

Code ▾

Ch6 Final Project - Testing For Treatment

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Step 1

Part 1

I will investigate the Cologuard test because it has a nice false-positive rate of 10%. The expected number of false positives in a group of five patients is $5 \times 0.1 = 0.5$

I will simulate 20 groups of 5 tests using R's built in random number function. 1 means a false positive and 0 means no false positive.

Code

Group	Test 1	Test 2	Test 3	Test 4	Test 5	Total
1	0	0	0	0	0	0
2	0	0	0	0	1	1
3	0	1	0	0	0	1
4	0	0	1	0	0	1
5	0	0	0	0	0	0
6	0	0	0	0	0	0
7	0	0	1	0	1	2
8	1	0	0	0	0	1
9	0	1	0	1	0	2
10	0	0	0	0	0	0
11	0	0	0	0	0	0
12	0	0	0	0	1	1
13	0	0	1	0	0	1
14	0	0	0	0	1	1
15	0	0	0	0	0	0
16	0	0	0	0	0	0
17	0	0	0	0	0	0
18	0	0	1	0	0	1
19	0	0	0	0	0	0
20	0	0	0	0	0	0

Part 2

From the simulated results above, I created this probability distribution:

Code

```
X      0    1    2    3 4 5
P(X) 0.5 0.4 0.1 0 0 0
```

Code

```
[1] "The simulated expected number of false positives(mean) is 0.6"
```

Code

```
[1] "The simulated variation of false positives(standard deviation) is 0.680557047378721"
```

Expected value = $0.5 \times 0 + 0.4 \times 1 + 0.1 \times 2 + 0 \times 3 + 0 \times 4 + 0 \times 5 = 0.6$

Standard deviation = $\sqrt{(0-0.6)^2 \times 0.5 + (1-0.6)^2 \times 0.4 + (2-0.6)^2 \times 0.1} = 0.681$

Step 2

To find the mean and standard deviation of $X \times 2100$, I simply multiply the mean and standard deviation by 2100

Code

```
[1] "The simulated expected unnecessary cost(mean) is 1260"
```

Code

```
[1] "The simulated variation of unnecessary costs(standard deviation) is 1429.16979949531"
```

Step 3

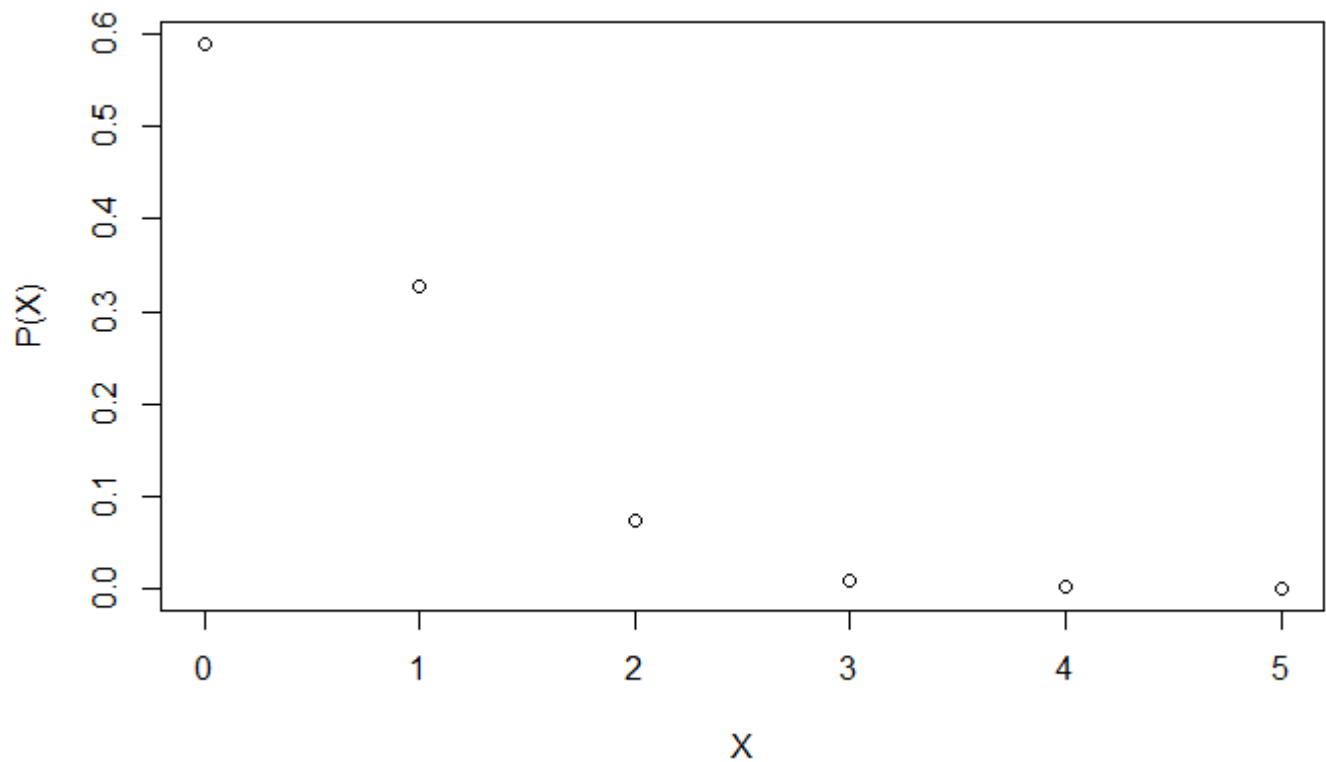
Part 1

I created this probability distribution from the binomial distribution formulas, not a simulation.

Code

X	0	1	2	3	4	5
P(X)	0.59049	0.32805	0.0729	0.0081	0.00045	1e-05

Code



1. It is in the shape of a binomial distribution
2. The expected number of false positives in a group of 5 is 0.5. $5 \times 0.1 = 0.5$
3. They were quite close to each other, with the simulated value being 0.6. This is less than 1/4 standard deviations away.

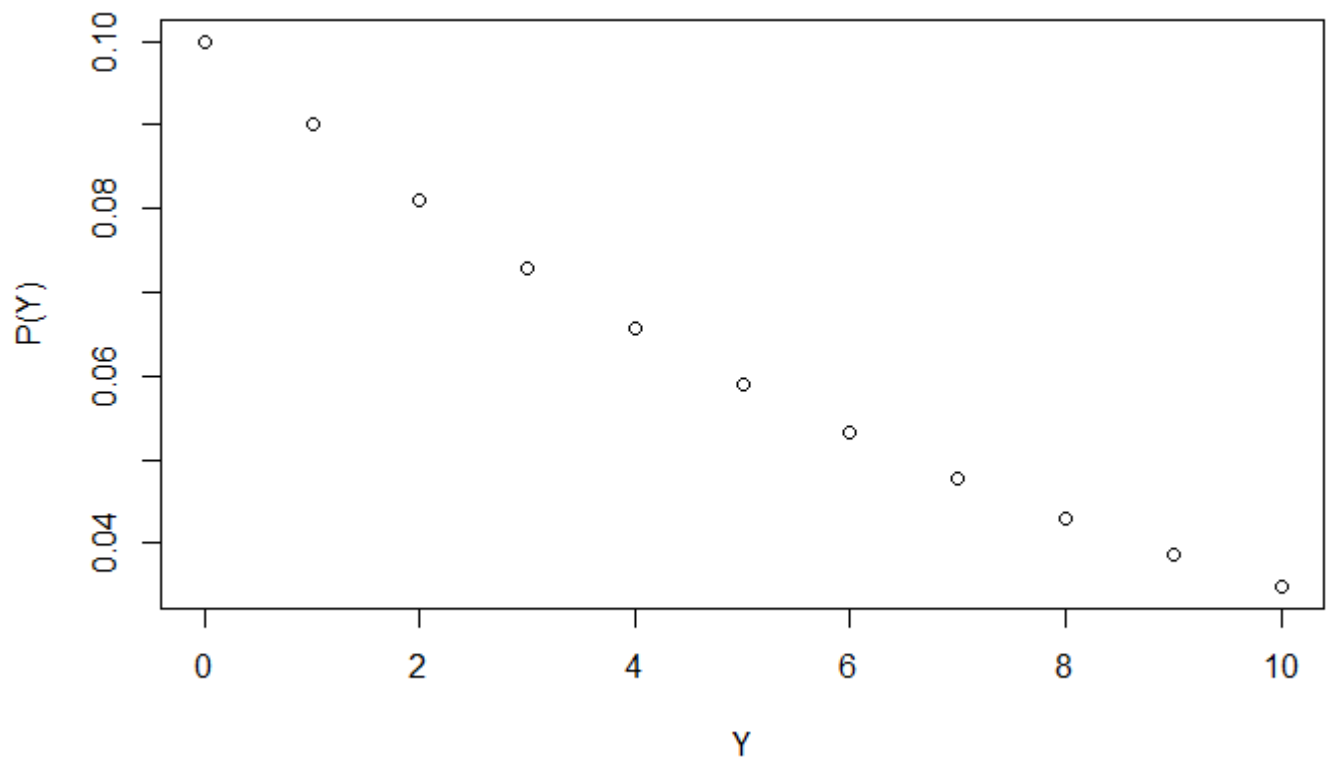
Part 2

This probability distribution is the probability that each trial is the first false positive.

Code

```
Y      0      1      2      3      4      5      6      7      8      9      10
P(Y) 0.1 0.09 0.081 0.0729 0.06561 0.059049 0.0531441 0.04782969 0.043046721 0.0387420489 0.0348
6784401
```

Code



1. It is in the shape of a geometric distribution
2. The expected number of tests to get a false positive is 10. $1/0.1 = 10$

Conclusion

In conclusion, I recommend the Cologuard test. It only has a 10% chance of giving a false positive, thus the expected number of tests before you get a false positive is 10. Also, the predicted unnecessary cost is \$210 per test (\$252 according to simulations), and over 5 tests, \$1050 (\$1260 according to simulations). I'd say that is a reasonable price for detecting colon cancer that could otherwise be fatal.