

## Majority Element II

[https://www.youtube.com/watch?v=Eua-UrQ\\_ANo](https://www.youtube.com/watch?v=Eua-UrQ_ANo)

By working through this “Majority Element II” problem end-to-end, you’re really touching on a handful of core algorithmic and coding concepts. Here’s what you’d learn or reinforce:

### 1. Pigeonhole Principle & Frequency Thresholds

- Recognizing that if you need elements appearing  $> \lfloor n/3 \rfloor$  times, there can be at most two such elements (because  $3 \times (\text{more than } n/3)$  would exceed  $n$ ).
- Translating “ $> \lfloor n/3 \rfloor$ ” into code via integer division (`len(nums) // 3`).

### 2. Boyer–Moore Voting Paradigm (Generalized)

- Understanding the idea of “cancelling out” votes between different candidates so that only true heavy hitters survive.
- Generalizing from the classic “ $> n/2$ ” majority vote to maintaining two candidate slots (for the “ $> n/3$ ” case).

### 3. Two-Pass vs. One-Pass with Verification

- First pass to identify up to two possible candidates (with cancellation).
- Second pass to **verify** true counts against the threshold.
- Appreciating why you can’t trust the provisional vote counts until you re-scan.

### 4. Constant Extra Space Analysis

- Designing an algorithm that only keeps a fixed number of variables or small dict entries, regardless of input size.
- Contrasting with a naïve hash-map solution that might store  $O(n)$  keys.

### 5. `defaultdict(int)` Convenience

- Automating zero-initialization for unseen keys so you can write `count[x] += 1` without a guard.
- Understanding how `defaultdict` differs from a normal `dict`.

### 6. Pruning Technique

- Implementing the “prune when you have three distinct keys” step by subtracting one vote from each and dropping zeros.
- Seeing how this directly embodies the cancellation logic in code.

### 7. Pythonic Loop Constructs & Conditionals

- Writing clear `for` loops, `if/elif/else` ladders to cover all cases (match candidate, assign new slot, or cancel).
- Proper use of `continue`, inner loops, and dict comprehensions or manual rebuilds.

### 8. Time Complexity Trade-offs

- Ensuring  $O(n)$  behavior by keeping all operations per element  $O(1)$  (pruning over  $\leq 3$  keys is constant work).
- Understanding the cost of `nums.count(cand)` in the verification pass (up to 2 full rescans), yet still  $O(n)$  overall.

### 9. Edge-Case Handling

- Very small arrays ( $n = 1$  or  $2$ ) where  $\lfloor n/3 \rfloor = 0$ , so every distinct element qualifies.
- Arrays with no majority ( $> n/3$ ), exactly one, or exactly two.

### 10. Putting It All Together: Correctness Proof Sketch

- Convincing yourself (or a reviewer) that no potential  $> n/3$  element can be pruned away permanently—because it outvotes all cancellations over the full scan.