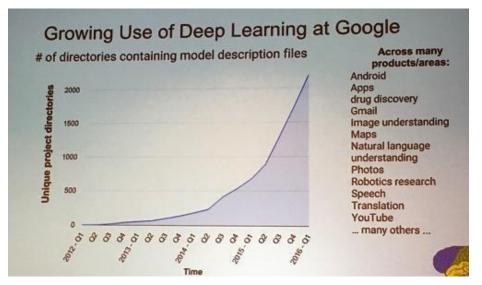
Neural Networks

Some of the contents are adapted from A. Ng, S. Kim, F. Li, and H. Lee

Deep learning attracts lots of attention.

 I believe you have seen lots of exciting results before.

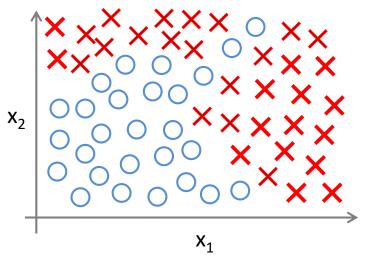


Deep learning trends at Google. Source: SIGMOD/Jeff Dean

History of Deep Learning

- 1958: Perceptron (linear model)
- 1969: Perceptron has limitation
- 1980s: Multi-layer perceptron
 - Do not have significant difference from DNN today
- 1986: Backpropagation
 - Usually more than 3 hidden layers is not helpful
- 1989: 1 hidden layer is "good enough", why deep?
- 2006: RBM initialization (breakthrough)
- 2009: GPU
- 2011: Start to be popular in speech recognition
- 2012: win ILSVRC image competition

Non-linear Classification



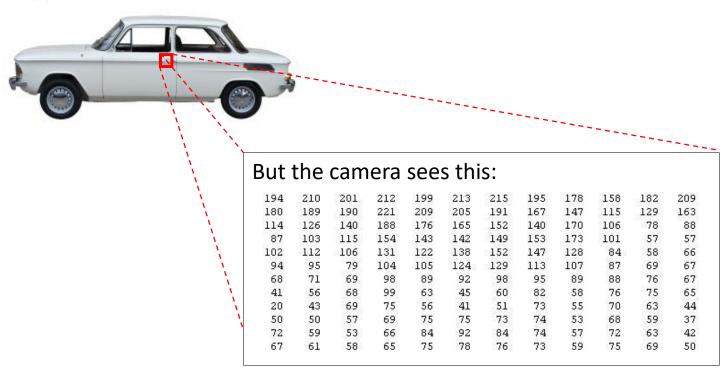
$$x_1 = ext{size}$$
 $x_2 = ext{\# bedrooms}$ $x_3 = ext{\# floors}$ $x_4 = ext{age}$

$$x_{100}$$

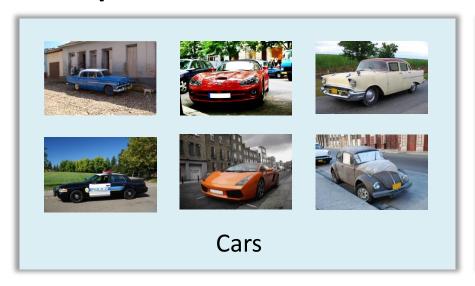
$$g(\theta_0 + \theta_1 x_1 + \theta_2 x_2 + \theta_3 x_1 x_2 + \theta_4 x_1^2 x_2 + \theta_5 x_1^3 x_2 + \theta_6 x_1 x_2^2 + \dots)$$

What is this?

You see this:



Computer Vision: Car detection





Testing:

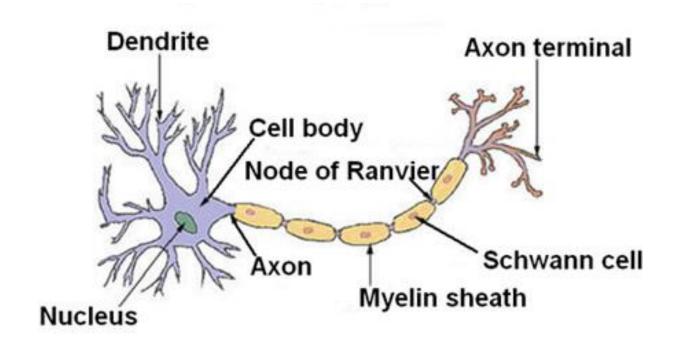


Neural Networks

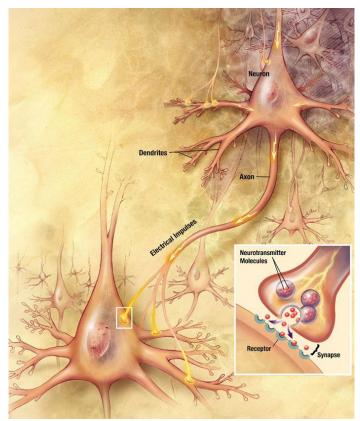
Origins: Algorithms that try to mimic the brain. Was very widely used in 80s and early 90s; popularity diminished in late 90s.

Recent resurgence: State-of-the-art technique for many applications

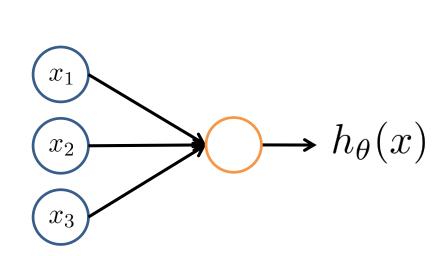
Neuron in the brain



Neurons in the brain

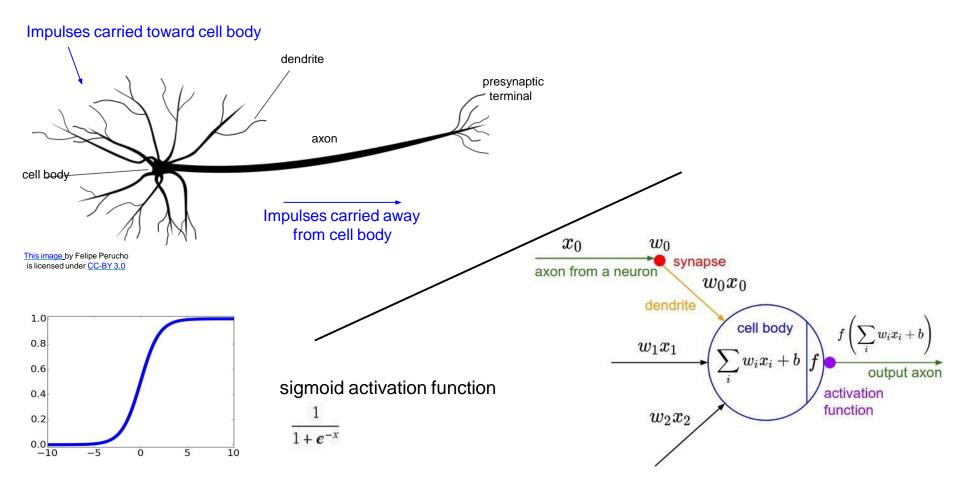


Neuron model: Logistic unit

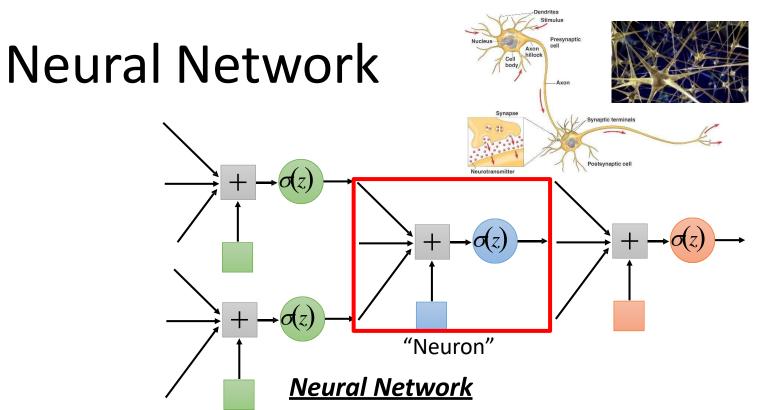


$$x = \begin{bmatrix} x_0 \\ x_1 \\ x_2 \\ x_3 \end{bmatrix} \quad \theta = \begin{bmatrix} \theta_0 \\ \theta_1 \\ \theta_2 \\ \theta_3 \end{bmatrix}$$

Sigmoid (logistic) activation function.



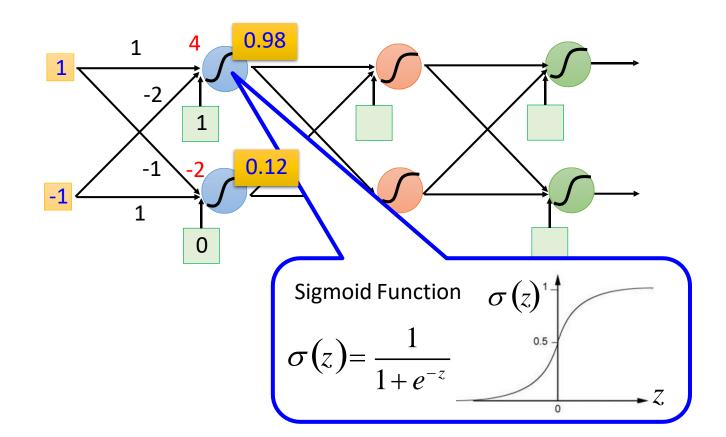
Fei-Fei Li & Justin Johnson & Serena Yeung



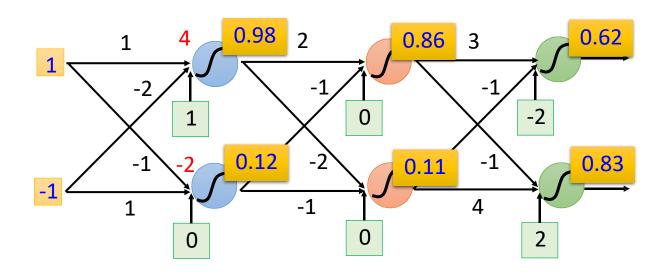
Different connection leads to different network structures

Network parameter θ : all the weights and biases in the "neurons"

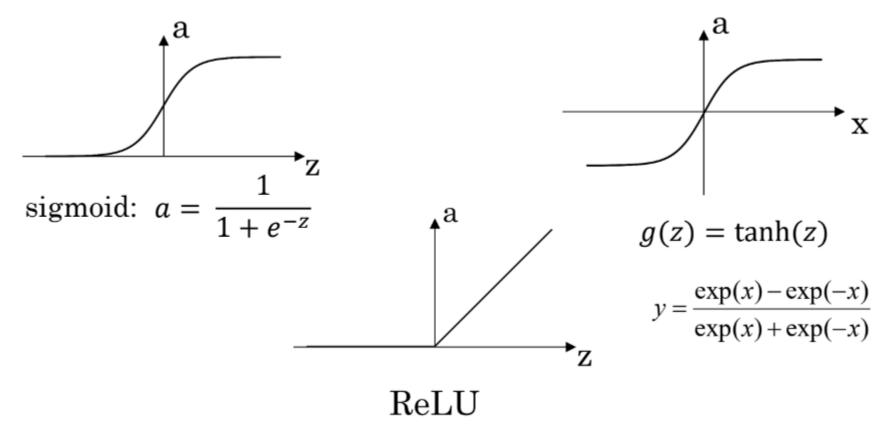
Fully Connect Feedforward Network



Fully Connect Feedforward Network



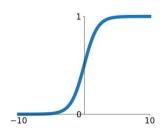
Activation Functions



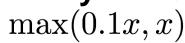
Activation functions

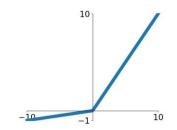
Sigmoid

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$



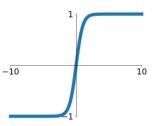
Leaky ReLU





tanh

tanh(x)

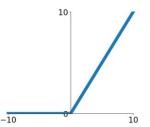


Maxout

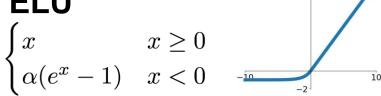
$$\max(w_1^T x + b_1, w_2^T x + b_2)$$

ReLU

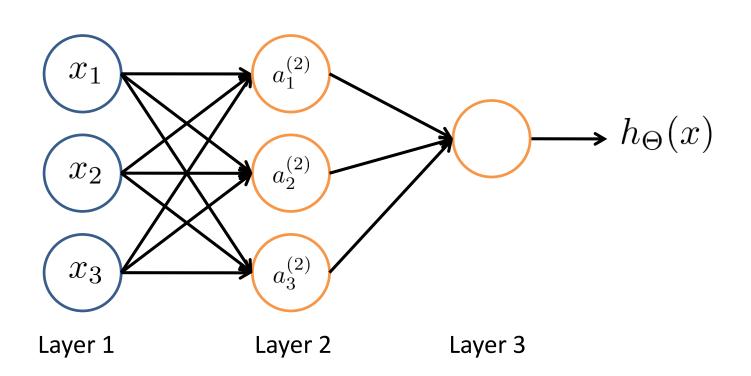
 $\max(0, x)$



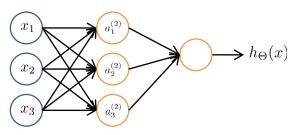
ELU



Neural Network



Neural Network



$$a_i^{(j)} =$$
 "activation" of unit i in layer j

 $\Theta^{(j)} = \text{matrix of weights controlling}$ function mapping from layer j to layer j+1

$$a_{1}^{(2)} = g(\Theta_{10}^{(1)}x_{0} + \Theta_{11}^{(1)}x_{1} + \Theta_{12}^{(1)}x_{2} + \Theta_{13}^{(1)}x_{3})$$

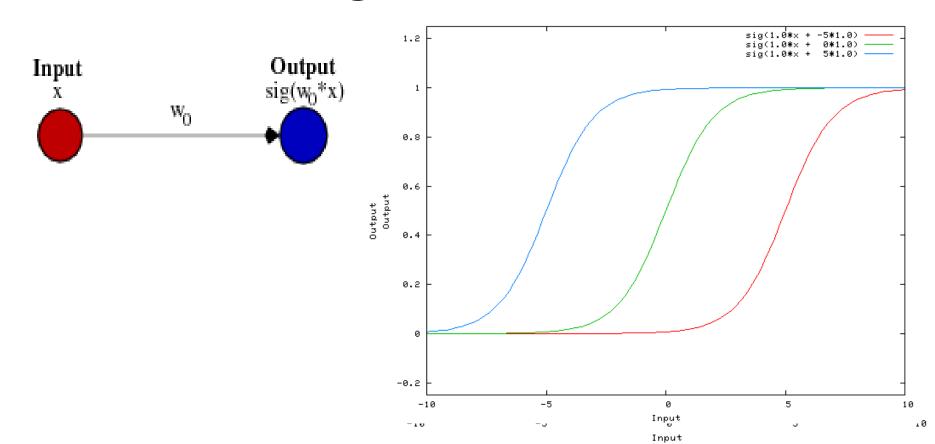
$$a_{2}^{(2)} = g(\Theta_{20}^{(1)}x_{0} + \Theta_{21}^{(1)}x_{1} + \Theta_{22}^{(1)}x_{2} + \Theta_{23}^{(1)}x_{3})$$

$$a_{3}^{(2)} = g(\Theta_{30}^{(1)}x_{0} + \Theta_{31}^{(1)}x_{1} + \Theta_{32}^{(1)}x_{2} + \Theta_{33}^{(1)}x_{3})$$

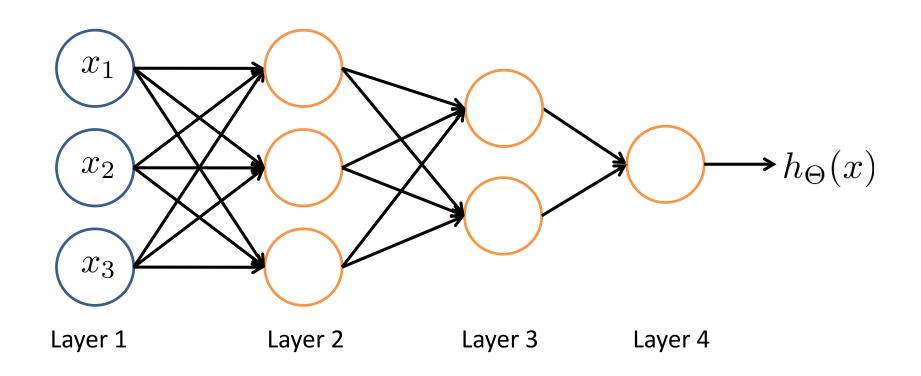
$$h_{\Theta}(x) = a_{1}^{(3)} = g(\Theta_{10}^{(2)}a_{0}^{(2)} + \Theta_{11}^{(2)}a_{1}^{(2)} + \Theta_{12}^{(2)}a_{2}^{(2)} + \Theta_{13}^{(2)}a_{3}^{(2)})$$

If network has s_j units in layer j, s_{j+1} units in layer j+1, then $\Theta^{(j)}$ will be of dimension $s_{j+1} \times (s_j+1)$.

Weights and Bias



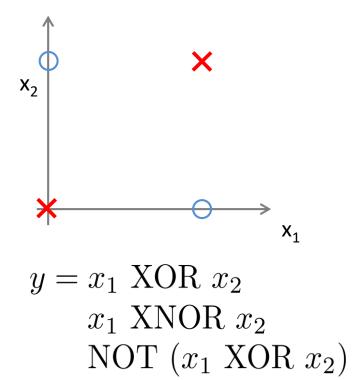
network architectures

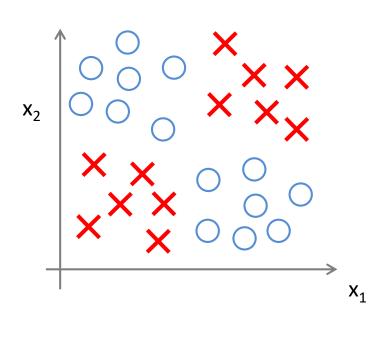


Non-linear classification example: XOR/XNOR

x1, x2 Features

 x_1 , x_2 are binary (0 or 1).

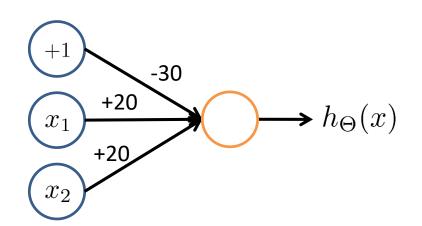


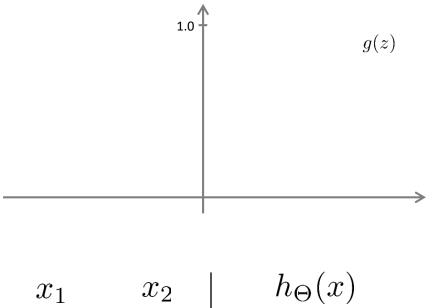


Simple example: AND

$$x_1, x_2 \in \{0, 1\}$$

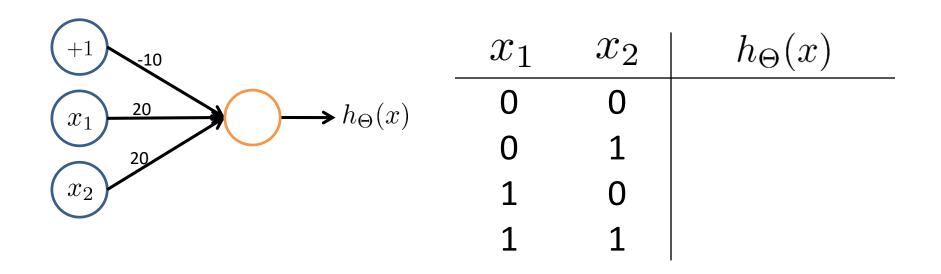
 $y = x_1 \text{ AND } x_2$



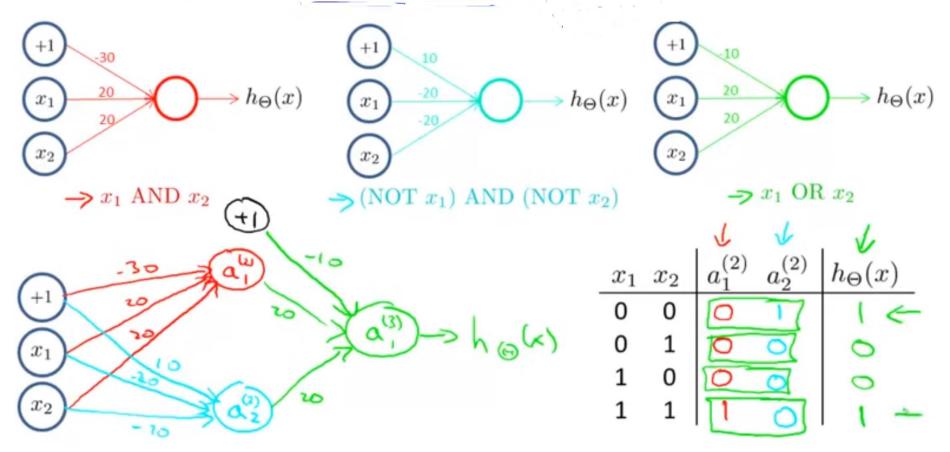


x_1	x_2	$h_{\Theta}(x)$
0	0	
0	1	
1	0	
1	1	

Example: OR function



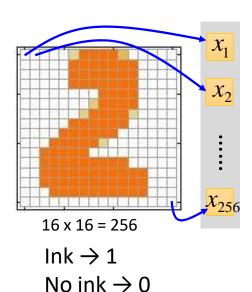
Putting it together: $x_1 \text{ XNOR } x_2$



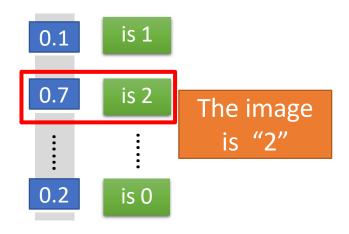
Example Application



Input



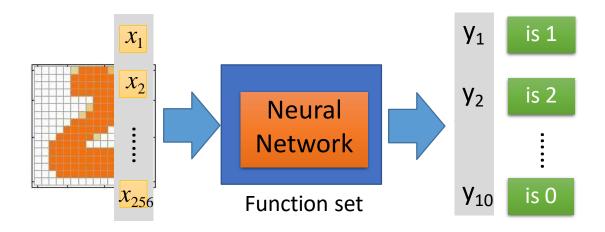
Output



Each dimension represents the confidence of a digit.

Example Application

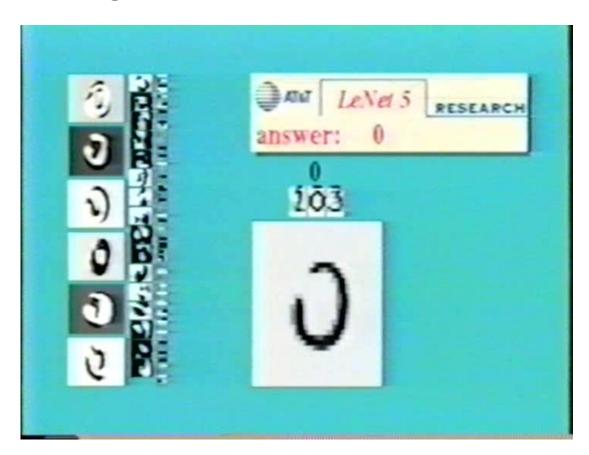
• Handwriting Digit Recognition



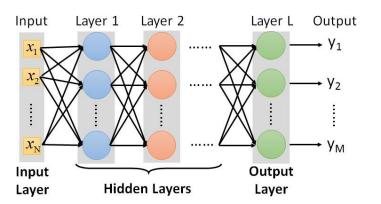
Input: 256-dim vector

output: 10-dim vector

Handwritten digit classification



FAQ



 Q: How many layers? How many neurons for each layer?

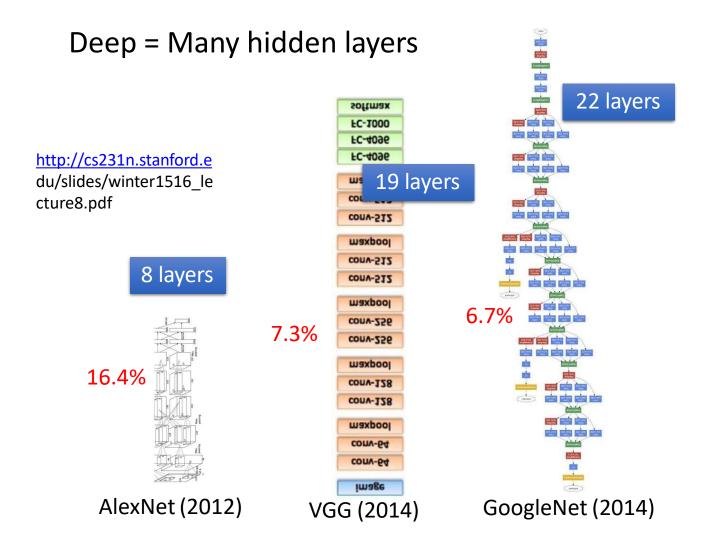
Trial and Error

Intuition

- Q: Can the structure be automatically determined?
 - E.g. Evolutionary Artificial Neural Networks
- Q: Can we design the network structure?

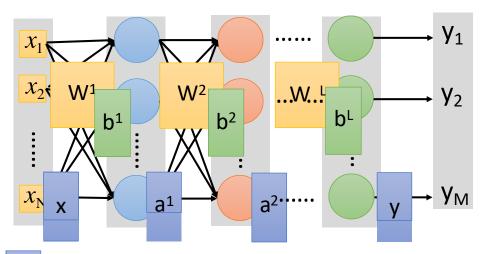
Convolutional Neural Network (CNN)

Neural Networks – Part 2



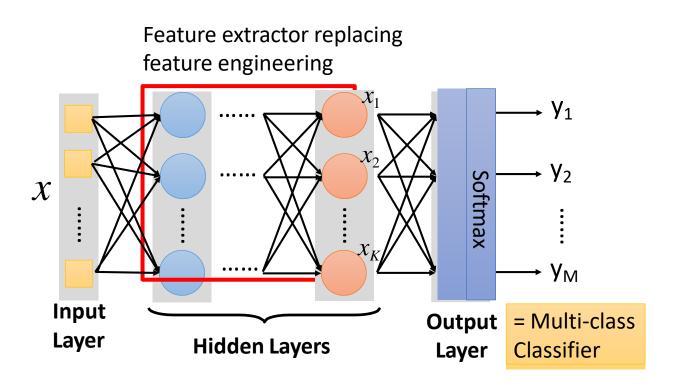
Deep = Many hidden layers 152 layers Special structure 3.57% COMMON CO 7.3% 6.7% 16.4% GoogleNet **AlexNet** VGG **Residual Net** (2014)(2012)(2014)(2015)

Neural Network



y =
$$f(x)$$
 Using parallel computing techniques to speed up matrix operation

Output Layer



Gradient Descent

This is the "learning" of machines in deep learning



Backpropagation

• Backpropagation: an efficient way to compute $\partial L/\partial w$ in neural network









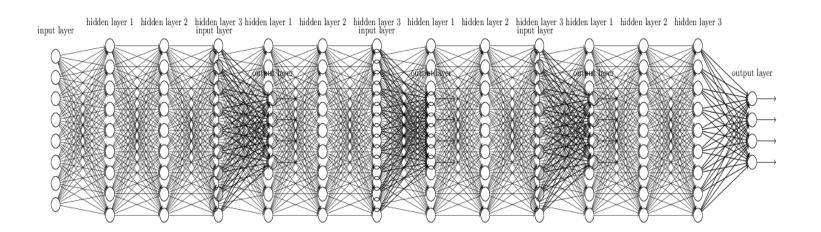




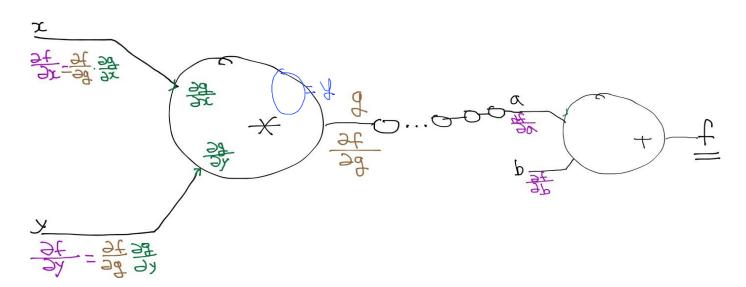




Back propagation



Backpropagation (chain rule)



chain rule

$$f_{1}\left(f_{2}\left(f_{3}(f_{4}(x))\right)\right)$$

$$\frac{\partial f_{1}}{\partial x} = \frac{\partial f_{1}}{\partial f_{2}} \cdot \frac{\partial f_{2}}{\partial f_{3}} \cdot \frac{\partial f_{3}}{\partial f_{4}} \cdot \frac{\partial f_{4}}{\partial x}$$

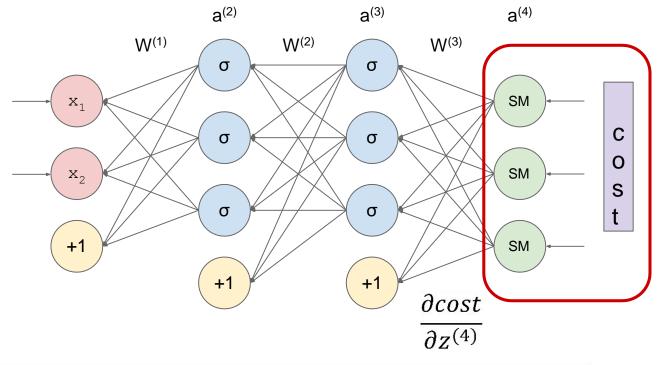
Back Propagation

Want:

 $\frac{\partial cost}{\partial W^{(1)}}$ $\frac{\partial}{\partial G}$

 $\frac{\partial cost}{\partial W^{(2)}}$

 $\frac{\partial cost}{\partial W^{(3)}}$



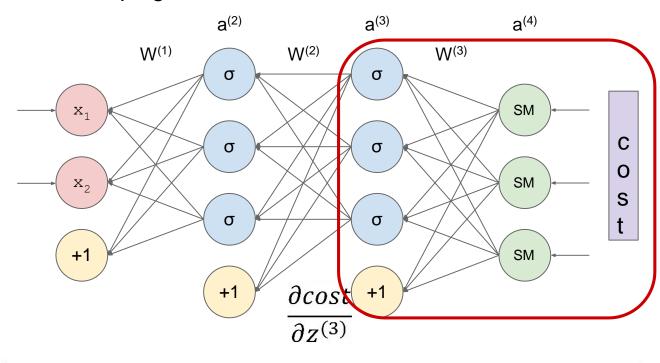
$$\frac{\partial cost}{\partial W^{(3)}} = \frac{\partial cost}{\partial z^{(4)}} \cdot \frac{\partial z^{(4)}}{\partial W^{(3)}} = \delta^{(4)} a^{(3)}_{\text{Sam Abrahams}}$$

Back Propagation

$$\frac{\partial \cos x}{\partial W^{(1)}} \qquad \frac{\partial \cos x}{\partial V}$$

$$\frac{\partial cost}{\partial W^{(2)}}$$

$$\frac{\partial cost}{\partial W^{(3)}}$$



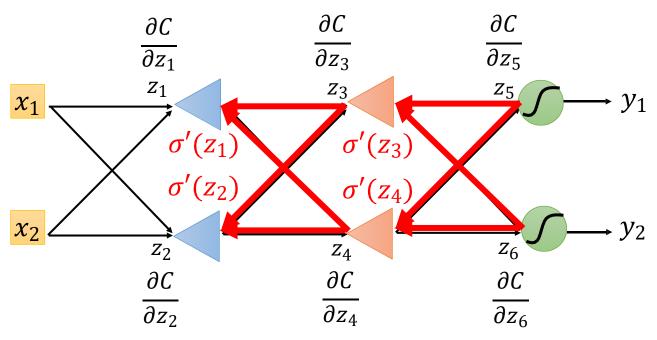
Want:

$$\frac{\partial cost}{\partial z^{(3)}} = \frac{\partial cost}{\partial z^{(4)}} \cdot \frac{\partial z^{(4)}}{\partial a^{(3)}} \cdot \frac{\partial a^{(3)}}{\partial z^{(3)}} = \delta^{(3)^{\text{rl}}}_{\text{Sam Abrahams}}$$

Backpropagation – Backward Pass

Compute $\partial C/\partial z$ for all activation function inputs z

Compute $\partial C/\partial z$ from the output layer



Pre-training for deep neural networks



TTER — Communicated by Yann Le Cun

A Fast Learning Algorithm for Deep Belief Nets

Geoffrey E. Hinton

hinton@cs.toronto.edu

Simon Osindero

osindero@cs.toronto.edu

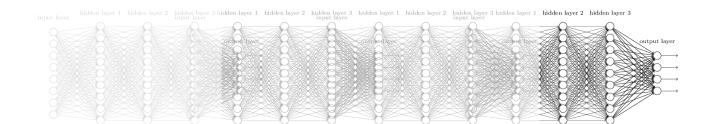
Department of Computer Science, University of Toronto, Toronto, Canada M5S 3G4

Yee-Whye Teh

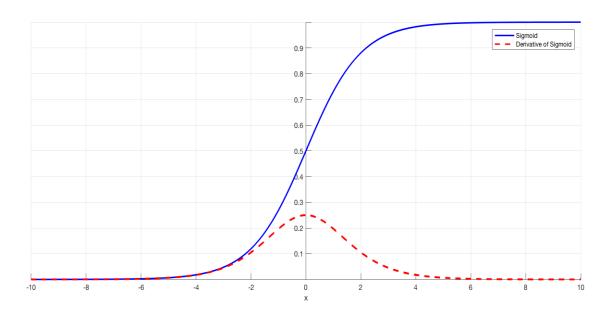
tehyw@comp.nus.edu.sg Department of Computer Science, National University of Singapore, Singapore 117543

We show how to use "complementary priors" to eliminate the explaining-away effects that make inference difficult in densely connected belief nets that have many hidden layers. Using complementary priors, we derive a fast, greedy algorithm that can learn deep, directed belief networks one layer at a time, provided the top two layers form an undirected associative memory. The fast, greedy algorithm is used to initialize a slower learning procedure that fine-tunes the weights using a contrastive version of the wake-sleep algorithm. After fine-tuning, a network with three hidden layers forms a very good generative model of the joint distribution of handwritten digit images and their labels. This generative model gives better digit classification than the best discriminative learning algorithms. The low-dimensional manifolds on which the digits lie are modeled by long ravines in the free-energy landscape of the top-level associative memory, and it is easy to explore these ravines by using the directed connections to display what the associative memory has in mind.

Vanishing gradient (NN winter2: 1986-2006)



Sigmoid!



https://isaacchanghau.github.io/img/deeplearning/activationfunction/sigmoid.png

NN Training

- 1. Do **forwards propagation**, calculate the input sum and activation of each neuron by iteratively do matrix-vector multiplication and taking component-wise transfer function of all neurons in every layer. Save the results for later.
- 2. Calculate the **error signal of the final layer** *L*, by obtaining the gradient of the cost function with respect to the outputs of the network.
- 3. Do backwards propagation, calculate the error signals of the neurons in each layer. The input sum of each neuron is required to do this, and it is also done by iteratively computing matrix-vector multiplications

NN training cont'd

- 4. Calculate the derivative of the cost function with respect to the weights, the activation of each neuron is required to do this. This will be a matrix with the same shape as the weight matrix.
- 5. Calculate the derivative of the cost function with respect to the biases (this can be skipped). This will only be a column vector.
- 6. Update the weights according to the a gradient descent learning rule.

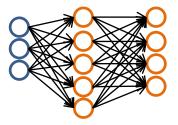
Xavier/He initialization

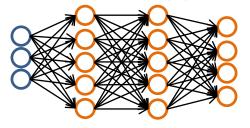
- Makes sure the weights are 'just right', not too small, not too big
- Using number of input (fan_in) and output (fan_out)

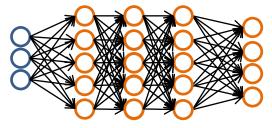
```
# Xavier initialization
# Glorot et al. 2010
W = np.random.randn(fan_in, fan_out)/np.sqrt(fan_in)
# He et al. 2015
W = np.random.randn(fan_in, fan_out)/np.sqrt(fan_in/2)
```

Training a neural network

Pick a network architecture (connectivity pattern between neurons)





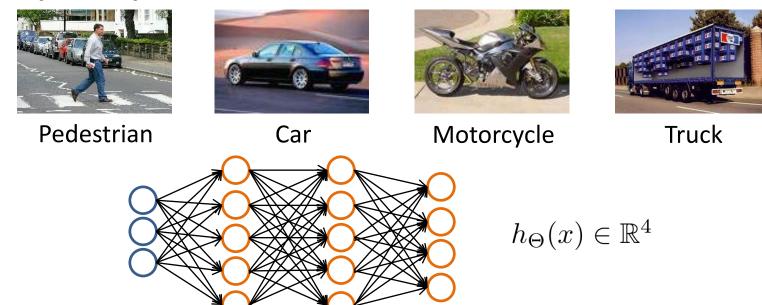


No. of input units: Dimension of features $x^{(i)}$

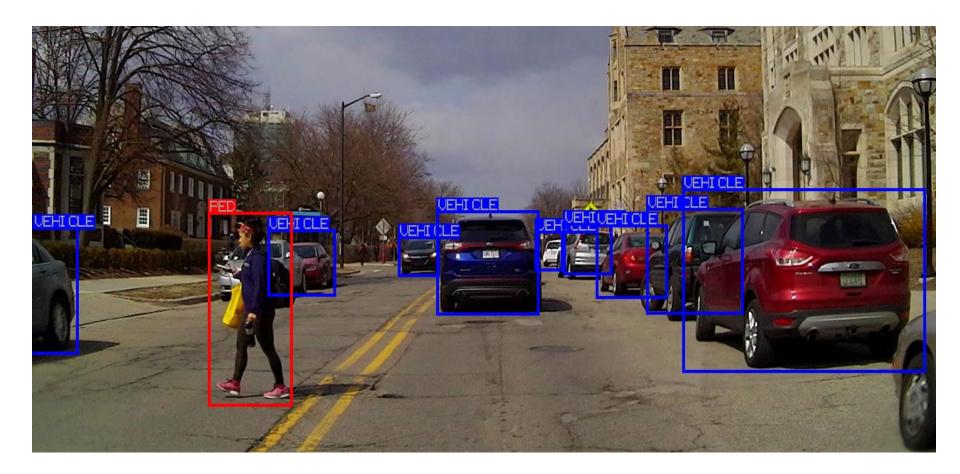
No. output units: Number of classes

Reasonable default: 1 hidden layer, or if >1 hidden layer, have same no. of hidden units in every layer (usually the more the better)

Multiple output units: One-vs-all.



Want
$$h_{\Theta}(x) \approx \begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$
, $h_{\Theta}(x) \approx \begin{bmatrix} 0 \\ 1 \\ 0 \\ 0 \end{bmatrix}$, $h_{\Theta}(x) \approx \begin{bmatrix} 0 \\ 0 \\ 1 \\ 0 \end{bmatrix}$, etc. when pedestrian when car when motorcycle



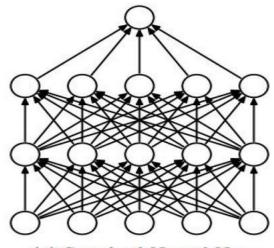
MNIST dataset (28x28 gray scale image)

The MNIST database contains 60,000 training images and 10,000 testing images

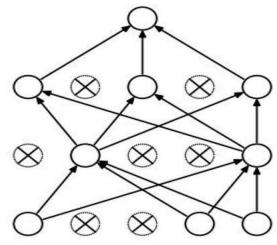


Regularization: **Dropout**

"randomly set some neurons to zero in the forward pass"



(a) Standard Neural Net



(b) After applying dropout.

[Srivastava et al., 2014]

Deeper is Better?

Layer X Size	Word Error Rate (%)
1 X 2k	24.2
2 X 2k	20.4
3 X 2k	18.4
4 X 2k	17.8
5 X 2k	17.2
7 X 2k	17.1

more parameters, better performance

Seide, Frank, Gang Li, and Dong Yu. "Conversational Speech Transcription Using Context-Dependent Deep Neural Networks." *Interspeech.* 2011.

Wide & Deep Learning

https://ai.googleblog.com/2016/06/wide-deep-learning-better-together-with.html

https://www.youtube.com/watch?v=NV1tkZ9Lq48&feature=emb_rel_end



Wide & Deep Learning for Recommender Systems

https://arxiv.org/pdf/1606.07792.pdf

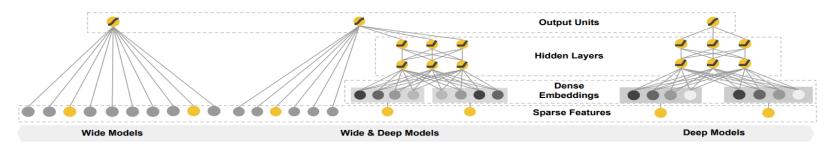


Figure 1: The spectrum of Wide & Deep models.

linear model with feature transformations for generic recommender systems with sparse inputs.

- The implementation and evaluation of the Wide & Deep recommender system productionized on Google Play, a mobile app store with over one billion active users and over one million apps.
- We have open-sourced our implementation along with a high-level API in TensorFlow¹.

While the idea is simple, we show that the Wide & Deep framework significantly improves the app acquisition rate

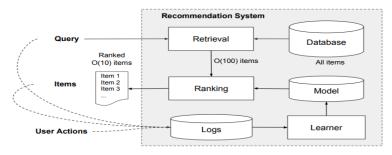


Figure 2: Overview of the recommender system.