

## Assignment 4: Solutions and rubric

- (1) The DP solution to this problem is given by the following recurrence relation.

$$T(n) = \sum_{i=1}^n T(i)T(n-1-i)$$

This number is also known as Catalan number.

Rubric: 5 for correct DP solution. -1 for DP solution but not correct pseudocode. -1/-2 for correct expression but no pseudocode/algorithm 2 for recursion with DP.

- (2) <https://leetcode.com/articles/knight-probability-in-chessboard/>.

Rubric: Top down approach - 6 marks Bottom up approach - 6 marks Time complexity - 3 marks.

- (3) We recurse on the maximum value subsequence ending at  $j$ :  $M(j) = \max(M(j-1) + a_j, a_j)$  if  $j = 0$ , return  $a_j$ .

In this case  $a_0 = 0$ .

This algorithm is also known as Kadane's algorithm. For detail refer to [https://en.wikipedia.org/wiki/Maximum\\_subarray\\_problem](https://en.wikipedia.org/wiki/Maximum_subarray_problem).

Rubric: Missing/ wrong max subarray : 2 marks have been deducted. Any uninitialized variable : 0.5 marks have been deducted. -ve number array not handled : 1 mark has been deducted

- (4) <https://www.geeksforgeeks.org/partition-a-set-into-two-subsets-such-that-the-difference-of-subset-sums-is-minimum/>.

Rubric: 10 marks for a DP-based approach (complexity being  $O(n * sum)$  or  $O(n^2 * m)$ )

If used only recursion (without memoization i.e  $O(2^n)$ ), 7 marks

1 mark cut for not initializing DP array / missing explanations etc