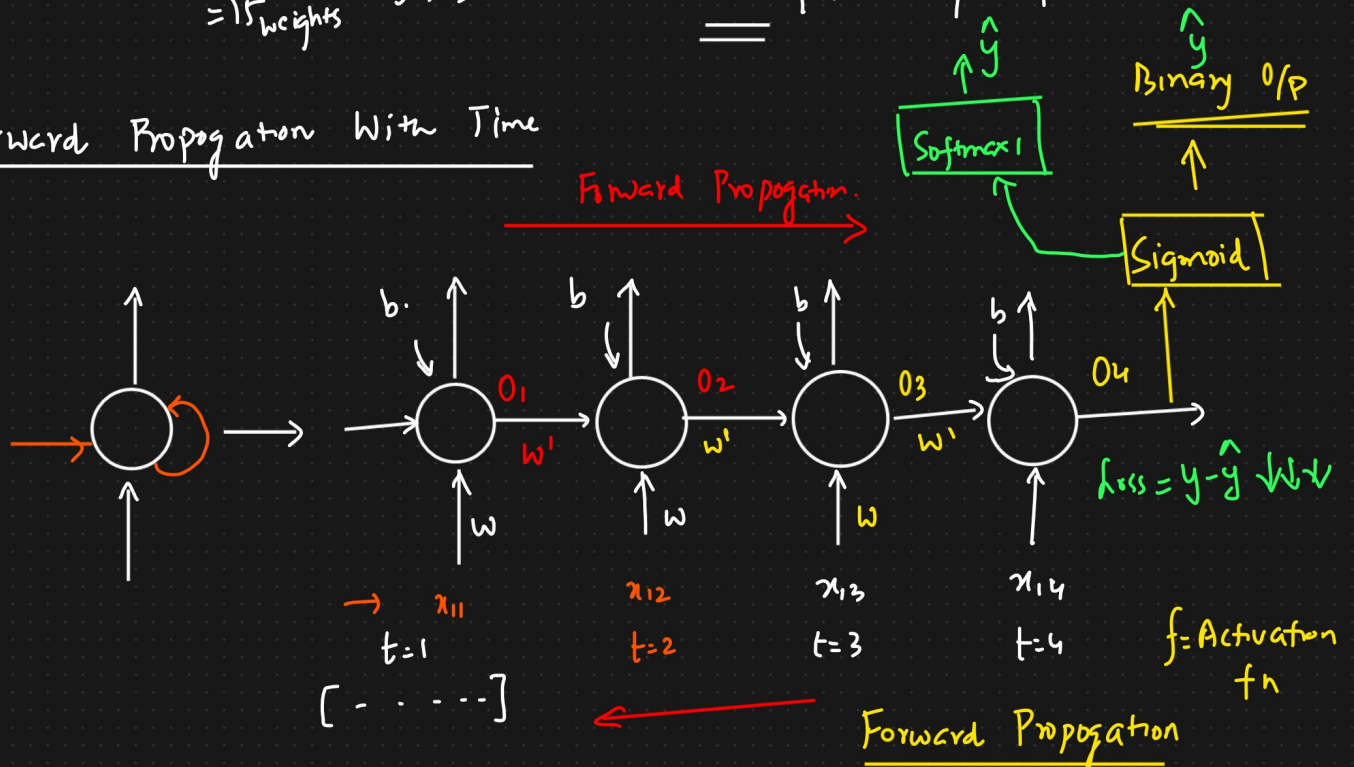


Forward Propagation With Time



Data at

The food is good
 x_{11} x_{12} x_{13} x_{14}

o/p
 1

$$O_1 = f(x_{11} \cdot w + b_1)$$

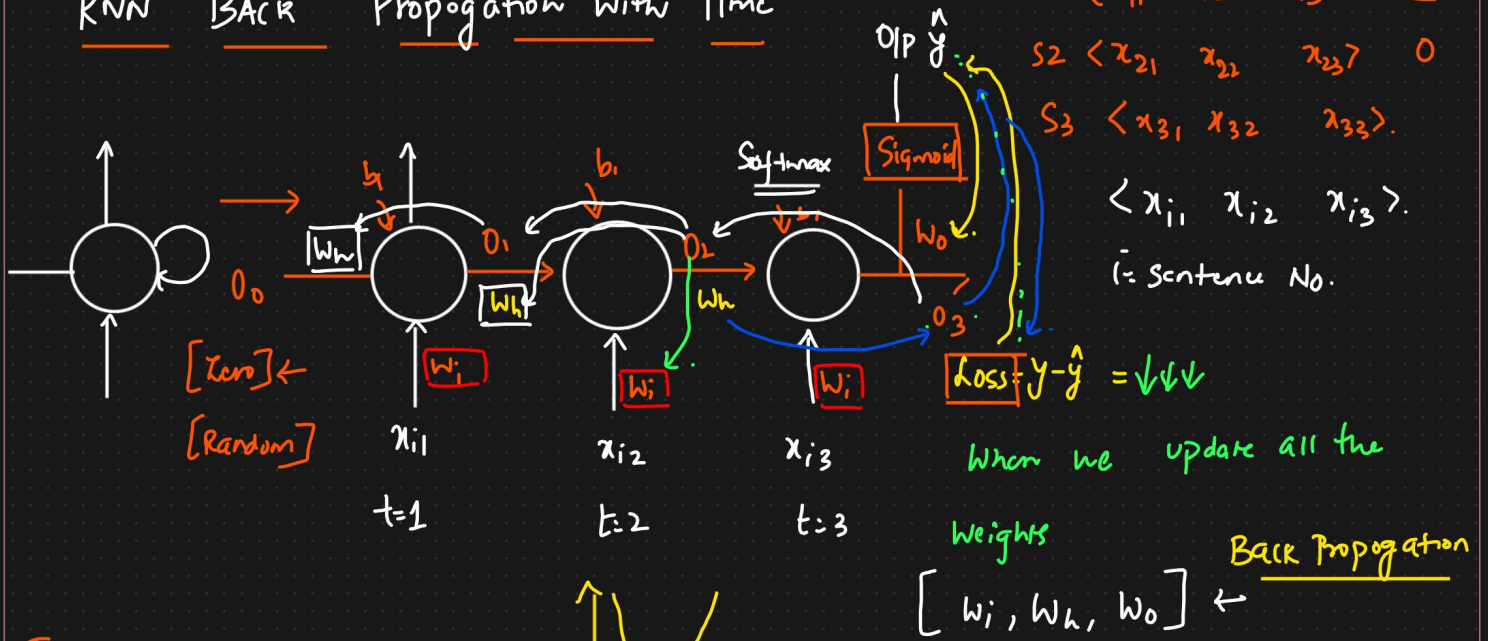
$$O_2 = f(x_{12} \cdot w + O_1 \cdot w' + b_1)$$

$$O_3 = f(x_{13} \cdot w + O_2 \cdot w' + b_1)$$

$$\vdots$$

$$O_n$$

RNN BACK Propagation With Time



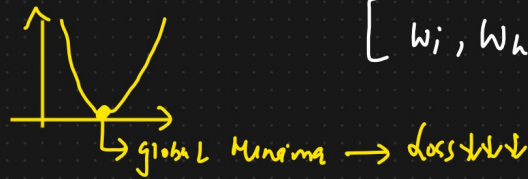
Forward Propagation

$$O_1 = f(x_{11} * w_i + O_0 w_h + b)$$

$$O_2 = f(x_{12} * w_i + O_1 * w_h + b)$$

$$O_3 = f(x_{13} * w_i + O_2 * w_h + b)$$

$$\hat{y} = \sigma(O_3 * w_o)$$



Backward Propagation with Time

Update $[w_i, w_h, w_o]$

Weight update formula

$$w_{\text{new}} = w_{\text{old}} - \eta \left[\frac{\partial L}{\partial w_{\text{old}}} \right]$$

Derivative, slope of
GRADIENT DESCENT

$$\eta = 0.001$$

$$w_{\text{new}} = w_{\text{old}} - \eta \left[\frac{\partial L}{\partial w_{\text{old}}} \right]$$

① Update w_o

Chain Rule of Derivative

$$\frac{\partial L}{\partial w_{\text{old}}} = \frac{\partial L}{\partial \hat{y}} \cdot \frac{\partial \hat{y}}{\partial w_{\text{old}}}$$

② Update w_h . [Hidden layer weights] → Time Stamps

$$w_{h_{\text{new}}} = w_{h_{\text{old}}} - \eta \left[\frac{\partial L}{\partial w_{h_{\text{old}}}} \right]$$

$t=1, 2, 3$

$$\Rightarrow \frac{\partial L}{\partial w_{old}} = \left[\frac{\partial L}{\partial \hat{y}} * \frac{\partial \hat{y}}{\partial o_3} * \frac{\partial o_3}{\partial w_h} \right]_{t=3} + \left[\frac{\partial L}{\partial \hat{y}} * \frac{\partial \hat{y}}{\partial o_3} * \frac{\partial o_3}{\partial o_2} * \frac{\partial o_2}{\partial w_h} \right]_{t=2}$$

$$+ \left[\frac{\partial L}{\partial \hat{y}} * \frac{\partial \hat{y}}{\partial o_3} * \frac{\partial o_3}{\partial o_2} * \frac{\partial o_2}{\partial o_1} * \frac{\partial o_1}{\partial w_h} \right]_{t=1}$$

③ Updating Weights $w_i \rightarrow$ Timestamp

$$w_{new} = w_{old} - \eta \left[\frac{\partial L}{\partial w_{old}} \right] \quad \downarrow \quad \{ \text{update } w_i \text{ weights} \}$$

$$\left[\frac{\partial L}{\partial w_{old}} \right] = \left[\frac{\partial L}{\partial \hat{y}} * \frac{\partial \hat{y}}{\partial o_3} * \frac{\partial o_3}{\partial w_{old}} \right]_{t=3} + \left[\frac{\partial L}{\partial \hat{y}} * \frac{\partial \hat{y}}{\partial o_3} * \frac{\partial o_3}{\partial o_2} * \frac{\partial o_2}{\partial w_{old}} \right]_{t=2}$$

$$+ \left[\frac{\partial L}{\partial \hat{y}} * \frac{\partial \hat{y}}{\partial o_3} * \frac{\partial o_3}{\partial o_2} * \frac{\partial o_2}{\partial o_1} * \frac{\partial o_1}{\partial w_{old}} \right]_{t=1}$$

