



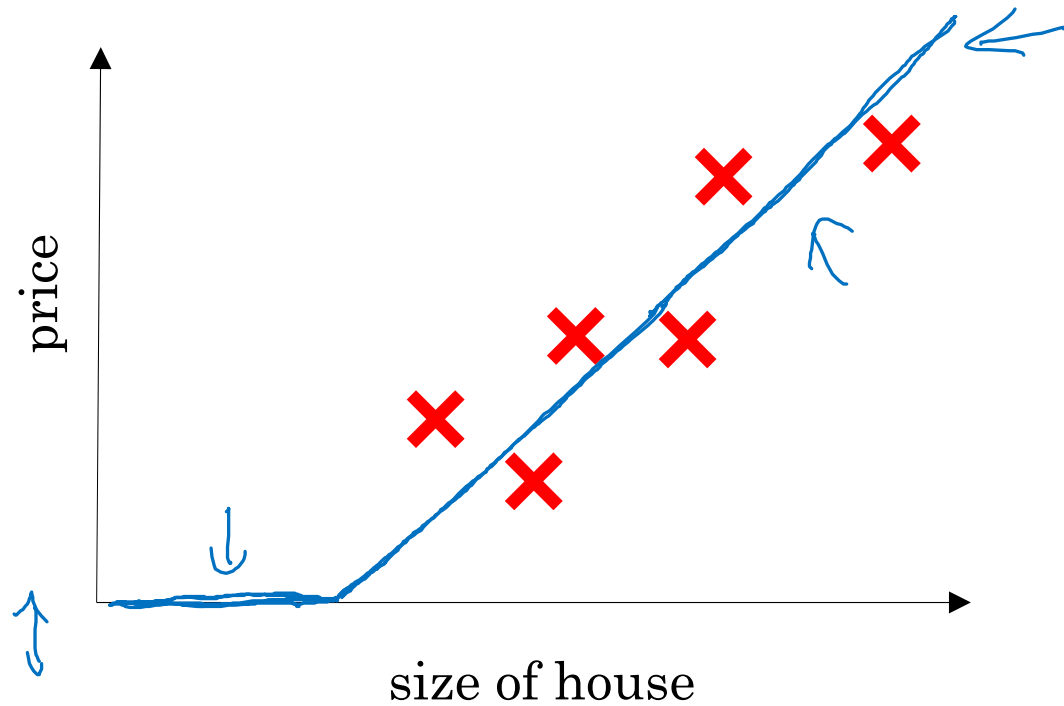
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# Introduction to Deep Learning

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## What is a Neural Network?

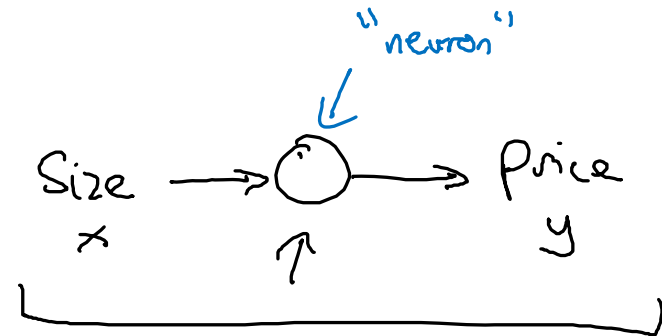
# Housing Price Prediction



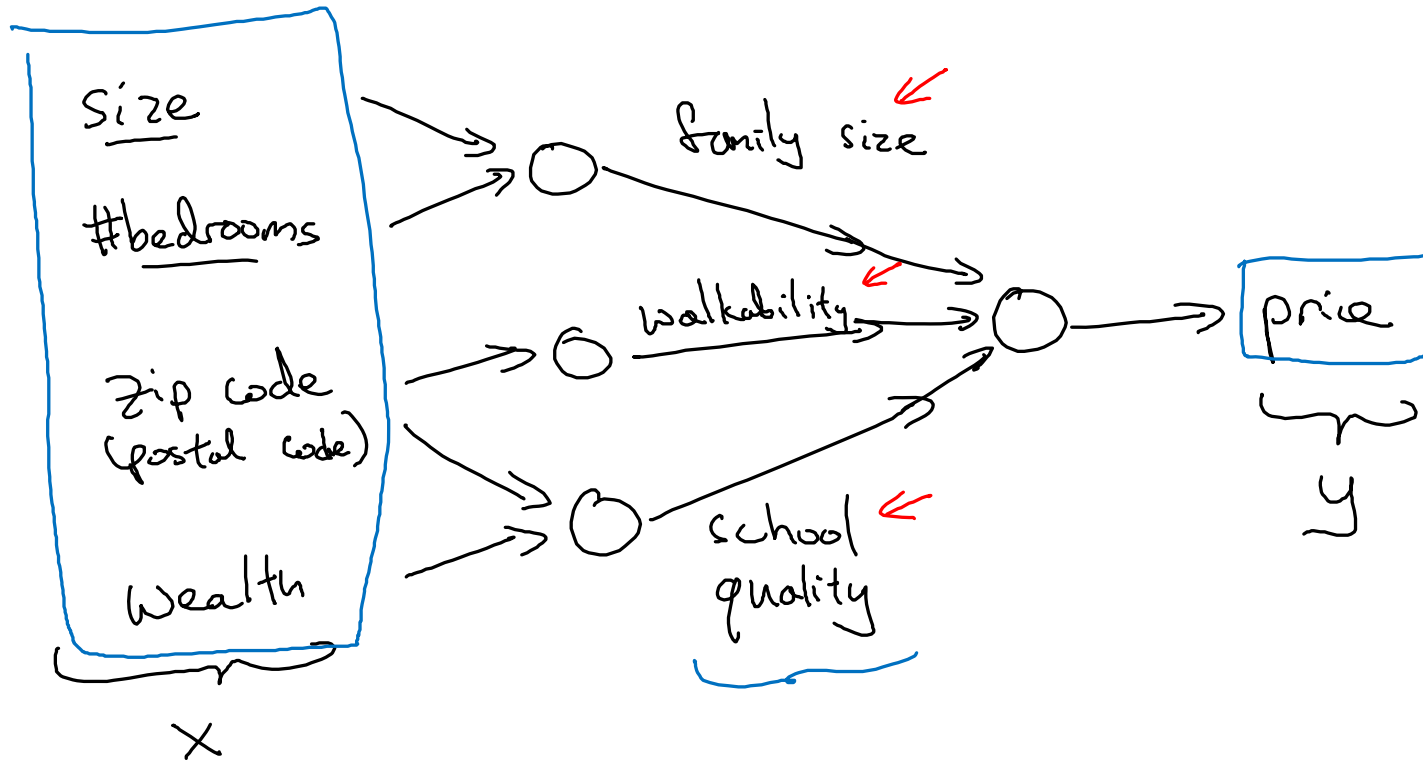
ReLU  
Rectified  
Linear  
Unit



A hand-drawn graph of the ReLU function, showing a horizontal line at zero for negative inputs and a diagonal line with a positive slope for positive inputs. A blue arrow points to the diagonal segment.

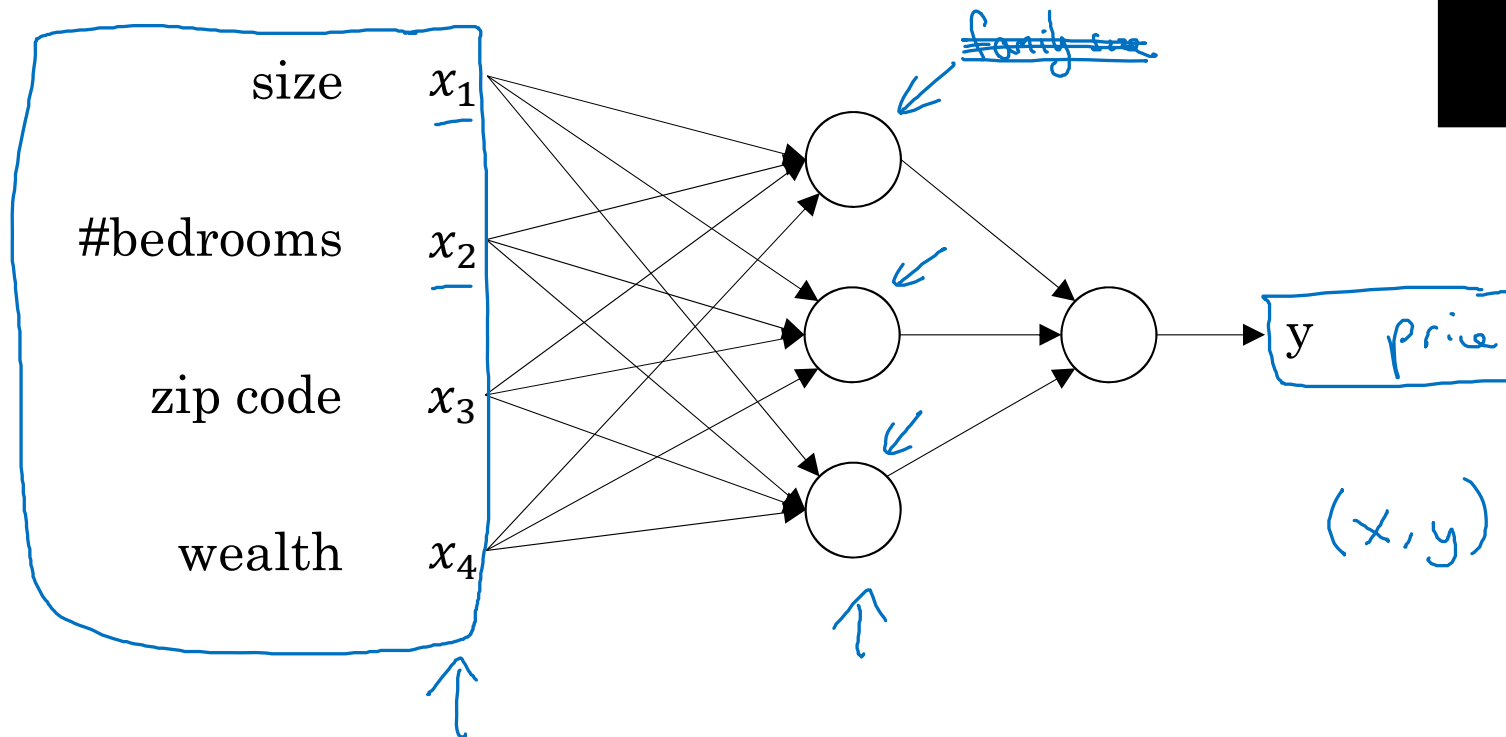


# Housing Price Prediction



# Housing Price Prediction

**Drawing of  
previous Image**














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# Introduction to Deep Learning

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## Supervised Learning with Neural Networks

# Supervised Learning

Input(x) 	Output (y) 	Application
Home features	Price	Real Estate 
Ad, user info 	Click on ad? (0/1)	Online Advertising
Image	Object (1,...,1000)	Photo tagging 
<u>Audio</u>	Text transcript	Speech recognition 
<u>English</u>	Chinese	Machine translation
<u>Image, Radar info</u> 	Position of other cars 	Autonomous driving 

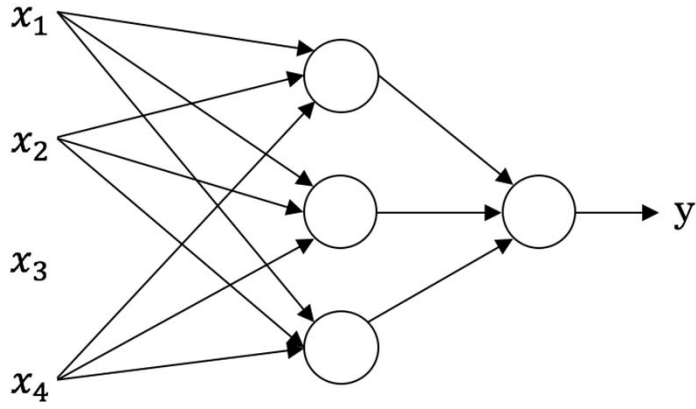
Standard NN

CNN

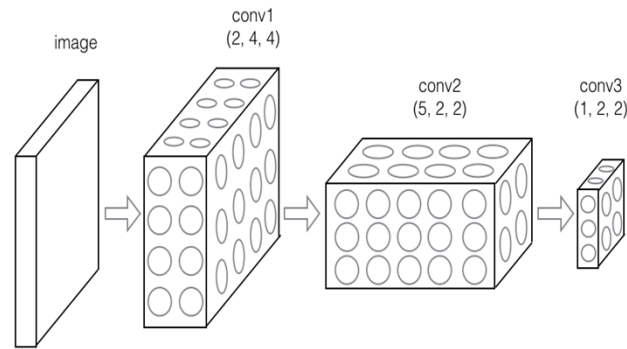
RNN

Custom/ Hybrid

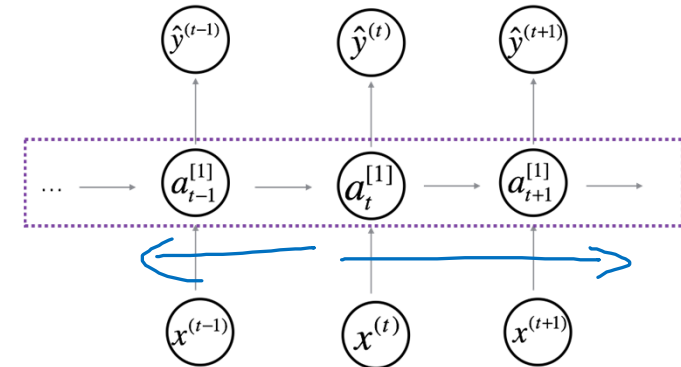
# Neural Network examples



Standard NN



Convolutional NN



Recurrent NN

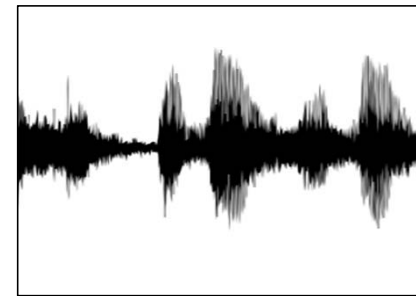
# Supervised Learning

## Structured Data

Size	#bedrooms	...	Price (1000\$s)
2104	3		400
1600	3		330
2400	3		369
⋮	⋮		⋮
3000	4		540

User Age	Ad Id	...	Click
41	93242		1
80	93287		0
18	87312		1
⋮	⋮		⋮
27	71244		1

## Unstructured Data



Audio



Image

Four scores and seven  
years ago...

Text





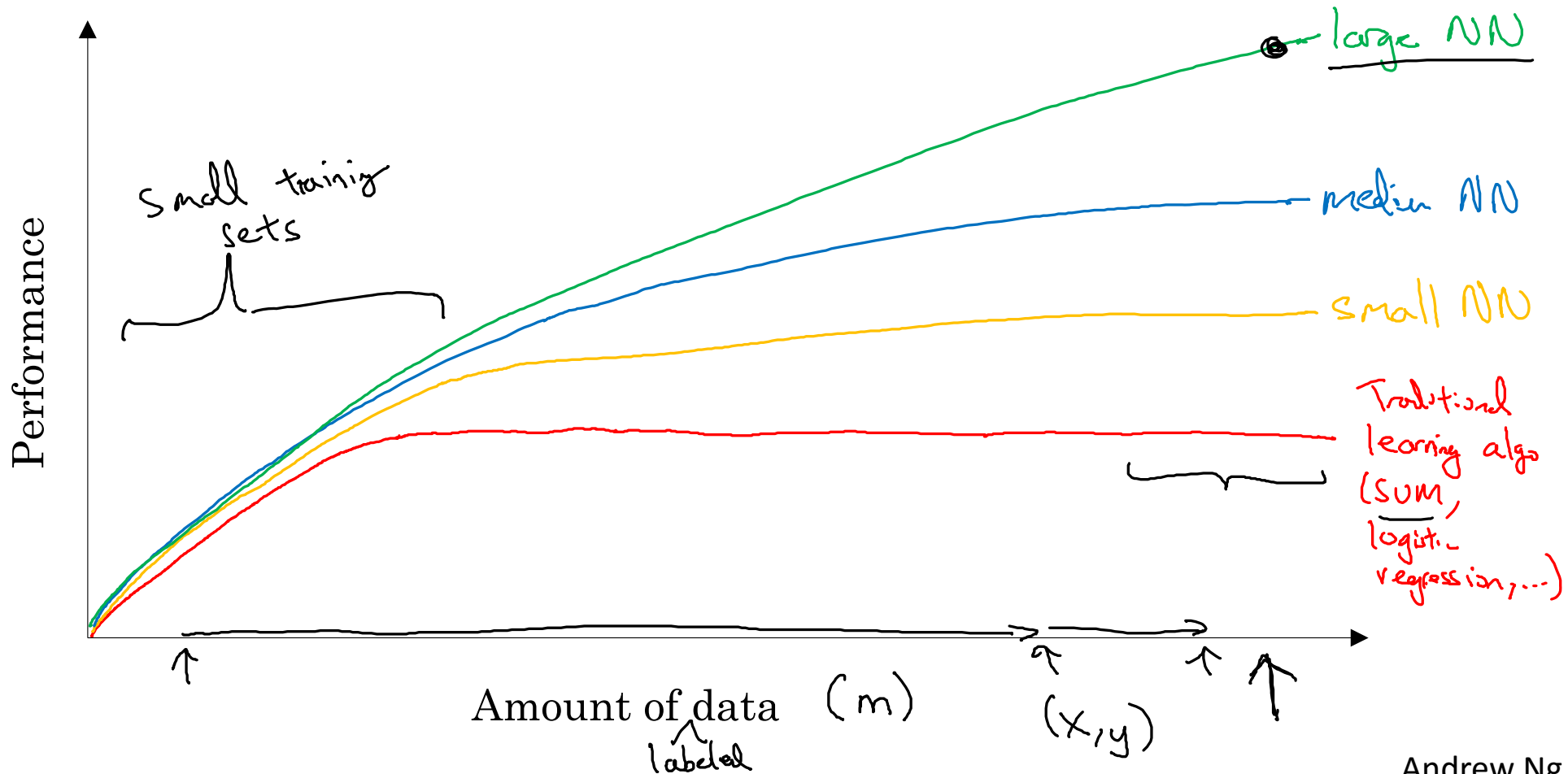
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# Introduction to Neural Networks

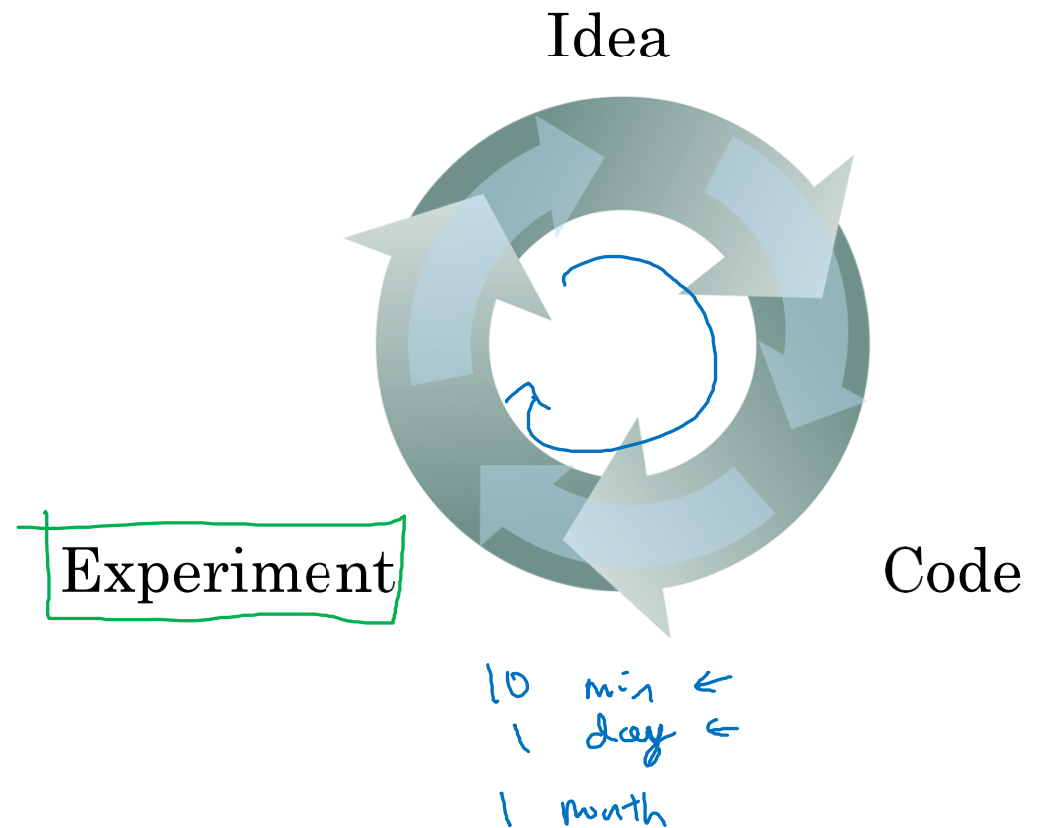
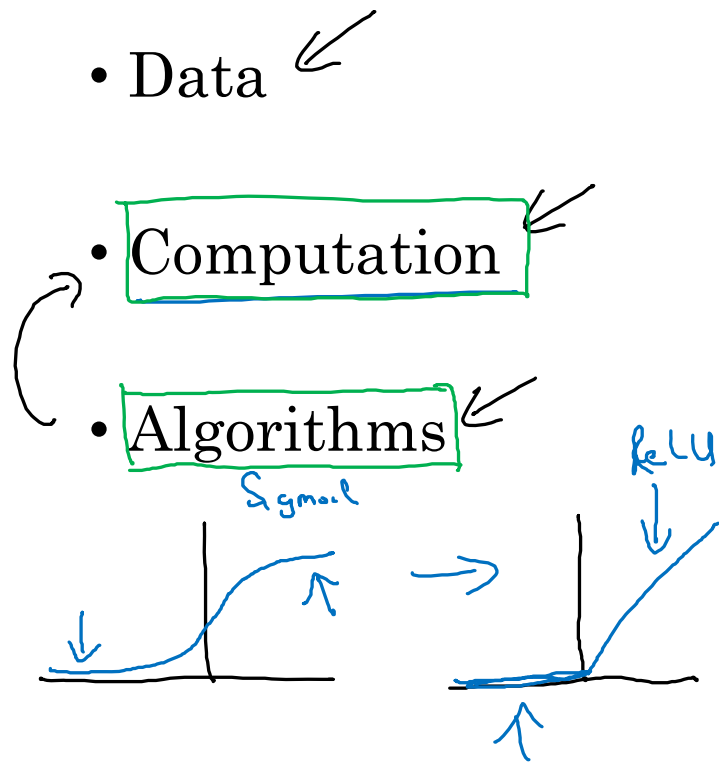
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## Why is Deep Learning taking off?

# Scale drives deep learning progress



# Scale drives deep learning progress





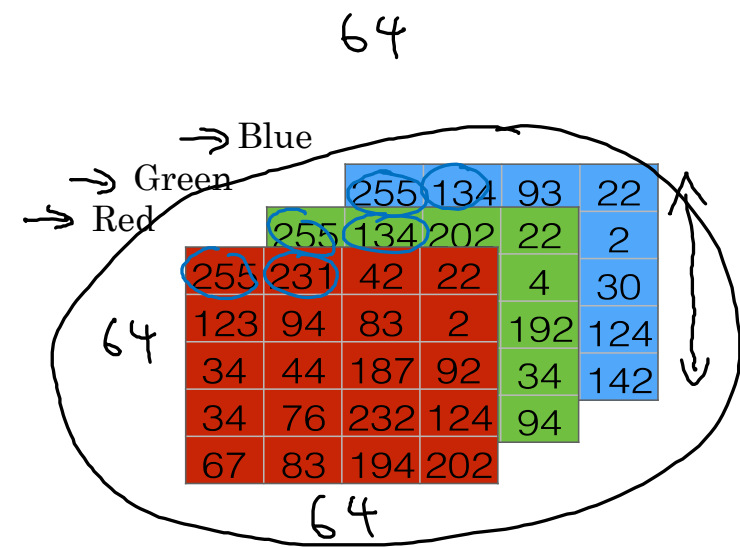
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# Basics of Neural Network Programming

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## Binary Classification

# Binary Classification



$$X = \begin{bmatrix} 255 \\ 231 \\ \vdots \\ 255 \\ 134 \\ \vdots \end{bmatrix}$$

$$64 \times 64 \times 3 = 12288$$

$$n = n_x = 12288$$

$$X \longrightarrow y$$

# Notation

$$(x, y) \quad x \in \mathbb{R}^{n_x}, y \in \{0, 1\}$$

$$m \text{ training examples} : \{(\underline{x}^{(1)}, \underline{y}^{(1)}), (\underline{x}^{(2)}, \underline{y}^{(2)}), \dots, (\underline{x}^{(m)}, \underline{y}^{(m)})\}$$

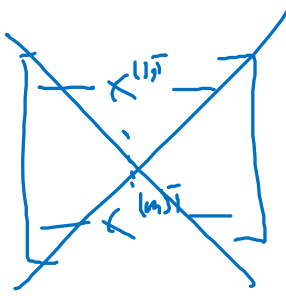
$$M = M_{\text{train}}$$

$$M_{\text{test}} = \# \text{test examples.}$$

$$X = \begin{bmatrix} | & | & & | \\ x^{(1)} & x^{(2)} & \dots & x^{(m)} \\ | & | & & | \end{bmatrix}$$

$X \in \mathbb{R}^{n_x \times m}$

$X.\text{shape} = (n_x, m)$



$$Y = [y^{(1)} \ y^{(2)} \ \dots \ y^{(m)}]$$

$$Y \in \mathbb{R}^{1 \times m}$$

$$Y.\text{shape} = (1, m)$$



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# Basics of Neural Network Programming

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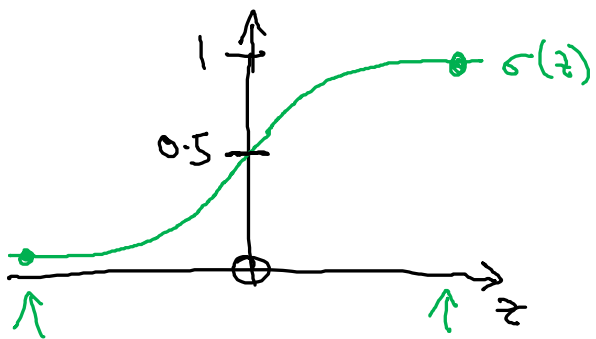
## Logistic Regression

# Logistic Regression

Given  $x$ , want  $\hat{y} = \frac{P(y=1|x)}{0 \leq \hat{y} \leq 1}$   
 $x \in \mathbb{R}^{n_x}$

Parameters:  $\underline{w} \in \mathbb{R}^{n_x}$ ,  $\underline{b} \in \mathbb{R}$ .

Output  $\hat{y} = \sigma(\underbrace{w^T x + b}_z)$



$$x_0 = 1, \quad x \in \mathbb{R}^{n_x+1}$$
$$\hat{y} = \sigma(\theta^T x)$$

$$\theta = \begin{bmatrix} \theta_0 \\ \theta_1 \\ \theta_2 \\ \vdots \\ \theta_{n_x} \end{bmatrix} \begin{matrix} \} b \leftarrow \\ \} w \leftarrow \end{matrix}$$

$$\sigma(z) = \frac{1}{1 + e^{-z}}$$

$$\text{If } z \text{ large } \sigma(z) \approx \frac{1}{1+0} = 1$$

If  $z$  large negative number

$$\sigma(z) = \frac{1}{1 + e^{-z}} \approx \frac{1}{1 + \text{Big num}} \approx 0$$





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# Basics of Neural Network Programming

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## Logistic Regression cost function

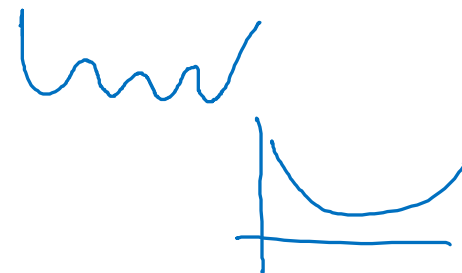
# Logistic Regression cost function

→  $\hat{y}^{(i)} = \sigma(w^T \underline{x}^{(i)} + b)$ , where  $\sigma(\underline{z}^{(i)}) = \frac{1}{1+e^{-z^{(i)}}}$   $\underline{z}^{(i)} = w^T x^{(i)} + b$

Given  $\{(\underline{x}^{(1)}, \underline{y}^{(1)}), \dots, (\underline{x}^{(m)}, \underline{y}^{(m)})\}$ , want  $\hat{y}^{(i)} \approx \underline{y}^{(i)}$ .

$x^{(i)}$   
 $y^{(i)}$   
 $z^{(i)}$  i-th example.

Loss (error) function:  $\underline{\mathcal{L}}(\hat{y}, y) = \frac{1}{2} (\hat{y} - y)^2$



$\mathcal{L}(\hat{y}, y) = - (y \log \hat{y} + (1-y) \log (1-\hat{y})) \leftarrow$

If  $y=1$ :  $\mathcal{L}(\hat{y}, y) = -\log \hat{y} \leftarrow$  Want  $\log \hat{y}$  large, Want  $\hat{y}$  large.

If  $y=0$ :  $\mathcal{L}(\hat{y}, y) = -\log (1-\hat{y}) \leftarrow$  Want  $\log (1-\hat{y})$  large .... Want  $\hat{y}$  small

Cost function:  $\underline{J}(w, b) = \frac{1}{m} \sum_{i=1}^m \mathcal{L}(\hat{y}^{(i)}, y^{(i)}) = \frac{1}{m} \sum_{i=1}^m [y^{(i)} \log \hat{y}^{(i)} + (1-y^{(i)}) \log (1-\hat{y}^{(i)})]$



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# Basics of Neural Network Programming

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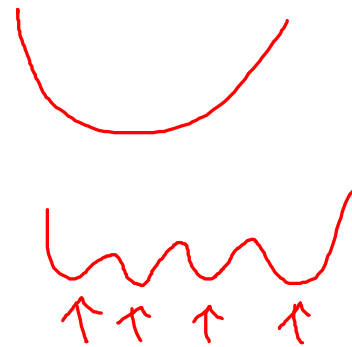
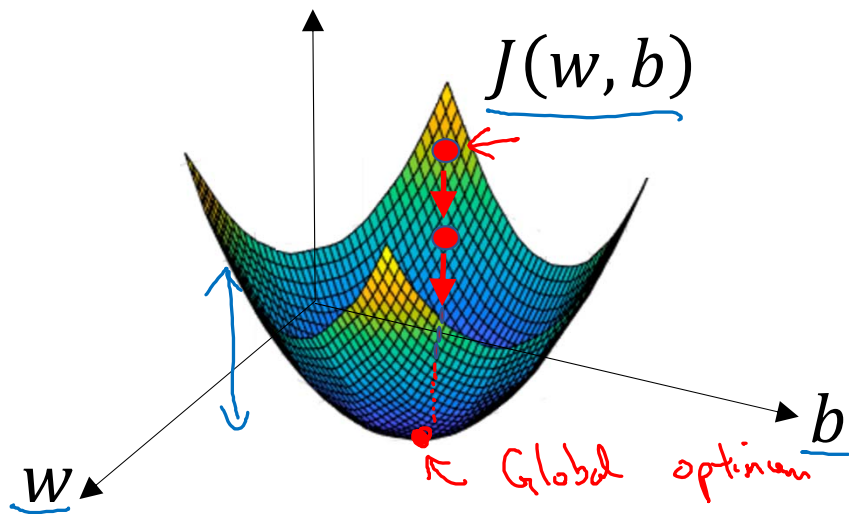
## Gradient Descent

# Gradient Descent

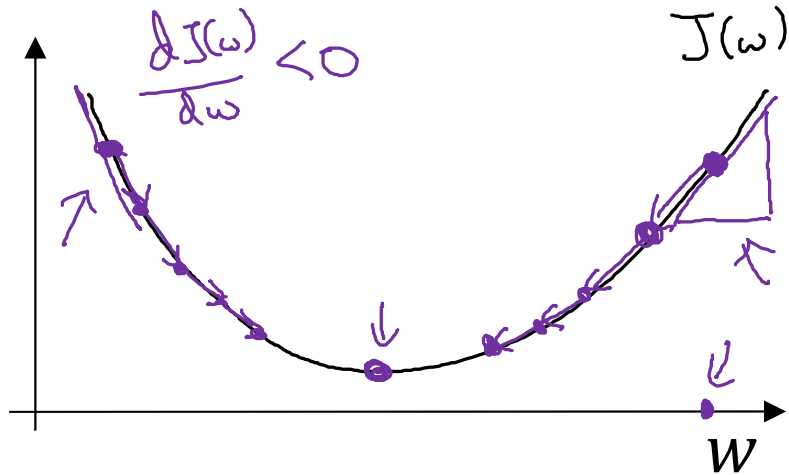
Recap:  $\hat{y} = \sigma(w^T x + b)$ ,  $\sigma(z) = \frac{1}{1+e^{-z}}$  ←

$$\underline{J(w, b)} = \frac{1}{m} \sum_{i=1}^m \underline{\mathcal{L}(\hat{y}^{(i)}, y^{(i)})} = -\frac{1}{m} \sum_{i=1}^m y^{(i)} \log \hat{y}^{(i)} + (1 - y^{(i)}) \log(1 - \hat{y}^{(i)})$$

Want to find  $w, b$  that minimize  $J(w, b)$



# Gradient Descent



Repeat {  
 $w := w - \alpha \frac{dJ(w)}{dw}$   
}

learning rate  $\alpha$

"dw"  $dw$

$w := w - \alpha dw$

$$\frac{dJ(w)}{dw} = ?$$

$J(w, b)$

$$w := w - \alpha \frac{\partial J(w, b)}{\partial w}$$

$$b := b - \alpha \frac{\partial J(w, b)}{\partial b}$$

$\frac{\partial J(w, b)}{\partial w}$

$\frac{\partial J(w, b)}{\partial b}$

$\partial$  "partial derivative"  $J$

$dw$

$db$



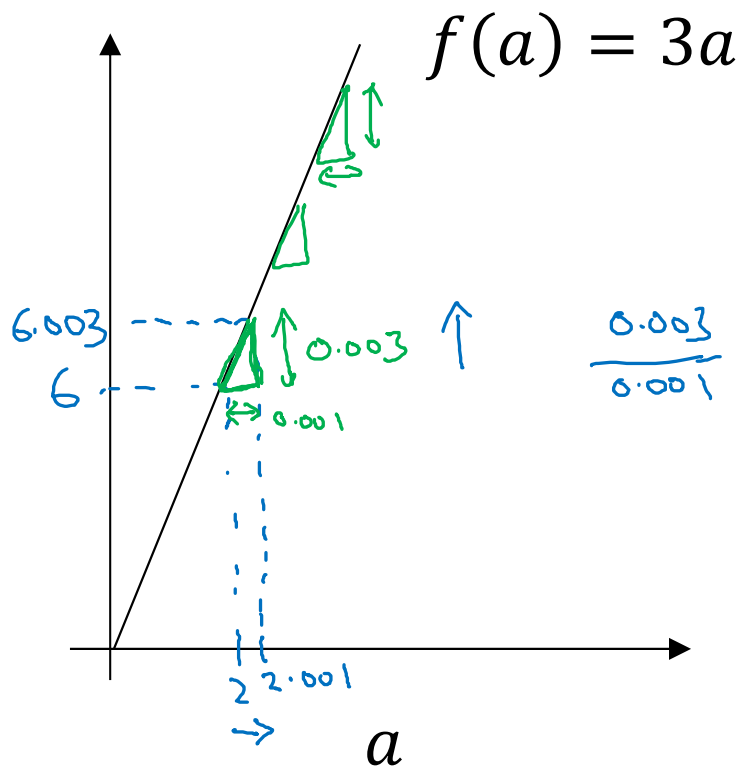
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# Basics of Neural Network Programming

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## Derivatives

# Intuition about derivatives



$$\begin{aligned} \rightarrow a &= 2 & f(a) &= 6 \\ a &= 2.001 & f(a) &= 6.003 \end{aligned}$$

slope (derivative) of  $f(a)$  at  $a=2$  is 3

$$\begin{aligned} \rightarrow a &= 5 & f(a) &= 15 \\ a &= 5.001 & f(a) &= 15.003 \end{aligned}$$

slope at  $a=5$  is also 3

$$\frac{df(a)}{da} = 3 = \frac{d}{da} f(a)$$

0.001 ←  
0.000000001  
0.0000000001



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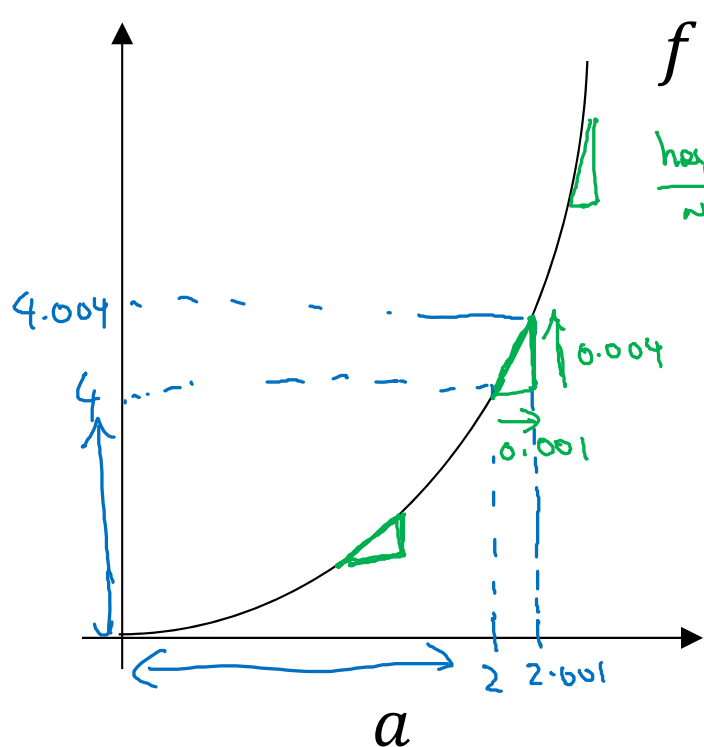
# Basics of Neural Network Programming

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## More derivatives examples



# Intuition about derivatives



$$f(a) = a^2$$

height  
width

$$\frac{d}{da} a^2 = 2a$$

$$0.001$$

$$(2a) \times 0.001$$

$0.001 \leftarrow$   
 $0.000000 \dots 01 \leftarrow$

$a = 2$        $f(a) = 4$   
 $a = 2.001$        $f(a) \approx 4.004$   
 (4.004004)  
 slope (derivative) of  $f(a)$  at  
 $a = 2$  is 4.

$$\frac{d}{da} f(a) = 4 \quad \text{when } a = 2$$

$a = 5$        $f(a) = 25$   
 $a = 5.001$        $f(a) \approx 25.010$

$$\frac{d}{da} f(a) = 10 \quad \text{when } a = 5$$

$$\frac{d}{da} f(a) = \frac{d}{da} a^2 = 2a$$

# More derivative examples

$$f(a) = a^2$$

$$\frac{d}{da} f(a) = \frac{2a}{4}$$

$$a = 2$$

$$f(a) = 4$$

$$a = 2.001$$

$$f(a) \approx 4.004$$

$$f(a) = a^3$$

$$\frac{d}{da} f(a) = \frac{3a^2}{3 \times 2^2 = 12}$$

$$a = 2$$

$$f(a) = 8$$

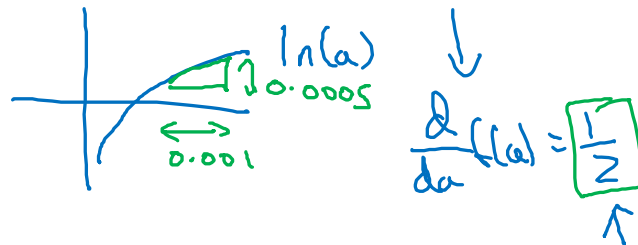
$$a = \underline{2.001}$$

$$f(a) \approx \underline{8.012}$$

$$f(a) = \log_e(a)$$

$$\ln(a)$$

$$\frac{d}{da} f(a) = \frac{1}{a}$$



$$a = 2$$

$$f(a) \approx 0.69315$$

$$a = \underline{2.001}$$

$$\underline{f(a) \approx 0.69365}$$

$$\downarrow$$

$$0.0005$$

$$\swarrow$$

$$0.0005$$

Andrew Ng



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# Basics of Neural Network Programming

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## Computation Graph

# Computation Graph

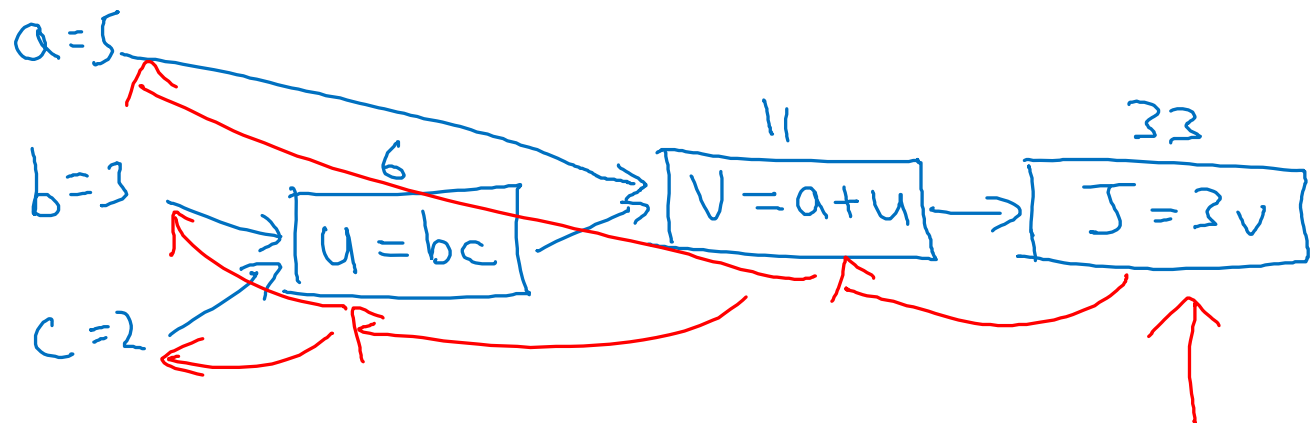
$$J(a, b, c) = 3(a + \underbrace{bc}_u) = 3(5 + \underbrace{3 \times 2}_v) = 33$$

$\underbrace{\hspace{1.5cm}}_J$

$$u = bc$$

$$V = a + u$$

$$J = 3v$$





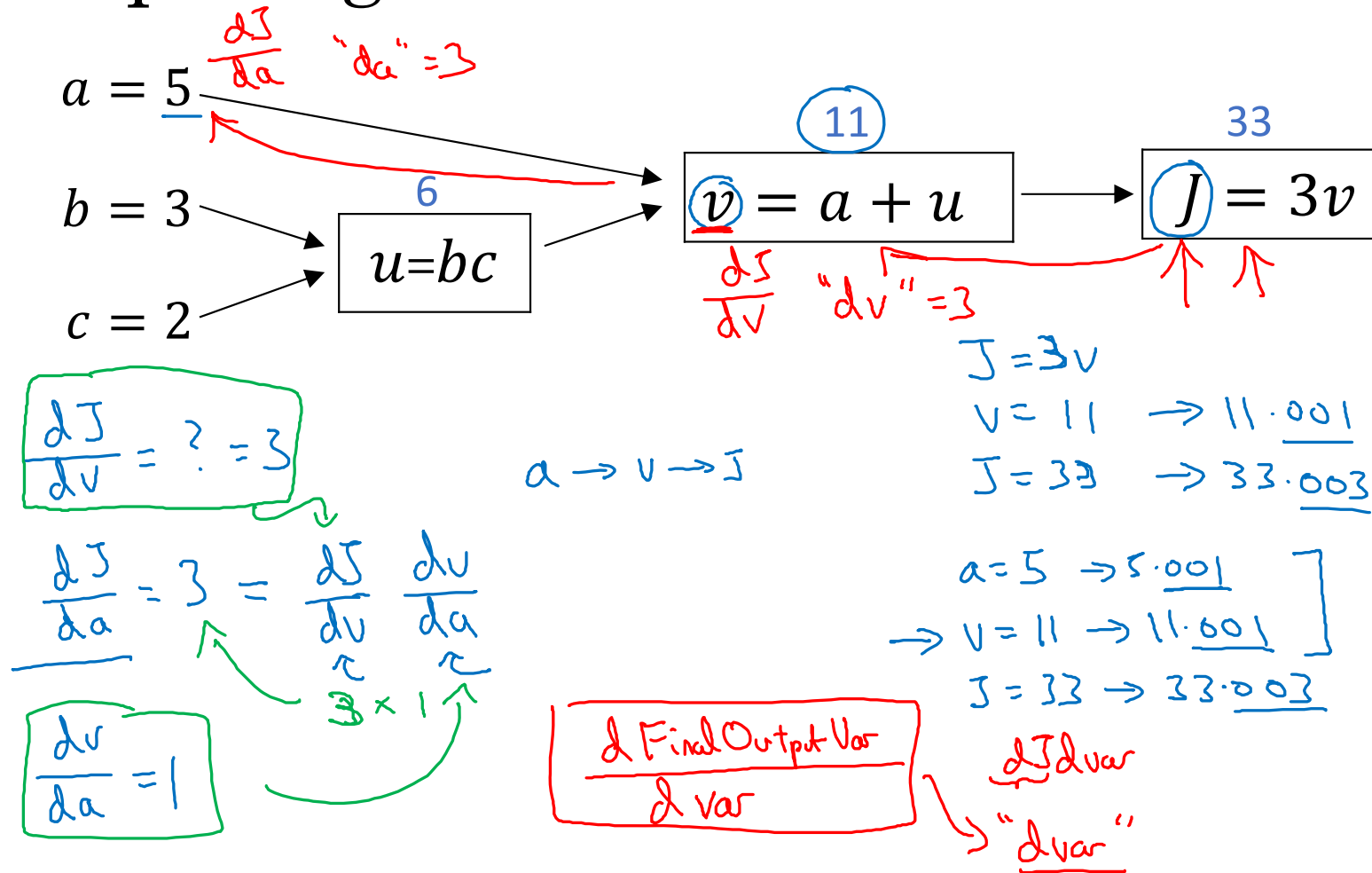
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# Basics of Neural Network Programming

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## Derivatives with a Computation Graph

# Computing derivatives



$$f(a) = 3a$$

$$\frac{df(a)}{da} = \frac{df}{da} = 3$$

$$J = 3v$$

$$\frac{dJ}{dv} = 3$$

$$J = 3v$$

$$v = 11 \rightarrow 11.001$$

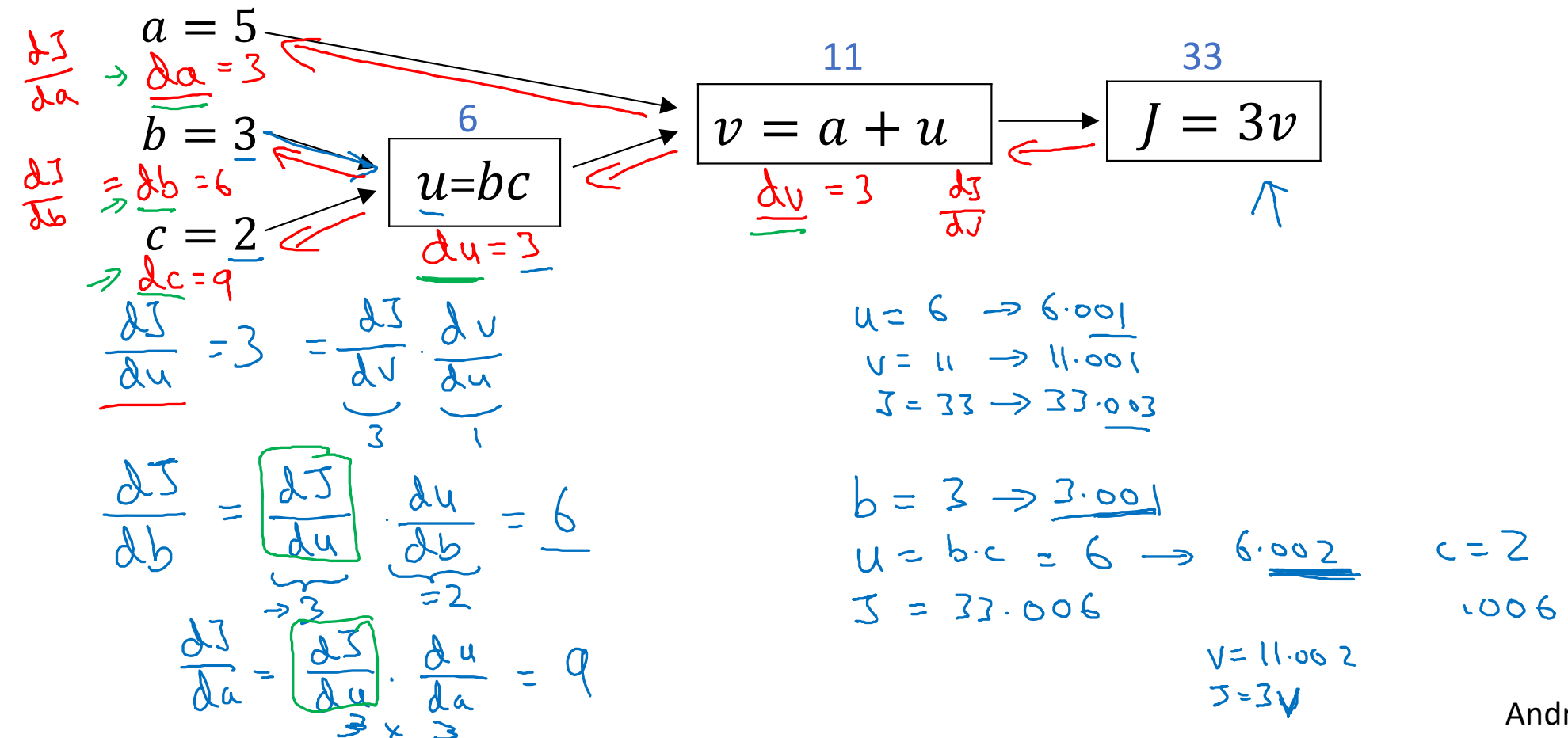
$$J = 33 \rightarrow 33.003$$

$$a = 5 \rightarrow 5.001$$

$$\rightarrow v = 11 \rightarrow 11.001$$

$$J = 33 \rightarrow 33.003$$

# Computing derivatives





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# Basics of Neural Network Programming

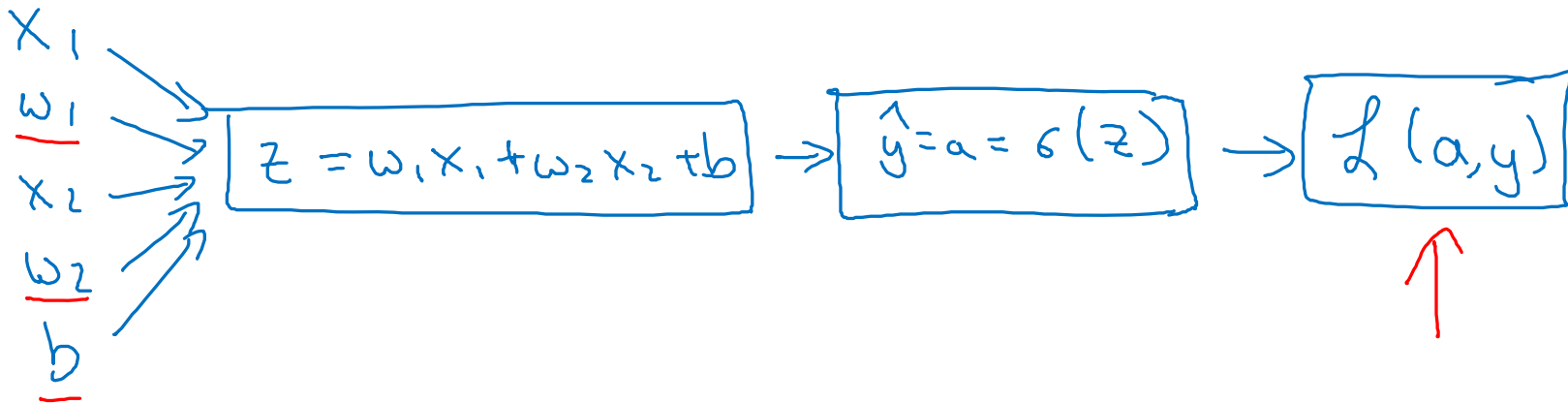
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Logistic Regression  
Gradient descent

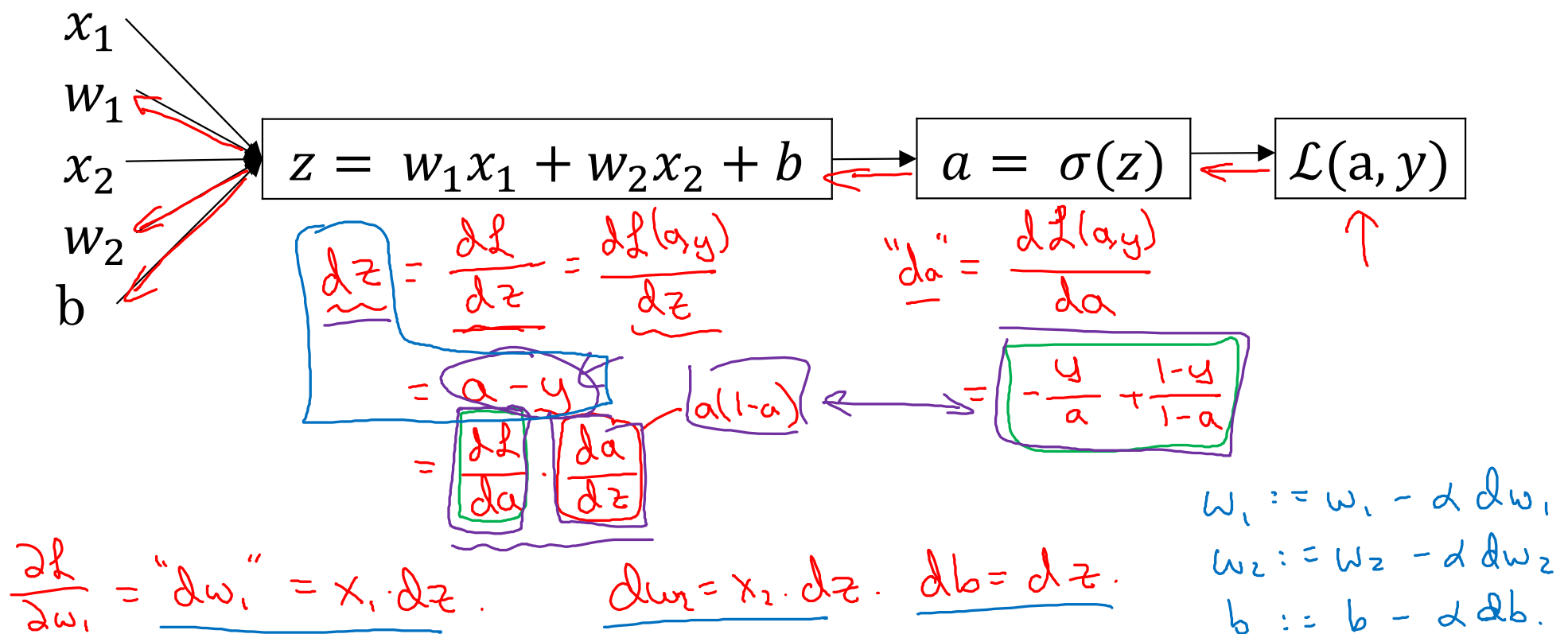


# Logistic regression recap

- $z = w^T x + b$
- $\hat{y} = a = \sigma(\underline{z})$
- $\mathcal{L}(a, y) = -(y \log(a) + (1 - y) \log(1 - a))$



# Logistic regression derivatives





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# Basics of Neural Network Programming

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Gradient descent  
on  $m$  examples

# Logistic regression on $m$ examples

$$\underline{J(w, b)} = \frac{1}{m} \sum_{i=1}^m \underline{\ell(a^{(i)}, y^{(i)})}$$

$$\rightarrow a^{(i)} = \hat{y}^{(i)} = \sigma(z^{(i)}) = \sigma(w^T x^{(i)} + b)$$

$$(x^{(i)}, y^{(i)})$$

$$\underline{dw_1^{(i)}}, \underline{dw_2^{(i)}}, \underline{db^{(i)}}$$

$$\underline{\frac{\partial}{\partial w_1} J(w, b)} = \frac{1}{m} \sum_{i=1}^m \underbrace{\frac{\partial}{\partial w_1} \ell(a^{(i)}, y^{(i)})}_{\underline{dw_1^{(i)}} - (x^{(i)}, y^{(i)})}$$

# Logistic regression on $m$ examples

$$J=0; \quad \underline{dw_1}=0; \quad \underline{dw_2}=0; \quad \underline{db}=0$$

→ For  $i=1$  to  $m$

$$z^{(i)} = w^T x^{(i)} + b$$

$$a^{(i)} = \sigma(z^{(i)})$$

$$J += -[y^{(i)} \log a^{(i)} + (1-y^{(i)}) \log(1-a^{(i)})]$$

$$\underline{dz^{(i)}} = a^{(i)} - y^{(i)}$$

$$\begin{array}{l} \uparrow \\ dw_1 += x_1^{(i)} dz^{(i)} \\ dw_2 += x_2^{(i)} dz^{(i)} \\ db += dz^{(i)} \\ \downarrow \end{array} \quad \begin{array}{l} \uparrow \\ n=2 \\ \downarrow \end{array}$$

$$J /= m \leftarrow$$

$$\begin{array}{ccc} dw_1 /= m & ; & dw_2 /= m; db /= m. \leftarrow \\ \uparrow & & \uparrow \end{array}$$

$$dw_1 = \frac{\partial J}{\partial w_1}$$

$$w_1 := w_1 - \alpha \underline{dw_1}$$

$$w_2 := w_2 - \alpha \underline{dw_2}$$

$$b := b - \alpha \underline{db}$$

Vectorization



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# Basics of Neural Network Programming

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## Vectorization

# What is vectorization?

$$z = \underline{w^T x} + b$$

Non-vectorized:

$$z = 0$$

for  $i$  in range( $n-x$ ):

$$z += w[i] * x[i]$$

$$z += b$$

$$w = \begin{bmatrix} : \\ : \\ : \end{bmatrix} \quad x = \begin{bmatrix} : \\ : \\ : \end{bmatrix}$$

$$w \in \mathbb{R}^{n_x}$$

$$x \in \mathbb{R}^{n_x}$$

Vectorized

$$z = \underbrace{\text{np.dot}(w, x)}_{w^T x} + b$$

→ GPU } SIMD - single instruction  
→ CPU } multiple data.



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# Basics of Neural Network Programming

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## More vectorization examples



# Neural network programming guideline

Whenever possible, avoid explicit for-loops.

# Neural network programming guideline

Whenever possible, avoid explicit for-loops.

$$u = Av$$

$$u_i = \sum_i \sum_j A_{ij} v_j$$

$$u = \text{np.zeros}(n, 1)$$

for i ... ←

for j ... ←

$$u[i] += A[i][j] * v[j]$$

$$u = \text{np.dot}(A, v)$$

# Vectors and matrix valued functions

Say you need to apply the exponential operation on every element of a matrix/vector.

$$v = \begin{bmatrix} v_1 \\ \vdots \\ v_n \end{bmatrix} \rightarrow u = \begin{bmatrix} e^{v_1} \\ e^{v_2} \\ \vdots \\ e^{v_n} \end{bmatrix}$$

```
→ u = np.zeros((n,1))  
→ for i in range(n): ←  
    → u[i] = math.exp(v[i])
```

```
import numpy as np  
u = np.exp(v) ←  
np.log(v)  
np.abs(v)  
np.maximum(v, 0)  
v**2      1/v
```

# Logistic regression derivatives

$$J = 0, \quad \boxed{\cancel{dw_1 = 0, dw_2 = 0}}, \quad db = 0$$

$$dw = np.zeros((n-x, 1))$$

→ for i = 1 to n:

$$z^{(i)} = w^T x^{(i)} + b$$

$$a^{(i)} = \sigma(z^{(i)})$$

$$J += -[y^{(i)} \log \hat{y}^{(i)} + (1 - y^{(i)}) \log(1 - \hat{y}^{(i)})]$$

$$dz^{(i)} = a^{(i)}(1 - a^{(i)})$$

$$\boxed{\begin{aligned} \cancel{dw_1 += x_1^{(i)} dz^{(i)}} \\ \cancel{dw_2 += x_2^{(i)} dz^{(i)}} \end{aligned}}$$

$$n_x = 2$$

$$dw += x^{(i)} dz^{(i)}$$

$$db += dz^{(i)}$$

$$J = J/m, \quad \boxed{\cancel{dw_1 = dw_1/m, dw_2 = dw_2/m}}, \quad db = db/m$$

$$dw /= m.$$



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# Basics of Neural Network Programming

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## Vectorizing Logistic Regression

# Vectorizing Logistic Regression

$$\begin{aligned} \Rightarrow \underline{z^{(1)}} &= \underline{w^T x^{(1)}} + b \\ \Rightarrow \underline{a^{(1)}} &= \sigma(z^{(1)}) \end{aligned} \quad \begin{aligned} \underline{z^{(2)}} &= \underline{w^T x^{(2)}} + b \\ \underline{a^{(2)}} &= \sigma(z^{(2)}) \end{aligned} \quad \begin{aligned} \underline{z^{(3)}} &= \underline{w^T x^{(3)}} + b \\ \underline{a^{(3)}} &= \sigma(z^{(3)}) \end{aligned}$$

$$\underline{X} = \begin{bmatrix} x^{(1)} & x^{(2)} & \dots & x^{(m)} \\ | & | & & | \\ | & | & & | \\ | & | & & | \end{bmatrix}$$

$$\begin{matrix} (n_x, m) \\ \mathbb{R}^{n_x \times m} \end{matrix}$$

$$\underline{w^T} \begin{bmatrix} x^{(1)} & x^{(2)} & \dots & x^{(m)} \\ | & | & & | \\ | & | & & | \end{bmatrix}$$

$$\underline{Z} = \begin{bmatrix} z^{(1)} & z^{(2)} & \dots & z^{(m)} \\ | & | & & | \end{bmatrix} = \underline{w^T X} + \begin{bmatrix} b & b & \dots & b \end{bmatrix}_{1 \times m} = \begin{bmatrix} \underline{w^T x^{(1)} + b} & \underline{w^T x^{(2)} + b} & \dots & \underline{w^T x^{(m)} + b} \end{bmatrix}_{1 \times m}$$

$$\Rightarrow \underline{Z} = \text{np.dot}(w.T, X) + \underline{b}$$

"Broadcasting"

$$\underline{A} = \begin{bmatrix} a^{(1)} & a^{(2)} & \dots & a^{(m)} \end{bmatrix} = \sigma(\underline{Z})$$



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# Basics of Neural Network Programming

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## Vectorizing Logistic Regression's Gradient Computation

# Vectorizing Logistic Regression

$$dz^{(1)} = a^{(1)} - y^{(1)}$$

$$dz^{(2)} = a^{(2)} - y^{(2)}$$

.....

$$dZ = \begin{bmatrix} dz^{(1)} & dz^{(2)} & \dots & dz^{(m)} \end{bmatrix} \quad 1 \times m$$

$$A = [a^{(1)} \dots a^{(m)}] \quad Y = [y^{(1)} \dots y^{(m)}]$$

$$\rightarrow dZ = A - Y = \begin{bmatrix} a^{(1)} - y^{(1)} & a^{(2)} - y^{(2)} & \dots \end{bmatrix}$$

$$\rightarrow dw = 0$$

$$dw += \frac{x^{(1)} dz^{(1)}}{m}$$

$$dw += \frac{x^{(2)} dz^{(2)}}{m}$$

⋮

$$dw /= m$$

$$db = 0$$

$$db += dz^{(1)}$$

$$db += dz^{(2)}$$

$$\vdots$$

$$db += dz^{(m)}$$

$$db /= m$$

$$db = \frac{1}{m} \sum_{i=1}^m dz^{(i)}$$

$$= \frac{1}{m} \text{np.sum}(dZ)$$

$$dw = \frac{1}{m} X dZ^T$$

$$= \frac{1}{m} \begin{bmatrix} x^{(1)} & \dots & x^{(m)} \\ 1 & & 1 \end{bmatrix} \begin{bmatrix} dz^{(1)} \\ \vdots \\ dz^{(m)} \end{bmatrix}$$

$$= \frac{1}{m} \left[ \underbrace{x^{(1)} dz^{(1)}}_{n \times 1} + \dots + \underbrace{x^{(m)} dz^{(m)}}_{n \times 1} \right]$$



# Implementing Logistic Regression

$J = 0, dw_1 = 0, dw_2 = 0, db = 0$

for  $i = 1$  to  $m$ :

$$z^{(i)} = w^T x^{(i)} + b \leftarrow$$

$$a^{(i)} = \sigma(z^{(i)}) \leftarrow$$

$$J += -[y^{(i)} \log a^{(i)} + (1 - y^{(i)}) \log(1 - a^{(i)})]$$

$$dz^{(i)} = a^{(i)} - y^{(i)} \leftarrow$$

$$\left[ \begin{array}{l} dw_1 += x_1^{(i)} dz^{(i)} \\ dw_2 += x_2^{(i)} dz^{(i)} \end{array} \right\} dw += x^{(i)} * dz^{(i)}$$

$$db += dz^{(i)}$$

$$J = J/m, dw_1 = dw_1/m, dw_2 = dw_2/m$$

$$db = db/m$$

for iter in range(1000):  $\leftarrow$

$$Z = w^T X + b$$

$$= np.dot(w.T, X) + b$$

$$A = \sigma(Z)$$

$$dZ = A - Y$$

$$dw = \frac{1}{m} X dZ^T$$

$$db = \frac{1}{m} np.sum(dZ)$$

$$w := w - \alpha dw$$

$$b := b - \alpha db$$



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# Basics of Neural Network Programming

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## Broadcasting in Python

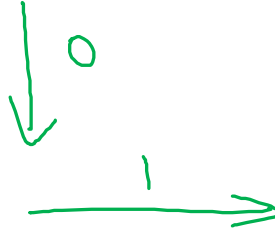
# Broadcasting example

Calories from Carbs, Proteins, Fats in 100g of different foods:

	Apples	Beef	Eggs	Potatoes
Carb	56.0	0.0	4.4	68.0
Protein	1.2	104.0	52.0	8.0
Fat	1.8	135.0	99.0	0.9

$= A$   
(3,4)

59 cal  
 $\frac{56}{59} \approx 94.9\%$



Calculate % of calories from Carb, Protein, Fat. Can you do this without explicit for-loop?

```
cal = A.sum(axis = 0)
percentage = 100 * A / (cal.reshape(1, 4))
```

↑(3,4) / (1,4)

# Broadcasting example

$$\begin{bmatrix} 1 \\ 2 \\ 3 \\ 4 \end{bmatrix} + \begin{bmatrix} 100 \\ 100 \\ 100 \\ 100 \end{bmatrix} \quad \text{100}$$

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix} \quad \begin{matrix} (m,n) & (2,3) \end{matrix} + \begin{matrix} \swarrow \\ \begin{bmatrix} 100 & 200 & 300 \\ 100 & 200 & 300 \end{bmatrix} \\ (1,n) \rightsquigarrow (m,n) \quad (2,3) \end{matrix}$$

↓      ↓      ↓

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix} \quad \begin{matrix} (m,n) \end{matrix} + \begin{matrix} \begin{bmatrix} 100 & 100 & 100 \\ 200 & 200 & 200 \end{bmatrix} \\ (m,1) \\ \downarrow \\ (m,n) \end{matrix} = \quad \begin{matrix} \leftarrow \\ \leftarrow \end{matrix}$$

# General Principle

$$\begin{array}{ccc}
 (m, n) & + & (1, n) \rightsquigarrow (m, n) \\
 \text{matrix} & * & \\
 \hline & / & (m, 1) \rightsquigarrow (m, n)
 \end{array}$$

$$\begin{array}{ccc}
 (m, 1) & + & \mathbb{R} \\
 \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix} & + & 100 = \begin{bmatrix} 101 \\ 102 \\ 103 \end{bmatrix} \\
 [1 \ 2 \ 3] & + & 100 = [101 \quad 102 \quad 103]
 \end{array}$$

Matlab/Octave: bsxfun



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# Basics of Neural Network Programming

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A note on python/  
numpy vectors

# Python Demo

# Python / numpy vectors

```
import numpy as np  
  
a = np.random.randn(5)  
  
a = np.random.randn(5, 1)  
  
a = np.random.randn(1, 5)  
  
assert(a.shape == (5, 1))
```





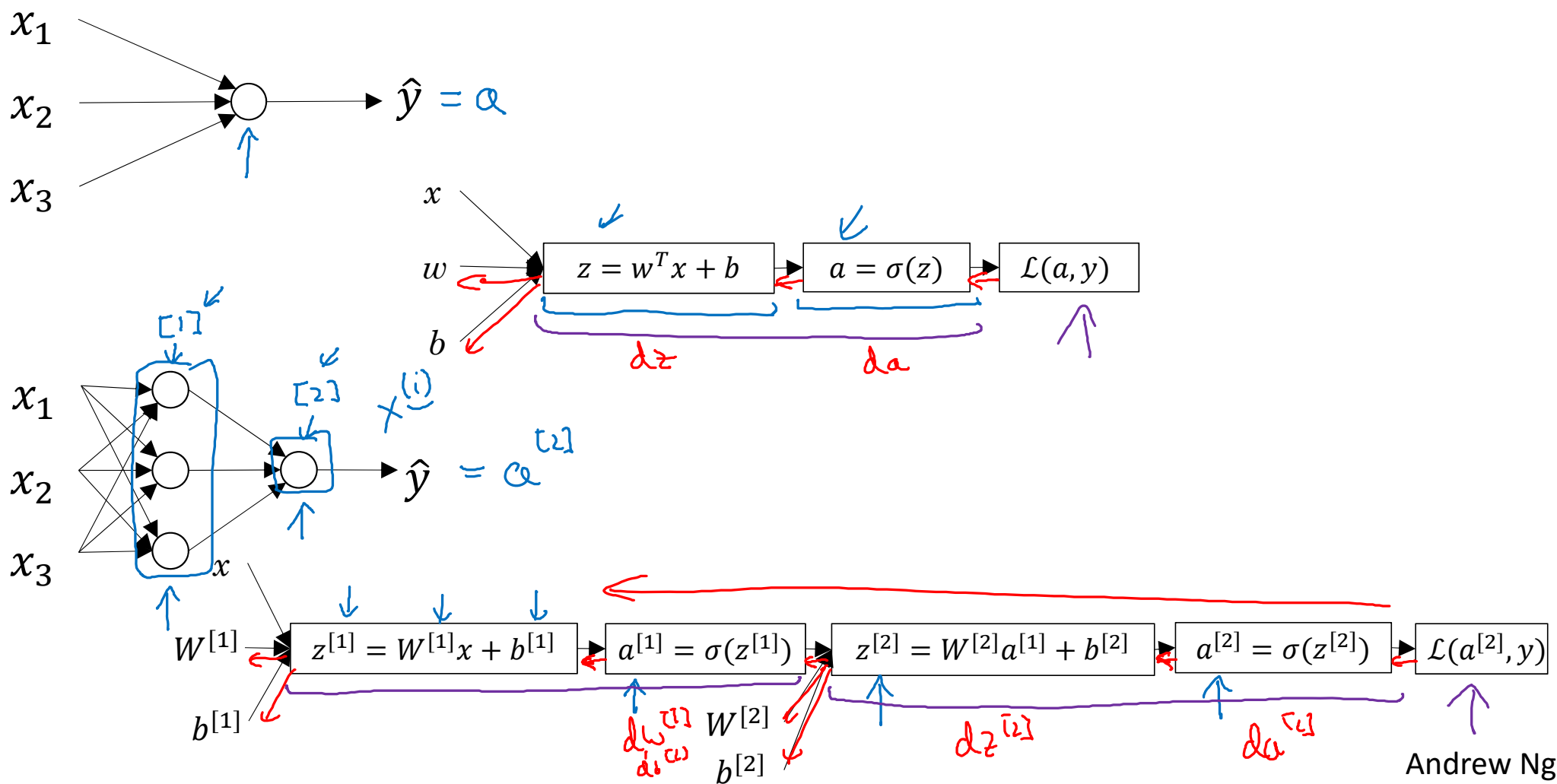
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One hidden layer  
Neural Network

---

# Neural Networks Overview

# What is a Neural Network?





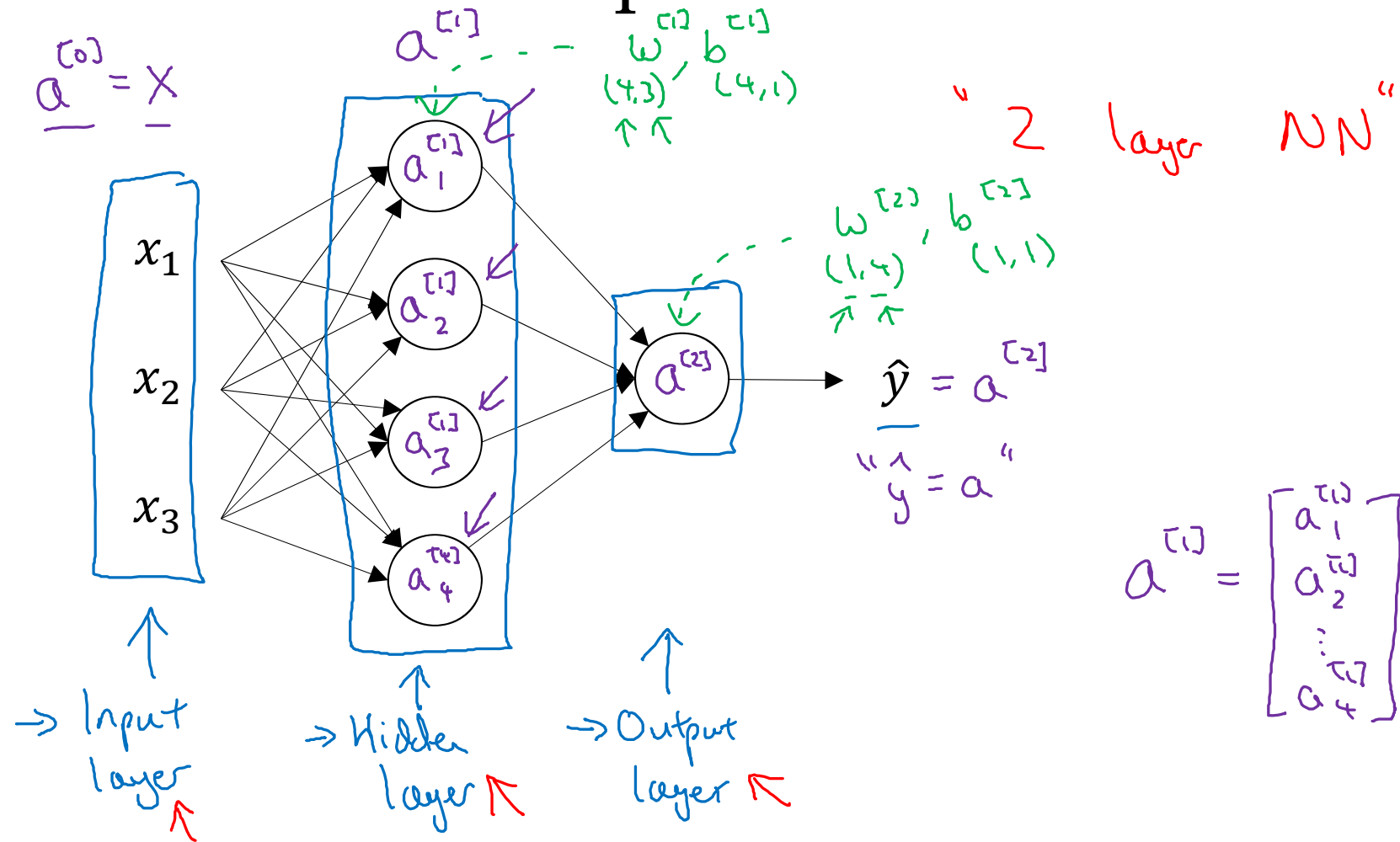
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One hidden layer  
Neural Network

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Neural Network  
Representation

# Neural Network Representation





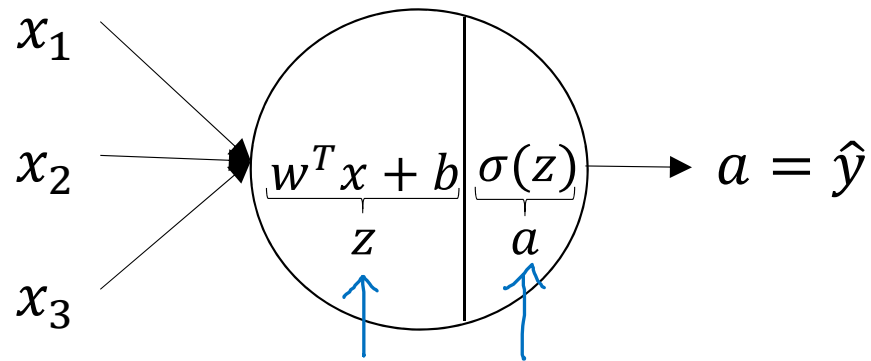
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# One hidden layer Neural Network

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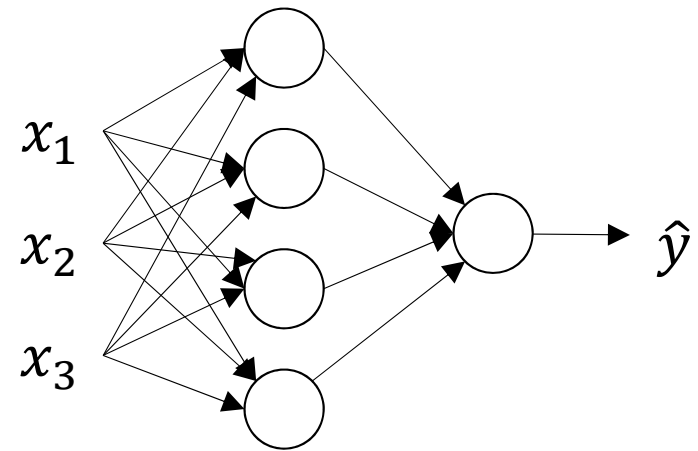
## Computing a Neural Network's Output

# Neural Network Representation

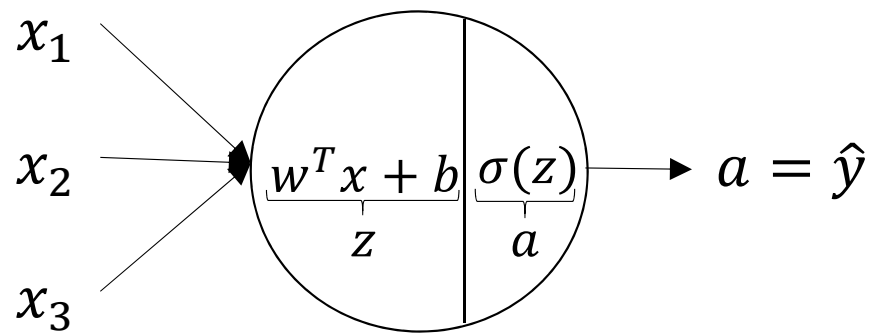


$$z = w^T x + b$$

$$a = \sigma(z)$$

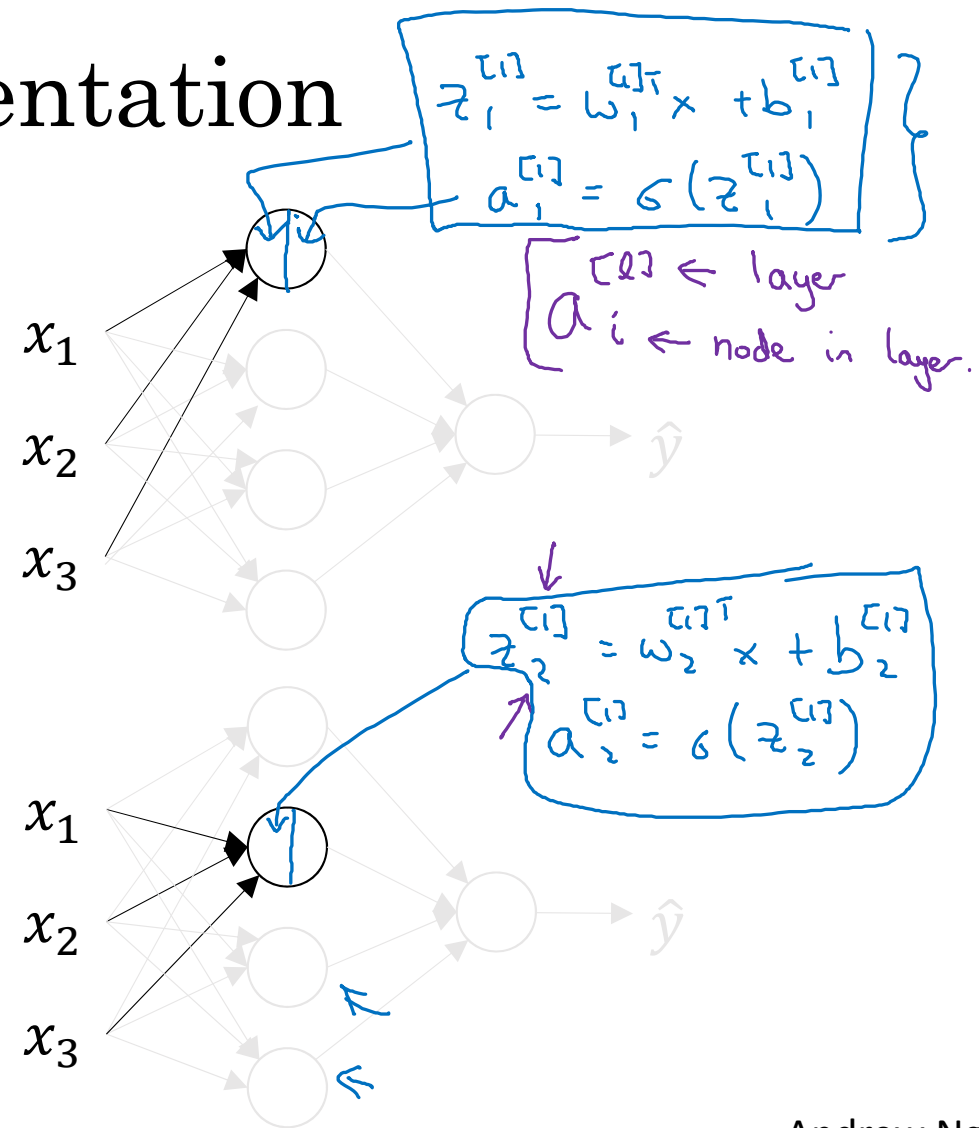


# Neural Network Representation

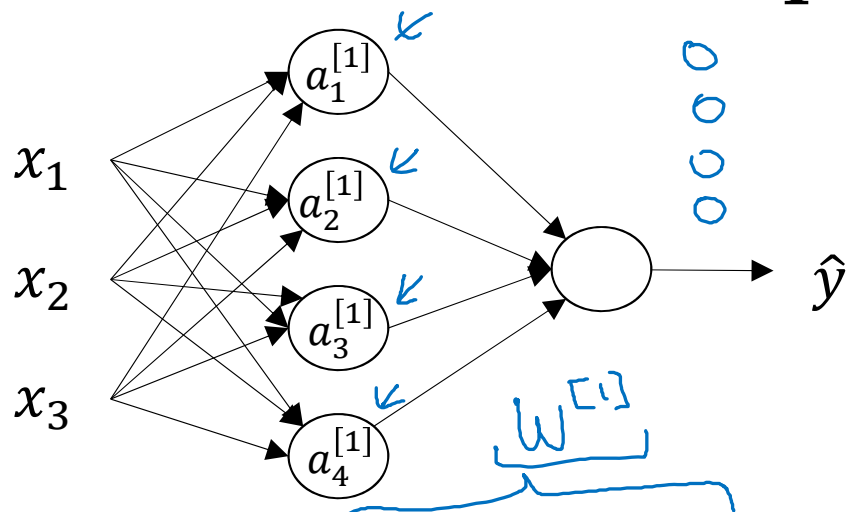


$$z = w^T x + b$$

$$a = \sigma(z)$$



# Neural Network Representation



$$\begin{aligned}
 z_1^{[1]} &= w_1^{[1]T} x + b_1^{[1]} & a_1^{[1]} &= \sigma(z_1^{[1]}) \\
 z_2^{[1]} &= w_2^{[1]T} x + b_2^{[1]} & a_2^{[1]} &= \sigma(z_2^{[1]}) \\
 z_3^{[1]} &= w_3^{[1]T} x + b_3^{[1]} & a_3^{[1]} &= \sigma(z_3^{[1]}) \\
 z_4^{[1]} &= w_4^{[1]T} x + b_4^{[1]} & a_4^{[1]} &= \sigma(z_4^{[1]})
 \end{aligned}$$

Handwritten notes and matrix representations:

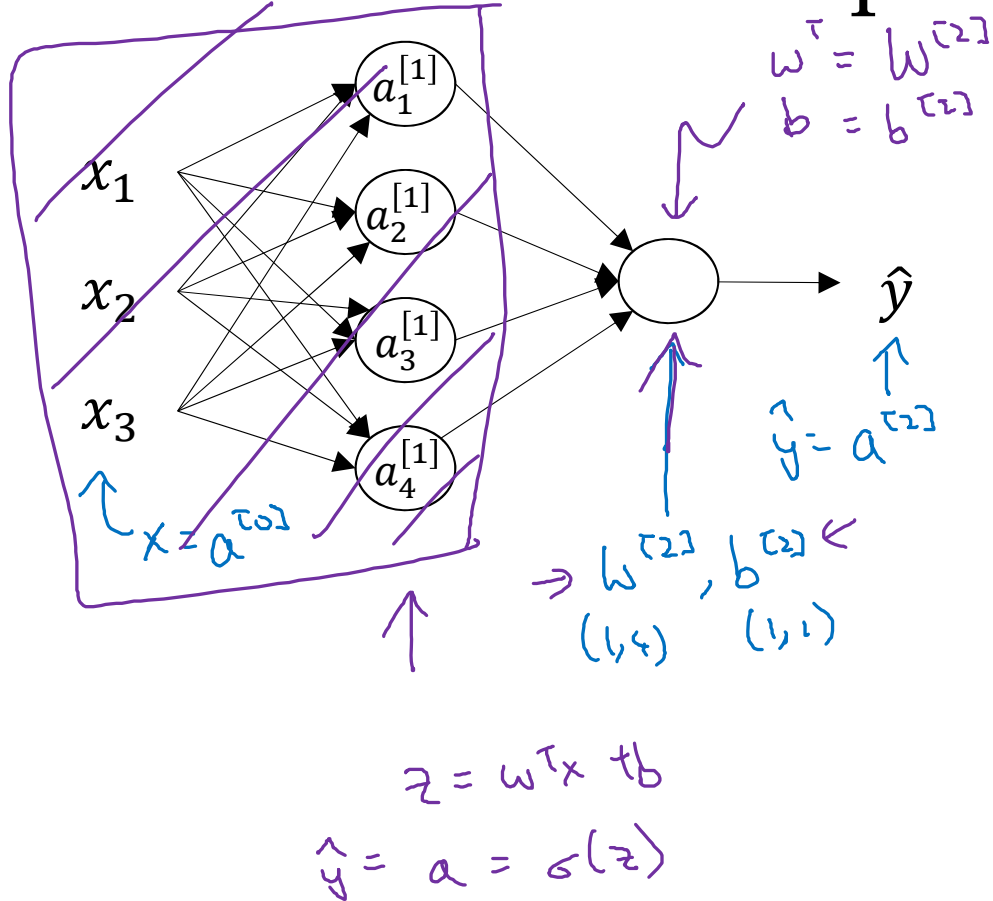
$\rightarrow z^{[1]} = \begin{bmatrix} w_1^{[1]T} \\ w_2^{[1]T} \\ w_3^{[1]T} \\ w_4^{[1]T} \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} + \begin{bmatrix} b_1^{[1]} \\ b_2^{[1]} \\ b_3^{[1]} \\ b_4^{[1]} \end{bmatrix} = \begin{bmatrix} w_1^{[1]T} x + b_1^{[1]} \\ w_2^{[1]T} x + b_2^{[1]} \\ w_3^{[1]T} x + b_3^{[1]} \\ w_4^{[1]T} x + b_4^{[1]} \end{bmatrix} = \begin{bmatrix} z_1^{[1]} \\ z_2^{[1]} \\ z_3^{[1]} \\ z_4^{[1]} \end{bmatrix}$

$\rightarrow a^{[1]} = \begin{bmatrix} a_1^{[1]} \\ \vdots \\ a_4^{[1]} \end{bmatrix} = \sigma(z^{[1]})$

Dimensions:  $w^{[1]} (4, 3)$ ,  $b^{[1]} (4, 1)$ ,  $z^{[1]} (4, 1)$ ,  $a^{[1]} (4, 1)$ .



# Neural Network Representation learning



Given input  $x$ :

$$\begin{aligned} \rightarrow z^{[1]} &= W^{[1]} a^{[0]} + b^{[1]} \\ &\quad \begin{matrix} (4,1) & (4,3) & (3,1) & (4,1) \end{matrix} \\ \rightarrow a^{[1]} &= \sigma(z^{[1]}) \\ &\quad \begin{matrix} (4,1) & (4,1) \end{matrix} \\ \rightarrow z^{[2]} &= W^{[2]} a^{[1]} + b^{[2]} \\ &\quad \begin{matrix} (1,1) & (1,4) & (4,1) & (1,1) \end{matrix} \\ \rightarrow a^{[2]} &= \sigma(z^{[2]}) \\ &\quad \begin{matrix} (1,1) & (1,1) \end{matrix} \end{aligned}$$



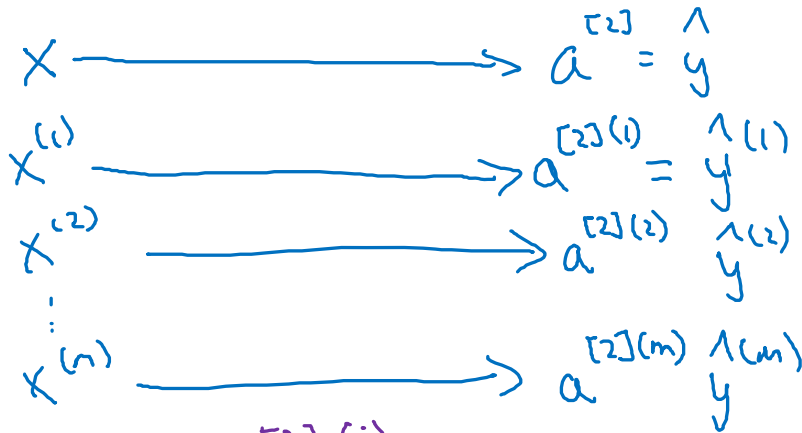
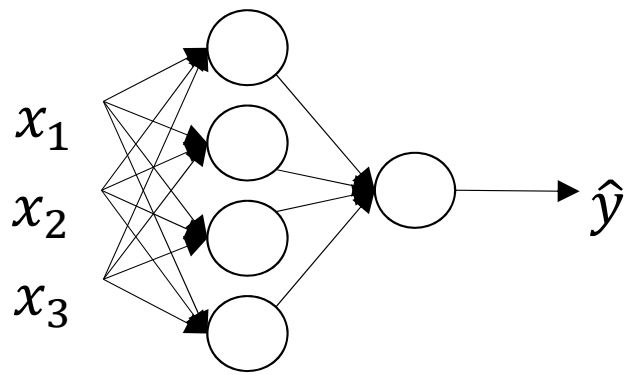
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# One hidden layer Neural Network

---

## Vectorizing across multiple examples

# Vectorizing across multiple examples



$a^{[2](i)}$   
 $\nwarrow \nearrow$  example  $i$   
 layer 2

$$z^{[1]} = W^{[1]}x + b^{[1]}$$

$$a^{[1]} = \sigma(z^{[1]})$$

$$z^{[2]} = W^{[2]}a^{[1]} + b^{[2]}$$

$$a^{[2]} = \sigma(z^{[2]})$$

→ for  $i = 1$  to  $m$ ,

$$z^{[1](i)} = W^{[1]}x^{(i)} + b^{[1]}$$

$$a^{[1](i)} = \sigma(z^{[1](i)})$$

$$z^{[2](i)} = W^{[2]}a^{[1](i)} + b^{[2]}$$

$$a^{[2](i)} = \sigma(z^{[2](i)})$$

# Vectorizing across multiple examples

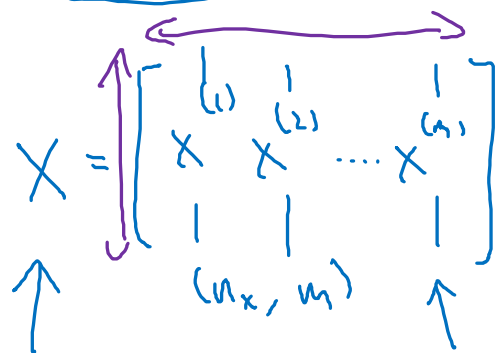
for  $i = 1$  to  $m$ :

$$z^{[1]}(i) = W^{[1]}x^{(i)} + b^{[1]}$$

$$a^{[1]}(i) = \sigma(z^{[1]}(i))$$

$$z^{[2]}(i) = W^{[2]}a^{[1]}(i) + b^{[2]}$$

$$a^{[2]}(i) = \sigma(z^{[2]}(i))$$



training examples

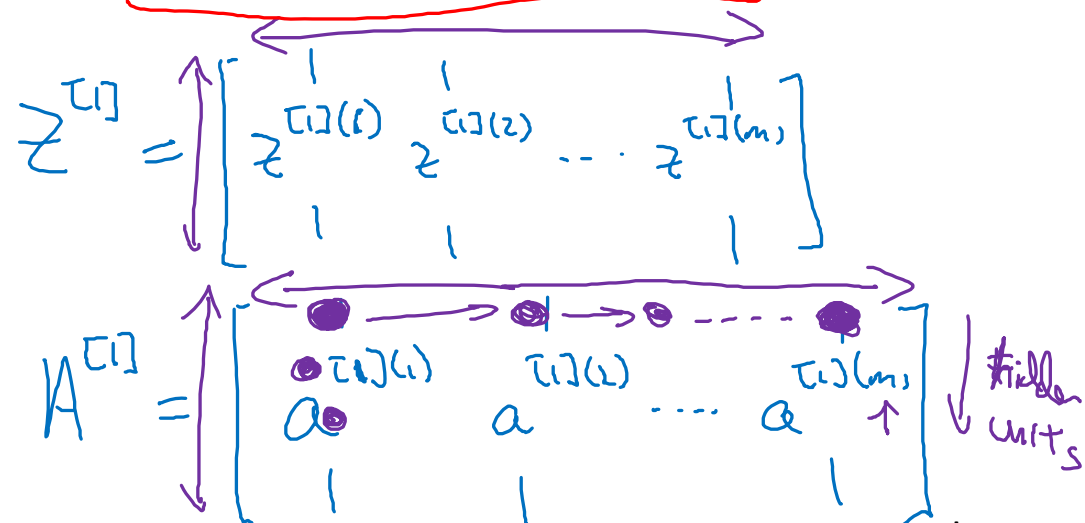
hidden units.

$$z^{[1]} = W^{[1]}X + b^{[1]}$$

$$\rightarrow A^{[1]} = \sigma(z^{[1]})$$

$$\rightarrow z^{[2]} = W^{[2]}A^{[1]} + b^{[2]}$$

$$\rightarrow A^{[2]} = \sigma(z^{[2]})$$



Andrew Ng



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# One hidden layer Neural Network

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Explanation  
for vectorized  
implementation

# Justification for vectorized implementation

$$\underline{z^{[1](1)}} = \underbrace{w^{[1]} x^{(1)}} + \cancel{b^{[1]}} \quad , \quad \underline{z^{[1](2)}} = \underbrace{w^{[1]} x^{(2)}} + \cancel{b^{[1]}} \quad , \quad \underline{z^{[1](3)}} = \underbrace{w^{[1]} x^{(3)}} + \cancel{b^{[1]}}$$

↑ 0
↑ 0
↑ 0

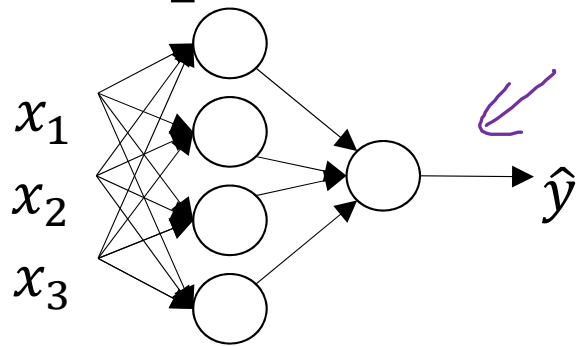
$$w^{[1]} = \begin{bmatrix} \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \end{bmatrix} \quad w^{[1]} x^{(1)} = \begin{bmatrix} \bullet \\ \bullet \\ \bullet \\ \bullet \end{bmatrix} \quad w^{[1]} x^{(2)} = \begin{bmatrix} \bullet \\ \bullet \\ \bullet \\ \bullet \end{bmatrix} \quad w^{[1]} x^{(3)} = \begin{bmatrix} \bullet \\ \bullet \\ \bullet \\ \bullet \end{bmatrix}$$

$$w^{[1]} \begin{bmatrix} | & | & | & \dots \\ x^{(1)} & x^{(2)} & x^{(3)} & \dots \\ | & | & | & \dots \end{bmatrix} = \begin{bmatrix} \bullet & \bullet & \bullet & \dots \\ \bullet & \bullet & \bullet & \dots \\ \bullet & \bullet & \bullet & \dots \\ \bullet & \bullet & \bullet & \dots \end{bmatrix} = \begin{bmatrix} | & | & | & \dots \\ z^{[1](1)} & z^{[1](2)} & z^{[1](3)} & \dots \\ | & | & | & \dots \end{bmatrix} = z^{[1]}$$

↑  $+ b^{[1]}$ 
↑  $+ b^{[1]}$ 
↑  $+ b^{[1]}$

$\hat{X} \rightarrow w^{[1]} \hat{X} = z^{[1]}$

# Recap of vectorizing across multiple examples



$$X = \begin{bmatrix} | & | & \dots & | \\ x^{(1)} & x^{(2)} & \dots & x^{(m)} \\ | & | & \dots & | \end{bmatrix}$$

$$\underline{A^{[1]}} = \begin{bmatrix} | & | & \dots & | \\ a^{[1](1)} & a^{[1](2)} & \dots & a^{[1](m)} \\ | & | & \dots & | \end{bmatrix}$$

for  $i = 1$  to  $m$

$$z^{[1](i)} = W^{[1]}x^{(i)} + b^{[1]}$$

$$\rightarrow a^{[1](i)} = \sigma(z^{[1](i)})$$

$$\rightarrow z^{[2](i)} = W^{[2]}a^{[1](i)} + b^{[2]}$$

$$\rightarrow a^{[2](i)} = \sigma(z^{[2](i)})$$

$$Z^{[1]} = W^{[1]}X + b^{[1]}$$

$$A^{[1]} = \sigma(Z^{[1]})$$

$$Z^{[2]} = W^{[2]}A^{[1]} + b^{[2]}$$

$$A^{[2]} = \sigma(Z^{[2]})$$

$$x = a^{[0]} \quad x^{(i)} = a^{[0](i)}$$

$$W^{[1]}A^{[0]} + b^{[1]}$$



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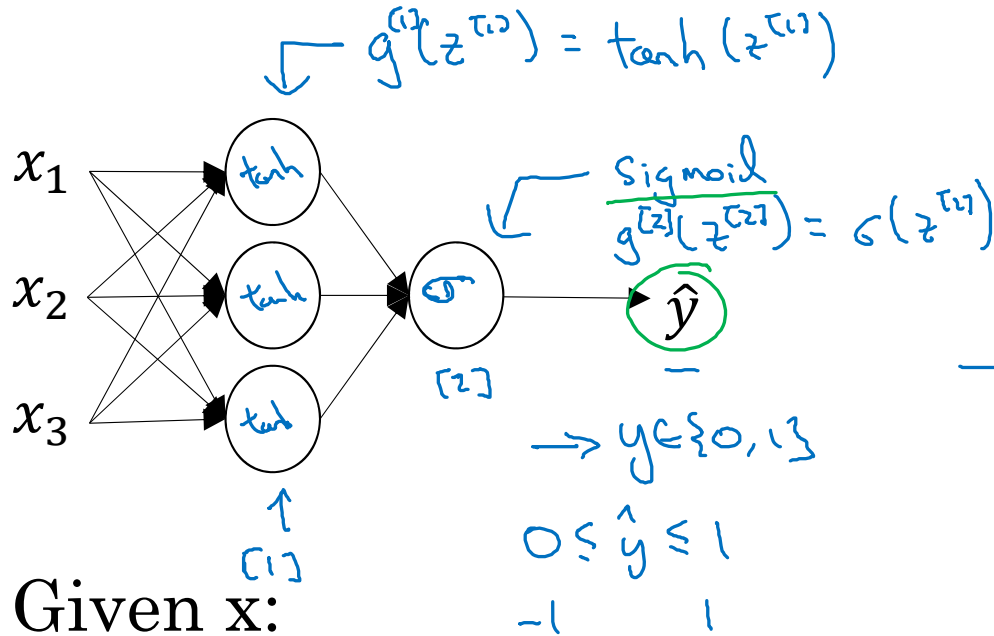
# One hidden layer Neural Network

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## Activation functions



# Activation functions



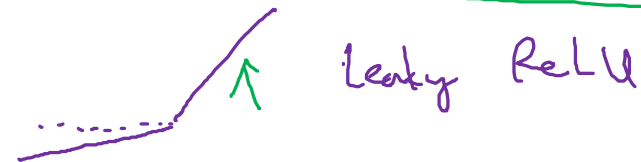
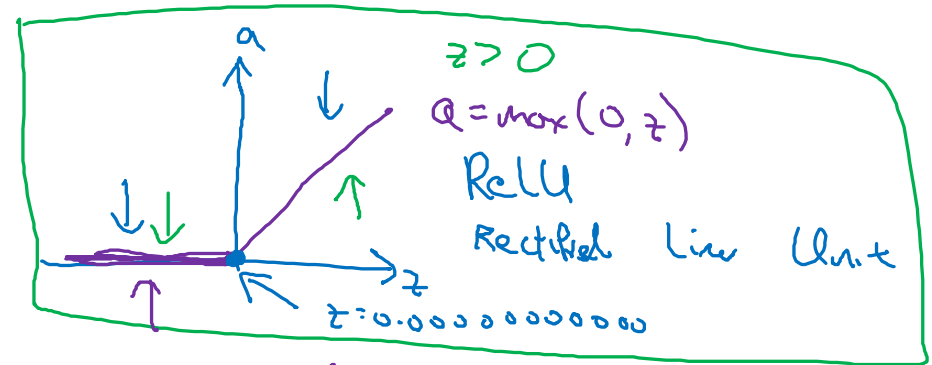
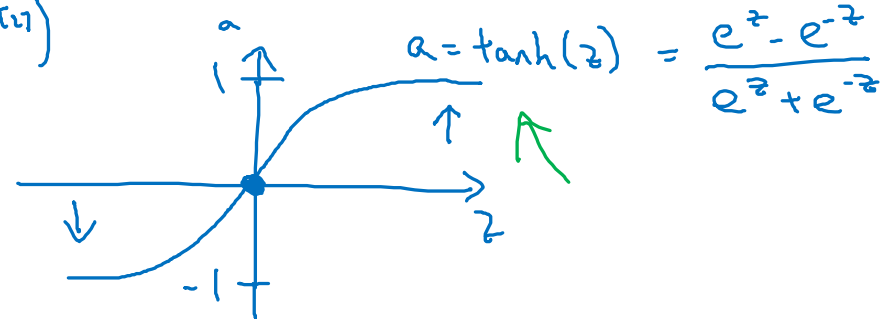
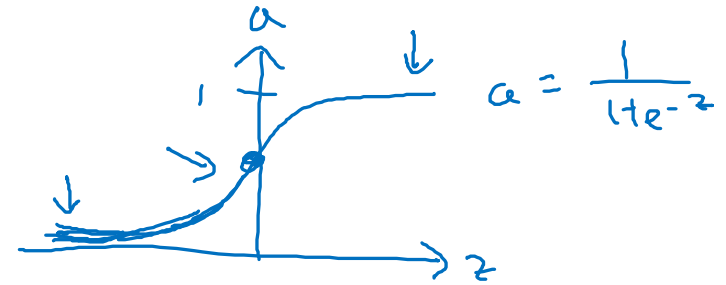
Given  $x$ :

$$z^{[1]} = W^{[1]}x + b^{[1]}$$

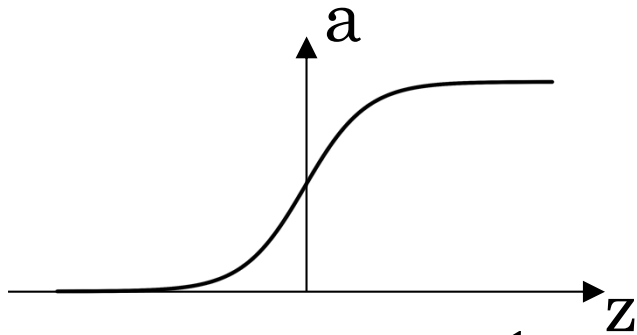
$$\rightarrow a^{[1]} = \cancel{\sigma(z^{[1]})} \quad g^{(1)}(z^{(1)})$$

$$z^{[2]} = W^{[2]}a^{[1]} + b^{[2]}$$

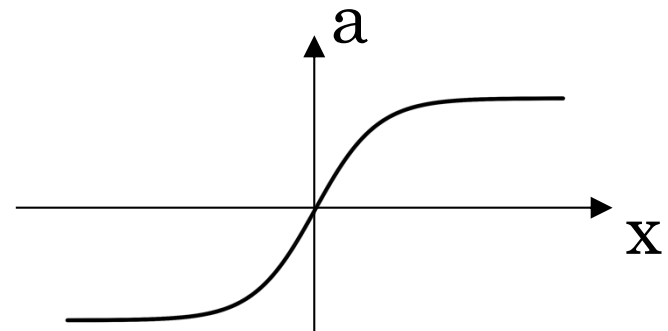
$$\rightarrow a^{[2]} = \cancel{\sigma(z^{[2]})} \quad g^{(2)}(z^{(2)})$$



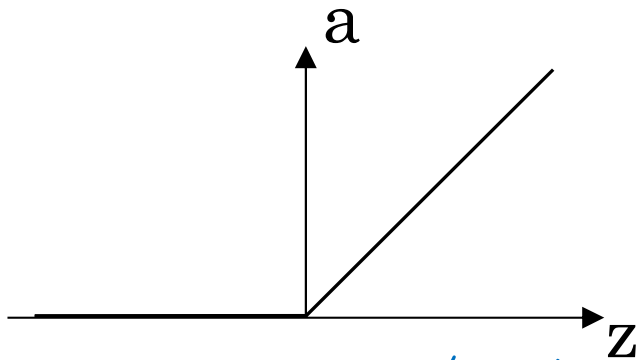
# Pros and cons of activation functions



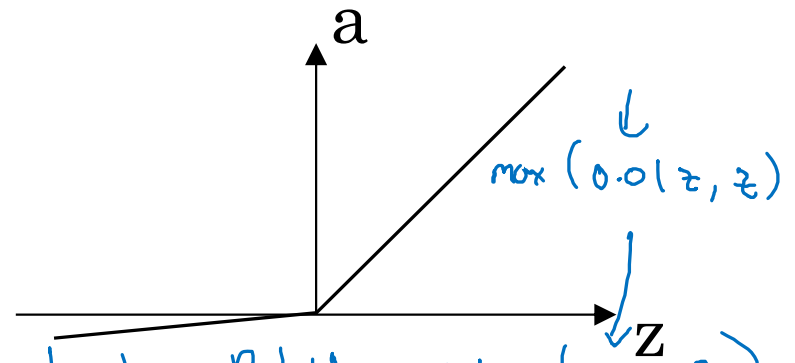
sigmoid:  $a = \frac{1}{1 + e^{-z}}$



tanh:  $a = \frac{e^z - e^{-z}}{e^z + e^{-z}}$



ReLU  $a = \max(0, z)$



Leaky ReLU  $a = \max(0.01z, z)$



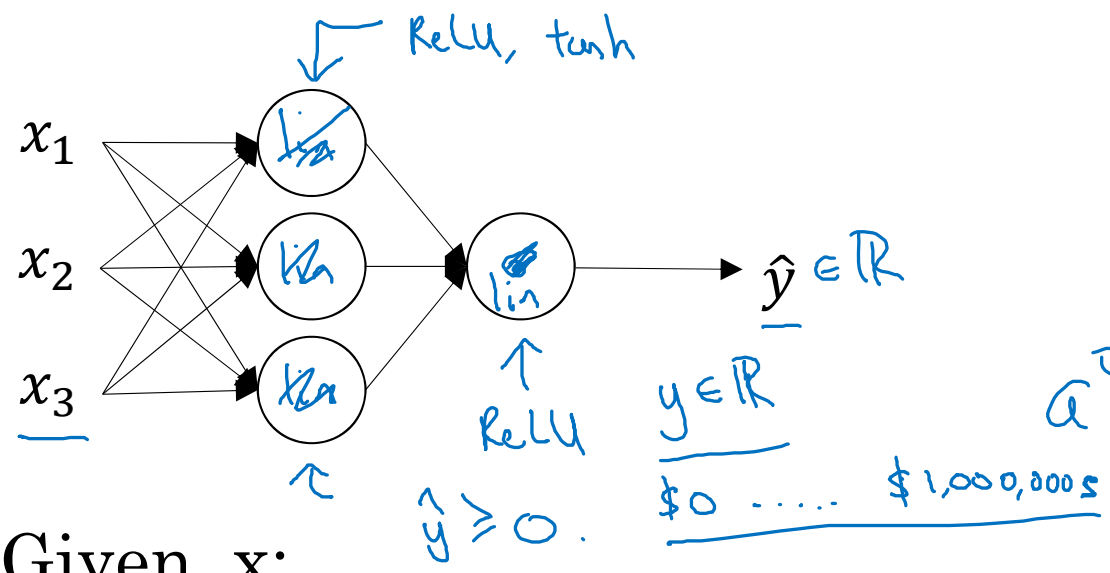
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# One hidden layer Neural Network

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Why do you  
need non-linear  
activation functions?

# Activation function



$$a^{[1]} = z^{[1]} = W^{[1]}x + b^{[1]}$$

$$a^{[2]} = z^{[2]} = W^{[2]}a^{[1]} + b^{[2]}$$

$$a^{[2]} = W^{[2]} \left( W^{[1]}x + b^{[1]} \right) + b^{[2]}$$

$$= \underbrace{(W^{[2]} W^{[1]})}_{w'} x + \underbrace{(W^{[2]} b^{[1]} + b^{[2]})}_{b'}$$

$$= w'x + b'$$

$$g(z) = z$$

- Given  $x$ :
- $\rightarrow z^{[1]} = W^{[1]}x + b^{[1]}$
  - $\rightarrow a^{[1]} = \cancel{g^{[1]}(z^{[1]})} z^{[1]}$
  - $\rightarrow z^{[2]} = W^{[2]}a^{[1]} + b^{[2]}$
  - $\rightarrow a^{[2]} = \cancel{g^{[2]}(z^{[2]})} z^{[2]}$

$g(z) = z$   
"linear activation function"



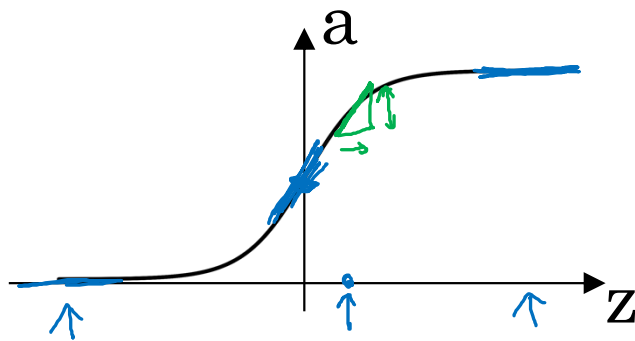
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# One hidden layer Neural Network

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## Derivatives of activation functions

# Sigmoid activation function



$$\underline{g(z) = \frac{1}{1 + e^{-z}}}$$

$$a = g(z) = \frac{1}{1 + e^{-z}}$$

$$\begin{aligned} \boxed{g'(z)} &= \boxed{\frac{d}{dz} g(z)} = \text{slope of } g(z) \text{ at } z \\ &= \frac{1}{1 + e^{-z}} \left( 1 - \frac{1}{1 + e^{-z}} \right) \\ &= g(z) (1 - g(z)) \leftarrow \\ &= \boxed{a(1-a)} \quad \left| \begin{array}{l} g'(z) = a(1-a) \\ \uparrow \\ a \end{array} \right. \end{aligned}$$

$$z = 10, \quad g(z) \approx 1$$

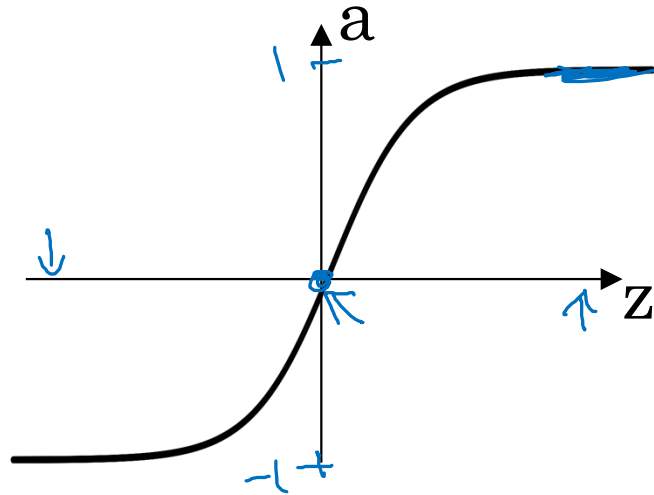
$$\frac{d}{dz} g(z) \approx 1(1-1) \approx 0$$

$$z = -10, \quad g(z) \approx 0$$

$$\frac{d}{dz} g(z) \approx 0 \cdot (1-0) \approx 0$$

$$\begin{aligned} z = 0, \quad g(z) &= \frac{1}{2} \\ \frac{d}{dz} g(z) &= \frac{1}{2} \left( 1 - \frac{1}{2} \right) = \frac{1}{4} \end{aligned}$$

# Tanh activation function



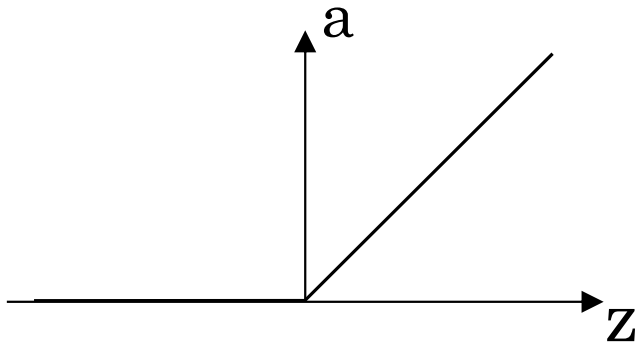
$$g(z) = \tanh(z) = \frac{e^z - e^{-z}}{e^z + e^{-z}}$$

$$g'(z) = \frac{d}{dz} g(z) = \text{slope of } g(z) \text{ at } z = \underline{1 - (\tanh(z))^2} \leftarrow$$

$$a = g(z), \quad g'(z) = 1 - \underset{\uparrow}{a^2}$$

$$\left| \begin{array}{ll} z=10 & \tanh(z) \approx 1 \\ & g'(z) \approx 0 \\ z=-10 & \tanh(z) \approx -1 \\ & g'(z) \approx 0 \\ z=0 & \tanh(z) = 0 \\ & g'(z) = 1 \end{array} \right.$$

# ReLU and Leaky ReLU



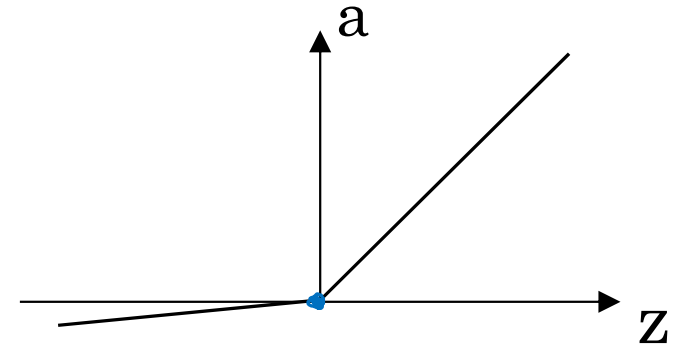
ReLU

$$g(z) = \max(0, z)$$

$$\rightarrow g'(z) = \begin{cases} 0 & \text{if } z < 0 \\ 1 & \text{if } z \geq 0 \end{cases}$$

~~undefined if  $z = 0$~~

$z = 0.000\ldots 0$



# Leaky ReLU

$$g(z) = \max(0.01z, z)$$
$$g'(z) = \begin{cases} 0.01 & \text{if } z < 0 \\ 1 & \text{if } z \geq 0 \end{cases}$$





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One hidden layer  
Neural Network

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Gradient descent for  
neural networks

# Gradient descent for neural networks

Parameters:  $W^{[1]}, b^{[1]}, W^{[2]}, b^{[2]}$   
 $(n^{[1]}, n^{[0]})$   $(n^{[1]}, 1)$   $(n^{[2]}, n^{[1]})$   $(n^{[2]}, 1)$

$$n_x = n^{[0]}, n^{[1]}, \underline{n^{[2]} = 1}$$

Cost function:  $J(W^{[1]}, b^{[1]}, \underline{W^{[2]}}, \underline{b^{[2]}}) = \frac{1}{m} \sum_{i=1}^m \ell(\hat{y}, y)$   
 $\uparrow \quad \uparrow \quad \uparrow a^{[2]}$

Gradient descent:

→ Repeat {

→ Compute predictions  $(\hat{y}^{(i)}, i=1, \dots, m)$

$$\underline{dW^{[1]}} = \frac{\partial J}{\partial W^{[1]}}, \quad \underline{db^{[1]}} = \frac{\partial J}{\partial b^{[1]}}, \dots$$

$$W^{[1]} := W^{[1]} - \alpha dW^{[1]}$$

$$b^{[1]} := b^{[1]} - \alpha db^{[1]}$$

$$W^{[2]} := \dots \quad b^{[2]} := \dots$$

}

# Formulas for computing derivatives

Forward propagation:

$$z^{[1]} = w^{[1]}x + b^{[1]}$$

$$a^{[1]} = g^{[1]}(z^{[1]}) \leftarrow$$

$$z^{[2]} = w^{[2]}a^{[1]} + b^{[2]}$$

$$a^{[2]} = g^{[2]}(z^{[2]}) = \underline{\sigma}(z^{[2]})$$

Back propagation:

$$dz^{[2]} = A^{[2]} - Y \leftarrow$$

$$dw^{[2]} = \frac{1}{n} dz^{[2]} A^{[1]T}$$

$$db^{[2]} = \frac{1}{n} \text{np.sum}(dz^{[2]}, \text{axis}=1, \text{keepdims}=\text{True})$$

$$dz^{[1]} = \underbrace{w^{[2]T} dz^{[2]}}_{(n^{[1]}, m)} \star \underbrace{g^{[1]'}(z^{[1]})}_{\text{element-wise product}} \quad (n^{[1]}, m)$$

$$dw^{[1]} = \frac{1}{n} dz^{[1]} x^T$$

$$db^{[1]} = \frac{1}{n} \text{np.sum}(dz^{[1]}, \text{axis}=1, \text{keepdims}=\text{True})$$

$\underline{(n^{[1]}, 1)}$        $(n^{[1]},)$        $\text{reshape} \uparrow$

$$Y = [y^{(1)} \ y^{(2)} \ \dots \ y^{(n)}]$$

$$(n^{[2]}) \leftarrow$$

$$\downarrow (n^{[2]}, 1) \leftarrow$$



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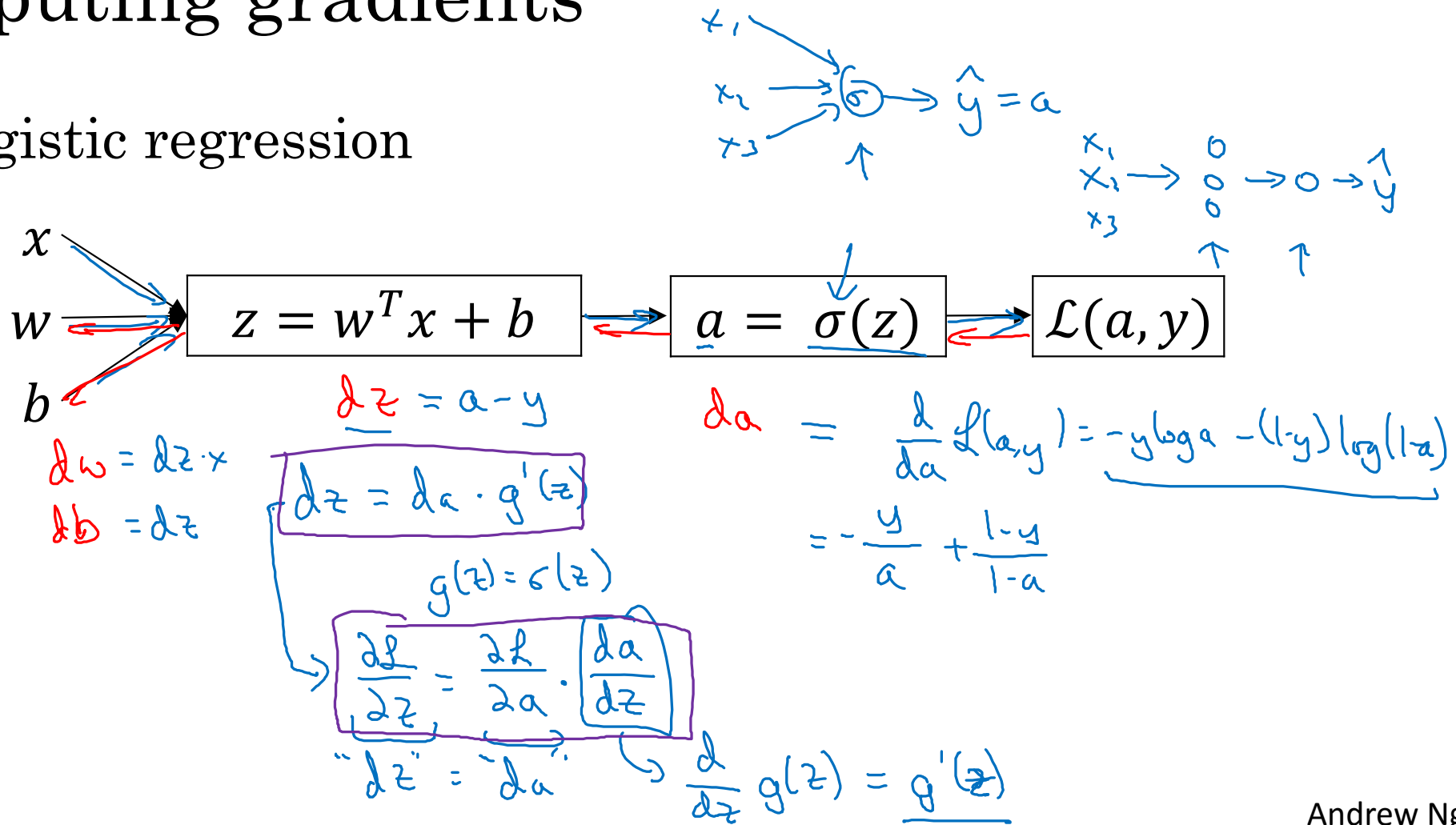
One hidden layer  
Neural Network

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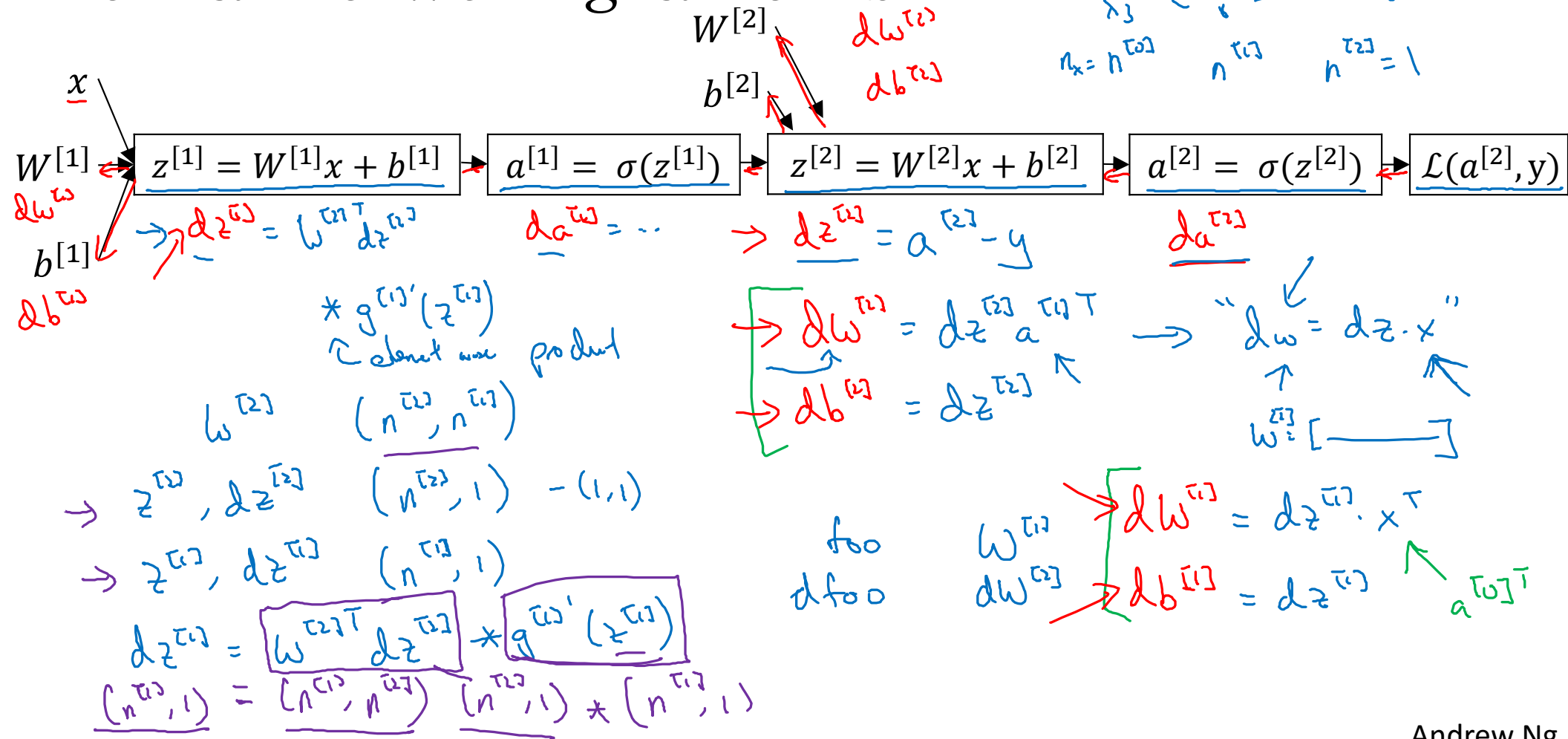
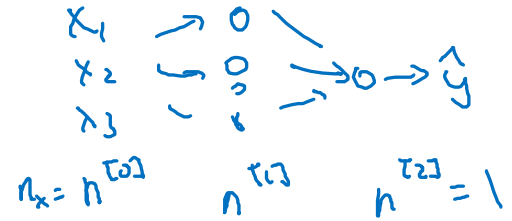
Backpropagation  
intuition (Optional)

# Computing gradients

## Logistic regression



# Neural network gradients



# Summary of gradient descent

$$dz^{[2]} = a^{[2]} - y$$

$$dW^{[2]} = dz^{[2]} a^{[1]T}$$

$$db^{[2]} = dz^{[2]}$$

$$dz^{[1]} = W^{[2]T} dz^{[2]} * g^{[1]'}(z^{[1]})$$

$$dW^{[1]} = dz^{[1]} x^T$$

$$db^{[1]} = dz^{[1]}$$

Vectorized Implementation:

$$z^{[2]} = W^{[2]} x + b^{[2]}$$
$$a^{[2]} = g^{[2]}(z^{[2]})$$
$$z^{[2]} = \begin{bmatrix} z^{[2](1)} \\ z^{[2](2)} \\ \vdots \\ z^{[2](n)} \end{bmatrix}$$
$$z^{[2]} = W^{[2]} X + b^{[2]}$$
$$A^{[2]} = g^{[2]}(z^{[2]})$$

# Summary of gradient descent

$$\underline{dz^{[2]}} = \underline{a^{[2]}} - \underline{y}$$

$$dW^{[2]} = dz^{[2]} a^{[1]T}$$

$$db^{[2]} = dz^{[2]}$$

$$\underset{(n^{[1]}, 1)}{dz^{[1]}} = W^{[2]T} dz^{[2]} * g^{[1]'}(z^{[1]})$$

$$dW^{[1]} = dz^{[1]} x^T$$

$$db^{[1]} = dz^{[1]}$$

$$\underline{dZ^{[2]}} = \underline{A^{[2]}} - \underline{Y}$$

$$dW^{[2]} = \frac{1}{m} dZ^{[2]} A^{[1]T}$$

$$db^{[2]} = \frac{1}{m} \text{np.sum}(dZ^{[2]}, \text{axis} = 1, \text{keepdims} = \text{True})$$

$$\underset{(n^{[2]}, m)}{dZ^{[1]}} = \underbrace{W^{[2]T} dZ^{[2]}}_{(n^{[2]}, m)} * \underbrace{g^{[1]'}(Z^{[1]})}_{(n^{[2]}, m)}$$

↙ elementwise product

$$dW^{[1]} = \frac{1}{m} dZ^{[1]} X^T$$

$$db^{[1]} = \frac{1}{m} \text{np.sum}(dZ^{[1]}, \text{axis} = 1, \text{keepdims} = \text{True})$$

$$J(\cdot) = \frac{1}{m} \sum_{i=1}^m \mathcal{L}(\hat{y}, y)$$





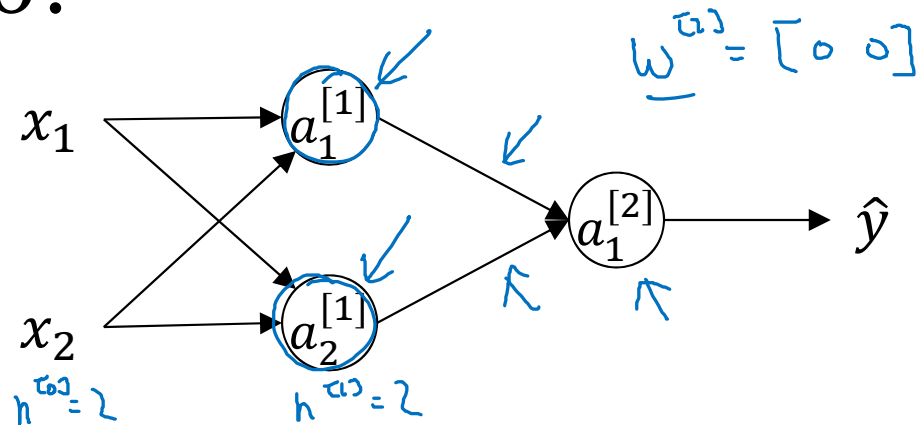
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# One hidden layer Neural Network

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## Random Initialization

# What happens if you initialize weights to zero?



$$W^{(1)} = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$$

$$a_1^{(1)} = a_2^{(1)}$$

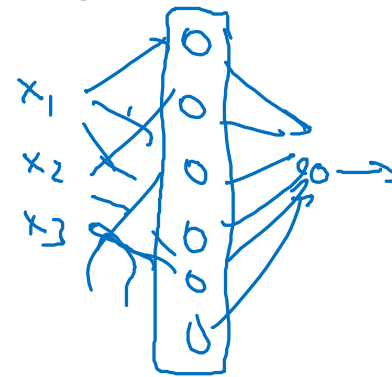
$$dW = \begin{bmatrix} u & v \\ u & v \end{bmatrix}$$

$$b^{(1)} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

$$dz_1^{(1)} = dz_2^{(1)}$$

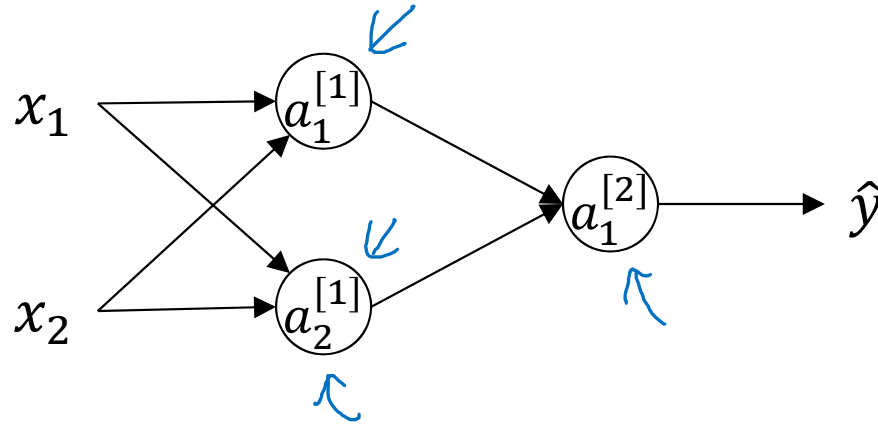
$$W^{(1)} = W^{(1)} - 2dW$$

Symmetric

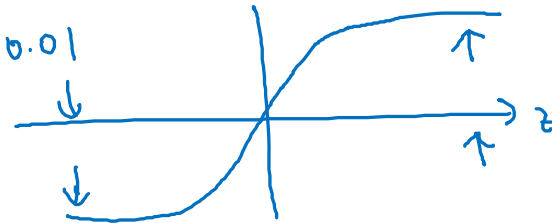


$$W^{(1)} = \begin{bmatrix} \dots & \cdot \\ \dots & \cdot \end{bmatrix}$$

# Random initialization



$\rightarrow w^{[1]} = \text{np.random.randn}(2,2) * \frac{0.01}{100?}$   
 $b^{[1]} = \text{np.zeros}(2,1)$   
 $w^{[2]} = \text{np.random.randn}(1,2) * 0.01$   
 $b^{[2]} = 0$



$$\begin{aligned} z^{[1]} &= w^{[1]}x + b^{[1]} \\ a^{[1]} &= g^{[1]}(z^{[1]}) \end{aligned}$$



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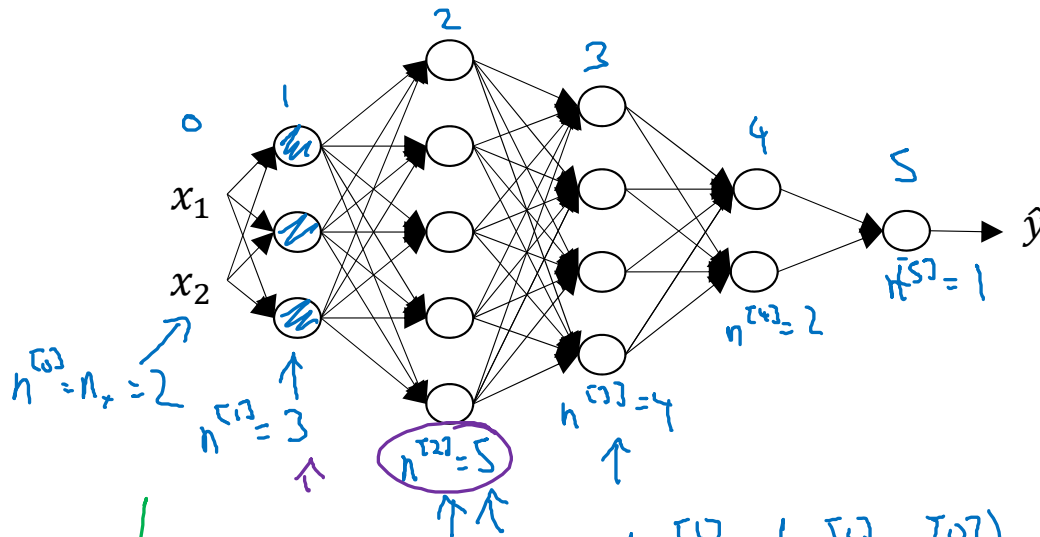
# Deep Neural Networks

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Getting your matrix  
dimensions right

# Parameters $W^{[l]}$ and $b^{[l]}$

$\downarrow z^{[L]} = g^{[L]}(a^{[L]})$   
 $\uparrow$   
 $\downarrow a^{[L]}$



$L=5$

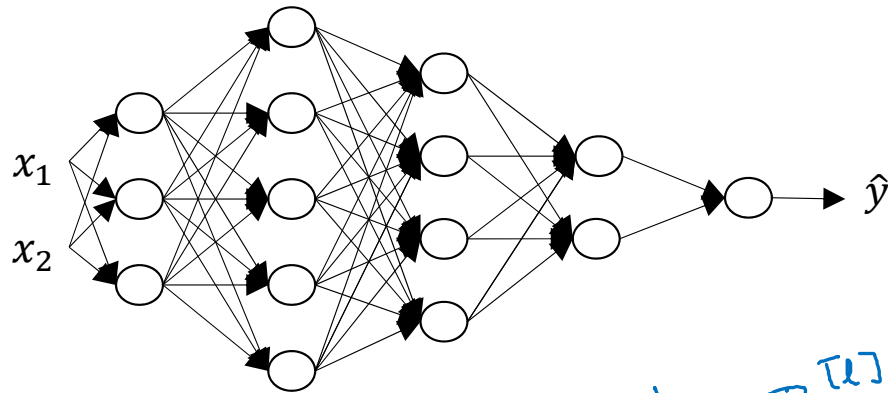
$\rightarrow W^{[L]}: (n^{[L]}, n^{[L-1]})$   
 $\rightarrow b^{[L]}: (n^{[L]}, 1)$   
 $\rightarrow \Delta W^{[L]}: (n^{[L]}, n^{[L-1]})$   
 $\rightarrow \Delta b^{[L]}: (n^{[L]}, 1)$

$\downarrow z^{[1]} = \boxed{W^{[1]} \cdot x} + \boxed{b^{[1]}}$   
 $(3,1) \leftarrow (3,2) \quad (2,1)$   
 $(n^{[1]},1) \quad (n^{[1]},n^{[0]}) \quad (n^{[0]},1)$   
 $(3,1)$   
 $(n^{[1]},1)$

$\begin{bmatrix} \vdots \\ \vdots \end{bmatrix} = \begin{bmatrix} \vdots \\ \vdots \end{bmatrix} \begin{bmatrix} \vdots \\ \vdots \end{bmatrix}$

$W^{[1]}: (n^{[1]}, n^{[0]})$   
 $W^{[2]}: (5, 3) \quad (n^{[2]}, n^{[1]})$   
 $z^{[2]} = \boxed{W^{[2]} \cdot a^{[1]}} + \boxed{b^{[2]}}$   
 $\uparrow \quad \uparrow \quad \uparrow$   
 $\rightarrow (5,1) \quad (5,3) \quad (3,1)$   
 $(5,1)$   
 $(n^{[2]},1)$   
 $W^{[3]}: (4, 5)$   
 $W^{[4]}: (2, 4) \quad , \quad W^{[5]}: (1, 2)$

# Vectorized implementation



$$z^{[l]} = W^{[l]} \cdot x + b^{[l]}$$

$(n^{[l]}, 1)$     $(n^{[l]}, n^{[l-1]})$     $(n^{[l]}, 1)$     $(n^{[l]}, 1)$

$[z^{[1]}, z^{[2]}, \dots, z^{[L]}]$

$$Z^{[l]} = W^{[l]} \cdot X + b^{[l]}$$

$(n^{[l]}, m)$     $(n^{[l]}, n^{[l-1]})$     $(n^{[l]}, m)$     $(n^{[l]}, 1)$

$(n^{[l]}, m)$

$$z^{[L]}, a^{[L]} : (n^{[L]}, 1)$$

$$Z^{[L]}, A^{[L]} : (n^{[L]}, m)$$

$l=0 \quad A^{[0]} = X = (n^{[0]}, m)$

$$dZ^{[L]}, dA^{[L]} : (n^{[L]}, m)$$



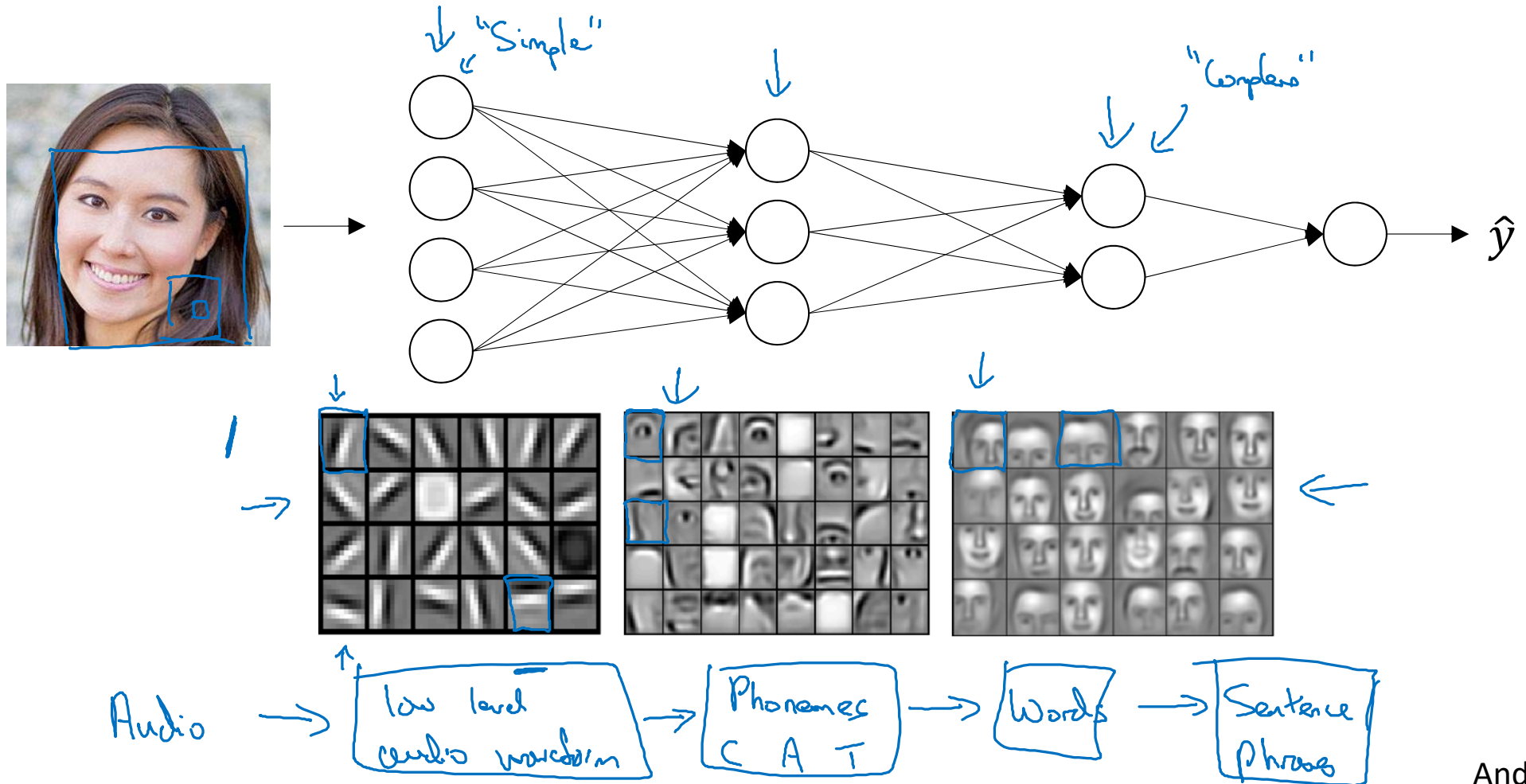
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# Deep Neural Networks

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Why deep  
representations?

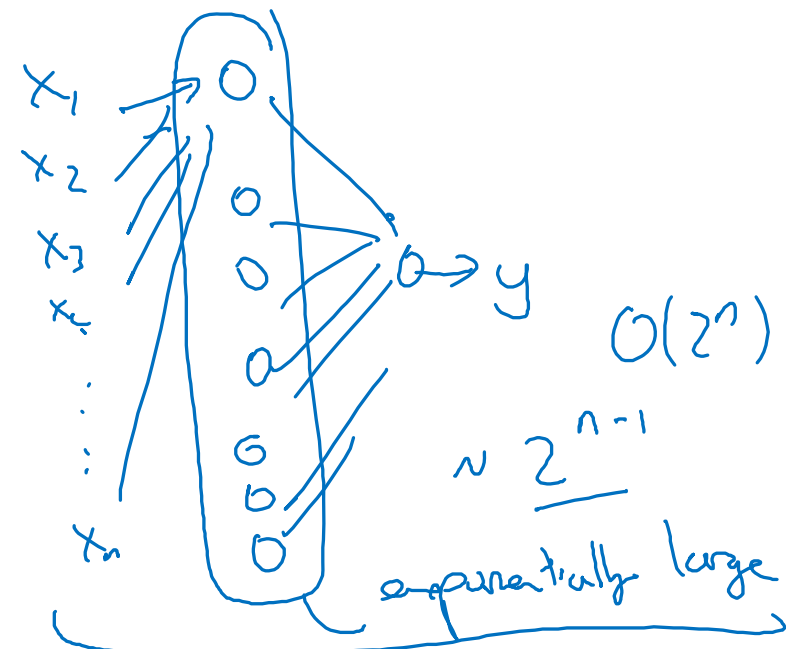
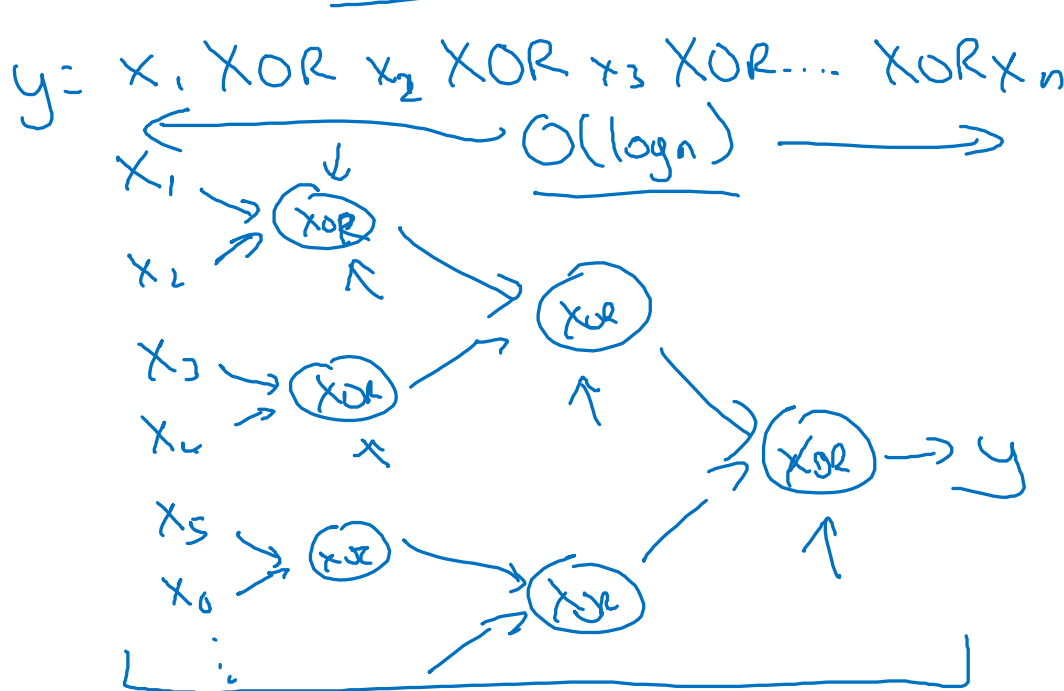
# Intuition about deep representation





# Circuit theory and deep learning

Informally: There are functions you can compute with a “small” L-layer deep neural network that shallower networks require exponentially more hidden units to compute.





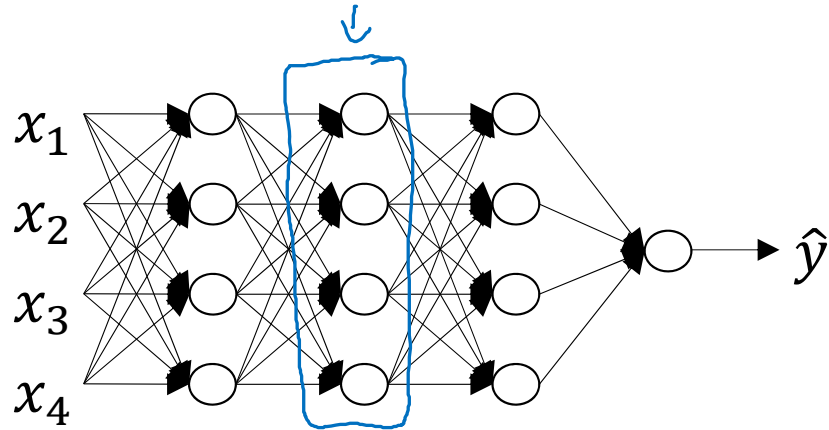
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# Deep Neural Networks

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Building blocks of  
deep neural networks

# Forward and backward functions



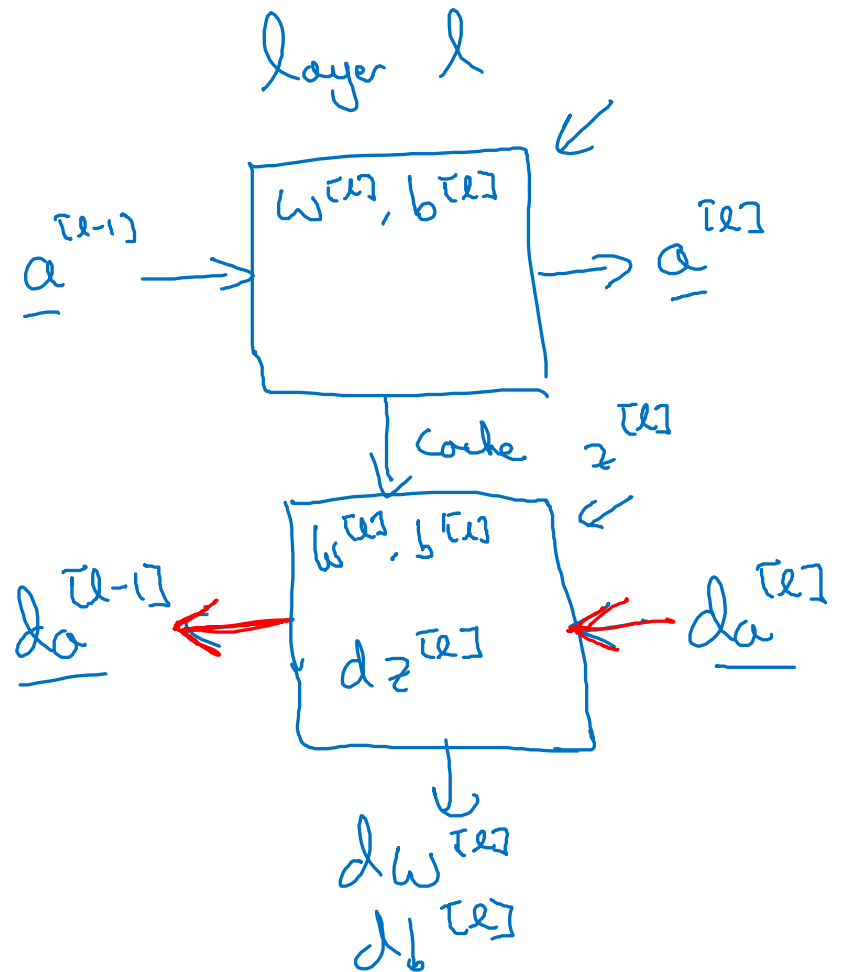
layer  $l$ :  $W^{[l]}, b^{[l]}$

→ Forward: Input  $a^{[l-1]}$ , output  $a^{[l]}$

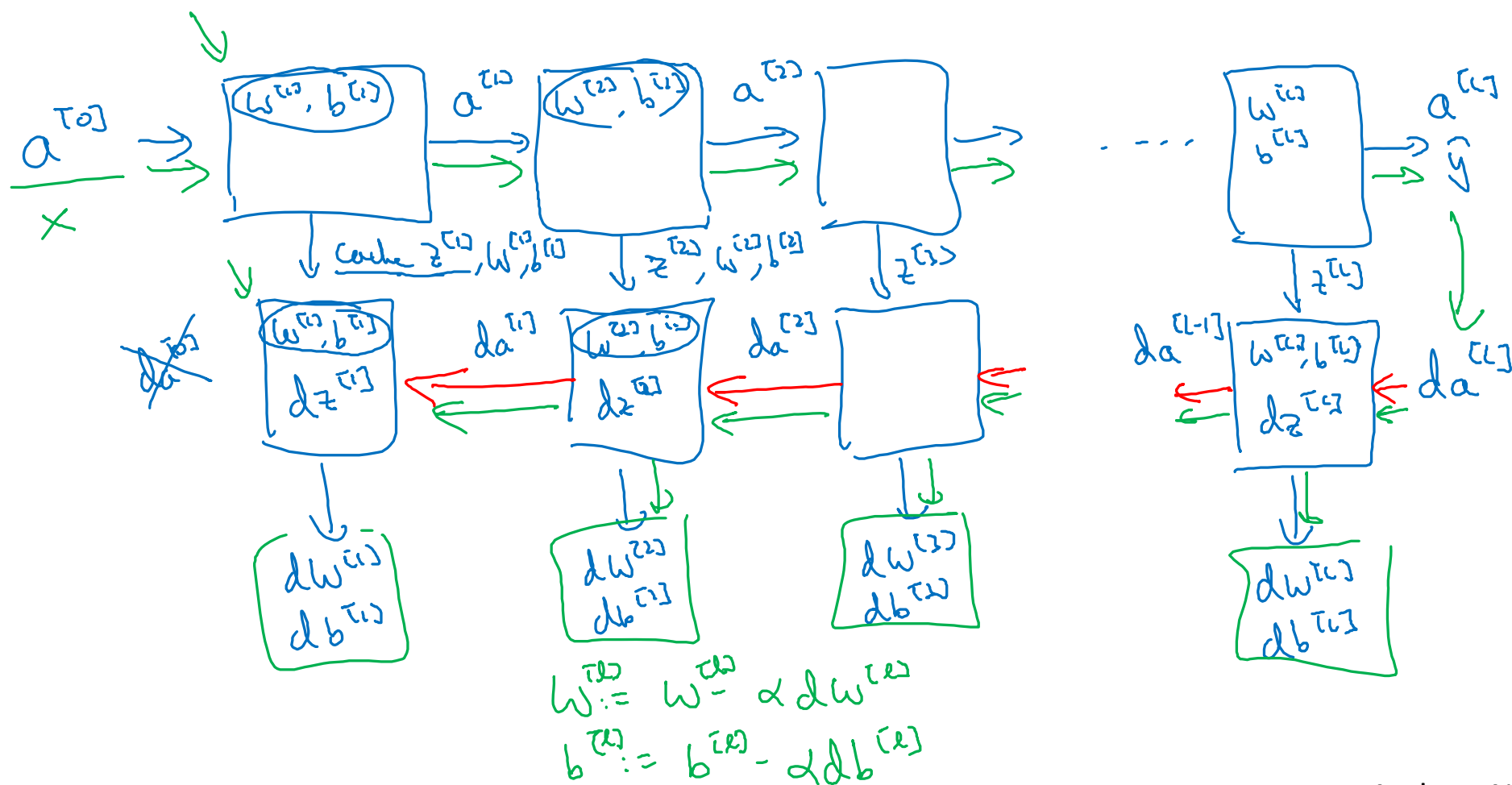
$$z^{[l]} = W^{[l]} a^{[l-1]} + b^{[l]} \quad \text{cache } z^{[l]}$$

$$a^{[l]} = g^{[l]}(z^{[l]})$$

→ Backward: Input  $da^{[l]}$ , output  $da^{[l-1]}$   
 cache  $(z^{[l]})$   
 $\frac{dL}{dW^{[l]}}$   
 $\frac{dL}{db^{[l]}}$



# Forward and backward functions





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# Deep Neural Networks

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Forward and backward  
propagation

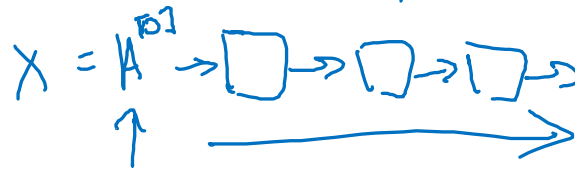
# Forward propagation for layer $l$

→ Input  $a^{[l-1]}$  ←

→ Output  $a^{[l]}$ , cache ( $z^{[l]}$ )

$$z^{[l]} = W^{[l]} \cdot a^{[l-1]} + b^{[l]}$$
$$a^{[l]} = g^{[l]}(z^{[l]})$$

$$a^{[0]}$$
$$A^{[0]}$$



Vectorized:

$$z^{[l]} = W^{[l]} \cdot A^{[l-1]} + b^{[l]}$$
$$A^{[l]} = g^{[l]}(z^{[l]})$$

# Backward propagation for layer $l$

→ Input  $da^{[l]}$

→ Output  $da^{[l-1]}$ ,  $dW^{[l]}$ ,  $db^{[l]}$

$$dz^{[l]} = da^{[l]} * g^{[l]'}(z^{[l]})$$

$$dW^{[l]} = dz^{[l]} \cdot a^{[l-1]}$$

$$db^{[l]} = dz^{[l]}$$

$$da^{[l-1]} = W^{[l]T} \cdot dz^{[l]}$$

$$dz^{[l]} = W^{[l+1]T} dz^{[l+1]} * g^{[l]'}(z^{[l]})$$

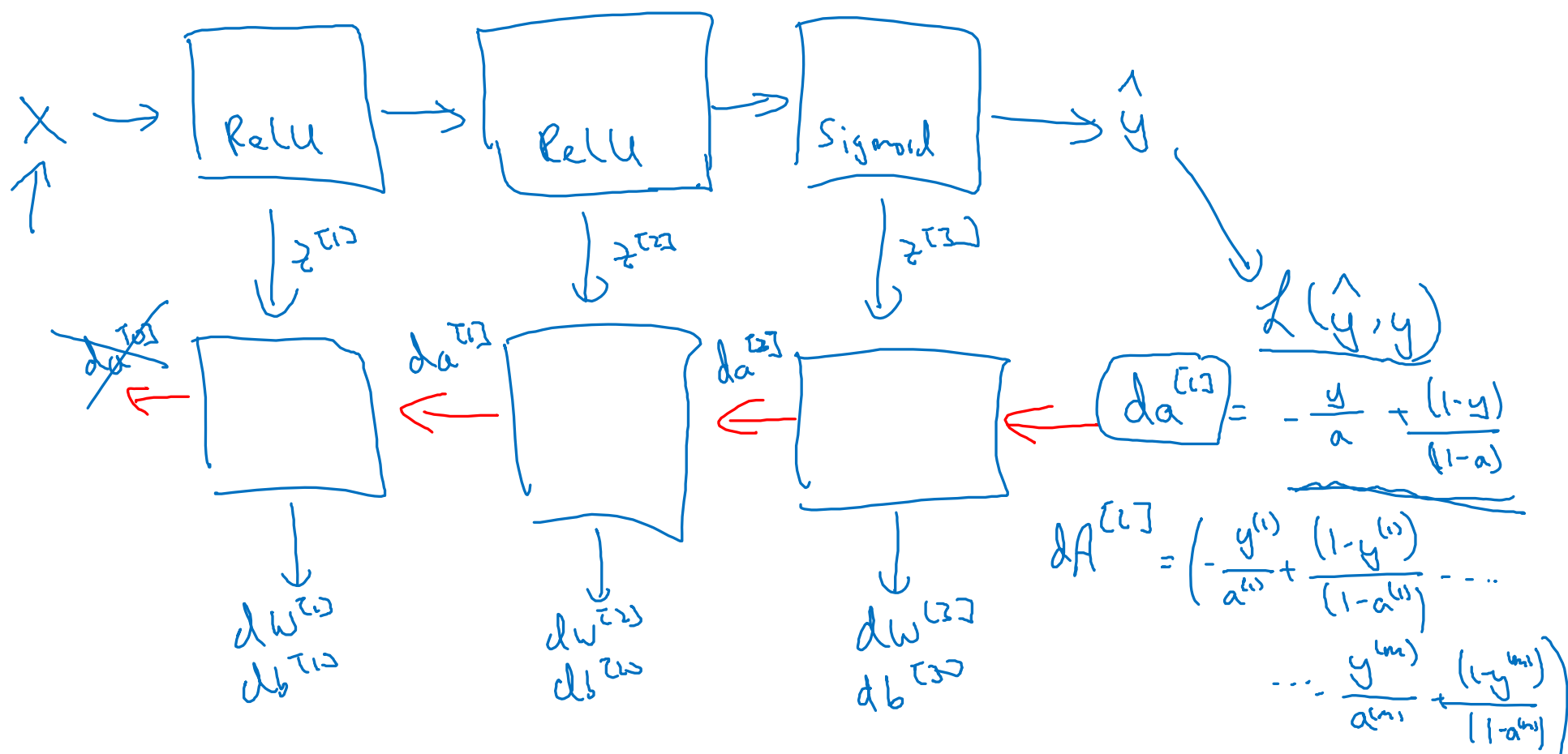
$$dz^{[l]} = dA^{[l]} * g^{[l]'}(z^{[l]})$$

$$dW^{[l]} = \frac{1}{n} dz^{[l]} \cdot A^{[l-1]T}$$

$$db^{[l]} = \frac{1}{n} \text{np.sum}(dz^{[l]}, \text{axis}=1, \text{keepdims}=\text{True})$$

$$dA^{[l-1]} = W^{[l]T} \cdot dz^{[l]}$$

# Summary







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# Deep Neural Networks

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## Parameters vs Hyperparameters

# What are hyperparameters?

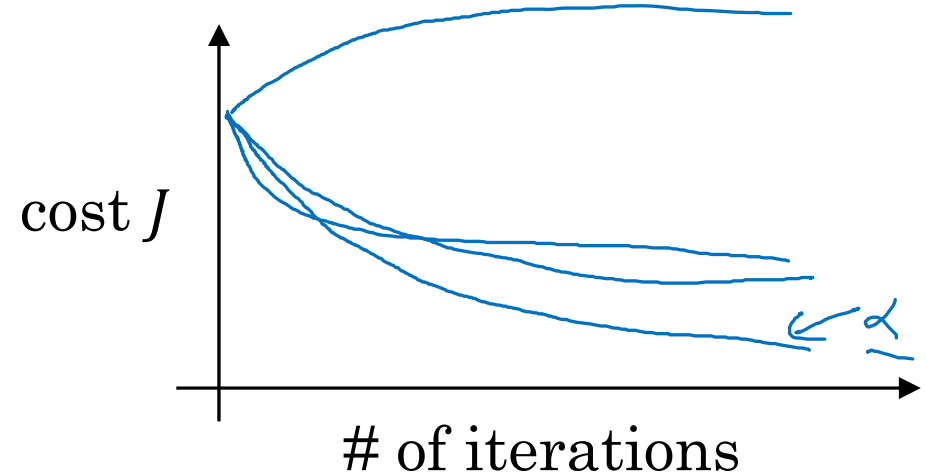
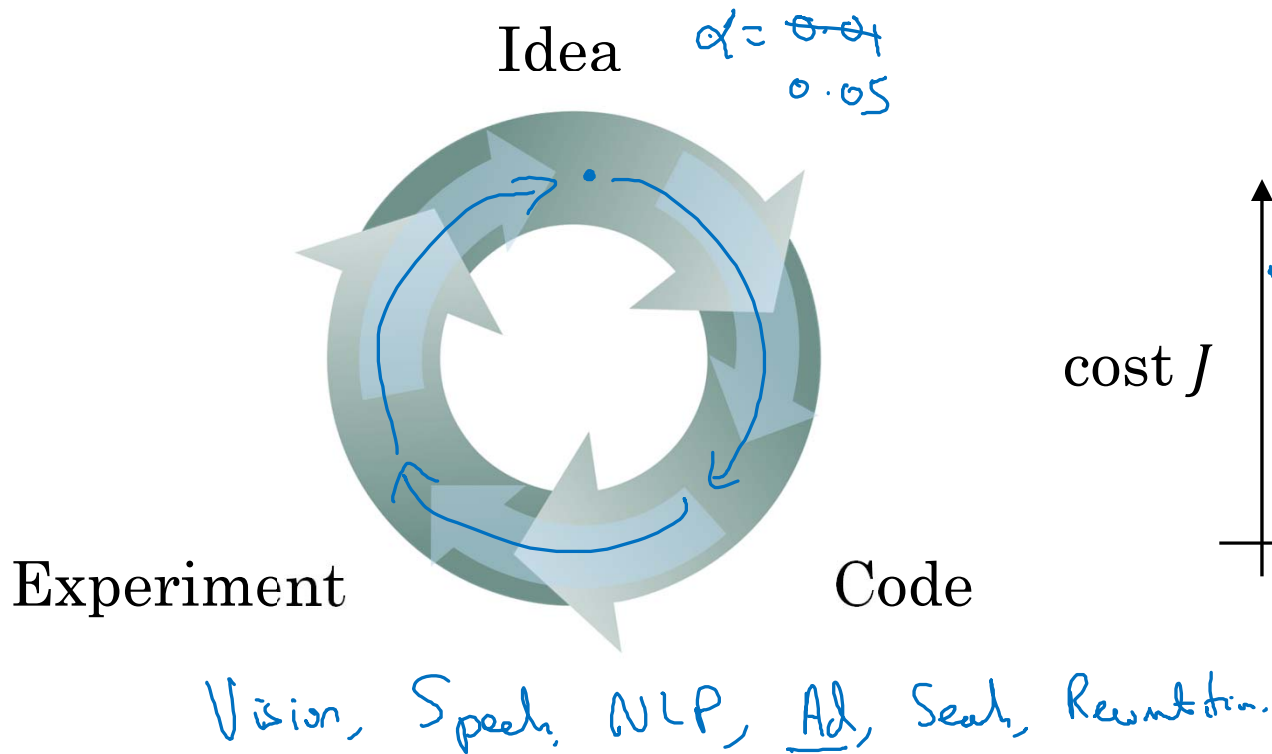
Parameters:  $W^{[1]}, b^{[1]}, W^{[2]}, b^{[2]}, W^{[3]}, b^{[3]} \dots$

Hyperparameters:

- learning rate  $\alpha$
- #iterations  $\tau$
- #hidden layers  $L$
- #hidden units  $n^{[1]}, n^{[2]}, \dots$
- choice of activation function

Later: Momentum, mini-batch size, regularizations, ...

# Applied deep learning is a very empirical process





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# Deep Neural Networks

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What does this  
have to do with  
the brain?

# Forward and backward propagation

$$\begin{aligned} Z^{[1]} &= W^{[1]}X + b^{[1]} \\ A^{[1]} &= g^{[1]}(Z^{[1]}) \\ Z^{[2]} &= W^{[2]}A^{[1]} + b^{[2]} \\ A^{[2]} &= g^{[2]}(Z^{[2]}) \\ &\vdots \\ A^{[L]} &= g^{[L]}(Z^{[L]}) = \hat{Y} \end{aligned}$$

$$\begin{aligned} dZ^{[L]} &= A^{[L]} - Y \\ dW^{[L]} &= \frac{1}{m} dZ^{[L]} A^{[L]T} \\ db^{[L]} &= \frac{1}{m} \text{np.sum}(dZ^{[L]}, \text{axis} = 1, \text{keepdims} = \text{True}) \\ dZ^{[L-1]} &= dW^{[L]T} dZ^{[L]} g'^{[L]}(Z^{[L-1]}) \\ &\vdots \\ dZ^{[1]} &= dW^{[L]T} dZ^{[2]} g'^{[1]}(Z^{[1]}) \\ dW^{[1]} &= \frac{1}{m} dZ^{[1]} A^{[1]T} \\ db^{[1]} &= \frac{1}{m} \text{np.sum}(dZ^{[1]}, \text{axis} = 1, \text{keepdims} = \text{True}) \end{aligned}$$

"It's like the brain."

