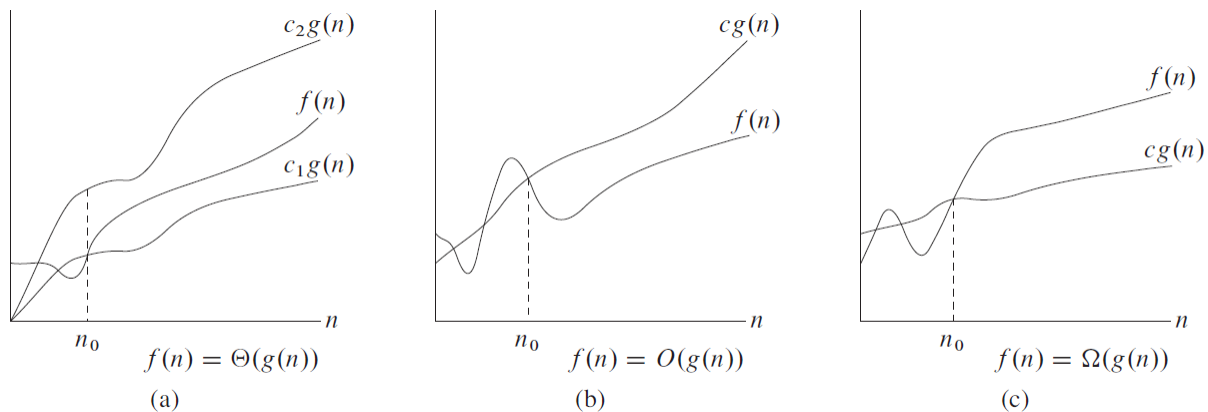


$O(g(n)) = \{f(n) : \text{there exist positive constants } c \text{ and } n_0 \text{ such that } 0 \leq f(n) \leq cg(n) \text{ for all } n \geq n_0\}.$

$\Omega(g(n)) = \{f(n) : \text{there exist positive constants } c \text{ and } n_0 \text{ such that } 0 \leq cg(n) \leq f(n) \text{ for all } n \geq n_0\}.$

$\Theta(g(n)) = \{f(n) : \text{there exist positive constants } c_1, c_2, \text{ and } n_0 \text{ such that } 0 \leq c_1g(n) \leq f(n) \leq c_2g(n) \text{ for all } n \geq n_0\}.$ <sup>1</sup>



### Question 1:

Arrange the functions  $\sqrt{n}$ ,  $1000 \log n$ ,  $n \log n$ ,  $2n!$ ,  $2^n$ ,  $3^n$ , and  $n^2/1000000$  in a list so that each function is *big-O* of the next function.

### Question 2:

Indicate, for each pair of expressions  $(A, B)$  in the table below, whether  $A$  is  $O$ ,  $o$ ,  $\Omega$ ,  $\omega$ , or  $\Theta$  of  $B$ . Assume that  $k \geq 1$ ,  $\epsilon > 0$ , and  $c > 1$  are constants. Your answer should be in the form of the table with “yes” or “no” written in each box.

	$A$	$B$	$O$	$o$	$\Omega$	$\omega$	$\Theta$
a.	$\lg^k n$	$n^\epsilon$					
b.	$n^k$	$c^n$					
c.	$\sqrt{n}$	$n^{\sin n}$					
d.	$2^n$	$2^{n/2}$					
e.	$n^{\lg c}$	$c^{\lg n}$					
f.	$\lg(n!)$	$\lg(n^n)$					

**Note:** Filling the columns corresponding to *little o* and *little omega* is optional

**Question 3:** Show that  $2^x = O(3^x)$ . Are the two functions of the same order? Justify your answer with proper reasoning.