

# Bond Prices and Yields

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Bodie, Kane, and Marcus  
*Essentials of Investments*,  
9<sup>th</sup> Edition

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# 10.1 Bond Characteristics

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- Bond
  - Security that obligates issuer to make payments to holder over time
- Face Value, Par Value
  - Payment to bondholder at maturity of bond
- Coupon Rate
  - Bond's annual interest payment per dollar of par value
- Zero-Coupon Bond
  - Pays no coupons, sells at discount, provides only payment of par value at maturity

# Figure 10.1 Prices/Yields of U.S. Treasury Bonds

**U.S. Treasury Quotes:** Treasury note and bond data are representative over-the-counter quotations as of 3pm Eastern time.

Maturity	Coupon	Bid	Asked	Change	Asked Yield
8/15/2012	1.750	101.570	101.594	-0.016	0.151
8/15/2014	4.250	111.547	111.594	-0.094	0.358
12/31/2015	2.125	105.789	105.820	-0.164	0.769
8/15/2017	4.750	120.219	120.266	-0.234	1.234
2/15/2020	8.500	152.063	152.094	-0.344	1.847
8/15/2023	6.250	137.406	137.438	-0.688	2.598
2/15/2027	6.625	145.547	145.594	-0.719	2.941
2/15/2031	5.375	130.266	130.297	-0.953	3.263
11/15/2039	4.375	111.766	111.813	-0.813	3.697
5/15/2041	4.375	111.719	111.750	-0.938	3.718

# 10.1 Bond Characteristics

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- Treasury Bonds and Notes
  - Accrued interest and quoted bond prices
    - Quoted prices do not include interest accruing between payment dates
  - Accrued interest =  $\frac{\text{Annual coupon payment}}{2} \times \frac{\text{Days since last coupon payment}}{\text{Days separating coupon payments}}$

# Figure 10.2 Listing of Corporate Bonds

ISSUER NAME	SYMBOL	COUPON	MATURITY	RATING	HIGH	LOW	LAST	CHANGE	YIELD %
				MOODY'S/S&P/ FITCH					
JPMORGAN CHASE & CO	JPM.LHD	3.125%	Dec 2011	Aaa/AA+/AAA	100.907	100.786	100.829	0.079	0.305
GOLDMAN SACHS GP	GS.AOK	5.250%	Jul 2021	—/A/—	103.899	99.790	100.490	−0.225	5.186
CITIGROUP	C.AGT	5.375%	Aug 2020	A3/A/A+	109.280	105.900	107.994	0.818	4.293
BP CAPITAL MARKETS PLC (DUPLICATE)	BP.JW	3.200%	Mar 2016	A2/A/A	106.350	105.783	105.827	−0.451	1.864
BANK OF AMERICA CORP	BAC.XQ	4.875%	Sep 2012	A2/A/A+	102.917	99.000	101.625	−0.930	3.333
AT&T	T.MA	4.450%	May 2021	A2/A—/A	111.614	108.500	110.129	1.720	3.230

# 10.1 Bond Characteristics

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- Corporate Bonds
  - Call provisions on corporate bonds
    - **Callable bonds:** May be repurchased by issuer at specified call price during call period
- Convertible bonds
  - Allow bondholder to exchange bond for specified number of common stock shares

# 10.1 Bond Characteristics

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- Corporate Bonds
  - Puttable bonds
    - Holder may choose to exchange for par value or to extend for given number of years
  - Floating-rate bonds
    - Coupon rates periodically reset according to specified market date

# 10.1 Bond Characteristics

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- Preferred Stock
  - Commonly pays fixed dividend
    - Floating-rate preferred stock becoming more popular
  - Dividends not normally tax-deductible
    - Corporations that purchase other corporations' preferred stock are taxed on only 30% of dividends received



# 10.1 Bond Characteristics

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- Other Domestic Issuers
  - State, local governments (municipal bonds)
  - Federal Home Loan Bank Board
  - Farm Credit agencies
  - Ginnie Mae, Fannie Mae, Freddie Mac

# 10.1 Bond Characteristics

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- International Bonds
  - Foreign bonds
    - Issued by borrower in different country than where bond sold, denominated in currency of market country
  - Eurobonds
    - Denominated in currency (usually that of issuing country) different than that of market

# 10.1 Bond Characteristics

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- Innovation in the Bond Market
  - Inverse floaters
    - Coupon rate falls when interest rates rise
  - Asset-backed bonds
    - Income from specified assets used to service debt
  - Pay-in-kind bonds
    - Issuers can pay interest in cash or additional bonds
  - Catastrophe bonds
    - Higher coupon rates to investors for taking on risk

# 10.1 Bond Characteristics

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- Innovation in the Bond Market
  - Indexed bonds
    - Payments tied to general price index/price of particular commodity
  - Treasury Inflation Protected Securities (TIPS):  
Par value of bond increases with consumer price index
  - Nominal return =  $\frac{\text{Interest} + \text{Price appreciation}}{\text{Initial price}}$
  - Real return =  $\frac{1 + \text{Nominal return}}{1 + \text{Inflation}} - 1$

# Table 10.1 Principal and Interest Payments

## Principal and interest payments for a Treasury Inflation Protected Security

Time	Inflation in Year Just Ended	Par Value	Coupon Payment	+	Principal Repayment	=	Total Payment
0		\$1,000.00					
1	2%	1,020.00	\$40.80		0		\$ 40.80
2	3	1,050.60	42.02		0		42.02
3	1	1,061.11	42.44		\$1,061.11		1,103.55

## 10.2 Bond Pricing

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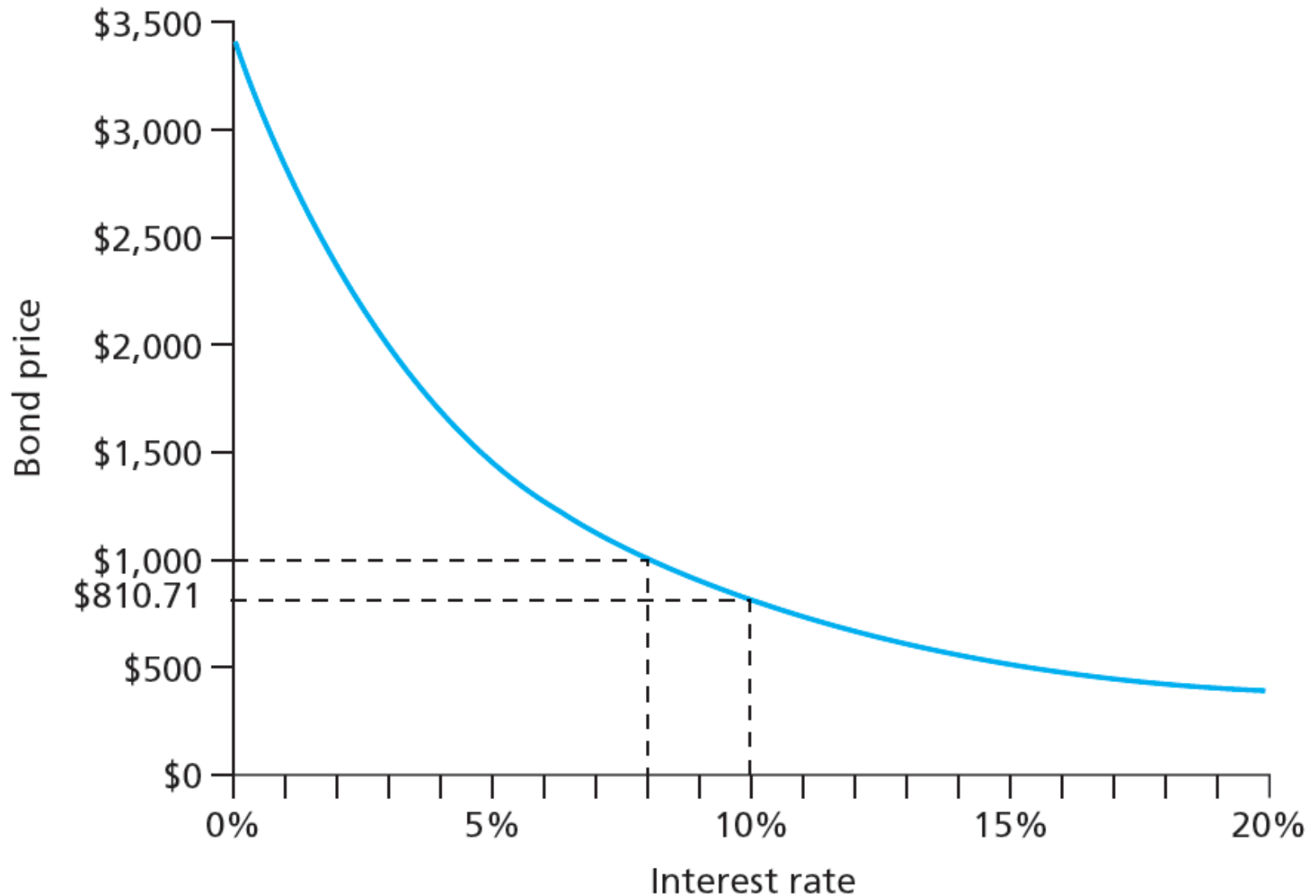
- Bond value = Present value of coupons + Present par value
- Bond value =  $\sum_{t=1}^T \frac{Coupon}{(1+r)^t} + \frac{Par\ value}{(1+r)^T}$ 
  - $T$  = Maturity date
  - $r$  = discount rate
- Bond price =  $Coupon \times \frac{1}{r} \left[ 1 - \frac{1}{(1+r)^T} \right] + Par\ value \times \frac{1}{(1+r)^T}$   
 $= Coupon \times Annuity\ factor(r, T) + Par\ value \times PV\ factor(r, T)$

## 10.2 Bond Pricing

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- Prices fall as market interest rate rises
- Interest rate fluctuations are primary source of bond market risk
- Bonds with longer maturities more sensitive to fluctuations in interest rate

# Figure 10.3 Inverse Relationship between Bond Prices and Yields





## Table 10.2 Bond Prices at Different Interest Rates

Time to Maturity	Bond Price at Given Market Interest Rate				
	2%	4%	6%	8%	10%
1 year	\$1,059.11	\$1,038.83	\$1,019.13	\$1,000.00	\$981.41
10 years	1,541.37	1,327.03	1,148.77	1,000.00	875.38
20 years	1,985.04	1,547.11	1,231.15	1,000.00	828.41
30 years	2,348.65	1,695.22	1,276.76	1,000.00	810.71

# 10.2 Bond Pricing

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- Bond Pricing between Coupon Dates
  - Invoice price = Flat price + Accrued interest
- Bond Pricing in Excel
  - =PRICE (settlement date, maturity date, annual coupon rate, yield to maturity, redemption value as percent of par value, number of coupon payments per year)

# Spreadsheet 10.1 Valuing Bonds

	6.25% coupon bond,		4.375% coupon bond,	8% coupon bond,
	<u>maturing August 15, 2023</u>	<u>Formula in column B</u>	<u>maturing Nov 15, 2039</u>	<u>30-year maturity</u>
Settlement date	8/15/2011	=DATE(2011,8,15)	8/15/2011	1/1/2000
Maturity date	8/15/2023	=DATE(2023,8,15)	11/15/2039	1/1/2030
Annual coupon rate	0.0625		0.04375	0.08
Yield to maturity	0.02598		0.03697	0.1
Redemption value (% of face value)	100		100	100
Coupon payments per year	2		2	2
Flat price (% of par)	137.444	=PRICE(B4,B5,B6,B7,B8,B9)	111.819	81.071
Days since last coupon	0	=COUPDAYBS(B4,B5,2,1)	92	0
Days in coupon period	184	=COUPDAYS(B4,B5,2,1)	184	182
Accrued interest	0	=(B13/B14)*B6*100/2	1.094	0
Invoice price	137.444	=B12+B15	112.913	81.071

# 10.3 Bond Yields

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- Yield to Maturity
  - Discount rate that makes present value of bond's payments equal to price.
- Current Yield
  - Annual coupon divided by bond price
- Premium Bonds
  - Bonds selling above par value
- Discount Bonds
  - Bonds selling below par value

# Spreadsheet 10.2 Finding Yield to Maturity

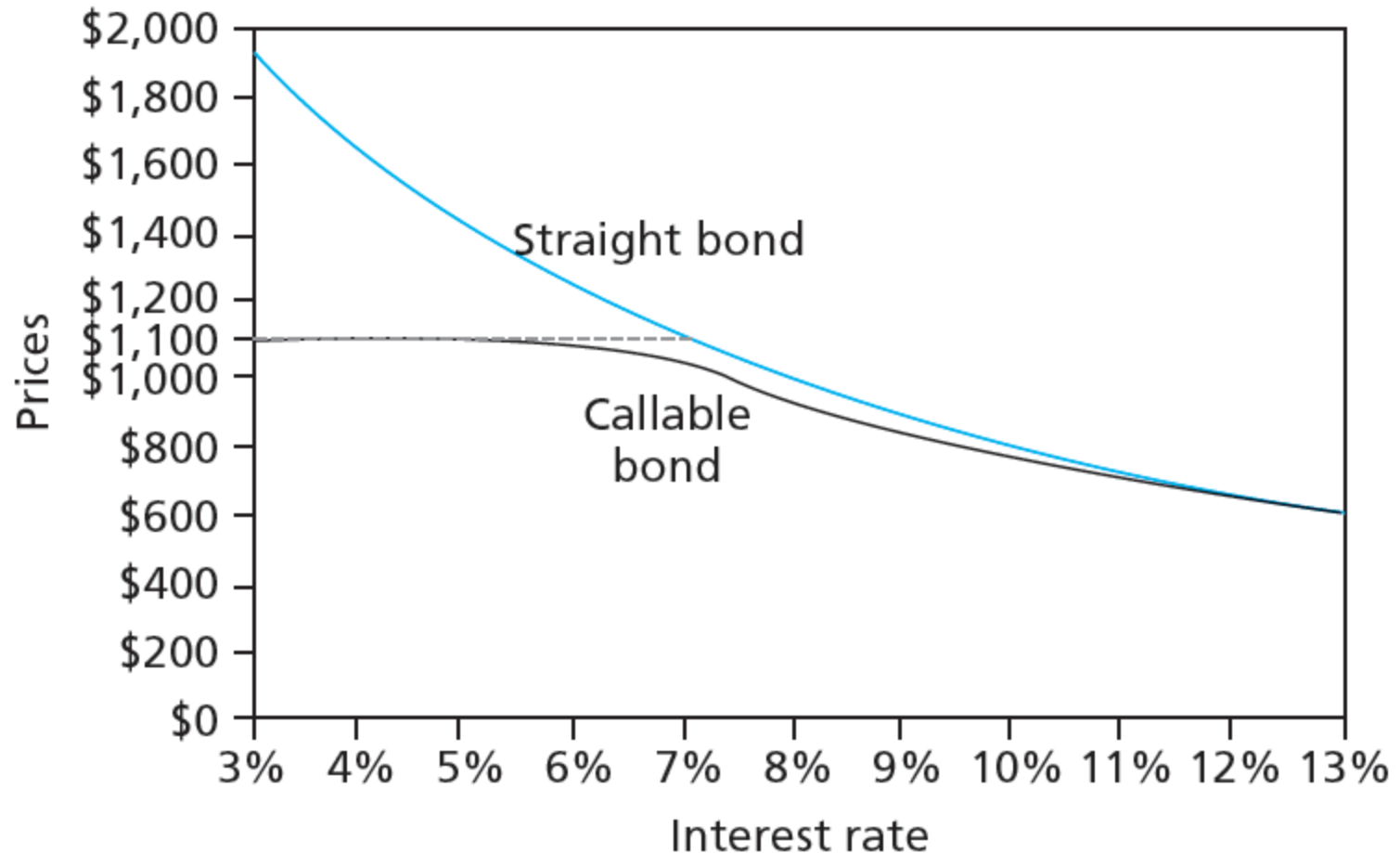
	Semiannual coupons		Annual coupons
Settlement date	1/1/2000		1/2/2000
Maturity date	1/1/2030		1/2/2030
Annual coupon rate	0.08		0.08
Bond price (flat)	127.676		127.676
Redemption value (% of face value)	100		100
Coupon payments per year	2		1
Yield to maturity (decimal)	0.0600		0.0599
The formula entered here is =YIELD(B3,B4,B5,B6,B7,B8)			

# 10.3 Bond Yields

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- Yield to Call
  - Calculated like yield to maturity
  - Time until call replaces time until maturity; call price replaces par value
  - Premium bonds more likely to be called than discount bonds

## Figure 10.4 Bond Prices: Callable and Straight Debt



# 10.3 Bond Yields

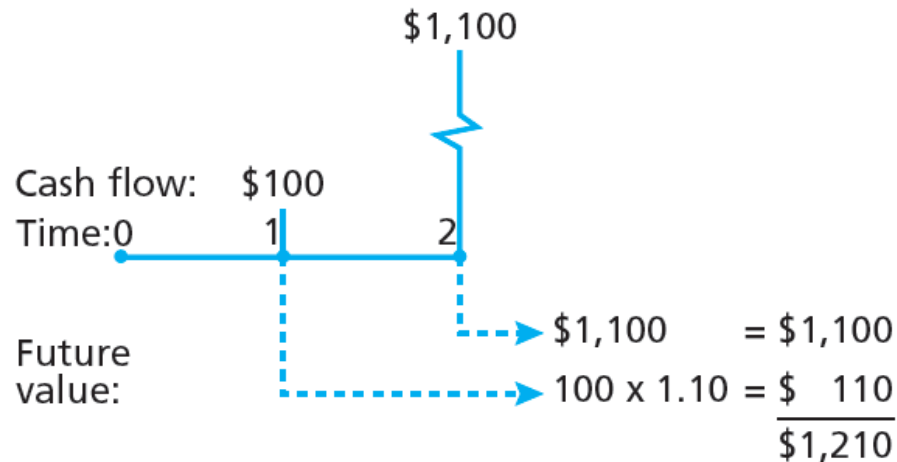
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- Realized Compound Returns versus Yield to Maturity
  - Realized compound return
    - Compound rate of return on bond with all coupons reinvested until maturity
  - Horizon analysis
    - Analysis of bond returns over multiyear horizon, based on forecasts of bond's yield to maturity and investment options
  - Reinvestment rate risk
    - Uncertainty surrounding cumulative future value of reinvested coupon payments

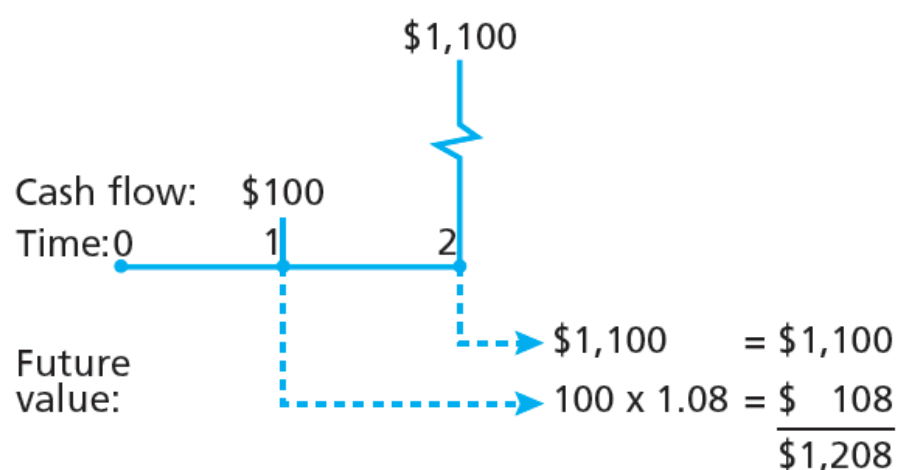


# Figure 10.5 Growth of Invested Funds

**A: Reinvestment rate = 10%**



**B: Reinvestment rate = 8%**

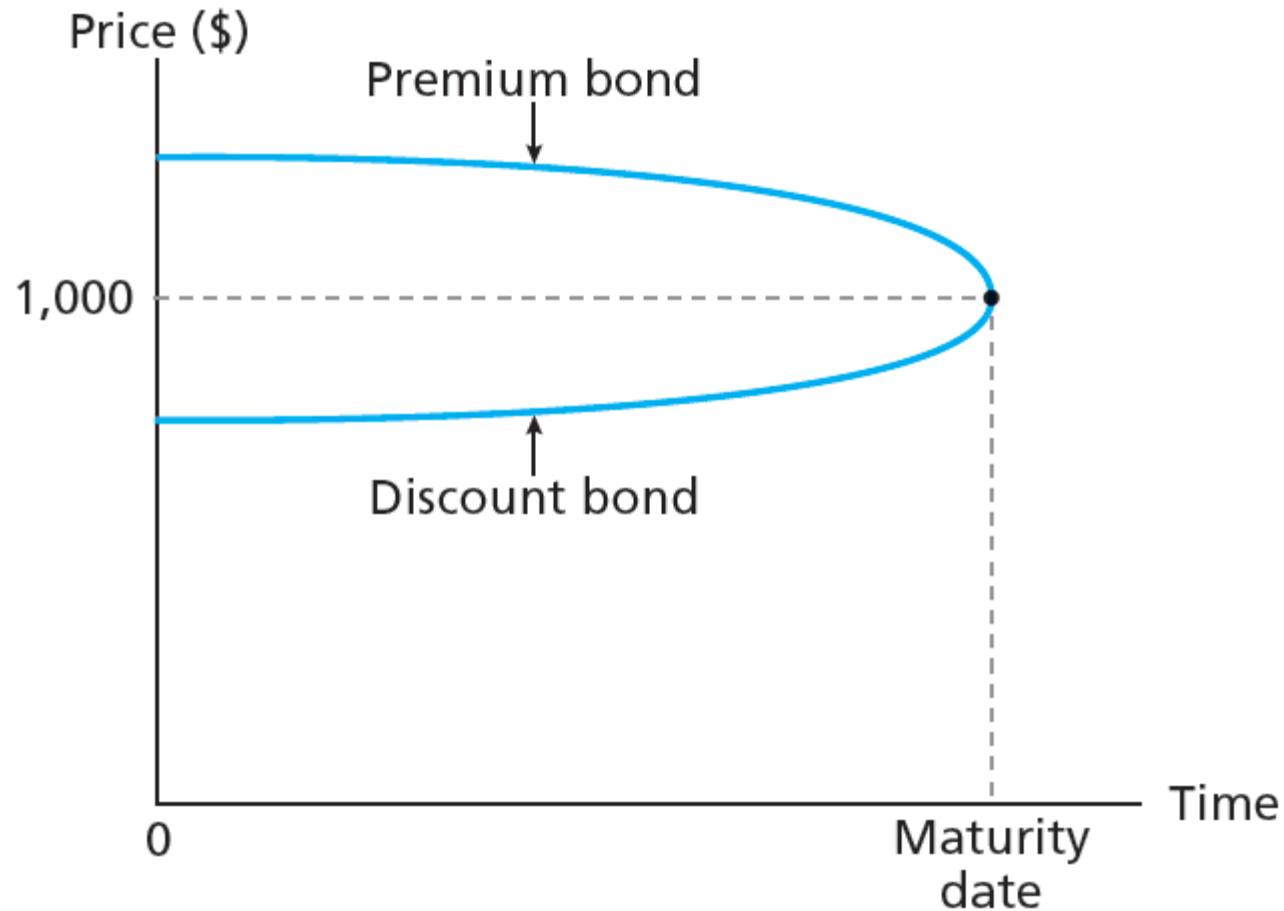


## 10.4 Bond Prices Over Time

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- Yield to Maturity versus Holding Period Return (HPR)
  - Yield to maturity measures average RoR if investment held until bond matures
  - HPR is RoR over particular investment period; depends on market price at end of period

## Figure 10.6 Price Paths of Coupon Bonds in Case of Constant Market Interest Rates

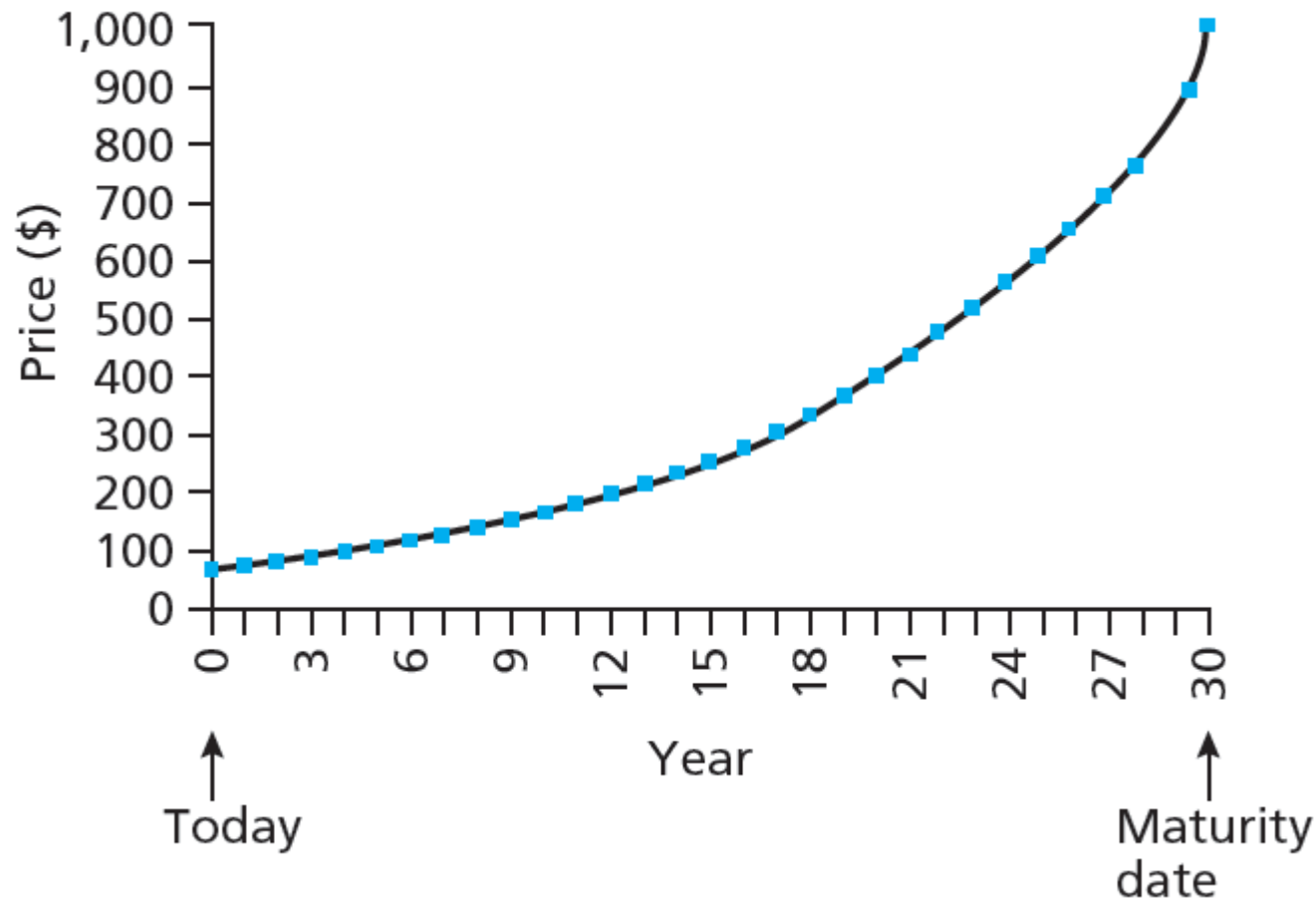


# 10.4 Bond Prices Over Time

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- Zero-Coupon Bonds and Treasury STRIPS
  - Zero-coupon bond: Carries no coupons, provides all return in form of price appreciation
  - Separate Trading of Registered Interest and Principal of Securities (STRIPS): Oversees creation of zero-coupon bonds from coupon-bearing notes and bonds

# Figure 10.7 Price of 30-Year Zero-Coupon Bond over Time at Yield to Maturity of 10%



# 10.4 Bond Prices Over Time

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- After-Tax Returns
  - Built-in price appreciation on original-issue discount bonds constitutes implicit interest payment to holder
  - IRS calculates price appreciation schedule to determine taxable interest income for built-in appreciation

# 10.5 Default Risk and Bond Pricing

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- Investment grade bond
  - Rated BBB and above by S&P or Baa and above by Moody's
- Speculative grade or junk bond
  - Rated BB or lower by S&P, Ba or lower by Moody's, or unrated

# Figure 10.8 Bond Rating Classes

	Bond Ratings							
	Very High Quality		High Quality		Speculative		Very Poor	
Standard & Poor's	AAA	AA	A	BBB	BB	B	CCC	D
Moody's	Aaa	Aa	A	Baa	Ba	B	Caa	C

At times both Moody's and Standard & Poor's use adjustments to these ratings. S&P uses plus and minus signs: A+ is the strongest A rating and A- the weakest. Moody's uses a 1, 2, or 3 designation, with 1 indicating the strongest.



# 10.5 Default Risk and Bond Pricing

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- Determinants of Bond Safety
  - Coverage ratios: Company earnings to fixed costs
  - Leverage ratio: Debt to equity
  - Liquidity ratios
    - Current: Current assets to current liabilities
    - Quick: Assets excluding inventories to liabilities
  - Profitability ratios: Measures of RoR on assets or equity
  - Cash flow-to-debt ratio: Total cash flow to outstanding debt

# Table 10.3 Financial Ratios and Default Risk

	Three-Year (2002 to 2004) Medians						
	AAA	AA	A	BBB	BB	B	CCC
EBIT interest coverage multiple	23.8	19.5	8.0	4.7	2.5	1.2	0.4
EBITDA interest coverage multiple	25.5	24.6	10.2	6.5	3.5	1.9	0.9
Funds from operations/total debt (%)	203.3	79.9	48.0	35.9	22.4	11.5	5.0
Free operating cash flow/total debt (%)	127.6	44.5	25.0	17.3	8.3	2.8	(002.1)
Total debt/EBITDA multiple	0.4	0.9	1.6	2.2	3.5	5.3	7.9
Return on capital (%)	27.6	27.0	17.5	13.4	11.3	8.7	3.2
Total debt/total debt + equity (%)	12.4	28.3	37.5	42.5	53.7	75.9	113.5

# 10.5 Default Risk and Bond Pricing

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- Bond Indentures
  - Indenture
    - Defines contract between issuer and holder
  - Sinking fund
    - Indenture calling for issuer to periodically repurchase some proportion of outstanding bonds before maturity

# 10.5 Default Risk and Bond Pricing

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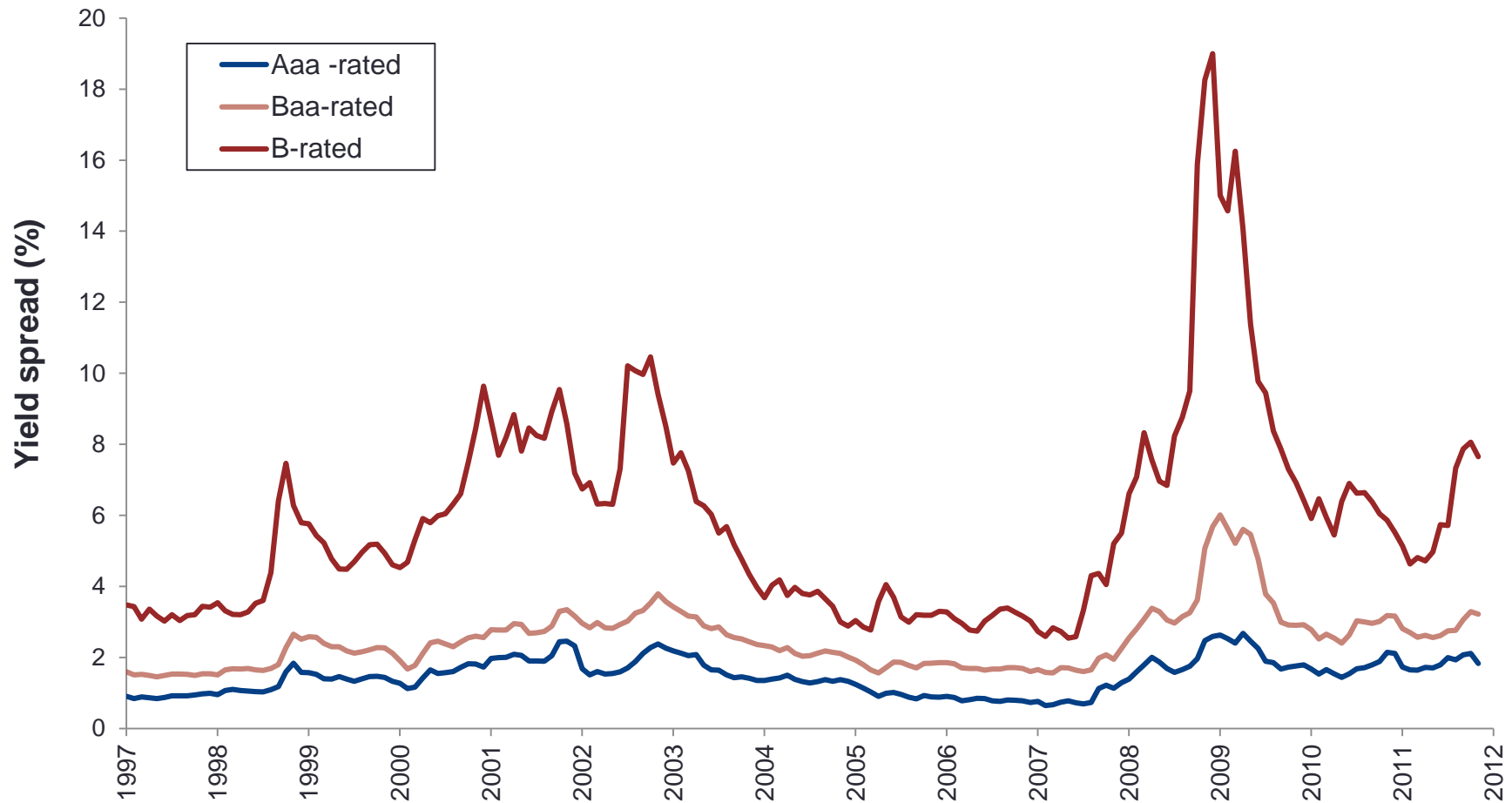
- Bond Indentures
  - Subordination clause
    - Restrictions on additional borrowing stipulating senior bondholders paid first in event of bankruptcy
  - Collateral
    - Specific asset pledged against possible default
- Debenture
  - Bond not backed by specific collateral

# 10.5 Default Risk and Bond Pricing

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- Yield to Maturity and Default Risk
  - Stated yield is maximum possible yield to maturity of bond
  - Default premium
    - Increment to promised yield that compensates investor for default risk

# Figure 10.10 Yield Spreads between Corporate and 10-Year Treasury Bonds

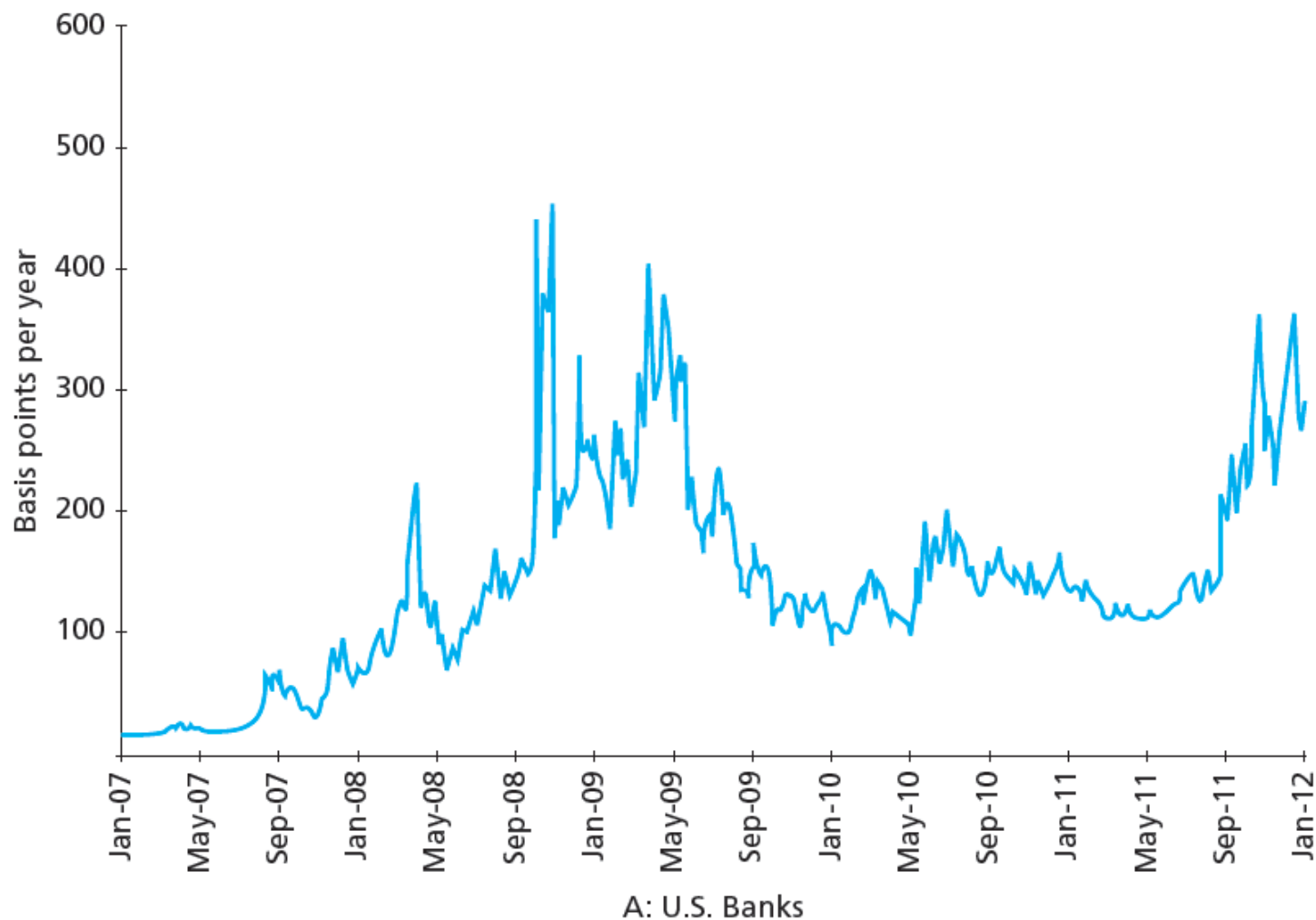


# 10.5 Default Risk and Bond Pricing

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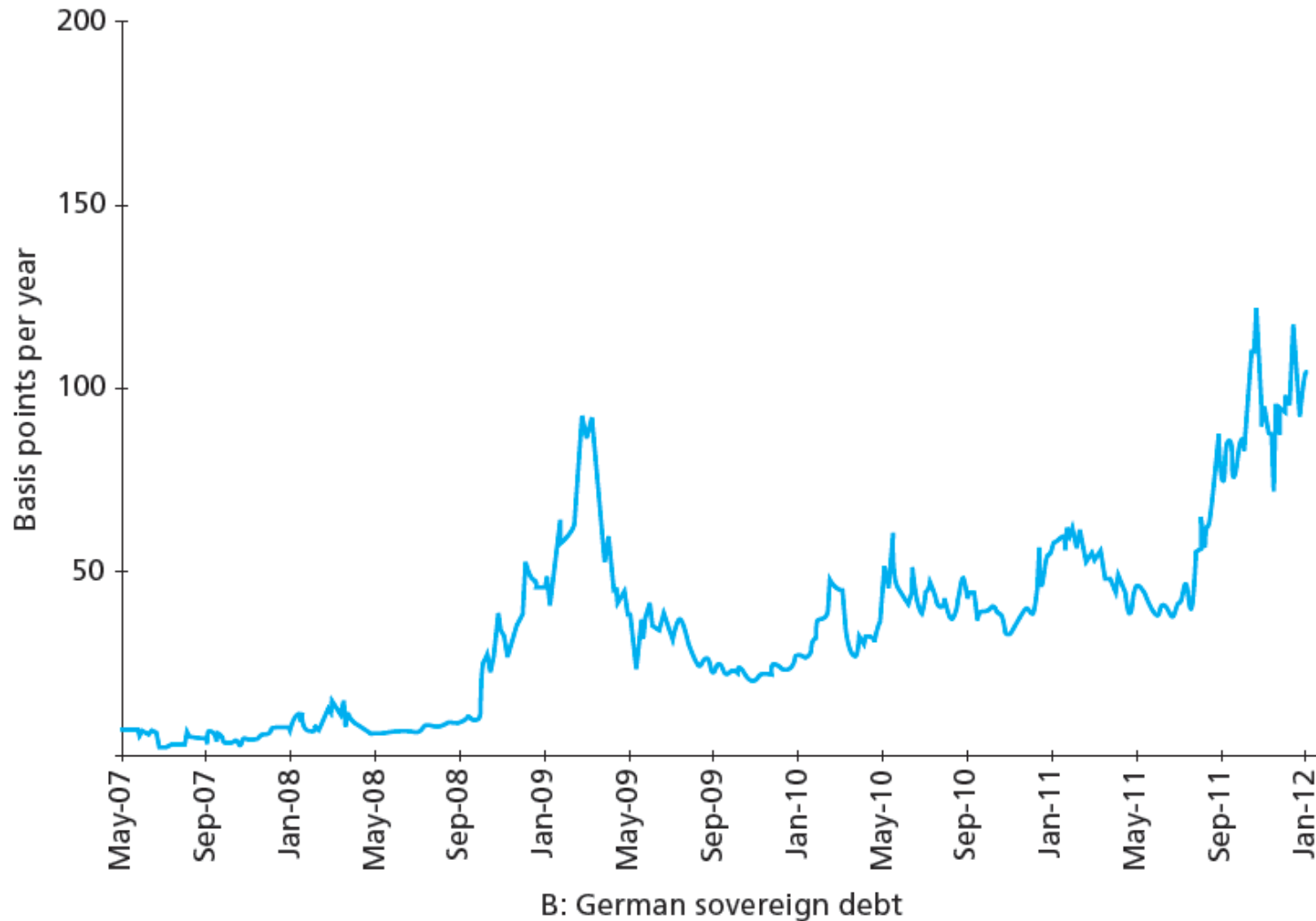
- Credit Default Swaps (CDS)
  - Insurance policy on default risk of corporate bond or loan
  - Designed to allow lenders to buy protection against losses on large loans
    - Later used to speculate on financial health of companies

# Figure 10.11A Prices of CDSs, U.S. Banks





# Figure 10.11B Prices of CDSs, German Sovereign Debt

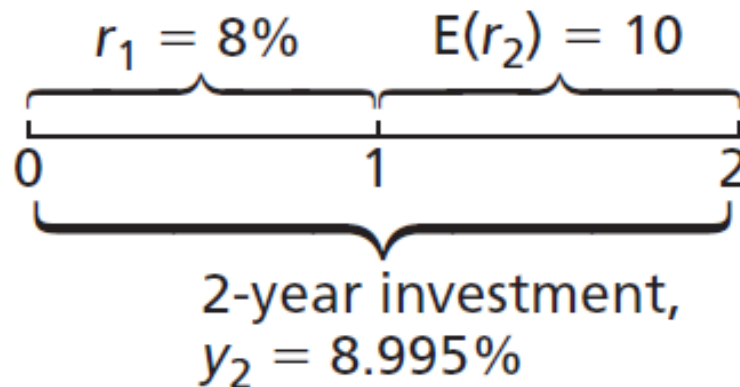


# 10.6 The Yield Curve

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- Yield Curve
  - Graph of yield to maturity as function of term to maturity
- Term Structure of Interest Rates
  - Relationship between yields to maturity and terms to maturity across bonds
- Expectations Hypothesis
  - Yields to maturity determined solely by expectations of future short-term interest rates

## Figure 10.13 Returns to Two 2-Year Investment Strategies



2-year cumulative  
expected returns

$$1.08 \times 1.10 = 1.188$$

$$1.08995^2 = 1.188$$

# 10.6 The Yield Curve

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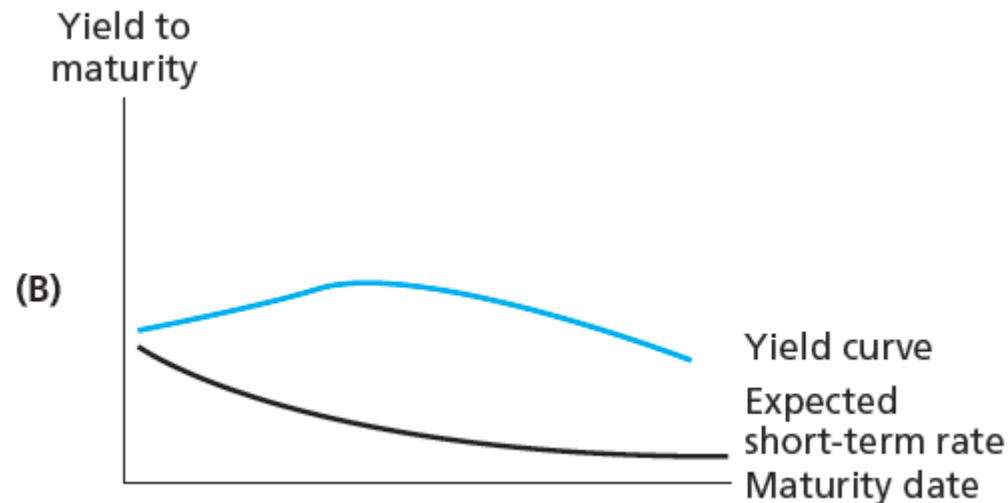
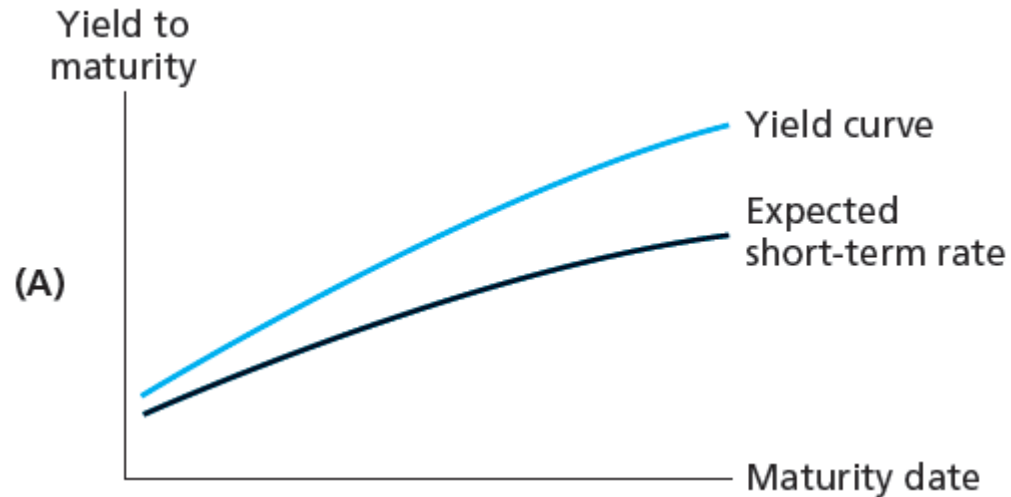
- Forward Rate
  - Inferred short-term ROI for future period, makes expected total return of long-term bond equal to that of rolling over short-term bonds
  - $(1 + y_n)^n = (1 + y_{n-1})^{n-1}(1 + f_n)$

# 10.6 The Yield Curve

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- Liquidity Preference Theory
  - Investors demand risk premium on long-term bonds
  - Liquidity premium
    - Extra expected return demanded by investors as compensation for greater risk of long-term bonds
  - Spread between forward ROI and expected short sale
    - $f_n = E(r_n) + \text{Liquidity premium}$

# Figure 10.14 Illustrative Yield Curves



## Figure 10.15 Term Spread: Yields on 10-Year versus 90-day Treasury Securities

