

Tutorial-2
IIIT-DELHI
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Question 1

a) Predict the output of the following program. What does the following fun() do in general?

```
#include<stdio.h>
int fun(int a, int b)
{
    if (b == 0)
        return 0;
    if (b % 2 == 0)
        return fun(a+a, b/2);
    return fun(a+a, b/2) + a;
}

int main()
{
    printf("%d", fun(4, 3));
    getchar();
    return 0;
}
```

b) In question 1, if we replace + with * and replace return 0 with return 1, then what does the changed function do? Following is the changed function.

```
#include<stdio.h>
int fun(int a, int b)
{
    if (b == 0)
        return 1;
    if (b % 2 == 0)
        return fun(a*a, b/2);
    return fun(a*a, b/2)*a;
}
```

```
int main()
{
    printf("%d", fun(4, 3));
    getchar();
    return 0;
}
```

Question 2

Explain the functionality of the following function

a)

```
int fun1(int x, int y)
{
    if(x == 0)
        return y;
    else
        return fun1(x - 1, x + y);
}
```

b)

```
void fun(int x)
{
    if(x > 0)
    {
        fun(--x);
        printf("%d\t", x);
        fun(--x);
    }
}
```

```
int main()
{
    int a = 4;
    fun(a);
    getchar();
    return 0;
}
```

c)

```
int fun(int n)
{
    if (n > 100)
        return n - 10;
    return fun(fun(n+11));
}
```

```
int main()
{
    printf(" %d ", fun(99));
    getchar();
    return 0;
}
```

d)

```
int fun(int count)
{
    printf("%d\n", count);
    if(count < 3)
    {
        fun(fun(fun(++count)));
    }
    return count;
}
```

```
int main()
{
    fun(1);
    return 0;
}
```

Question 3

Consider the following Java method (assume that it will only be called with $0 \leq k$ and $k \leq n$):

```
int choose (int n, int k) {  
    if ((k == 0) || (k == n)) return 1;  
    return choose (n-1, k) + choose (n-1, k-1);  
}
```

Explain why the running time will not be polynomial in n in general. Describe (in code or in English) how to revise the algorithm to be polynomial time in n . Carefully determine and justify a big-O bound on the running time of your improved version.

Question 4

True or false with justification: Let k be any positive integer constant greater than 1. Then the recurrence $T(n) = kT(n/k) + O(n)$, with $T(1) = O(1)$, has the same big-O solution for any such k . (You may assume that $T(n)$ is evaluated only when n is a power of k .)

Question 5

Consider the following algorithm `strangeSort`, which sorts n Comparable items in a list A . assumption: the n items are all distinct. Otherwise, the algorithm below fails to terminate if given a list of two or more items that are all equal.:

- 1) If $n \leq 1$, return A unchanged
- 2) For each item x in A , scan A and count how many other items in A are less than x
- 3) Put the items with counts less than $n/2$ in a list B
- 4) Put the other items in a list C
- 5) Recursively sort B and C using `strangeSort`
- 6) Append the sorted C to the sorted B and return the result

a) Prove by induction on n that `strangeSort` correctly sorts all lists of length n , with smaller items first.

b) Formulate a recurrence for the running time $T(n)$ of `strangeSort` on an input list of size n . Solve this recurrence to get the best possible big-O bound on $T(n)$ -- you may assume if you like that n is a power of 2.

Question 6

Given s_1 , s_2 , s_3 , find whether s_3 is formed by the interleaving of s_1 and s_2 .

Example,

Given:

$s_1 = \text{"aabcc"}$,

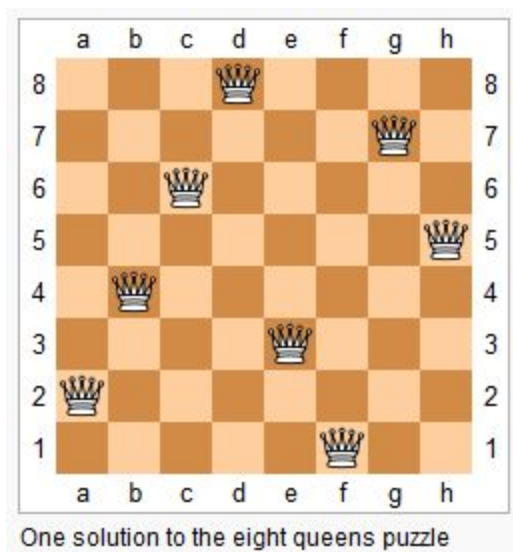
$s_2 = \text{"dbbca"}$,

When $s_3 = \text{"aadbcbcbac"}$, return true.

When $s_3 = \text{"aadbabbacc"}$, return false.

Question 7

The n-queens puzzle is the problem of placing n queens on an $n \times n$ chessboard such that no two queens attack each other.



Given an integer n , return all distinct solutions to the n -queens puzzle.

Each solution contains a distinct board configuration of the n -queens' placement, where 'Q' and '.' both indicate a queen and an empty space respectively.

For example,

There exist two distinct solutions to the 4-queens puzzle:

```
[
  [".Q..", // Solution 1
   "...Q",
   "Q...",
   "..Q."],
  ["Q...",
   "Q...",
   ".Q..",
   "..Q."]]
```

```

"..Q."],

["..Q.", // Solution 2
 "Q...",
 "...Q",
 ".Q.."]
]

```

Question 8

Given a string s , partition s such that every string of the partition is a palindrome.

Return all possible palindrome partitioning of s .

For example, given $s = "aab"$,

Return

```

[
  ["a","a","b"],
  ["aa","b"],
]

```

Question 9:

The set $[1,2,3,\dots,n]$ contains a total of $n!$ unique permutations.

By listing and labeling all of the permutations in order,

We get the following sequence (ie, for $n = 3$) :

1. "123"
2. "132"
3. "213"
4. "231"
5. "312"
6. "321"

Given n and k , return the k th permutation sequence.

For example, given $n = 3$, $k = 4$, $ans = "231"$