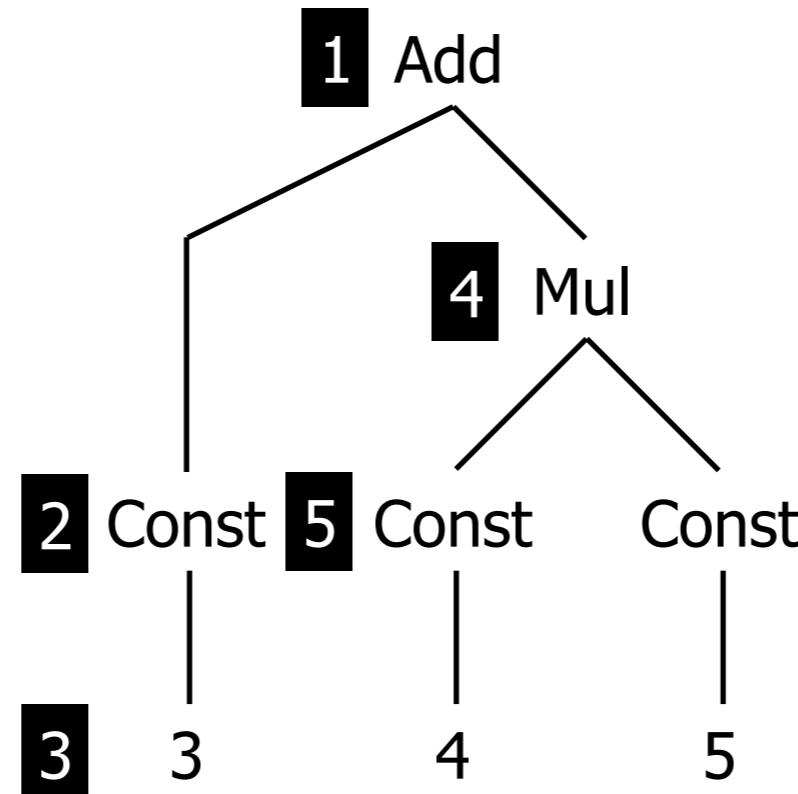
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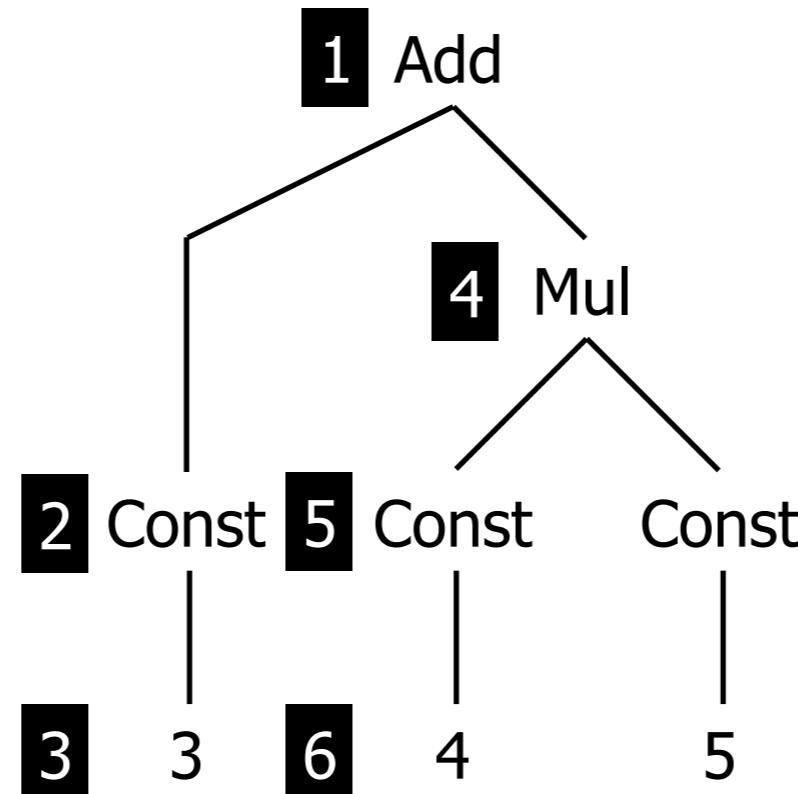
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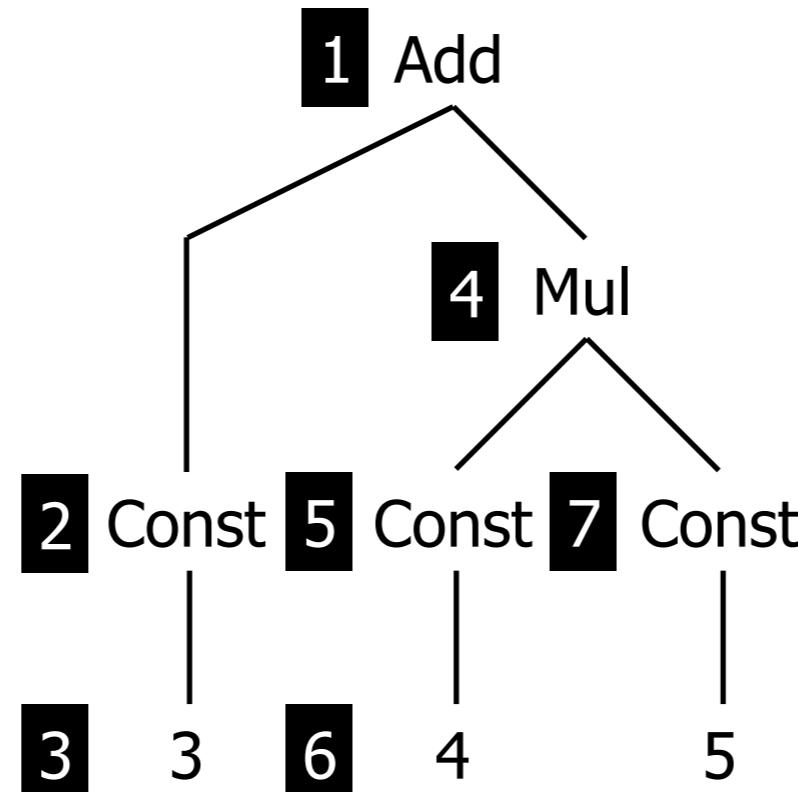
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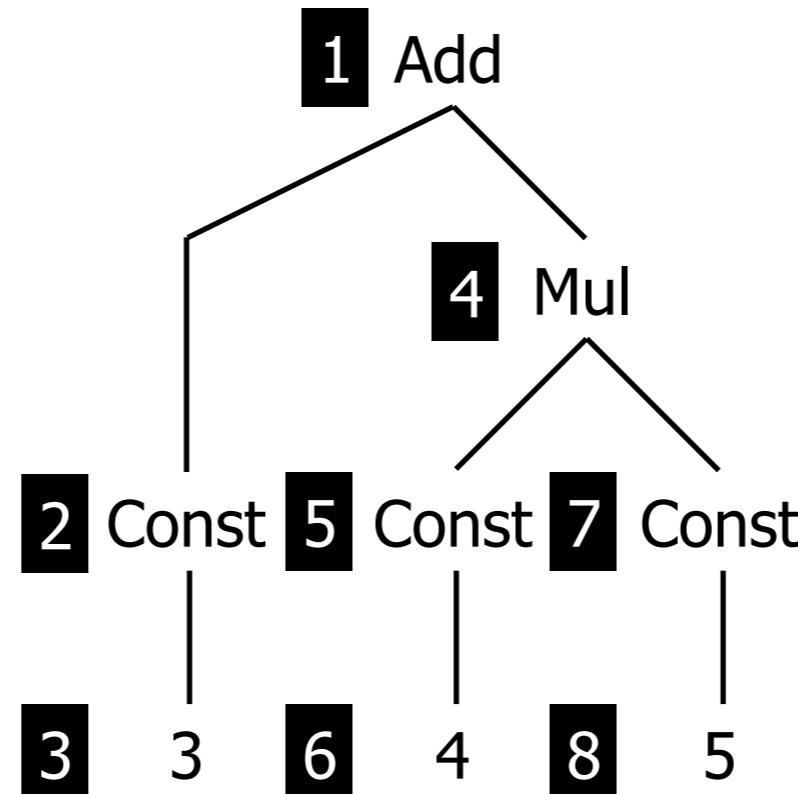
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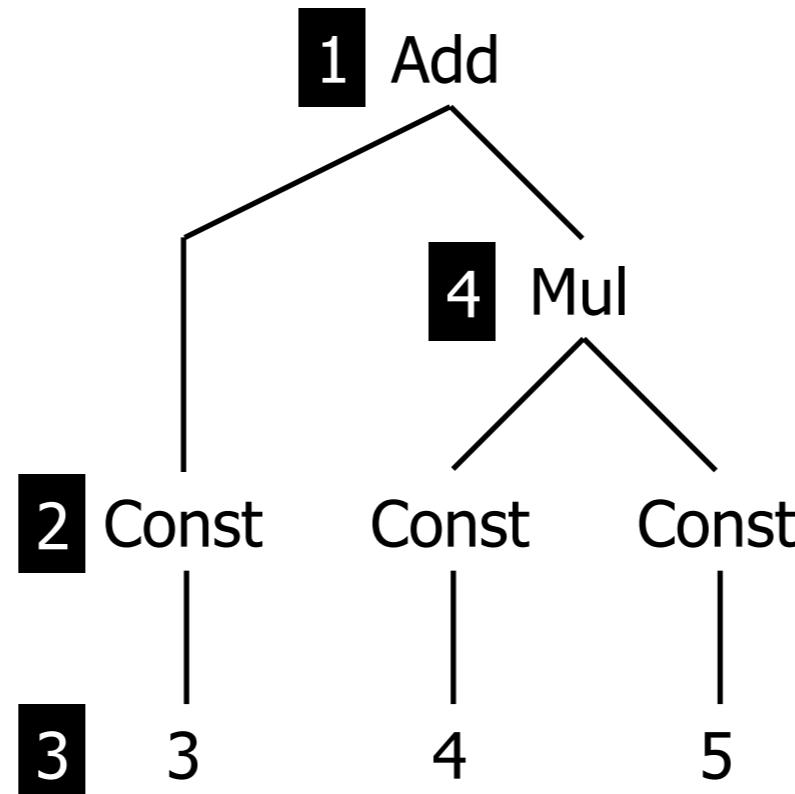
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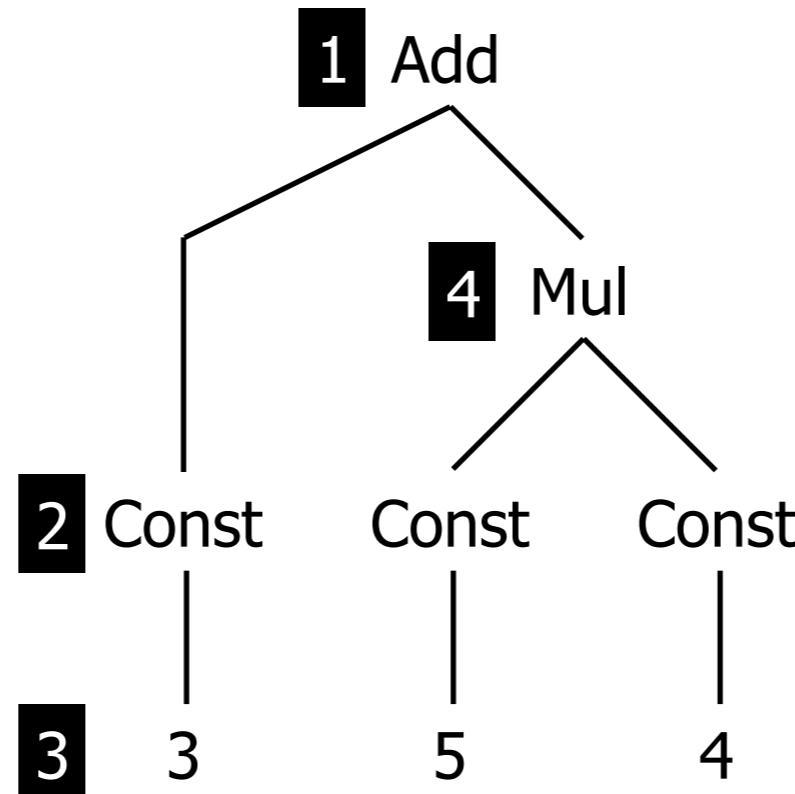
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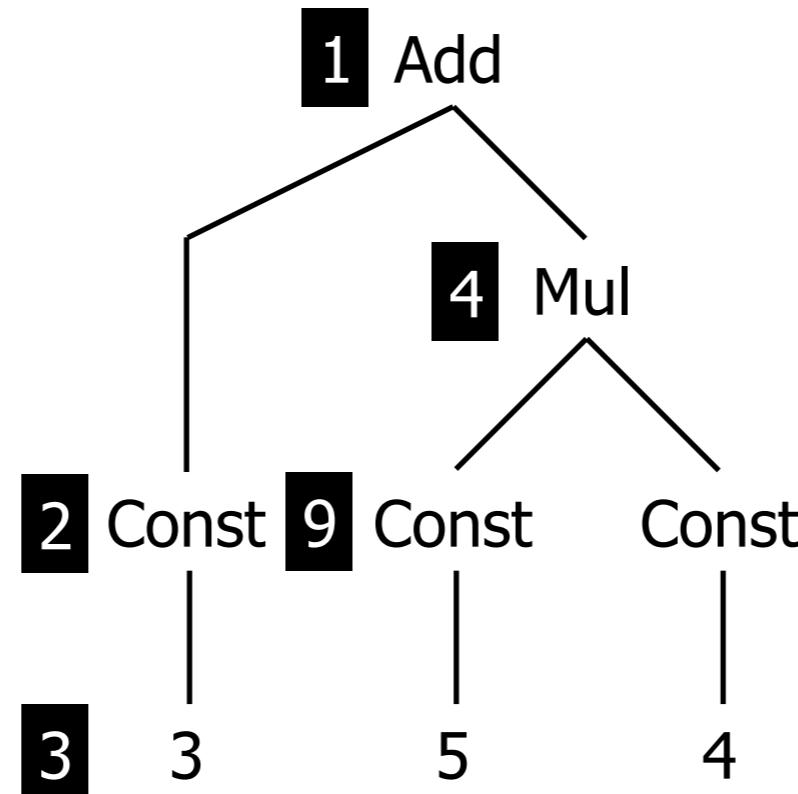
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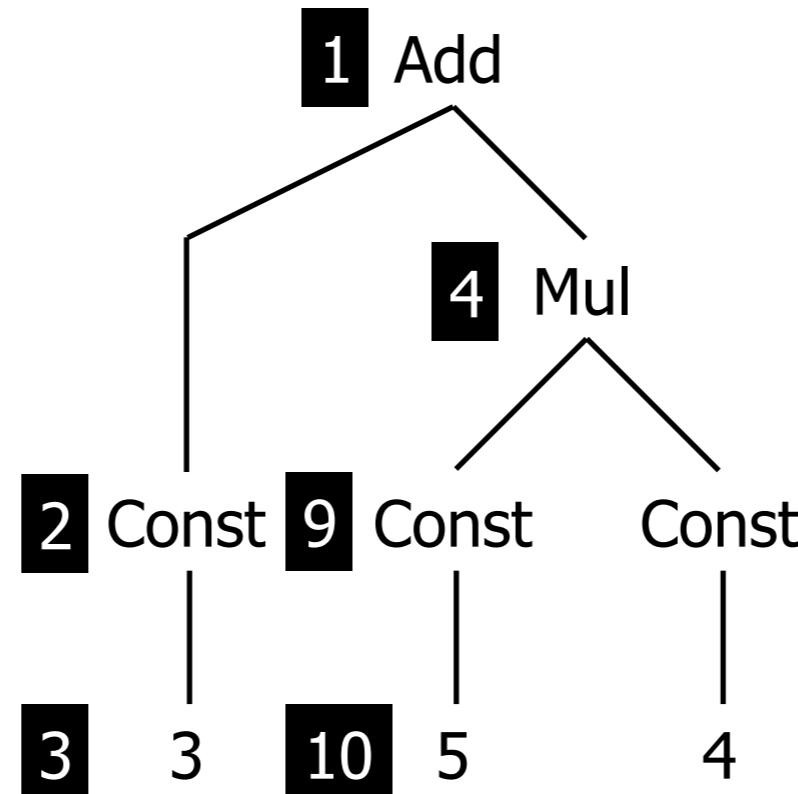
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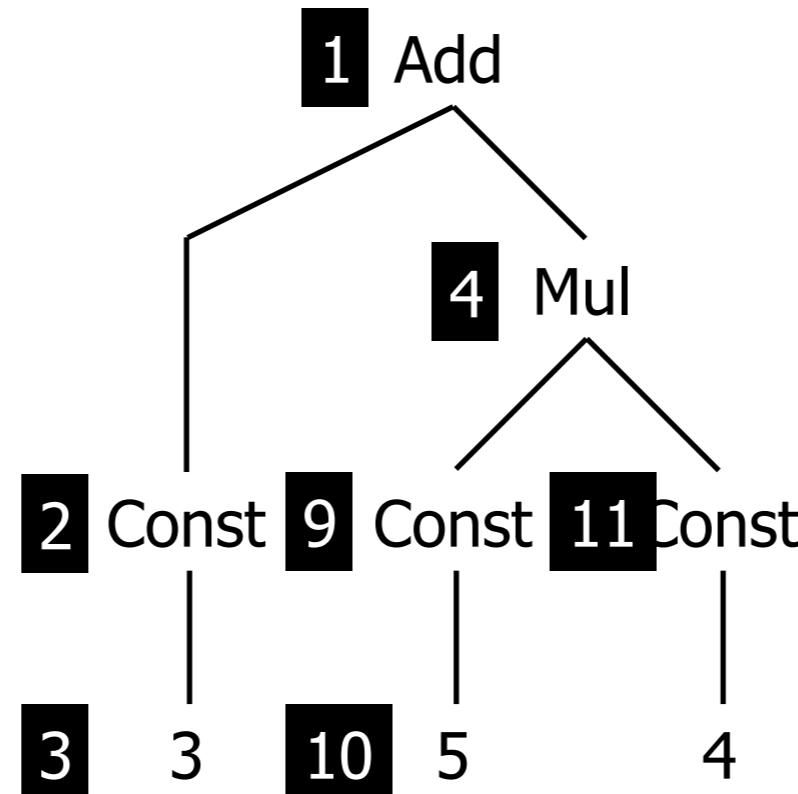
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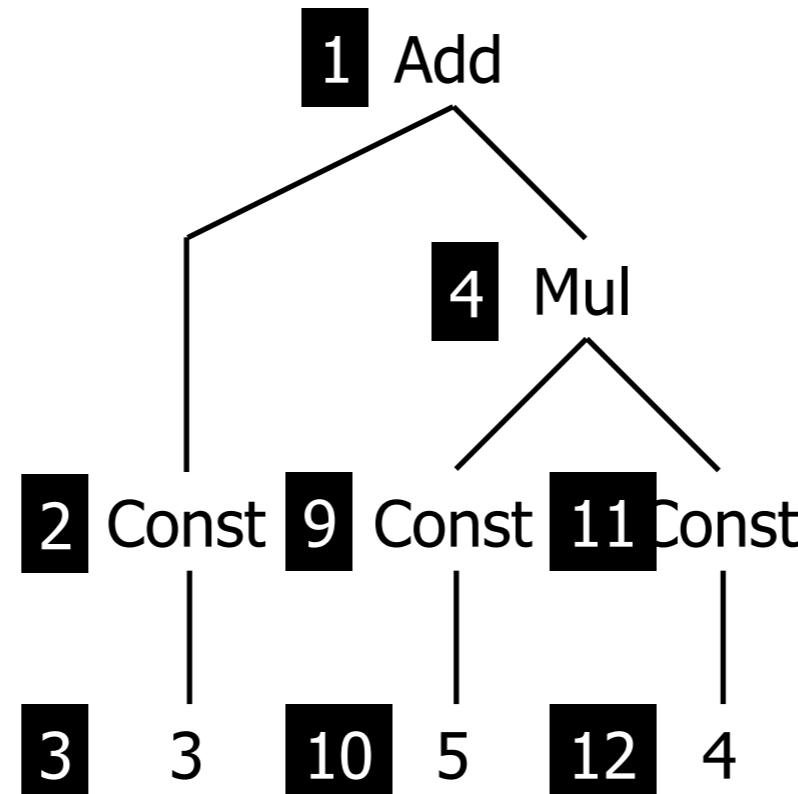
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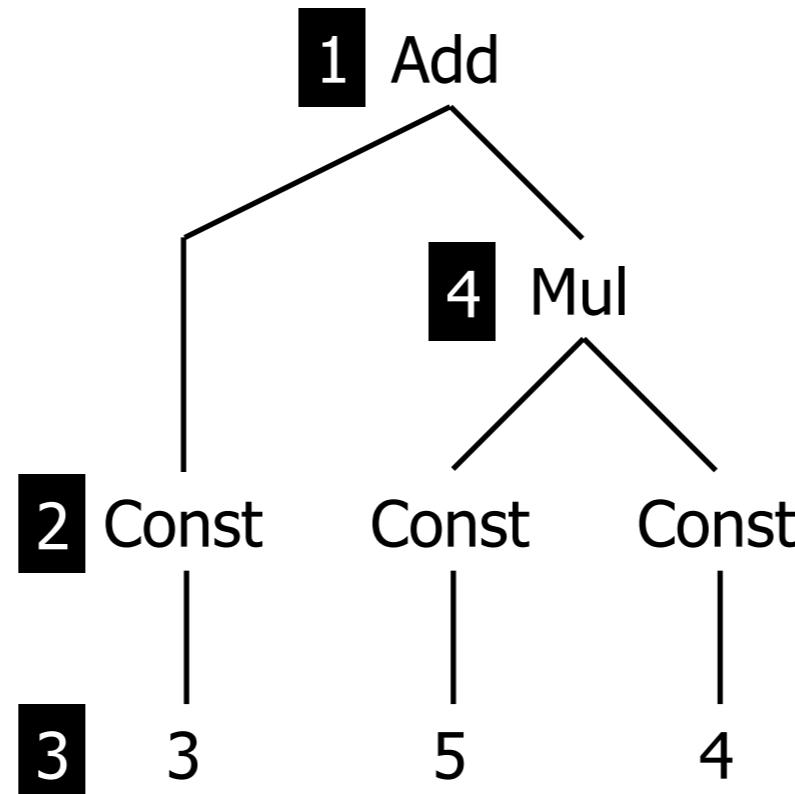
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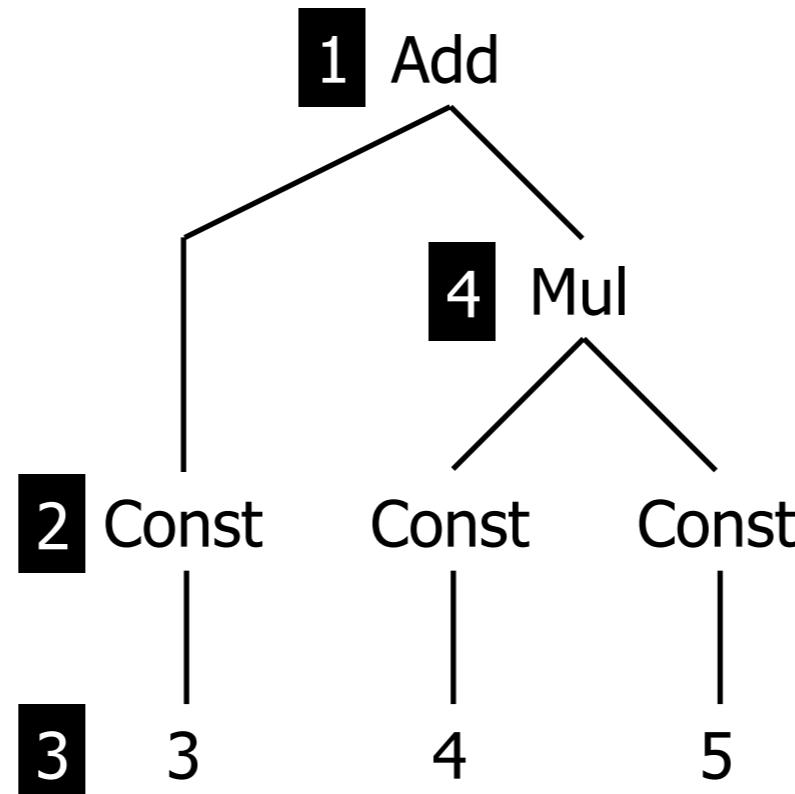
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VI

summary

Summary

lessons learned

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How do you define AST transformations in Stratego?

- signatures
- rewrite rules
- rewrite strategies
- strategy combinators

Summary lessons learned

How do you define AST transformations in Stratego?

- signatures
- rewrite rules
- rewrite strategies
- strategy combinators

What kind of strategies can you find in the Stratego library?

- arithmetics
- map, zip, foldr
- generic traversals

Literature

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Literature

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Spoofax

Lennart C. L. Kats, Eelco Visser: The Spooftax Language Workbench.
Rules for Declarative Specification of Languages and IDEs. OOPSLA
2010

<http://www.spooftax.org>

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Stratego

Martin Bravenboer, Karl Trygve Kalleberg, Rob Vermaas, Eelco Visser:
Stratego/XT 0.17. A language and toolset for program transformation.
Science of Computer Programming, 72(1-2), 2008.

<http://www.strategoxt.org>

Outlook coming next

declarative semantics definition

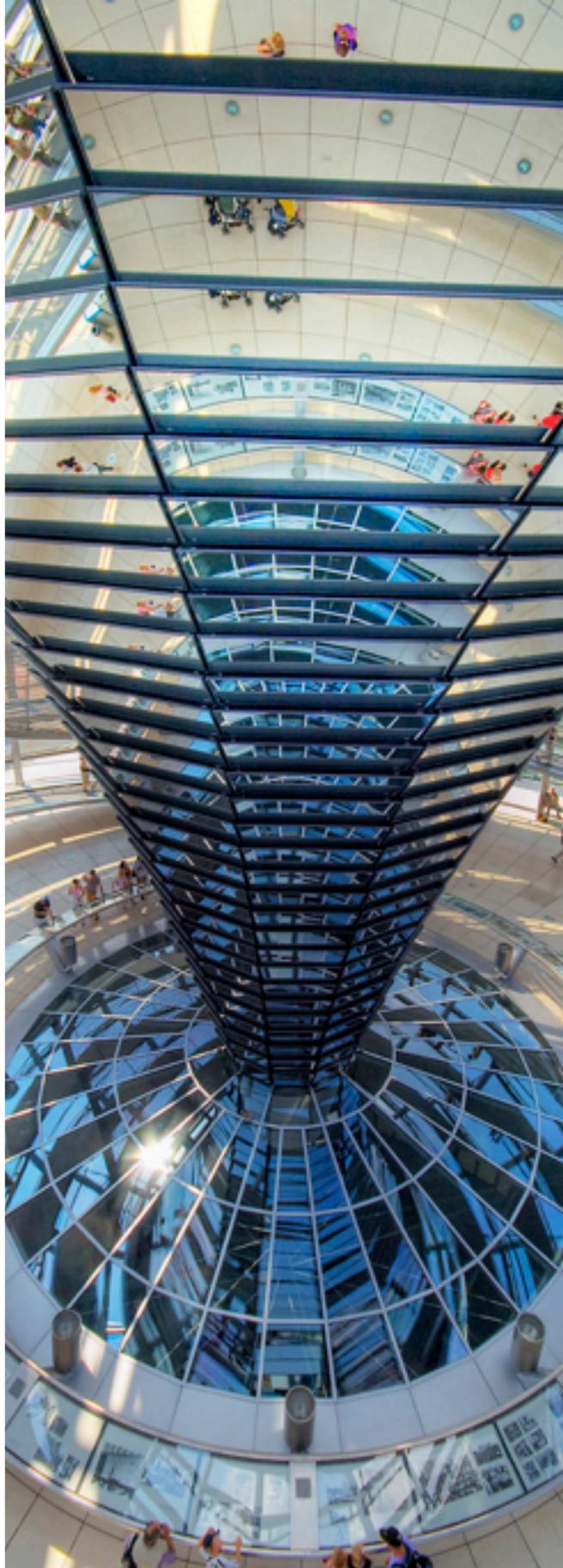
- Lecture 5: Static Analysis and Error Checking
- Lecture 6: Code Generation

Assignment Oct 3: MiniJava grammar in SDF

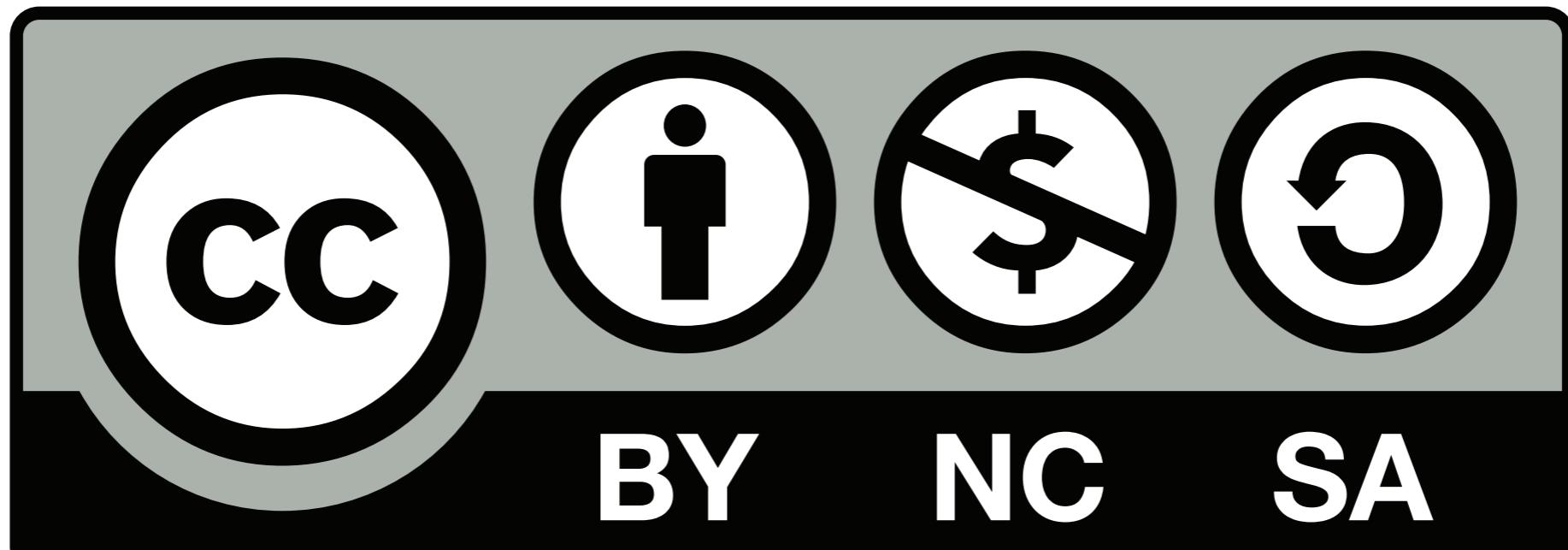
- submit on Blackboard

Lab Oct 04

- pretty-printer for MiniJava
- syntactic editor services



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