FEATURE BASED ADAPTIVE MOTION MODEL

by

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Abstract

We present a method to learn and adapt the motion model. The motion model can be influenced by environmental properties and is a crucial part of the navigation system.Examples are the drift that is accounted in the motion model can be different for carpets and tiles. The AUV can have a change in their motion model when they are moving from fresh water to sea water. Our algorithm is based on the Expectation Maximization Framework which help us to learn the right parameters for the model. The Expectation Step is completed by particle filtering and smoothing. The Maximization step involves finding the parameters for the model.We use side sonar images to extract landmarks which can gives us position estimates to help us evolve our motion model.This leads to a better position estimate of the robot. We found that the our learning motion model adapted well to the change in parameters and had low localization error compared to static motion model. This algorithm eliminates the need for laborious and hand-tuning calibration process. The main significance of learning the motion model is to have better navigation algorithms and also its a step towards robots being able to adapt to environment without human intervention. We validate our approach by recovering a good motion model when the density,temperature of the water is changed in our simulations.

Acknowledgements

Thanks to all the little people who make me look tall.

Chapter 1

Introduction

1.1 Motivation

The core of human environment interaction is the ability of a person to know its position in surrounding environment. The process of estimating the robots position and orientation in the world is termed as Localization [20]. A common approach to determine the location of a robot is through the use of Global Positioning System (GPS), a segries of satellites in low earth orbit that use differential positioning to determine a location for a receiver. Another approach is to provide a prior map of the environment and with help of sensors a robot perceives the world and localizes itself in it. An additional challenge to the localization is when sensing of the external environment is impossible or incomplete due to unreliability and inaccessibility of the sensors. In this case the localization estimate can be updated using self-generated cues such as acceleration and velocity.

An example for such a scenario from underwater robotics is maintaining a pose estimate of an Autonomous Underwater Vehicle, such as Hugin 4500 (Figure 1.1). In AUV the pose estimation relies on Inertial Navigation Systems (INS) which gives an estimate of the velocity, position and orientation. All INS systems suffer from drift i.e. small errors in measurement of acceleration and angular velocity are integrated into progressively larger error. To compensate for the drift systems such as Doppler Velocity Log (DVL), surface GPS etc. are used [12] [14]. Hegrenaes et al [?] pointed out that there are situations where these systems fail or readings from these sensors need to be discarded due to poor quality. An example of such a situation is the non-feasibility of the vehicle to surface. In such situations they proposed to use the self-generated velocity estimates to aid INS systems.

The estimates can be difficult to acquire and maintain due to uncertainties in way a robot interacts and senses its environment. These uncertainties can arise due to noisy and incomplete sensing of the environment, uncertain movements of a robot
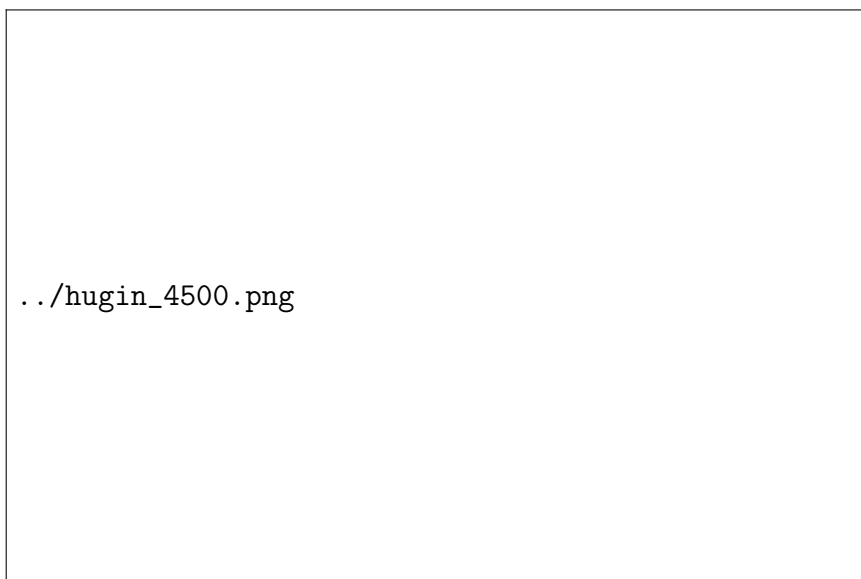
Figure 1.1: Hugin 4500 autonomous underwater vehicles. When submerged, the vehicle uses dead reckoning, incorporating DVL and compass input to maintain an estimate on current positioning.

in the environment and changes in the environment itself. To address these issues Sebastian Thrun [20] represented the motion and sensor models probabilistically. He defines it as instead of relying on single best guess as to what might be the case, probabilistic algorithms represent the information by probability distributions over a whole space of guesses. To update the state of a robot probabilistically there are algorithms such as Kalman Filter [11], Particle Filter [8] etc. which are based on Bayes filter.

In probabilistic robotics the motion and sensors models are represented by a distribution which is defined by its parameters. The process of determining parameters to kinematic model is termed as calibration [?] [21]. Generally the parameters to the models are hand tuned and are derived by conducting calibration experiments. Such calibration methods are impractical for two reasons. Firstly these processes are labour intensive and require prior information about the environment and robot. Secondly, changes in robot (e.g.-: general wear and tear) and environment (e.g.-: moving from fresh water to sea water). The changes in underwater environments can be due to change in density, temperature etc. of water. These changes require recalibration of

a robot while it is in operation which in most cases is not possible to do. The inaccuracies in the models will effect results for higher level tasks such as path planning [13], Simultaneous Localization and Mapping (SLAM) [20] [9] etc.

Roy and Thrun [17] proposed an online calibration method for land robots which can be performed without human intervention. They approached the calibration process as maximum likelihood estimation problem which gives an estimate of parameters for the given data. The calibration parameters are iteratively estimated by comparing pair of subsequent sensor readings. The algorithm proposed worked well for systematic drifts and the results showed the position error reduced by approximately by 83

Alizar and Parr [6] continued the work further by estimating non-systematic drifts. They proposed an algorithm to learn the right parameters of a motion model for a land robot using Expectation Maximization Framework [3]. It is an unsupervised machine learning technique that alternated between the expectation and maximization step. In the Expectation Step it creates an expectation of the log-likelihood using the current estimate of the parameters and the Maximization step which computes parameters maximizing the expected log-likelihood found in the Expectation Step. They were able to learn accurate motion models with very little user input.

Yapp [22] took Alizar and Parr [6] work further and proposed an algorithm to learn the motion and sensor models for land robots. They used the same Expectation Maximization framework to learn the right parameters for the models. To calculate the like trajectory of a robot both the algorithms implemented particle filtering [15] [2] and smoothing [4]. The algorithm started with an estimate of initial parameters and iteratively optimized the parameters based on the data collected during robots operation. The algorithm assumed that a prior map of the environment is provided.

In my thesis I specifically deal with water environments such as oceans, rivers etc. which are highly dynamic. The algorithm proposed here is different from the work done before in two ways. Firstly the algorithm is meant to learn the right parameters for an AUVs motion model. Secondly, the algorithm can learn motion model for unknown environments by generating landmarks using side sonar images and therefor doesnt have to rely on static maps. Sound Navigation and Ranging (SONAR) is a technique based on sound propagation used for detecting objects underwater. Side

scan sonar is a specific type of sonar used to image the topography of a sea floor. The SONAR sensor is the only imaging tool that can work at high depth.

My algorithm uses EM algorithm to calculate the most likely parameters for a data set. The trajectories are calculated by implementing particle filtering and smoothing. Particle Filters are chosen because they can mode non-linear transformations as well as have no restrictions in model. Particle smoothing was performed because Russel and Norving [refer] pointed out that the state of the system is better estimated by smoothing as it incorporates more information that just filtering.

The remainder of the thesis is structured as follows. Chapter 2 will explain the motion model for AUV as well as give an insight on particle filtering and smoothing. Chapter 3 will give an overview of Expectation Maximization and show how this framework is used to adapt parameters for a motion model. Chapter 4 will give explain how landmarks are extracted from side sonar images. The reliability of the landmarks are shown by extracting motion information and the algorithm to do that is described in Chapter 4. Chapter 5 consist results of a simulated experiment to show the effectiveness of the algorithm. This chapter also includes the comparison of motion estimation using side sonar images to DVL.

1.2   Contributions

The main contributions of the algorithm are-:

1) **Adaptive Motion Model**-: The motion model for AUVs adapt to changing environment. This automated process of calibration of the robots lead to no hand tuning of the models and gives us an online process which can be preformed during the robot's mission.

2) **Motion Estimation from Side Sonar Images**-: We present an approach to estimate the movement from side sonar images which can be coupled with existing motion model and can improve localization. It can be easily be performed on-board as limited amount of interest points are used which lead to lesser computation and memory usage.

Chapter 2

Background

In the chapter we start by discussing how motion models are probabilistically represented as well as give an insight about motion models for AUV. This helps us in understanding on how motion model captures the probabilistic movements of robots. We then discuss a probabilistic state estimation algorithm such as particle filter [15] [2] which is at the heart of my algorithm as well as many other robotics systems. Lastly we discuss about particle smoothing [4] [5] which gives an estimate of ground truth by calculating the distribution of past states with taking into account all the evidence up to present.

2.1   Motion Model

A motion model is responsible for capturing the relationship between the control input and the change in robot's configuration. Thrun [20] models the motion of a robot probabilistically because the same control inputs will never reproduce the same motion. A good motion model will capture the errors such as drift that are encountered during the motion of the robot. The motion model is a necessary ingredient of many algorithms such as localization,mapping etc.

Let $X = (x, y, \theta)$ be the initial pose of the robot in x-y space. Mathematically the motion model can be described as $P(X'|X, u)$, where X' is the pose after executing the motion command u. Based on the control input Thrun [20] divided the motion model in two classes 1) Odometry based motion model 2) Velocity based motion model.

The first class of motion models are used for robots equipped with wheel encoders. Odometry is generally obtained by integrating wheel encoders information and is more accurate than velocity. Velocity based models calculate the new position based on velocities and time elapsed. These models are implemented for Autonomous Underwater Vehicle(AUV) and Unmanned Aerial Vehicles(UAV). Both odometry as well as

velocity suffer from drift and slippage therefore the same control commands will not generally produce the same motion and the motion model $P(X'|X, u)$ is represented as probability distribution.

The velocity motion model proposed by Thrun [20] assumes that robot can be controlled through two velocities a rotational and translational velocity. The translational velocity at time t is denoted by v_t and rotational velocity by w_t. Hence the control input u_t can be represented by

$$u_t = \begin{pmatrix} v_t \\ w_t \end{pmatrix}$$

The assumption is that positive rotational velocities w_t induce a counterclockwise rotation whereas positive translational velocities v_t correspond to forward motion. The set of equations to compute the next state of a robot for a velocity motion model are

$$x_t = x_{t-1} + V_{t-1}/W_{t-1} \sin(\theta_{t-1}) + V_{t-1}/W_{t-1} \cos(\theta_{t-1} + W_{t-1}\delta t) \qquad (2.1)$$

$$y_t = y_{t-1} + V_{t-1}/W_{t-1} \cos(\theta_{t-1}) - V_{t-1}/W_{t-1} \sin(\theta_{t-1} + W_{t-1}\delta t) \qquad (2.2)$$

$$\theta_t = \theta_{t-1} + W_{t-1}\delta t \qquad (2.3)$$

In an AUV a velocity motion model is implemented and to represent AUV's motion, 6 independent coordinates are necessary to determine the position and orientation of the rigid body. The notations used for marine vehicles are described in Table 2.1.

The pose of AUV can be represented as $s = (x, y, z, \theta, \phi, \psi)$. The first three coordinates correspond to the position along the x,y,z axes while the last three coordinates describe the orientation. Fossen [19] in his book describes the motion of a marine vehicle in 6 DOF using two coordinate systems as shown in Figure 2.1. X_0, Y_0, Z_0 represent the moving coordinate frame and is called as body-fixed reference frame. The earth-fixed reference frame is denoted by X, Y, Z. The origin of the body-reference frame is denoted by O and is chosen to coincide with the center of gravity denoted by CG.

DOF		forces and moments	linear and angular vel.	positions and Euler angles
1	motions in the x-direction (surge)	X	u	x
2	motions in the y-direction (sway)	Y	v	y
3	motions in the z-direction (heave)	Z	w	z
4	rotation about the x-axis (roll)	K	p	ϕ
5	rotation about the y-axis (pitch)	M	q	θ
6	rotation about the z-axis (heave)	N	r	ψ

Table 2.1: Notation used for marine vehicles. Table from [19]

To estimate the position of an AUV we need to calculate the velocity at which the AUV is currently moving. The velocity can be computed in two ways-: 1) Static Motion model 2) Dynamic Motion model

Hegrenaes [10] points that a way to implement a simple static motion model as table look-up based on experimental data.

$$u_r = f(n_s) \tag{2.4}$$

u_r, n_s are the water relative linear velocity in x direction and control system set point respectively. In a similar manner an expression can be established for v_r.

Another way to implement the motion model is through dynamics. The 6 Degrees of Freedom (DOF) rigid body equations of motion described by Fossen [19] are

$$X = m[\dot{u} - vr + wq - x_G(q^2 + r^2) + y_G(pq - \dot{r}) + z_G(pr + \dot{q})] \tag{2.5}$$

$$Y = m[\dot{v} - wp + ur - y_G(r^2 + p^2) + z_G(qr - \dot{p}) + x_G(qp + \dot{r})] \tag{2.6}$$
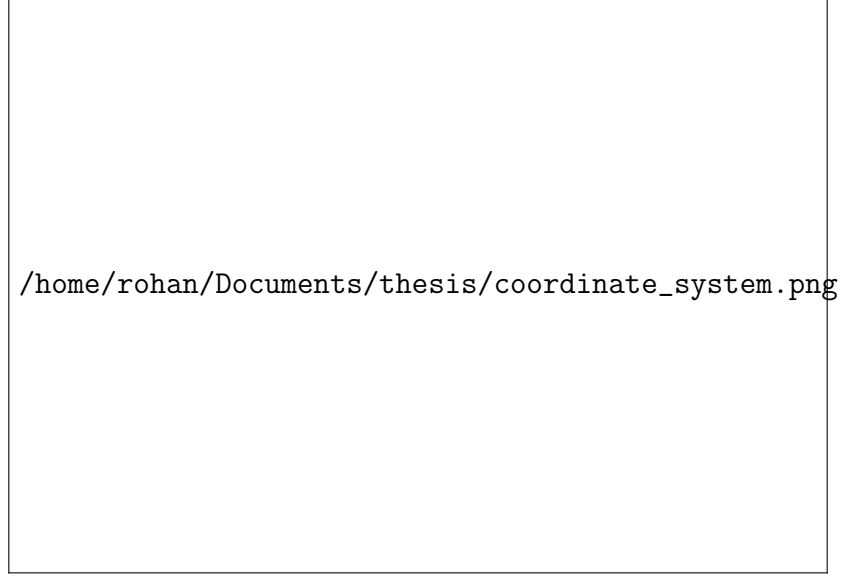
Figure 2.1: Body-fixed and earth-fixed reference frames. Figure from [19]

$$Z = m[\dot{w} - uq + vp - z_G(p^2 + q^2) + x_G(rp - \dot{q}) + y_G(rq + \dot{p})] \qquad (2.7)$$

$$K = I_x\dot{p} + (I_z - I_y)qr - (\dot{r} + pq)I_{xz} + (r^2 - q^2)I_{yz} + (pr - \dot{q})I_{xy} + m[y_G(\dot{w} - uq + vp) - Z_g(\dot{v} - wp + ur)] \qquad (2.8)$$

$$M = I_y\dot{q} + (I_x - I_z)rp - (\dot{p} + qr)I_{xy} + (p^2 - r^2)I_{zx} + (qp - \dot{r})I_{yz} + m[y_G(\dot{u} - vr + wq) - z_g(\dot{w} - uq + vp)] \qquad (2.9)$$

$$N = I_z\dot{r} + (I_y - I_x)pq - (\dot{q} + rp)I_{yz} + (q^2 - p^2)I_{xy} + (rq - \dot{p})I_{zx} + m[x_G(\dot{v} - wp + ur) - y_g(\dot{u} - vr + wq)] \qquad (2.10)$$

The equations described above can be expressed in a more compact form:

$$M_{RB}\dot{\mathcal{V}} + C_{RB}(\mathcal{V})\mathcal{V} = \tau_{RB} \qquad (2.11)$$

Here $\mathcal{V} = [u, v, w, p, q, r]^T$ is the body fixed linear and angular velocity and $\tau_{RB} = [X, Y, Z, K, M, N]$ is generalized vector of external forces and moments. M_{RB} is the rigid body inertia matrix and C_{RB} is Coriolis and centripetal matrix.

The right hand side of the vector 2.11 represents the external forces and moments acting on the vehicle. Fossen [19] classifies the forces into 1) Radiation-induced forces 2) Environmental Forces 3) Propulsion Forces

τ_{RB} can be represented as the sum of these forces.

$$\tau_{RB} = \tau_H + \tau_E + \tau \tag{2.12}$$

Here τ_H is the radiation induced forces and moments, τ_E is used to describe the environmental forces and moments and τ is the propulsion forces and moments. Equations 2.11 and equation 2.12 can be combined to yield the following representation of 6 DOF dynamic equations of motion:

$$M\mathcal{V}^{\cdot} + C(\mathcal{V})\mathcal{V} + D(\mathcal{V})\mathcal{V} + g(\eta) = \tau_E + \tau \tag{2.13}$$

where

$M \triangleq M_{RB} + M_A \; ; \; C(\mathcal{V}) \triangleq C_{RB}(\mathcal{V} + C_A(\mathcal{V})$

M_A is the added inertia matrix $C_A(\mathcal{V})$ is the matrix of hydrodynamic Coriolis and centripetal terms. $g(\eta)$ is the restoring force.

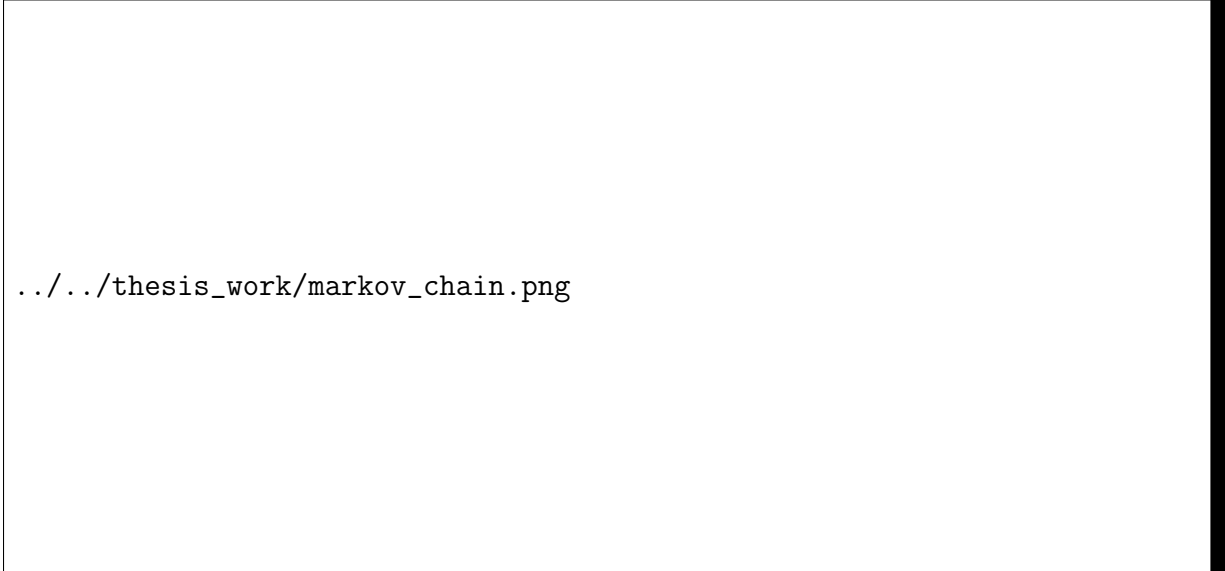Lammas [12] pointed out that navigation equation of an underwater vehicle is-:

$$\mathcal{V}^{\cdot} = M^{-1}(\tau - C(\mathcal{V})\mathcal{V} - D(\mathcal{V})\mathcal{V} - g(\eta)) \tag{2.14}$$

$\mathcal{V}^{\cdot}$ can be integrated with time to get velocity.

In the static model the velocity is calculated from a lookup table. In the other model we are computing forces and moments on the fly but the parameters to these forces are considered to be static. The parameters such as density, temperature etc of water can change with time and lead to an inaccurate estimate of velcoity in both the models. Hence the velocity needs to be adapted and Chapter **??** explains how it is done in my algorithm.

2.2   Particle Filter

Particle Filter is a state estimation algorithm based on a sampling method for approximating a distribution. Thrun [20] defines particle fitler as an alternative non-parametric implementation of the Bayes filter. It also can be called as a Sequential

../../thesis_work/markov_chain.png

Figure 2.2: A temporal Bayesian model with hidden states x_t, observations z_t and controls u_t. Figure taken from [20]

Monte Carlo(SMC) algorithm. The first attempt to use SMC was seen in simulations of growing polymers by M.N Rosenbluth and A.W. Rosenbluth [16]. Gordon et al. [8] provided the first true implementation of sequential monte carlo algorihtm.

Thrun [20] stated that the key idea behind particle filter is to represent the posterior bel(x_t) by a set of random state samples drawn from this posterior. Instead of representing the distribution by a parametric form particle filter represents a distribution by a set of samples drawn from this distribution. In Figure 2.3 the belief if represented by a set of particles. The representation is a approximation but it is nonparametric and therefore there are advantages of using particle filters as an alternative to Extended Kalman Filter and Unscented Kalman Filter. Particle Filters can represent a broader space of distributions for example non-Gaussian and can model non linear transformations of random variables. In Figure 2.3 particle filters are shown to model non-linear transformations.

The objective of particle filters is to estimate the state of the system given the observation variables. They are designed for Hidden Markov Models(Fig 2.2, where the system consists of hidden and observed variables. In this model the state x_t is the hidden random variable as it is not directly observed. The state at time t is only dependent upon the state at time $t-1$ and external influences such as control u_t. The

/home/rohan/Documents/thesis_work/particle_filter_non_gaussian_thru
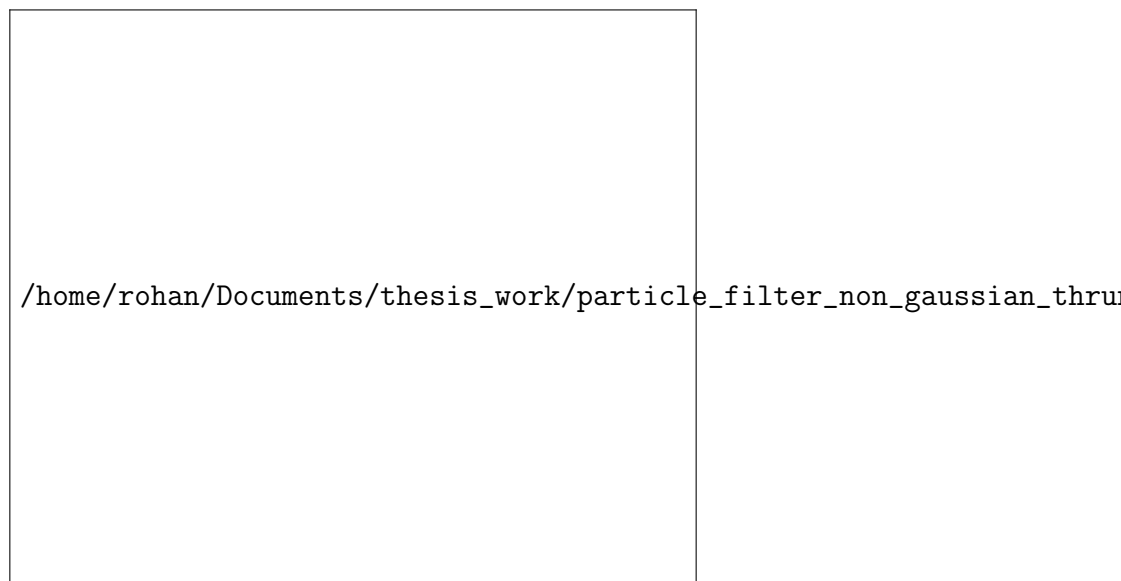
Figure 2.3: The "particle" representation used by particle filters. The lower upper right graphs shows samples drawn from a Gaussian random variable, X. These samples are passed through the nonlinear function shown in the upper right graph. The resulting samples are distributed according to the random variable Y. Figure taken from [20]

measurement z_t depends on the state at time t. The knowledge about the influence of the control on the system can be used to calculate a new expected location and the measurement can be combined in a Bayesian way.

The algorithm for particle filters is described below-:

Input: X_{t-1}: particle set

u_t: most recent control

z_t: most recent measurement

Output: X_t:particle set

begin

> **for** *m=1 to M do* **do**
> | sample x_t^m $p(x_t|u_t, x_{t-1}^m)$ $w_t^m = p(z_t|x_t^m)$ $X_t^- = X_t^- + (x_t^m, w_t^m)$
> **end**
>
> **for** *m=1 to M do* **do**
> | draw i with probability $\propto w_t^{[i]}$
> | add $x_t^{[i]}$ to X_t
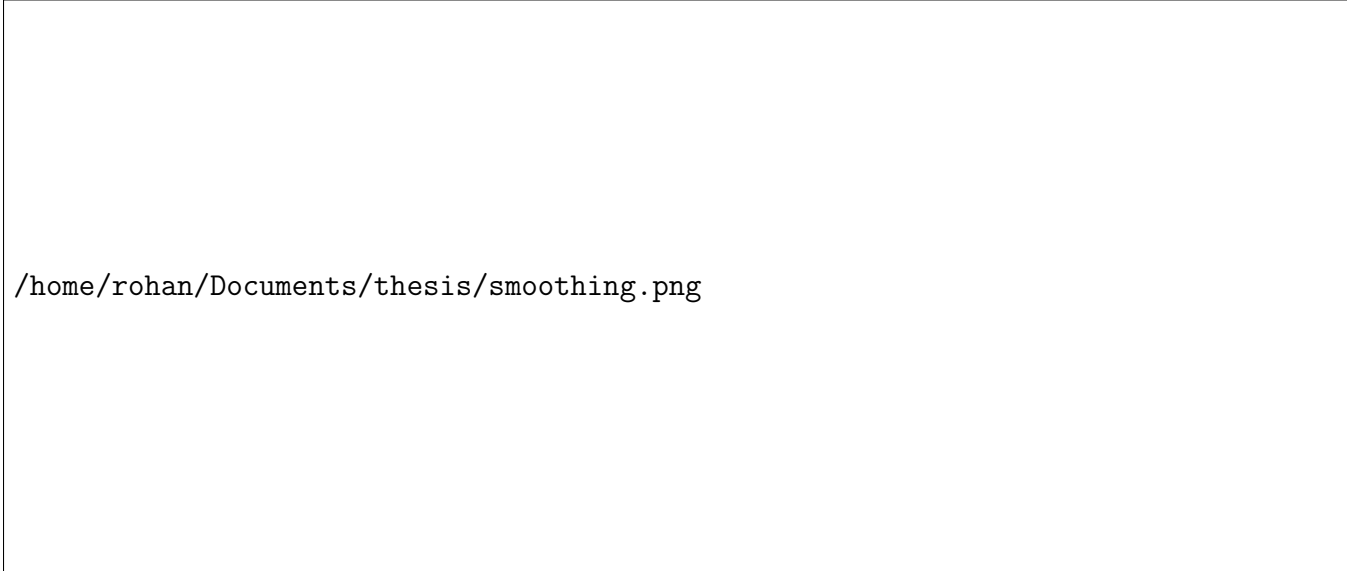> **end**
>
> return X_t

end

Algorithm 1: Particle Filter Algorithm. Algorithm taken from [20]

In algorithm 1 each particle x_t^m is instantiation of the state at time t. The first step is to generate a hypothetical state x_t^m for time t based on previous state x_{t-1}^m and control u_t. The particles are samples from the state transition distribution $p(x_t|u_t, x_{t-1})$. The importance factor for each particle x_t^m is calculated and denoted by w_t^m. Importance factor is defined as the probability of measurement z_t under the particle x_t^m. Thus importance factor are used to incorporate the measurements into the particle set. In practice, the number of particles used are a large number(e.g.-:1000).

The key part of the algorithm is the re-sampling step in particle filter algorithm. The algorithm draws M particles with replacement from a temporary particle set X_t^-. The probability of drawing the particles is given by the importance factor. The re-sampling step is a probabilistic implementation of the Darwinian idea of survival of the fittest. It refocuses the particle set to regions in state space with high posterior probability.

Particle Filters is an integral part of my algorithm to learn the right parameters of the motion model and the way it is used is explained in 3.2.2.

/home/rohan/Documents/thesis/smoothing.png

Figure 2.4: Smoothing computes $P(X_k|e_{1:t})$, the posterior distribution of the state at some past time k given a complete sequence of observations from 1 to t. Figure taken from [18]

.

2.3   Particle smoothing

The particle filter algorithm as described before is the first step in the Expectation process. The next algorithm that completes the Expectation Step is the particle smoothing. Doucet [5] in his paper stated that filtering based on observations received up to the current time is used to estimate the distribution of the current state of an Hidden Markov Model (HMM) whereas smoothing is used to estimate distribution of state at a particular time given all the observations up to some later time (Figure **??**). Russel and Norving [18] showed that the state of the system is better estimated by smoothing as it incorporates more information than just filtering. We use particle smoothing algorithm proposed by Teddy N Yap and Christian R. Shelton [22] which was based on the technique presented by Docuet et al. [4] and Godsill et al. [7].

Particle smoothing is carried out in order to generate samples from the entire joint smoothing density $p(x_{0:T}|u_{1:T}, z_{1:T})$. The equations described by Yapp [22] are

$$p(x_{0:T}|u_{1:T}, z_{1:T} = \prod_{t=0}^{T} p(x_t|x_{t+1:T}, u_{1:T}, z_{1:T}) \tag{2.15}$$

where,

$$
\begin{aligned}
p(x_t|x_{t+1:T}, u_{1:T}, z_{1:T}) &= p(x_t|x_{t+1}, u_{1:t+1}, z_{1:t}) && (2.16) \\
&= \frac{p(x_{t+1}|x_t, u_{1:t+1}, z_{1:t})p(x_t|u_{1:t+1}, z_{1:t})}{p(x_{t+1}|u_{1:t+1}, z_{1:t})} && (2.17) \\
&= \frac{p(x_{t+1}|x_t, u_{t+1})p(x_t|u_{1:t}, z_{1:t})}{p(x_{t+1}|u_{1:t+1}, z_{1:t})} && (2.18) \\
&\alpha \;\; p(x_{t+1}|x_t, u_{t+1})p(x_t|u_{1:t}, z_{1:t}) && (2.19)
\end{aligned}
$$

Equation 2.19 is used to generate states backwards in time give future states. $p(x_{t+1}|x_t, u_{t+1})$ is the state transition probability and $p(x_t|u_{1:t}, z_{1:t})$ is obtained by peforming partilce filtering.

Algorithm 2 shows the step involved to sample from the entire joint smoothing density.

Input: $X_t, t = 0, 1, ..., T$: particle approximations to the posterior pdfs

$p(x_t|c_{1:t}, s_{1:t}), t = 0, 1, .., T$

$c_{1:T} = (c_1, c_2, ..., c_T)$: set of controls from time 1 to time T

Output: $x'_{0:T} = (x'_0, x'_1, ..., x'_T)$: a sample from the entire joint smoothing

density $p(x_{0:T}|c_{1:T}, s_{1:T})$

begin

    draw i with probability $\propto w_T^{[i]}$ $x'_T \leftarrow x_T^{[i]}$

    for $t \leftarrow T - 1$ *down to 0 do* **do**

        for $i \leftarrow 1 to N_s$ *do* **do**

            $w_{t|t+1}^{[i]} \leftarrow w_t^{[i]} p(x'_{t+1}|x_t^{[i]}, u_{t+1})$

        end

        draw i with probability $\propto w_{t|t+1}^{[i]}$

        $x' \leftarrow x_t^{[i]}$

    end

end

Algorithm 2: Sample the entire joint smoothing density $p(x_{0:T}|c_{1:T}, s_{1:T})$

In the first step of the algorithm a particle is drawn with probability proportional to the filtered weight of the particles. The next step is to move a time step back and modify the weights of the particles by calculating the new smoothed weights. The new smoothed weights are the product of state transition probability $p(x'_{t+1}|x_t^{[i]}, u_{t+1})$ and the weight of the particle $w_t^{[i]}$. The next step in the algorithm is to draw particles with

probability proportional to new smoothed weights $w^{[i]}_{t|t+1}$. The sequence of particles x' drawn from joint smoothing density $p(x_{0:T}|c_{1:T}, s_{1:T})$ from time 0 to time T form a sampled trajectory $x'_{0:T} \triangleq (x'_0, x'_1, ..., x'_T)$.

Chapter 3

Learning the motion model

3.1 Introduction

3.1.1 Work done so far on learning motion model

The process of calibration has been discussed right from when robotics was introduced and the literature is full of different methods to calibrate a robot (eg-: [**?**] [21]). Virtually all the methods discussed before Roy's work [17] required human intervention and assumed the world to be static. These methods required a human to have experience and a device to measure the exact movement of a robot to calibrate. The most important assumption that these methods made was that the physics of a robot never changed and operated in a static environment.

Roy and Thrun first proposed an online self-calibration method [17] in 1999 that adapted to changes that occurred during the lifetime of a robot. The algorithm was designed for land robots where the final pose was given by equations described below

$$x^{'} = x + Dcos(\theta + T)y^{'} = y + Dsin(\theta + T)\theta^{'} = (\theta + T)mod2\pi \qquad (3.1)$$

D and T are the true translational and rotation of a robot. The measured translational and rotational is d and t and if robot's odometry is accurate then $D = d$ and $T = t$. In practice there is a difference and Roy represents D and T by equations 3.2 and 3.3 respectively.

$$D = d + \sigma_{trans}d + \epsilon_t rans \qquad (3.2)$$

$$T = t + \sigma_{rot}d + \epsilon_{rot} \qquad (3.3)$$

$\epsilon_t rans$ and ϵ_{rot} are the random variables with zero mean. σ_{trans} and σ_{rot} are the systematic error, drift. The algorithm they propose is used to estimate σ_{trans} and σ_{rot}

using sensor data collected throughout robot's motion. They treat the problem as maximum likelihood estimation problem where the parameters are estimated under a dataset z (equations 3.4) .

$$(\sigma^*_{trans}, \sigma^*_{rot}) = argmaxP(\sigma_{trans}, \sigma_{rot}|z) \tag{3.4}$$

Austin and Eliazar [6] proposed a different method to achieve the same goals proposed by Roy and Thrun. Their algorithm was different from Roy and Thrun for two reasons. Firstly, Austin ad Eliazar used a more general model which incorporated independence of motion terms. Secondly, the method was able to estimate parameters for non systematic errors as well. The motion model proposed by them to account is described below.

$$\begin{aligned} x^{'} &= x + Dcos(\theta + T/2) \\ y^{'} &= y + Dsin(\theta + T/2) \\ \theta^{'} &= (\theta + T/2)mod2\pi \end{aligned} \tag{3.5}$$

As the turn and drive commands are performed independently therefore to not violate this assumption this model makes T reasonably small and it is absorbed as part of noise. To estimate non-systematic errors the true translational(D and rotation(T) are represented by normal distribution with mean d and t and the variance will scale with d^2 and t^2 as shown in equation 3.6

$$\begin{aligned} D &\sim \mathcal{N}(d\mu_{D_d} + t\mu_{D_t}, d^2\sigma^2_{D_d} + t^2\sigma^2_{D_t}) \\ T &\sim \mathcal{N}(d\mu_{T_d} + t\mu_{T_t}, d^2\sigma^2_{T_d} + t^2\sigma^2_{T_t}) \end{aligned} \tag{3.6}$$

where μ_{A_b} is the coefficient for the contribution of odometry term b to the mean of the distribution over A. The algorithm is used to learn these set of mean and variances.

The method by Austin an Eliazar used Expectation Maximization framework to learn the parameters of the motion model for land robots. In the E step particle filtering and smoothing were performed to get a set of trajectories. In M step the maximum likelihood values of parameters given the trajectories was calculated. Teddy Yapp [22] used the same framework and learned parameters for motion as well as sensor model of land robots (Figure). They adopted the same motion model by with slight different noise model as shown in equation 3.7.
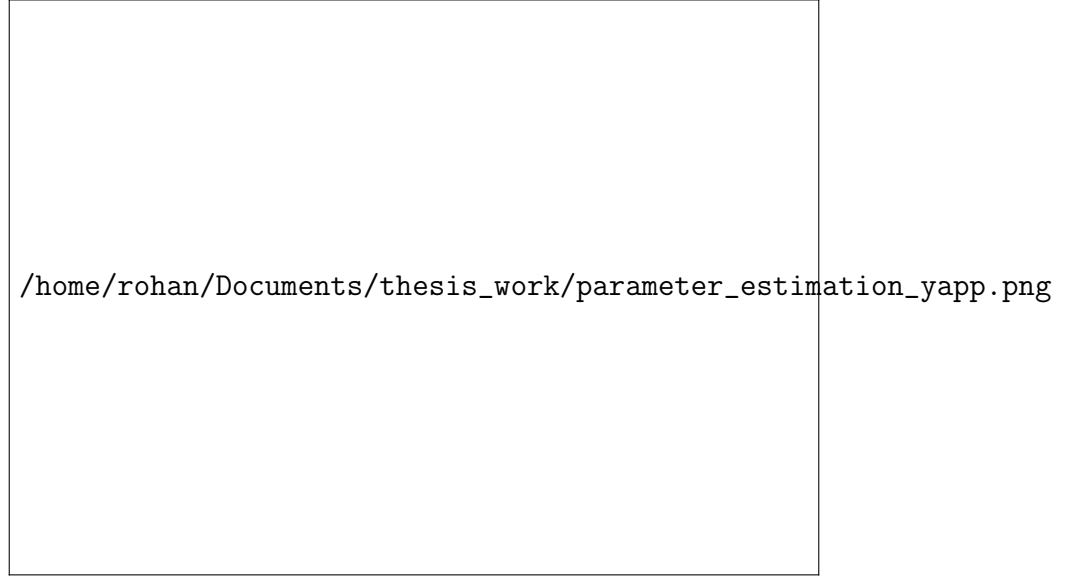
Figure 3.1: Block Diagram for the parameter estimation framework. Figure taken from [**?**].

$$
\begin{aligned}
D &\sim \quad \mathcal{N}(d, d^2\sigma_{D_d}^2 + t^2\sigma_{D_t}^2 + \sigma_{D_1}^2) \\
T &\sim \quad \mathcal{N}(t, sigma_{T_d}^2 + t^2\sigma_{T_t}^2 + \sigma_{T-1}^2)
\end{aligned}
\tag{3.7}
$$

The extra constant terms σ_{D_1} and σ_{T_1} are added to account for the errors that are not proportional to the translation or rotation of a robot.

All the work above was done to calibrate our models and Hegrenaes [**?**] in his work showed the importance of motion model for navigation in underwater vehicle. The proposed an novel approach for navigation systems in which knowledge about the vehicle dynamics was used to aid the Inertial Navigation System(INS). The new navigation system was tested on real dataset collected by an AUV.

For navigation in AUV velocity of the vehicle needs to be estimated and sensors such as IMU, DVL etc. are used. In a traditional INS system the key component is an IMU and a set of navigation equations. The reading from accelerometer and gyroscope are integrated to get an estimate of velocity, position and orientation. The reading from such sensors consist of inherent errors and leads to drift in the INS system. Generally sensors such as surface GPS, DVL etc. are an aiding system to the INS (Figure **??**). Combination of such as system leads to better estimate of velocity, position and orientation [14].

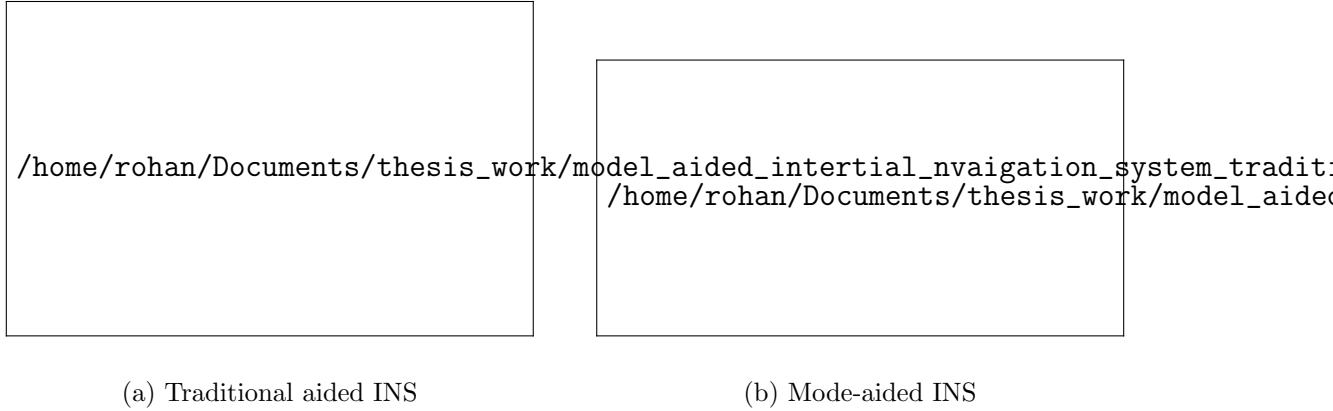(a) Traditional aided INS   (b) Mode-aided INS

Figure 3.2: High level system outline. The vehicle model can be used in parallel to external aiding sensors. Figure taken from [**?**]

Hergreanaes points out an alternative velocity information such as velocity estimate through vehicle dynamics is required because there are situations where it is not possible for the AUV to surface and get a GPS reading or DVL measurement needs to be discarded due to poor quality. The high level system outline for such a model is shown in Figure 3.2(b).

The system is very similar to traditional INS except that the vehicle model output in also integrated to the system. The vehcile model output doesn't require any extra instruments therefore can be easily applied to any vehicle. An alternative velocity estimate aids the INS where DVL readings are lacking as well as gives redundancy to the system.

All the above calibration methods are designed for odometric based motion models and for land robots. The use of vehicle model to aid the INS for navigation purposes shows us the importance of an adaptive motion model. The algorithm that I propose is for underwater vehicles and velocity based motion model. The process to adapt the motion model is similar to the previous work by Yapp and Eliazar and our approach is described in rest of the chapters.

3.1.2 General Architecture

In this section we give an overview of the system and point out the differences in my system(Figure **??**) as compared to the existing system proposed by Yapp [22].

Diagram1.jpeg

Figure 3.3: Block diagram for adapting motion model.

Figure **??** is an outline of the proposed system. The motion and sensor models are initialized with a set of parameters. Given the motion model $p(x_t|x_{t-1}, u_t)$, sensor model $p(z_t|x_t)$ and the pose $p(x_{t-1})$ of a robot we can perform particle filtering using Algorithm 1. It is performed to estimate the pose $p(x_t)$ of a robot at next time step.

The key ingredient to learn the motion model is to have an estimate of ground truth. To get an idea of ground truth particle smoothing (algorithm 2) is performed on the particle set produced by particle filtering. The algorithm can be repeated several times to get a set of trajectories. Particle filtering and smoothing are the key algorithm for the Expectation Step.

The reported translational and rotational movement of a robot is recorded for every time step. Based on the trajectories and reported movements the errors are calculated at each time step. After we have a set of errors we perform Newton Conjugate gradient on the error function to estimate the set of parameters. This completes the Maximization Step.

The learned parameters are reassigned to the motion model and helps in adapting our model to changes in robot and the environment. The whole algorithm is repeated at every time step so that we can dynamically learn the right parameters.

The system proposed for parameter estimation is similar to the system by Yapp

[22]. I use the same EM framework and conjugate gradient to learn the right parameters for the model. The difference lies that the motion model learned is a velocity based motion model as compared to odometry based model. Secondly we focus on underwater environments and therefore use side sonar images to calculate landmarks on the fly for our sensor model as compared to a static map.

3.2 Adapting Motion Model

3.2.1 Expectation Maximization

Expectation Maximization is an iterative process of finding maximum likelihood of parameters of a model which depend upon hidden variables. It is used to estimate unknown parameters θ given the observed data X. A complete dataset can be represented by X, Z where Z is a non-observed (hidden, latent) variable. In practice a complete dataset is not given and only a set of observations or incomplete dataset X is found. The hidden variables are important to a problem but complicate the learning process [18]. In order to learn with hidden variables Dempster et al. [3] proposed a method to maximize the probability of the parameters θ give the dataset X with hidden variables Z called as EM.

$$\theta^* = argmax_\theta \int p(\theta, Z|X)dZ \tag{3.8}$$

The key idea behind the EM algorithm is to alternate between estimating parameters θ and hidden variable Z. The E step consists of finding the posterior distribution of hidden variables $p(Z|X, \theta^{old})$ given the current estimate of parameters θ^{old}. The posterior distribution it used to find a expectation of the likelihood of the data for some parameter θ as shown in equation **??**.

$$\mathcal{Q}(\theta, \theta^{old}) = \sum_Z p(Z, X|\theta^{old}) \ln p(X, Z|\theta) \tag{3.9}$$

In the M step we maximize the function as shown in to estimate the new parameters θ^{new}.

$$\theta^{new} = argmax_{theta} \mathcal{Q}(\theta, theta^{old}) \tag{3.10}$$

The objective as described by Minka [**?**] is to maximize $\mathcal{Q}(\theta, \theta^{old})$ and we want an

updated estimate of θ^{new} such that

$$\theta^{new} > \theta^{old} \tag{3.11}$$

or we want to maximize the difference,

$$\mathcal{Q}(\theta^{new}) - \mathcal{Q}(\theta^{old}) = \ln P(X|\theta^{new}) - \ln P(X|\theta^{old}) \tag{3.12}$$

The above equations with hidden variables can be written as

$$\mathcal{Q}(\theta^{new}) - \mathcal{Q}(\theta^{old}) = \ln(\sum P(X|z, \theta^{new})P(Z|\theta^{new})) - \ln P(X|\theta^{old}) \tag{3.13}$$

Using Jensen's Equality it can be show that,

$$\ln \sum_{i=1}^{n} \lambda_i x_i \geq \sum_{i=1}^{n} \lambda_i \ln(x_i) \tag{3.14}$$

for constants $\lambda_i \geq 0$ with $\sum_{i=1}^{n} \lambda_i = 1$. This can be applied to equation **??** and $\lambda = P(Z|X, \theta^{old})$. As $P(Z|X, \theta^{old})$ is a probability measure we have $P(Z|X, \theta^{old}) \geq 0$ and $\sum_Z P(Z|X, \theta^{old}) = 1$.

$$
\begin{aligned}
Q(\theta^{new}) - Q(\theta^{old}) &= \ln(\sum_Z P(X|Z, \theta^{new})P(Z|\theta)) - \ln P(X|\theta^{old}) \tag{3.15} \\
&= \ln(\sum_Z P(X|Z, \theta^{new})P(Z|\theta) \cdot \frac{P(Z|X, \theta^{old})}{P(Z|X, \theta^{old})}) - \ln P(X|\theta^{old}) \tag{3.16} \\
&= \ln(\sum_Z P(z|X, \theta^{old}) \frac{P(X|Z, \theta^{new})P(Z|\theta^{new}}{P(Z|X, \theta^{old})}) - \ln P(X|\theta^{new}) \tag{3.17} \\
&\geq \sum_Z P(Z|X, \theta^{old}) \ln(\frac{P(X|Z, \theta^{new})P(Z|\theta^{new})}{P(Z|X, \theta^{old})}) - \ln P(X|\theta^{old}) \tag{3.18} \\
&= \sum_Z P(Z|X, \theta^{old}) \ln(\frac{P(X|Z, \theta^{new})P(Z|\theta^{new})}{P(Z|X, \theta^{old})P(X|\theta^{old})}) \tag{3.19} \\
&\triangleq \triangle(\theta^{new}|\theta^{old}) \tag{3.20}
\end{aligned}
$$

We continue by writing

$$\mathcal{Q}(\theta^{new}) \geq \mathcal{Q}(\theta^{old}) + \triangle(\theta^{new}|\theta^{old})$$

and for convenience define,

$$q(\theta^{new}|\theta^{old}) \triangleq \mathcal{Q}(\theta^{old}) + \triangle(\theta^{new}|\theta^{old})$$

The function $q(\theta^{new}|\theta^{old})$ is bounded by the likelihood functions $\mathcal{Q}(\theta^{new})$. We need to choose values of θ^{new} so that $\mathcal{Q}(\theta^{new})$ is maximized. The new updated value is denoted by θ_{n+1}.

$$
\begin{aligned}
\theta_{n+1} &= argmax_\theta\{q(\theta^{new}|\theta^{old})\} & (3.21) \\
&= argmax_\theta\{\mathcal{Q}(\theta^{old}) + \sum_Z P(Z|X,\theta^{old})\ln(\frac{P(X|Z,\theta^{new})P(Z|\theta^{new})}{P(Z|X,\theta^{old})P(X|\theta^{old})})\} & (3.22) \\
&= argmax_\theta\{\sum_Z P(Z|X,\theta^{old})\ln(P(X|Z,\theta^{new})P(Z|\theta^{new}))\} & (3.23) \\
&= argmax_\theta\{\sum_Z P(Z|X,\theta^{old})\ln P(X,Z|\theta^{new})\} & (3.24) \\
& & (3.25)
\end{aligned}
$$

We use the EM algorithm as described by Christopher M. Bishop in his book [1]. The steps taken in EM algorithm are described below -:

1. Have an initial estimate of the parameters θ^{old}

2. **E Step:** Evaluate $p(Z|X,\theta^{old})$

3. **M Step:** Evaluate $\theta^{new} = argmax_\theta L(\theta,\theta^{old})$

   where $L(\theta,\theta^{old}) = \Sigma_Z p(Z|X,\theta_{old})\log p(X,Z|\theta)$

4. Check for the convergence of either the log likelihood or the parameter values. If the convergence criterion is not satisfied then let

   $$\theta \leftarrow \theta^{new}$$

and return to step 2

There are various convergence techniques that can be applied in step 4. In our algorithm we use Newton Conjugate Gradient to estimate the right parameters. It is important to point that EM algorithm is local optimization technique and there are situations where it can get stuck in local optimum.

3.2.2 Parameter Estimation

In this section we give a detailed explanation of the method proposed to learn motion model. As stated in Chapter 2.1 to calculate the position of AUV we need to estimate velocity and feed it to the navigation equation 2.14. As we are operating in a dynamic environment there are various factors that can lead to changes in our motion model. To adapt the motion model we represent the velocity as a Gaussian distribution. We

assume the distribution to be Gaussian as sum of several random noises leads to a such a distribution. The algorithm described here is used to estimate parameters of the distribution. Another assumption for the algorithm that we represent the pose of an AUV in two dimension as compared to six.

The velocity based motion model equations used in the algorithm are

$$x_t = x_{t-1} + V_{t-1}/W_{t-1} \sin(\theta_{t-1}) + V_{t-1}/W_{t-1} \cos(\theta_{t-1} + W_{t-1}\delta t) \tag{3.26}$$

$$y_t = y_{t-1} + V_{t-1}/W_{t-1} \cos(\theta_{t-1}) - V_{t-1}/W_{t-1} \sin(\theta_{t-1} + W_{t-1}\delta t) \tag{3.27}$$

$$\theta_t = \theta_{t-1} + W_{t-1}\delta t \tag{3.28}$$

where,

$$V \sim \mathcal{N}(v_t, v_t^2\sigma_{V_v}^2 + w_t^2\sigma_{V_w}^2 + \sigma_{V_1}^2) W \sim \mathcal{N}(w_t, v_t^2\sigma_{W_v}^2 + w_t^2\sigma_{W_w}^2 + \sigma_{W_1}^2) \tag{3.29}$$

The translational and rotational velocity are represented by a Gaussian distribution with mean as reported translational v and rotational t velocity respectively. σ_{A_b} represents the contribution of the velocity term b to the variance of the distribution over A. σ_{V_1} and σ_{w_1} are added to the motion model to account for errors that are not directly proportional to the translation and rotation of a robot.

Putting the whole problem of estimating parameters in EM framework, we define the parameters of the motion model that we want to learn are $\theta = \sigma_{V_v}^2, \sigma_{V_w}^2, \sigma_{V_1}^2, \sigma_{W_v}^2, \sigma_{W_t}^2, \sigma_{W_1}^2$ The data Z from which the parameters can be learnt are

$Z = u_{1:T}, z_{1:T}$ where, $u_{1:T}$ and $z_{1:T}$ are the history of control and sensor readings.

The robot's trajectory is the hidden variable in the system as it not directly observable. $r = x_{0:T}$

The first step in an EM algorithm is to initialize the set of parameters θ with some initial values. In the E step we calculate the expectation of $\log p(r, Z|\theta)$ with respect to distribution $p(r|Z, \theta)$. The distribution can be also be represented by the entire join smoothing density $p(x_{0:T}|u_{1:T}, z_{1:T})$. To approximate the E step joint smoothing density particle filtering and smoothing is performed to calculate a set

of robot trajectories as discussed in section 2.3. In the M step we treat the set of trajectories as ground truth as use them to compute the maximum likelihood of parameters. The algorithm keeps on alternating between the E and M step until convergence.

For calculating the maximum likelihood values for parameters we need to calculate the motion errors $epsilon_{T_t}, epsilon_{D_t}$ based on robot trajectory and the contribution of translational v and rotational t velocity to the errors.

$$\epsilon_{T_t}^{[j]} = (\theta_{t+1}^{'[j]} - \theta_t^{'[j]} - r_t^{''})mod2\pi \tag{3.30}$$

$$\epsilon_{D_t}^{[j]} = (x_{t+1}^{'[j]} - x_t^{'[j]})cos(\theta_t^{'[j]} + \frac{r_t^{''} + \epsilon_{T_t}^{[j]}}{2} + (y_{t+1}^{'[j]} - y_t^{'[j]})sin(\theta_t^{'[j]} + \frac{r_t^{''} + \epsilon_{T_t}^{[j]}}{2}) - d_t^{''} \tag{3.31}$$

The distribution that represents these errors are

$$\epsilon_{V_t}^{[j]} \sim \mathcal{N}(0, v_t^2\sigma_{V_v}^2 + w_t^2\sigma_{V_w}^2 + \sigma_{V_1}^2) \tag{3.32}$$

$$\epsilon_{W_t}^{[j]} \sim \mathcal{N}(0, v_t^2\sigma_{w_v}^2 + w_t^2\sigma_{V_w}^2 + \sigma_{W_1}^2) \tag{3.33}$$

where j stands for sampled trajectory.

The likelihood functions are

$$\mathcal{Q}_{\epsilon_D}(\sigma_{V_v}^2, \sigma_{V_r}^2, \sigma_{V_1}^2) = p(\{\epsilon_{V_v}^{[j]}\}|u_{1:T}, \{k_{0:T}^{[j]}\}) \tag{3.34}$$

$$= \prod_j \prod_{t=0}^{T-1} \frac{1}{\sqrt{2\pi(v_t^2\sigma_{V_v}^2 + r_t^2\sigma_{V_r}^2 + \sigma_{V_1}^2)}} * exp(\frac{(\epsilon_{V_t}^{[j]})^2}{2(d_t^2\sigma_{V_v}^2 + r_t^2\sigma_{V_r}^2 + \sigma_{V_1}^2)}) \tag{3.35}$$

$$\mathcal{Q}_{\epsilon_T}(\sigma_{W_d}^2, \sigma_{W_r}^2, \sigma_{W_1}^2) = p(\{\epsilon_{W_t}^{[j]}\}|u_{1:T}, \{k_{0:T}^{[j]}\})$$

$$= \prod_j \prod_{t=0}^{T-1} \frac{1}{\sqrt{2\pi(v_t^2\sigma_{W_d}^2 + r_t^2\sigma_{W_r}^2 + \sigma_{W_1}^2)}} * exp(\frac{(\epsilon_{W_t}^{[j]})^2}{2(v_t^2\sigma_{W_d}^2 + r_t^2\sigma_{W_r}^2 + \sigma_{W_1}^2)})$$

The estimate the parameters we get the maximum likelihood estimates

$$\sigma_{V_v}^{2*}, \sigma_{V_r}^{2*}, \sigma_{V_1}^{2*} = argmax_{\sigma_{V_v}^2, \sigma_{V_r}^2, \sigma_{V_1}^2} \mathcal{Q}(\sigma_{V_v}^2, \sigma_{V_r}^2, \sigma_{V_1}^2) \tag{3.36}$$

$$\sigma_{W_d}^{2*}, \sigma_{W_r}^{2*}, \sigma_{W_1}^{2*} = argmax_{\sigma_{W_d}^2, \sigma_{W_r}^2, \sigma_{W_1}^2} \mathcal{Q}(\sigma_{W_d}^2, \sigma_{W_r}^2, \sigma_{W_1}^2) \tag{3.37}$$

We maximize the log likelihood function via Newton conjugate gradient method with respect to motion model parameters. Conjugate gradient is a method to determine the minimum or maximum of a function [**?**]. Generally it requires the gradient of the function. In this method the gradient of the function is taken as the first search direction while the next search direction are chosen in such a way that they are orthogonal to all previous search directions. The gradient of log likelihood functions are

$$
\mathcal{L}(\sigma^2_{V_v}, \sigma^2_{V_w}, \sigma^2_{V_1}) = -\frac{1}{2} \sum_j \sum_{t=0}^{T-1} [\log 2\pi + \log(v_t^2 \sigma^2_{V_v} + w_t^2 \sigma^2_{V_w} + \sigma^2_{V_1}) + \frac{(\epsilon_{V_t}^{[j]})^2}{v_t^2 \sigma^2_{V_v} + w_t^2 \sigma^2_{V_r} + \sigma^2_{V_1}} \quad (3.38)
$$

$$
\mathcal{L}(\sigma^2_{W_v}, \sigma^2_{W_w}, \sigma^2_{W_1}) = -\frac{1}{2} \sum_j \sum_{t=0}^{T-1} [\log 2\pi + \log(v_t^2 \sigma^2_{W_v} + w_t^2 \sigma^2_{W_w} + \sigma^2_{W_1}) + \frac{(\epsilon_{W_t}^{[j]})^2}{v_t''^2 \sigma^2_{W_v} + w_t''^2 \sigma^2_{W_w} + \sigma^2_{W_1}} \quad (3.39)
$$

Chapter 4

Results and Experimental Setup

In this chapter we describe the experimental setup of the simulator to test our algorithm. To demonstrate the effectiveness of our approach the results from the simulated experiment are also shown.

4.1 Experimental Setup

To test our algorithm for learning the motion model we create a simulated world(Figure 4.1). The world size of our simulation is 400X400 with four landmarks shown in blue dots. The red * shows the location of the robot and blue triangle is the location estimate of the robot by particle filters. The robot is moving with a constant forward and rotational velocity throughout the experiment. In simulation the robot can measure its distance from all four landmarks at all time. The sensor noise in the simulation can be varied in between the experiment. The particle size is 500 and is constant throughout the experiment. Table **??** shows the summary of variables for the experiment to test the effectiveness of our algorithm to learn a motion model.

	Experiment
World Size	400 units X 400 units
Total timesteps	400
No. of sensor readings	400
Translational Velocity	3 units/timestep
Rotational Velocity	01. units/timestep

Table 4.1: Summary of adapting motion model experiment.

At the start of the experiment the initial location of the robot and particle filters are randomly initialized (Figure 4.2 (a)). The robot is moved by a constant velocity and Figure **??** shows the updated location of the robot as well as an estimate by particle filters of the robot's location.
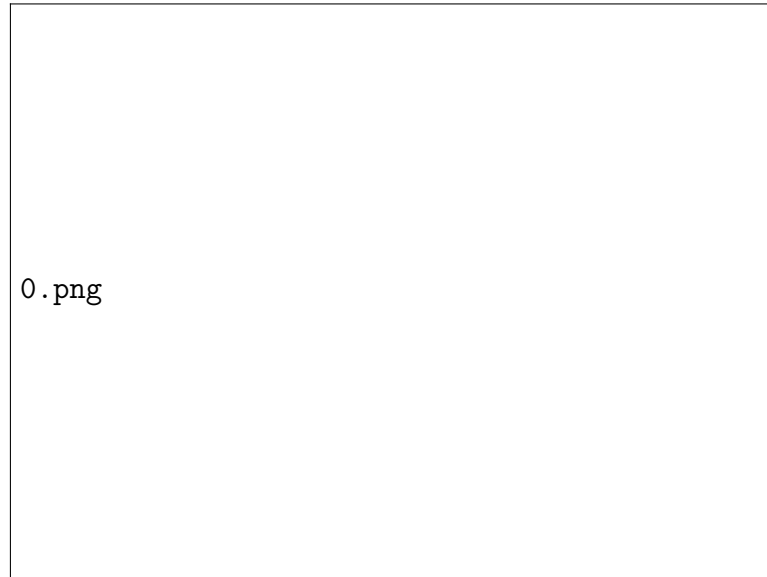
```
0.png
```

Figure 4.1: The simulation environment consisting of the robot(triangle) and the particle estimate of teh location(star). The blue dots represent the landmarks.

4.2   Results

Table shows the various experiments that are performed to show the effectiveness of the algorithm proposed. show all the plots

1)Drifts 1.1) with lower sensor noise it can recover fast

1.2) with higher sensor noise it can recover later 2) Motion Model noise

3) Explain why have you plotted the weights. 1) as our sigma of sensor noise is higher we can see that it recovers and keeps like that

2) when we have drift then we can see that it recovers but its failing to keep it in bound . It takes time to come back. 4) Explain all plots -: In the start it varies a lot

5) more trajectories Plots with varying trajectories. See if you can go for a bounded optimization.
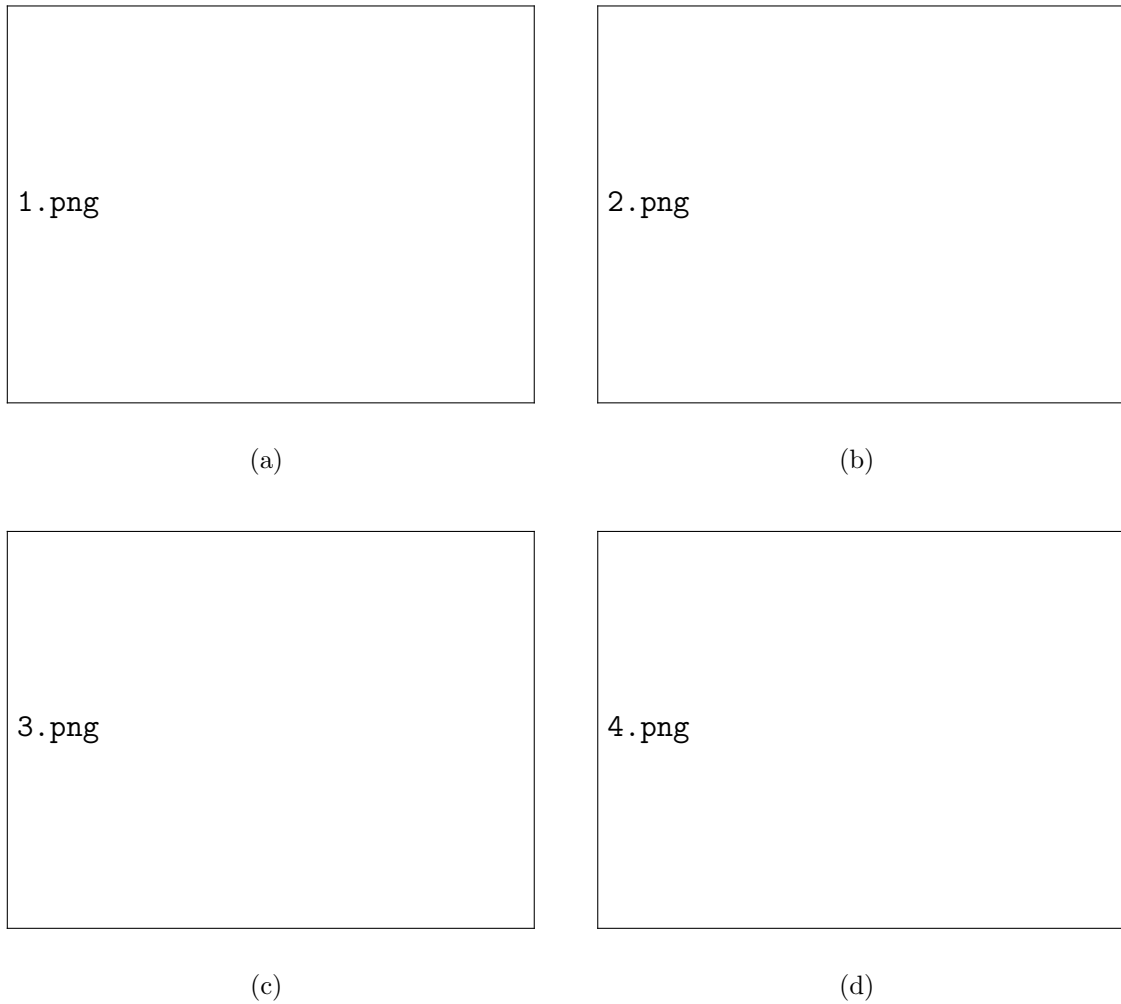
(a)

(b)

(c)

(d)

Figure 4.2: Particle Filters estimating the position of the robot The robot is moved at a constant velocity of 5 units/timestep in each case. The particle filters estimate the location of the robot (star) by integrating the motion and sensor models.

Chapter 5

Landmarks extraction using Side Sonar Images

5.1 Introduction

5.1.1 Side Scan Sonar

5.1.2 Speeded Up Robust Features

5.2 Dynamic Landmarks

In the particle filtering algorithm the sensor model is responsible to assign weights to the particles.The sensor model describes the process by which sensor measurements are generated in the physical world.It is generally done by using some sort of references in the world aka landmarks. Austin and Elizar in their papers used static maps of known environments to generate references for their sensor model. The probability of having static maps for underwater environments is pretty low and thus lead us to use side sonar images as references for the sensor model. As you can see in the image there

Figure 5.1: Side Sonar Image

```
/home/rohan/Documents/thesis_work/visual_sonar/sonar_59/18.jpg
```
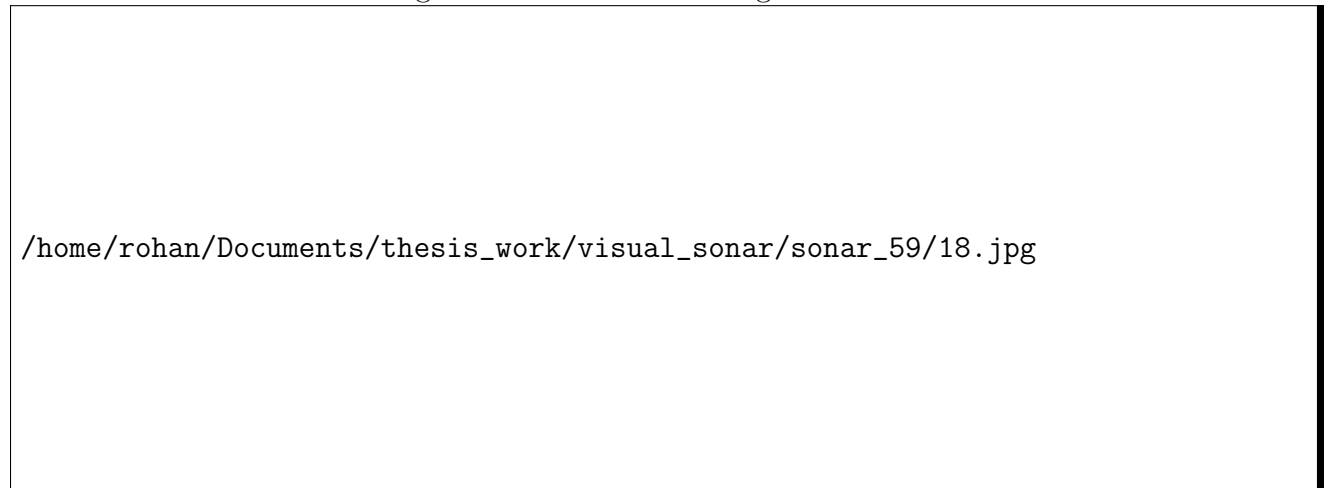
are lot of horizontal lines which we treat as noise. For us to use the side sonar images we performed a pre-processing step in which we used a median filter on the image.

This helped us in getting rid of major noises in terms of horizontal lines but also blurred the image. In order to generate some landmarks we ran feature extractions techniques like SURF. This algorithm helped us in detecting interest points in the image and are shown below in circles. Andrew Vardyrefer the paper) ran multiple image registration techniques such as phase matching (you need to mention more) on side sonar images and showed that SURF performs better than the rest .

Figure 5.2: SURF Keypoints

/home/rohan/Documents/thesis_work/visual_sonar/landmarks.png

These interest points can be treated as landmarks. We use a high Hessian threshold so that we have a maximum of 4 landmarks. The distance of the robot and the particles to these landmarks are used to assign weights to the particles.

The output of a side sonar is a ping of the surface and for an image to be created we need to combine pings over time. Andrew Vardy in his paper explains on how to combine pings to create an meaningful image. For our algorithm to run on the AUV we can use Andrew's algorithm as a black box and run our feature extraction on the output i.e. images of the seabed. This method allows us independence from a static map as well as helps in learning the motion model on the fly in a new environment.

5.3 Motion Estimation using side sonar images

In AUV the motion estimation is generally done through dead-reckoning. It is a process of calculating the current position based upon the previous position and the speed of vessel. The velocity of the AUV can be estimated by the acceleration measurement supplied by an Inertial Measurement Unit. Another way is to use a Doppler Velocity Log(DVL) that measures velocity in water by measuring the Doppler

effect on scattered sound waves. Dead reckoning may have significant errors as the velocity and direction must be accurately known at every time step.

In this algorithm we propose to get motion estimates using side sonar images. As stated before we run SURF on the images and generate some key points. These key points are matched in the next image using a KNN based matcher. The matched key points gives us an estimate on the movement of the vehicle. In the figure we show two consecutive images and in the first image we have the key points marked in circle. In the next image we have the matched key points marked in green circles. This

Figure 5.3: SURF Keypoints

/home/rohan/Documents/thesis_work/visual_sonar/surf_working.jpeg

estimate can be coupled with the previous estimate to calculate the current position. The visual input to the dead reckoning algorithm has its pros and cons.The main advantage of using a visual estimate is that it doesn't suffer from drift which is prime concern for underwater vehicles. The disadvantage lies in the fact that we don't have side sonar images available every time. We can solve the problem by combining the visual input with the velocity estimates. We can pass the visual motion estimate and

the DVL estimate to a Kalman Filter and use the output as an input to our dead-reckoning estimate. The second disadvantage is the computation power available on AUV. To specifically deal with the problems we use a high Hessian threshold to extract maximum of 4 landmarks so that feature matching is not computationally expensive.

We validate our algorithm on datasets consisting of side sonar images and the total distance the AUV moves.

Chapter 6

Results

6.1 Adapting Motion Model

We use a simulation to demonstrate the effectiveness of learning the motion model. The simulation mainly consists of particle filter SLAM. We use a motion model described in the above chapters. The sensor model basically measures the distance from the four static landmarks defined at the start of the experiment. The experiment runs over 100 time steps and at every 5th time step we change the parameters of the motion model. As described in the above chapters the parameters that we intended to learn are $\sigma^2_{D_d}, \sigma^2_{T_d}, \sigma^2_{D_1}, \sigma^2_{D_r}, \sigma^2_{T_r}, \sigma^2_{D_1}, \sigma^2_{T_1}$. In the first stage of the experiment at every 5th time step we change $\sigma^2_{D_d}$ or $\sigma^2_{T_r}$ in our motion model. The following table and plots describes the five experiments that were conducted in the simulation.

No.	σ_{D_d}	σ_{T_r}	$\sigma^*_{D_d}$	$\sigma^*_{T_r}$	Sensor Noise
1	0.05	0.05	0.2	0.05	2.0
2	0.05	0.05	0.2	0.05	5.0
4	0.05	0.05	0.5	0.05	2.0
5	0.05	0.05	0.5	0.05	5.0
6	0.05	0.05	0.05	0.2	5.0
7	0.05	0.05	0.05	0.5	5.0

$\sigma_{D_d}, \sigma_{T_r}$ are the parameters values that the motion model was initialized. These values are altered in order to simulate a change in the motion model and they are described by $\sigma^*_{D_d}, \sigma^*_{T_r}$. The sensor noise can be described as the confidence the robot has in its sensor model . The impact of the noise on the localization error can be seen in the following plots.
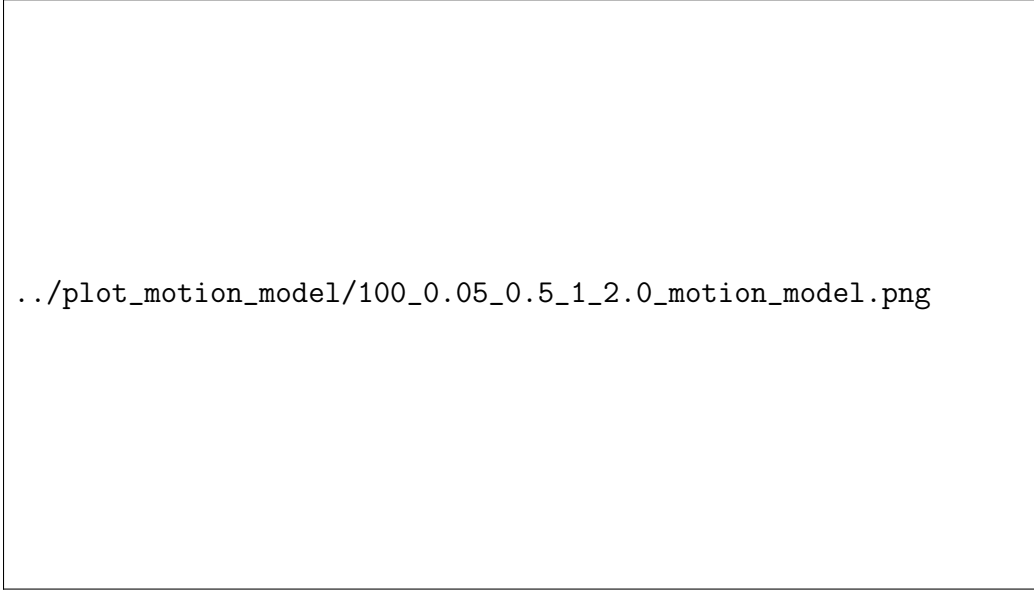
Figure 1 and Figure 2 are plots of the localization error with different sensor noises. We can see in both the cases the learned motion model performed better than the static motion model. Another important point is that the average error is less

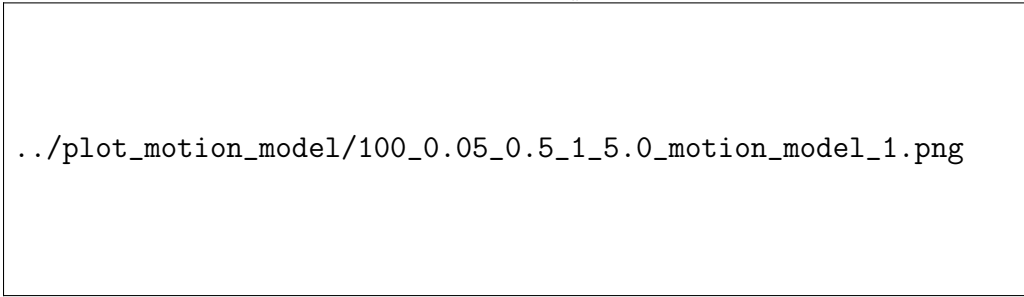Figure 6.1: σ_{D_d}=0.05 $\sigma_{D_d}^* = 0.2$ Sensor Noise= 2.0

../plot_motion_model/100_0.05_0.2_1_2.0_motion_model_1.png

Figure 6.2: σ_{D_d}=0.05 $\sigma_{D_d}^* = 0.2$ Sensor Noise= 5.0

../plot_motion_model/100_0.05_0.2_1_5.0_motion_model_1.png

Figure 6.3: σ_{D_d}=0.05 $\sigma^*_{D_d} = 0.5$ Sensor Noise= 2.0

../plot_motion_model/100_0.05_0.5_1_2.0_motion_model.png

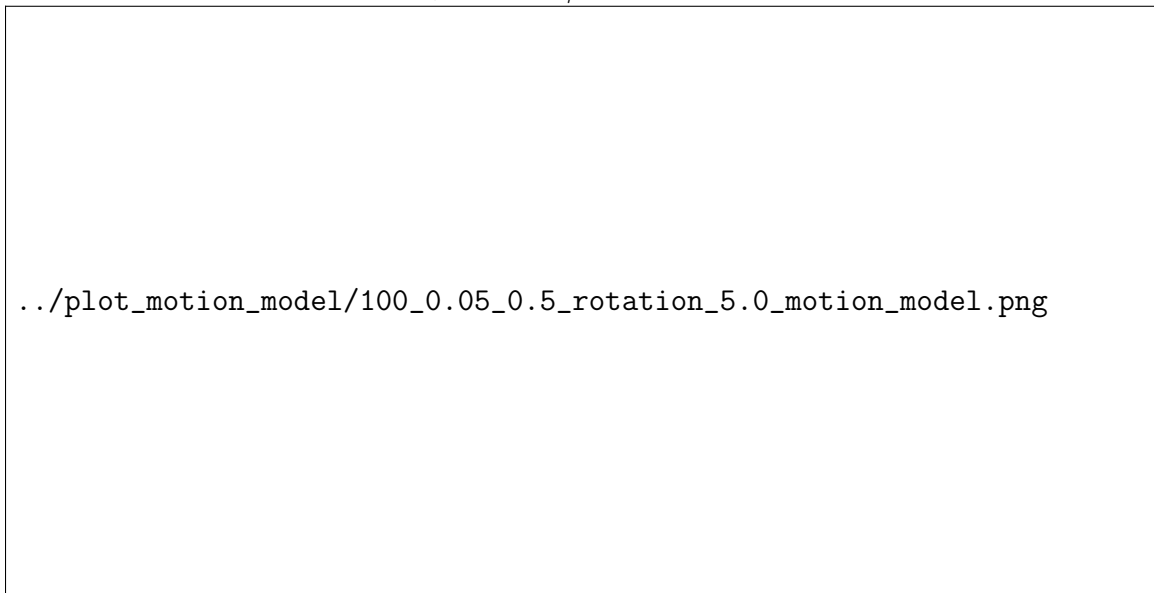Figure 6.4: σ_{D_d}=0.05 $\sigma^*_{D_d} = 0.5$ Sensor Noise= 5.0

../plot_motion_model/100_0.05_0.5_1_5.0_motion_model_1.png

when the sensor noise is 2.0 as compared to the second case. This can be accounted for the fact that our localization algorithm is more confident on the sensor model as compared to the motion model.

As we can see in Figure 3 and Figure 4 at 5th time step the error shooting up but the learned motion model brings back the error whereas the static motion model takes time to recover back depending upon the sensor noise. In both the figures we can see that the error is pretty static in the learned motion model whereas in the static motion model there is a lot of fluctulation.

Figure 5 and Figure 6 describe the errors when the robot rotational motion is much more than the translational motion. We can clearly see that the learned motion model quickly adapts to the changes whereas the static motion model struggles to get the

Figure 6.5: σ_{T_r}=0.05 $\sigma_{T_r}^* = 0.2$ Sensor Noise= 5.0

../plot_motion_model/100_0.05_0.2_rotation_5.0_motion_model.png

Figure 6.6: σ_{T_r}=0.05 $\sigma_{T_r}^* = 0.5$ Sensor Noise= 5.0

../plot_motion_model/100_0.05_0.5_rotation_5.0_motion_model.png

error down.

In all the cases it was very clear that we could see the adaptive motion model performing better than the static. The sensor noise had its impact on the overall error. Robot calibration is important to process in mobile robotics. The proposed algorithm is an automated process which can help us in better navigation of the robots and can be used for any motion model.

6.2   Motion estimation using side sonar images

Chapter 7

Conclusion

Did it!

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