

Assignment 4

```
In [1]: #All the necessary codes imported from the library

import library as lib #importing library of functions
```

Q1 LU decomposition using Doolittle and crout

```
In [6]: #Doolittle algorithm
M = lib.matrixtxt('input.txt') #storing the given matrix
b = lib.matrixtxt('values.txt') #storing the RHS of equation
print ("Using Doolittle, ")
lib.LUDoolittle(M) #calling function for LU using Doolittle
L = lib.LUDoolittle.L #storing L and U from the function
U = lib.LUDoolittle.U

#calling forward backward substitution to calculate x and printing it simultaneously
print("The values of x1,x2,x3,x4 from Doolittle algorithm are ", lib.forwardbackward(L, U, b), " respectively ")
```

```
Using Doolittle,
Lower Triangular
[1, 0, 0, 0]
[0.0, 1, 0, 0]
[0.5, 1.5, 1, 0]
[0.5, -0.5, -3.0, 1]
Upper Triangular
[2.0, 1.0, 3.0, -2.0]
[0, 1.0, -2.0, 0.0]
[0, 0, 0.5, 1.0]
[0, 0, 0, 6.0]
The values of x1,x2,x3,x4 from Doolittle algorithm are  [[1.0], [-1.0], [1.0], [2.0]]  respectively
```

```
In [7]: #Crout's algorithm to calculate Lu
print ("\nNow using Crout, ")
M = lib.matrixtxt('input.txt') #storing the matrix
lib.LUCrout(M)                  #calling LU crout
L2 = lib.LUCrout.L              #storing L and U from the function
U2 = lib.LUCrout.U
d = lib.matrixtxt('values.txt') #storing RHS

#calling forward backward on L and U, and simultaneously printing the result
print("The values of x1,x2,x3,x4 from Crout algorithm are ", lib.forwardbackward(L2,U2,d), " respectively ")
```

Now using Crout,
Lower Triangular
[2.0, 0, 0, 0]
[0.0, 1.0, 0, 0]
[1.0, 1.5, 0.5, 0]
[1.0, -0.5, -1.5, 6.0]

Upper Triangular
[1, 0.5, 1.5, -1.0]
[0, 1, -2.0, 0.0]
[0, 0, 1, 2.0]
[0, 0, 0, 1]

The values of x1,x2,x3,x4 from Crout algorithm are [[1.0], [-1.0], [1.0], [2.0]] respectively

Q2 Calculating inverse using LU decomposition

```
In [4]: #storing identity matrix
I = lib.matrixtxt('identity.txt')
#storing the matrix given
A = lib.matrixtxt('inverse.txt')
print ("The given matrix is " , A, "\n")

#calling the function to calculate inverse
X = lib.inverseLU(A,I)
print ("\nTo verify we multiply inverse by original matrix to get an identity matrix")
#verifying the calculated inverse by multiplying with matrix
verification = lib.multipliesquare(X,A)
```

The given matrix is $\begin{bmatrix} 0.0 & 2.0 & 8.0 & 6.0 \\ 0.0 & 0.0 & 1.0 & 2.0 \\ 0.0 & 1.0 & 0.0 & 1.0 \\ 3.0 & 7.0 & 1.0 & 0.0 \end{bmatrix}$

Lower Triangular

```
[1, 0, 0, 0]
[0.0, 1, 0, 0]
[0.0, 0.5, 1, 0]
[0.0, 0.0, -0.25, 1]
```

Upper Triangular

```
[3.0, 7.0, 1.0, 0.0]
[0, 2.0, 8.0, 6.0]
[0, 0, -4.0, -2.0]
[0, 0, 0, 1.5]
```

The inverse of the given matrix is

```
[0.3333333333333333, -0.25000000000000006, -1.8333333333333333, 1.6666666666666667]
[0.0, 0.08333333333333337, 0.8333333333333333, -0.6666666666666667]
[-0.0, 0.16666666666666666, -0.3333333333333333, -0.3333333333333333]
[0.0, -0.08333333333333333, 0.16666666666666666, 0.6666666666666666]
```

To verify we multiply inverse by original matrix to get an identity matrix

The product of

```
[0.3333333333333333, -0.25000000000000006, -1.8333333333333333, 1.6666666666666667]
[0.0, 0.08333333333333337, 0.8333333333333333, -0.6666666666666667]
[-0.0, 0.16666666666666666, -0.3333333333333333, -0.3333333333333333]
[0.0, -0.08333333333333333, 0.16666666666666666, 0.6666666666666666]
```

and

```
[3.0, 7.0, 1.0, 0.0]
[0.0, 2.0, 8.0, 6.0]
[0.0, 1.0, 0.0, 1.0]
```

```
[0.0, 0.0, 1.0, 2.0]
is
[1.0, 0, 0, 0]
[0, 1.0, 0, 0]
[0, 0, 1.0, 0]
[0, 0, 0, 1.0]
```

Q3 Solving the given equation using Cholesky decomposition

```
In [5]: B = lib.matrixtxt('cholesky.txt')    #storing the given matrix from a txt file
lib.Cholesky_Decomposition(B,4)             #calling function to use Cholesky decomposition
L = lib.Cholesky_Decomposition.L            #storing L from the function in a variable
U = lib.Cholesky_Decomposition.U            #storing U from the function in a variable
c = lib.matrixtxt('valuesC.txt')            #storing RHS of equation

#forward backward substitution of LU and printing the result
print ("The values of x1,x2,x3,x4 are: ")
for i in range (len(lib.forwardbackward(L,U,c))):
    x = lib.forwardbackward(L,U,c)[i][0]
    print (round(x,2))
```

Lower Triangular

```
[3.16, 0, 0, 0]
[0.32, 3.45, 0, 0]
[0.0, -0.09, 3.08, 0]
[0.79, 0.25, 0.01, 2.31]
```

Upper Triangular

```
[3.16, 0.32, 0.0, 0.79]
[0, 3.45, -0.09, 0.25]
[0, 0, 3.08, 0.01]
[0, 0, 0, 2.31]
```

The values of x1,x2,x3,x4 are:

```
0.1
0.2
0.3
0.4
```

