

Array Rotation Trick

<https://www.youtube.com/watch?v=BHr381Guz3Y>

When you work through “rotate an array by k steps,” you’ll naturally touch on a handful of core algorithm-and-data-structure concepts. Here’s a structured list of those concepts, with a brief explanation of how each shows up in this problem:

1. Array Indexing and Zero-Based Positions

- Understanding that `nums[0]` is the first element and `nums[n-1]` is the last.
- Realizing that rotating “right by 1” means the element at `nums[n-1]` wraps around to index 0, and everything else shifts one slot to the right.

2. Modular Arithmetic (%) for Circular Shifts

- Noticing that rotating by any multiple of n returns you to the original array (so $k \% n$ is enough).
- Computing $(i + k) \% n$ to find the new position of element i if you use an auxiliary array, or computing $(start + i) \% n$ if you “simulate” the rotation by index offset.

3. In-Place Reversal Technique (Three-Step Reversal Pattern)

- Learning that you can accomplish a right-rotation by:
 4. Reversing the entire array,
 5. Reversing the first k elements,
 6. Reversing the last $n-k$ elements.
- Seeing how each reversal “mirrors” two elements at once, and why three reversals in that order end up with the correct rotated order.

4. Two-Pointer (Head/Tail) Reversal Pattern

- Practicing the classic “swap `nums[l]` with `nums[r]` and then $l++$, $r--$, stop when $l \geq r$.”
- Counting exactly $\lfloor m/2 \rfloor$ swaps to reverse any subarray of length m , and recognizing that each swap is $O(1)$.

5. Time Complexity (Big-O) Analysis

- Observing that each reversal pass visits $\sim m/2$ pairs, so reversing m elements is $\Theta(m)$ time.
- Summing $\Theta(n) + \Theta(k) + \Theta(n-k) = \Theta(2n) = \Theta(n)$ total for the three reversals, so the algorithm is $O(n)$.

6. Space Complexity and In-Place Constraints

- Distinguishing between an $O(n)$ auxiliary-array solution (copy-and-write-back) versus the $O(1)$ “three reversals” approach that uses only a few integer variables.
- Understanding why physically rearranging n elements must cost at least $\Omega(n)$ in time, and that you can’t genuinely move all elements in $O(1)$ time.

7. Edge Case Handling

- Realizing that if $k == 0$ or $k \% n == 0$, you should leave the array untouched (one of the first checks in code).
- Verifying behavior when $n = 1$, or when $k > n$ (hence $k = k \% n$).

8. Problem Decomposition and Pattern Recognition

- Breaking the problem into smaller sub-problems (e.g., “how do I rotate by 1?”, “how do I rotate by k?”, “can I do it without extra space?”).
 - Spotting the “reverse-all, reverse-first-k, reverse-remaining” pattern as a reusable trick for many array-rotation or cyclic-shift tasks.
9. **Alternative In-Place Approaches (like the Juggling Algorithm)**
- Knowing that there’s also a GCD-based “cycle” method (sometimes called the juggling algorithm) that moves elements in cycles of length $\text{gcd}(n, k)$, visiting each position exactly once.
 - Comparing why the reversal method tends to be simpler to code and just as efficient ($O(n)/O(1)$).
10. **Simulating a Rotation Without Physically Moving (Index Offsetting)**
- Learning that if all you need is to “answer queries” as if the array were rotated (rather than actually rewrite it), you can store a single integer offset “start = $(n - k) \% n$,” and answer “rotated[i]” by looking up `nums[(start + i) % n]`.
 - Seeing the difference between “logical” rotation ($O(1)$ per lookup, no array change) versus “physical” rotation ($O(n)$ to modify in place).
11. **Consistency Checks via Examples**
- Tracing small examples by hand (e.g. `[1, 2, 3, 4, 5]`, $k=2$) to confirm that each step of “reverse all \rightarrow reverse first 2 \rightarrow reverse last 3” produces exactly the desired result.
 - Ensuring your implementation matches those hand-computed examples.
12. **Writing Clean, Modular Code**
- Recognizing that “reverse a subarray” can be factored into its own helper function (e.g. `def reverse(nums, left, right): ...`).
 - Writing each of the three reversal calls as `reverse(nums, 0, n-1), reverse(nums, 0, k-1), reverse(nums, k, n-1)`.
 - Documenting why $k = k \% n$ is necessary inside your main `rotate(...)` function.

Putting It All Together

When you solve “rotate array” in place, you end up practicing:

- Array indexing and boundary checks
- Modulo arithmetic for wrapping around
- The two-pointer reversal pattern
- Counting swaps to analyze $\Theta(n)$ time
- Distinguishing $O(n)$ vs. $O(1)$ extra space
- Edge cases ($n=1$, $k \geq n$, $k=0$)
- Problem decomposition into reversible sub-arrays
- Potential alternative techniques (auxiliary array, juggling/GCD cycles, simulated offset lookup)

By understanding each of those pieces, you build a small but solid toolkit that applies not only to array rotations but to many other array-manipulation tasks in coding interviews and real-world coding.