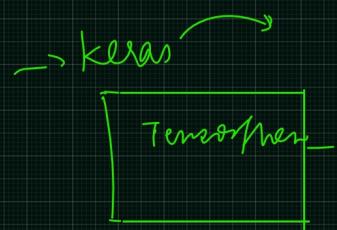


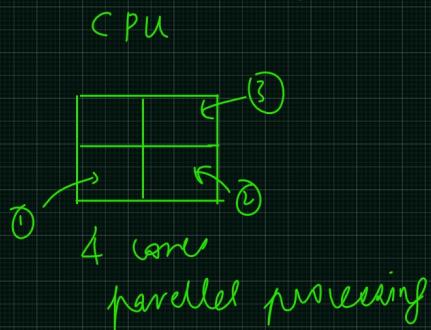
def se(y, \hat{y}):
return $(y - \hat{y})^2$



. pyTorch lightning .



with respect to deep learning training



GPU
cuda cores \rightarrow 1000



$w \cdot x$

$$\begin{bmatrix} 1 & 2 & 3 \end{bmatrix} \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} = \underbrace{1 \times 1}_{1}, \underbrace{2 \times 1}_{1}, \underbrace{3 \times 1}_{1} + + +$$

assume for each multiplication I see

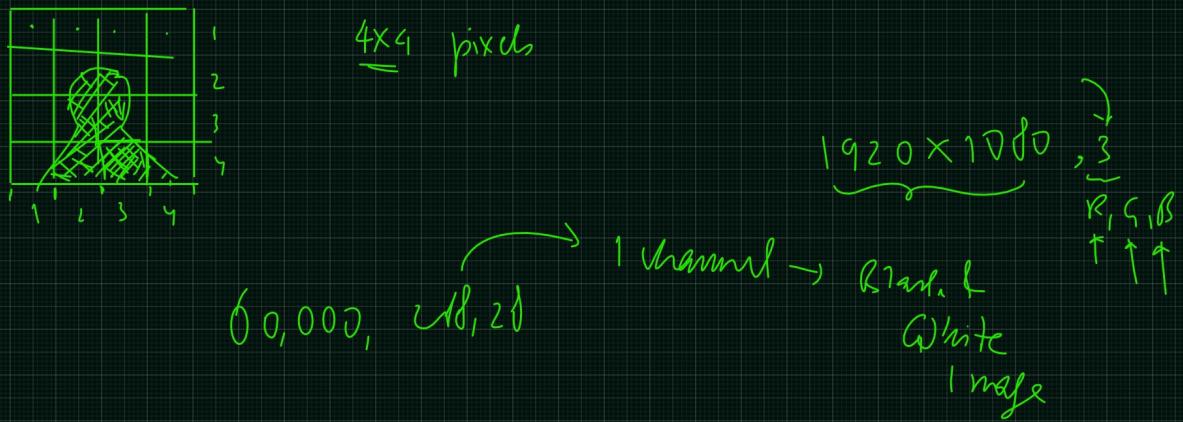
if using single core

total time = 3 sec

$$\left[\quad \right]_{1 \times n} \left[\quad \right]_{n \times 1} = \underbrace{n}_{\text{---}}$$

$n = \underbrace{1 \times 3}$

$4 \rightarrow \underbrace{2 \times 2}_{\text{---}}$



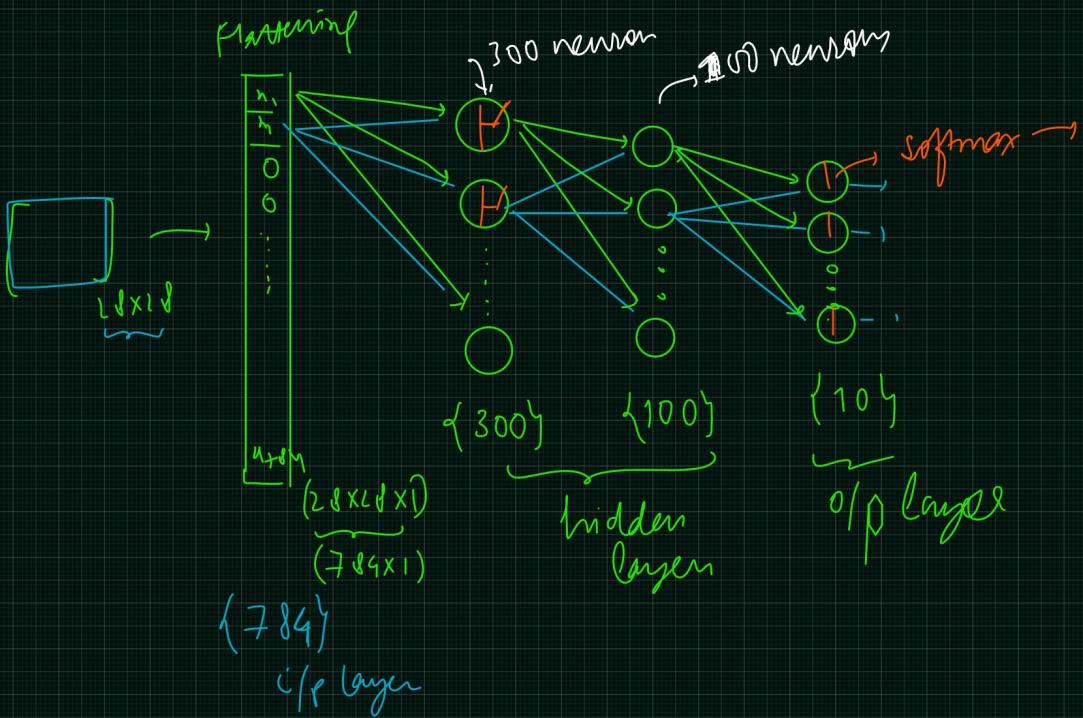
$$60,000 \left[\begin{array}{c} 1 \\ \vdots \\ 1 \end{array} \right]_{18 \times 20}$$

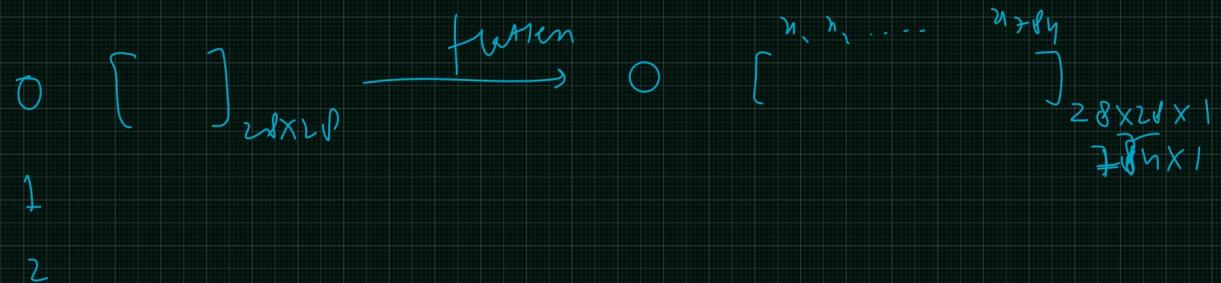
8 bit image each pixel $2^8 = 256$

$$\boxed{\underline{1 \ 1 \ 1 \ 1}} \quad 0 \rightarrow 256-1 \\ 0 \rightarrow \underline{255}$$

$$\frac{49 \text{ unit}}{255 \text{ unit}} \quad \frac{\cancel{255}}{\cancel{255}} \quad 1$$

$$0 \rightarrow \underline{1}$$





softmax

$$\hat{y}_1 = \frac{e^{z_1}}{e^{z_1} + e^{z_2} + e^{z_3}} \rightsquigarrow D_r$$

$$\hat{y}_2 = \frac{e^{z_2}}{(e^{z_1} + e^{z_2} + e^{z_3})}$$

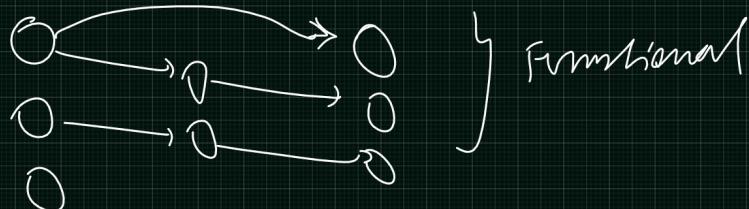
$$\hat{y}_3 = \frac{e^{z_3}}{(e^{z_1} + e^{z_2} + e^{z_3})}$$

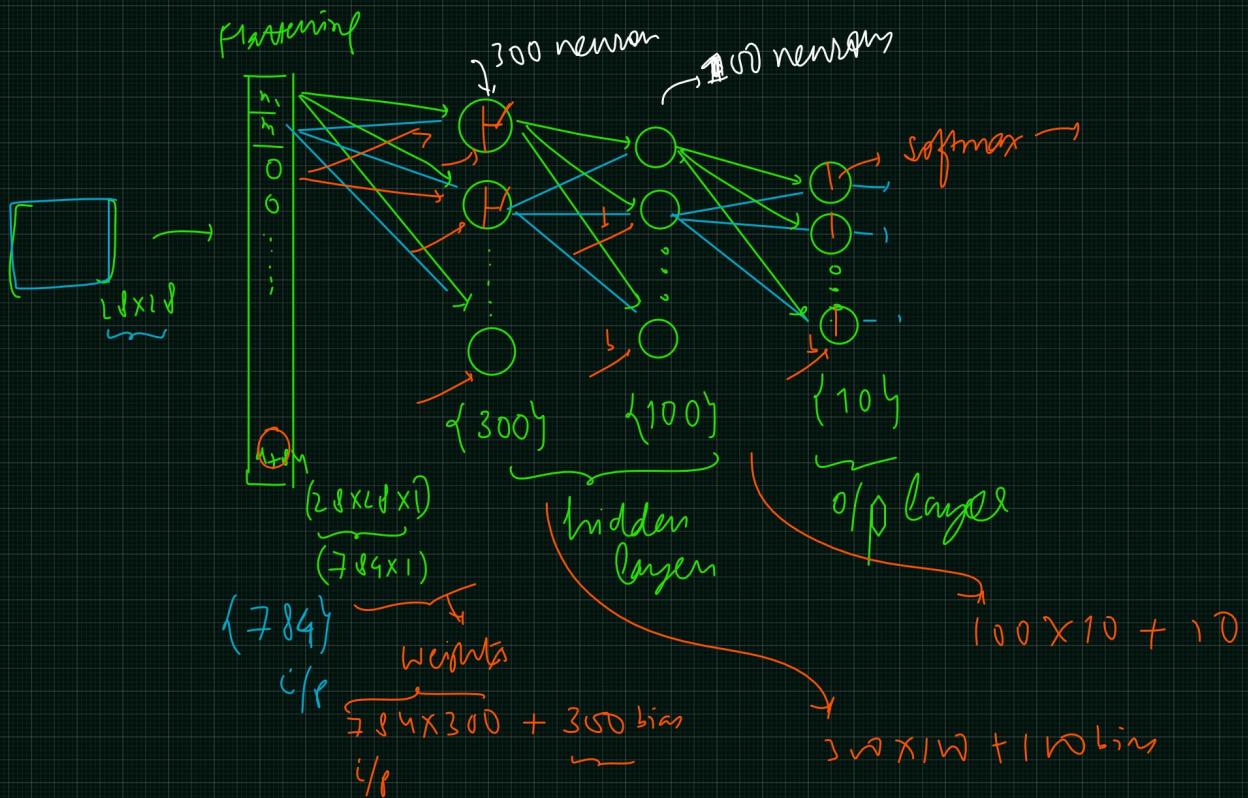
$$\frac{e^{z_1}}{D_r} + \frac{e^{z_2}}{D_r} + \frac{e^{z_3}}{D_r} = \frac{e^{z_1} + e^{z_2} + e^{z_3}}{D_r} = 1$$

$$\hat{y}_1 = \frac{e^1}{e^1 + e^0 + e^0} = \frac{e^1}{e^1 + 1 + 1} \underset{\approx 0.50}{\sim} \frac{e^1}{e^1 + 2} = \frac{1}{4,23} \simeq 0.23$$

$$\hat{y}_2 = \frac{e^0}{e^1 + e^0 + e^0} = \frac{1}{e^1 + 2} = \frac{1}{4,23} \simeq 0.23$$

$$\hat{y}_3 = \frac{1}{e^1 + 2} = \frac{1}{4,23} \simeq 0.23$$





$$\rightarrow \text{loss_fn}(y, \hat{y}) = \underbrace{L}_{\downarrow} \downarrow$$

Optimizer (= SGD)

metrics = "accuracy"

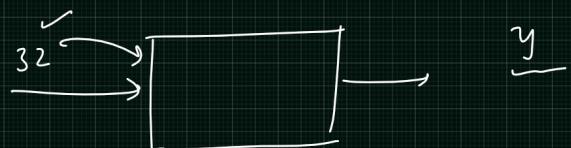
Train $\rightarrow 55,000$

Batch size $\rightarrow 32$ default

Epochs = 30

$$\text{Batches} = \frac{55,000}{32} \cong 1719.$$

every epoch \rightarrow steps per epoch $\rightarrow \underbrace{1719}$



Epoch : 30
Train data = 55,000

Batch size = 32

$$\text{Steps per epoch} = \frac{\text{Total data points}}{\text{Batch size}} \approx 1719$$

$$32, (28, 28) \\ \underbrace{\quad}_{1 \text{ batch}}$$

$$32 \times 784$$

e₁

e₂

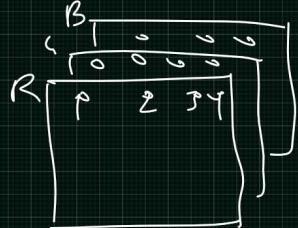
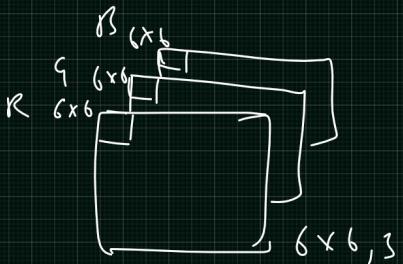
e₃

⋮

e₃₂

back propagation ← av. error

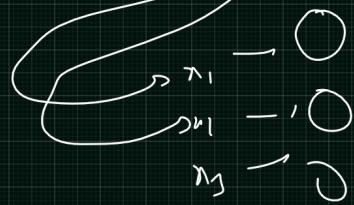
$$\text{back prop} = \underbrace{1719}_{\text{per epoch}}$$



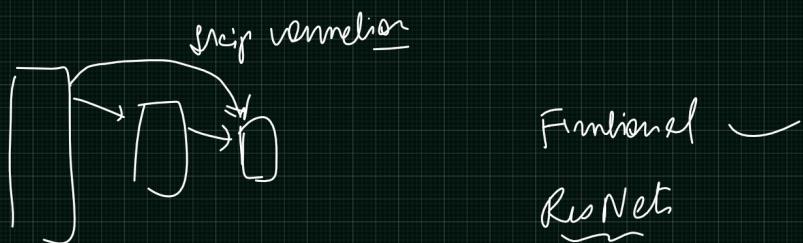
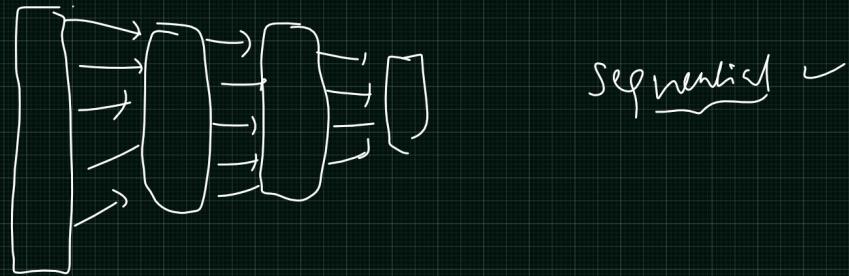
(r, g, b, a)
↑
Transparency

(r, g, b) -

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix}_{3 \times 3} \longrightarrow \begin{bmatrix} 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 \end{bmatrix}_{1 \times 9}$$



$$\begin{array}{c} 3 \times 2 \\ 512 \\ \hline 2 \end{array} \quad \begin{array}{c} 1 \times 2 \\ 256 \\ \hline 2 \end{array}$$



100 parameters → w, b → responsible for Inference.



w_1 = float → float 32 float 64

32 bit × 1 w 3200 bits

$$\underbrace{\text{f.ex. h5}}_{\downarrow} \xrightarrow{\quad} 3200 \text{ bits} = \underbrace{3.2 \text{ kbit}}$$

Classification

binary

- ─, softmax, 2 neuron
- ─, Sigmoid, 1 neuron

multiclass

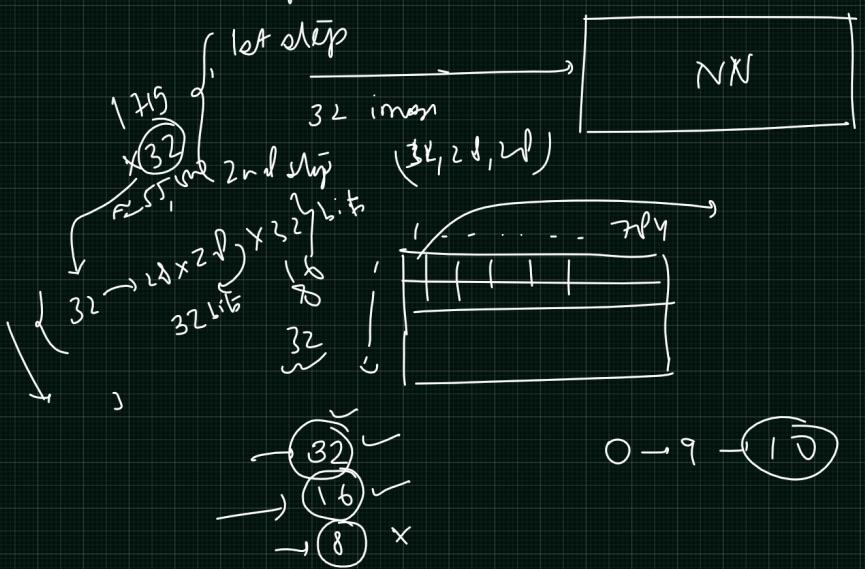
softmax

Regression -

- ─, Not required
- ─,

55000 → 1719 → 32 images

1st epoch



$$\begin{matrix} e_1 \\ e_2 \\ e_3 \\ \vdots \\ e_{32} \end{matrix}$$

$$0 \rightarrow 9 \rightarrow 10$$

$$32, 16, \underbrace{2}_{\text{binary}} \rightarrow \underbrace{2}_{\text{if else}}$$

$$\left\{ \begin{array}{c} 1 \\ 0 \xrightarrow{\quad} 1 \\ 0 \end{array} \right\} \rightarrow \begin{array}{c} 1 \\ 0 \end{array}$$

$$1 \quad \underbrace{1}_{\text{link}} \quad -1$$

$$1M \quad \underbrace{10^6} \quad \underbrace{10^5}$$

$$10, 100 \checkmark$$

$$70\% \quad 30\%$$



$$95\% \quad 5\%$$

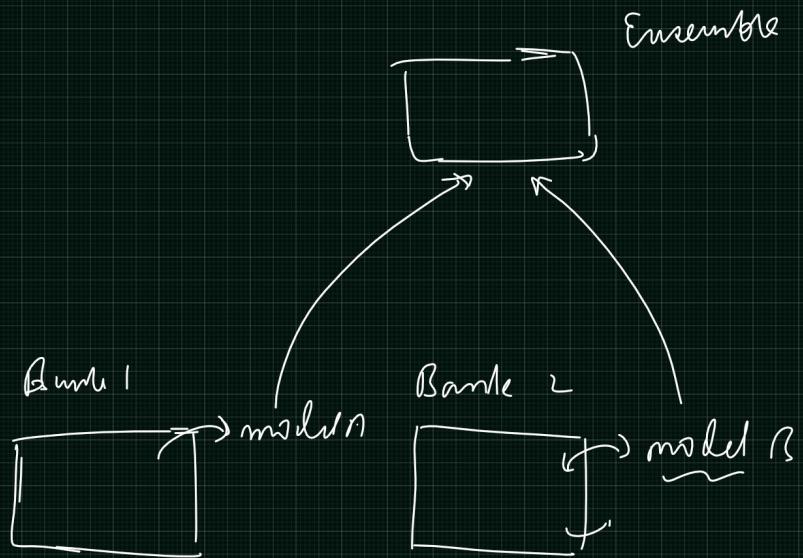
ANN

CNN

RNN

Transformers

VGG16
Architektur



x_-

epoch = 30

$$\begin{array}{c|c} \hat{y} & y \\ \hline \lambda & \hat{y} \\ \vdots & | \end{array}$$

$$x \rightarrow \omega \rightarrow (\varepsilon | f) \rightarrow \hat{y} \quad y$$

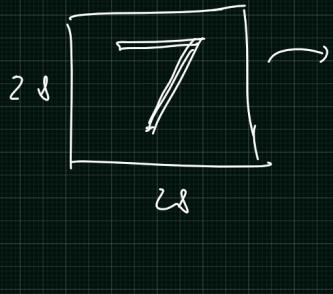
$$\hat{y} = f(\omega x)$$

$$\textcircled{32} = \text{bwm} \\ \frac{1 \text{ m}}{32} \approx \frac{3}{\text{m}}$$

$$\omega = \omega - \eta \frac{\partial e}{\partial \omega}$$

$$\text{error} = (\hat{y} - y) = e$$

$$\underbrace{\omega}_{\omega}$$



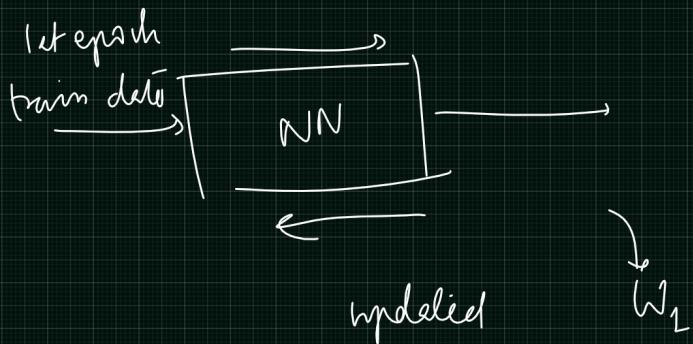
$$\begin{matrix} 0 & & & & \\ 0 & 0 & 0 & \leftarrow & 0 \\ 0 & 0 & 0 & \rightarrow & 0 \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ 0 & 0 & 0 & \leftarrow & 0 \\ \vdots & \vdots & \vdots & \rightarrow & \vdots \\ 0 & 0 & 0 & \leftarrow & 0 \\ 1 & n & 1 & \leftarrow & 1 \\ 1 & 0 & 0 & \rightarrow & 0 \end{matrix}$$

| \hat{y} | y |
|-----------|-------------------|
| 0 | $0 \leftarrow y,$ |
| 0 | 0 |
| 0.75 | 0 |
| 0.4 - 1 | 1 |
| 0.5 | 0 |
| 0.5 | 0 |
| 0 | 0 |

$$y \ln \hat{y} - \sum_0^q y \ln \hat{y}$$

$$- y_0 \ln \hat{y}_0 - y_1 \ln \hat{y}_1 - \dots - y_q \ln \hat{y}_q =$$

$- 1 \ln 0.4 = -1 (-0.4) = 0.4$



$$x_v w_1 = z \Rightarrow f(z) = \hat{y} - y_{\text{valid}}$$

error

Callback \rightarrow Early stopping

$$784 \times 3w = [] 784 \times 3w [] 3w \times 1w$$

$$[\omega]^T \quad []$$

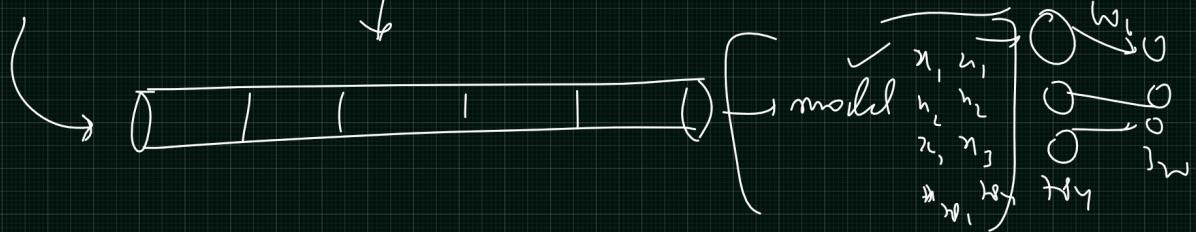
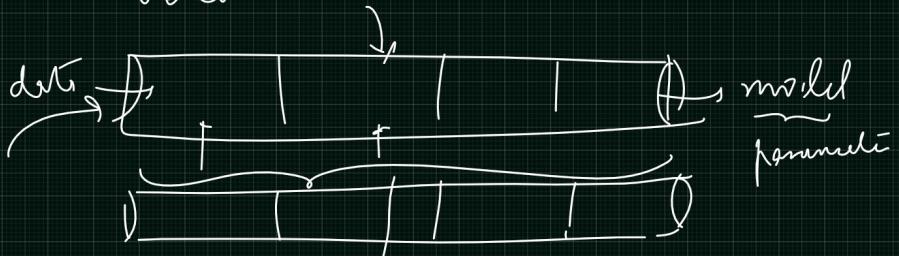
784x3060 784x72

$$\left[\begin{array}{c} \omega_{3w \times 784} \\ \times 784 \times 32 \end{array} \right]$$

$$\left[\begin{array}{c} \ell_1 \\ e_1 \\ p_1 \end{array} \right]_{32 \times 1}$$

ℓ

Research



Fraction

$$\frac{32}{32} \cdot \left(\frac{28}{28}, \frac{12}{12} \right) = \left(\frac{32}{32}, \frac{1+8}{1+8} \right)$$

$$W_{3w \times 2} X_{2 \times 3} + \underbrace{\left[\begin{array}{c} \\ \\ \end{array} \right]_{3w \times 32}}_{= Z_{3w \times 32}}$$

$$z_2 = \left(\begin{array}{c} n_1 \\ n_2 \\ n_3 \end{array} \right)$$

$$W_{2 \times 3} X_{3 \times 32} = \left(\begin{array}{c} \\ \\ \end{array} \right)_{2 \times 32}$$

$$\left[\begin{array}{c} \\ \\ \end{array} \right]_{2 \times 32} =$$

$$A_{3w \times 32} + \underbrace{\beta_{3w \times 32}}_{= Z_{3w \times 32}}$$

$$n_1 \rightarrow \circ$$

$$\overbrace{A_{2 \times 32}} + \beta_{2 \times 32} = Z_{2 \times 32}$$

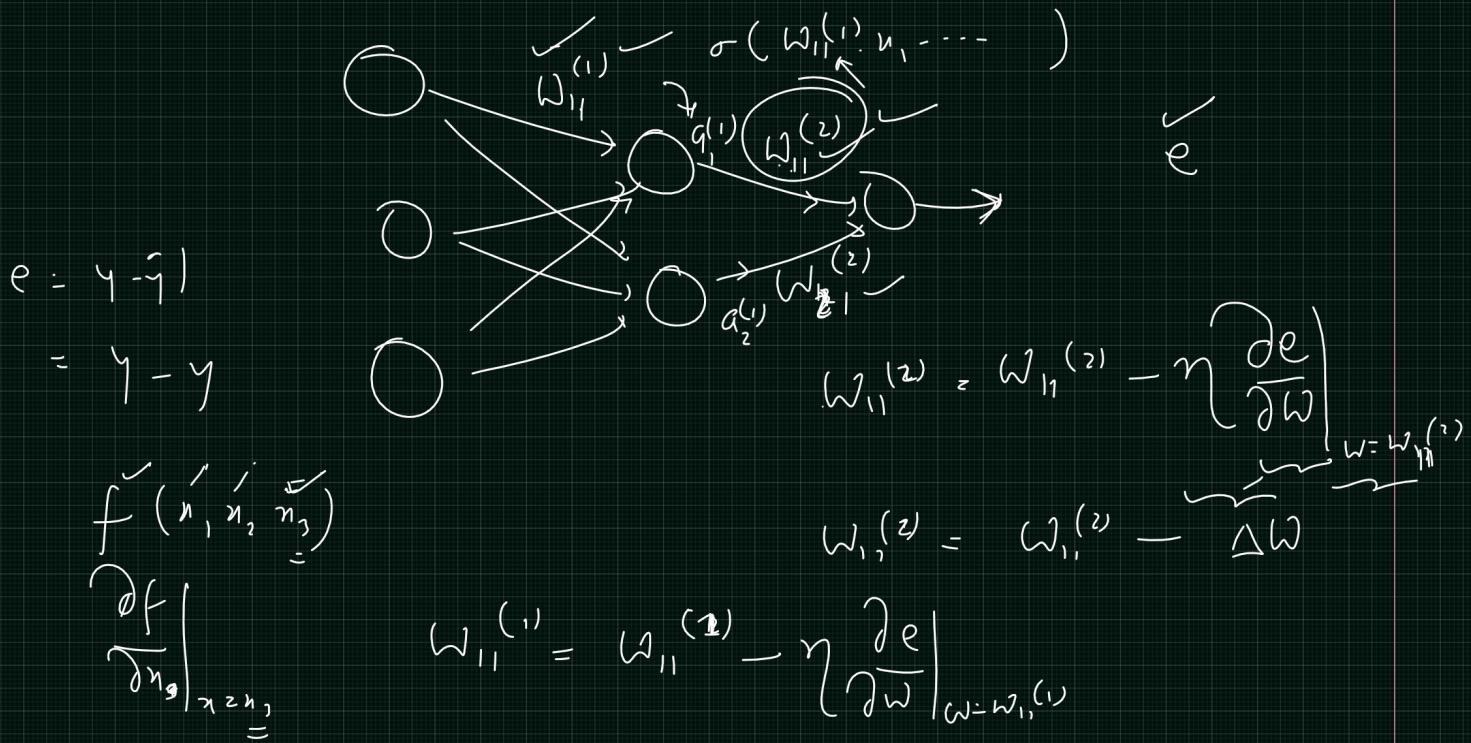
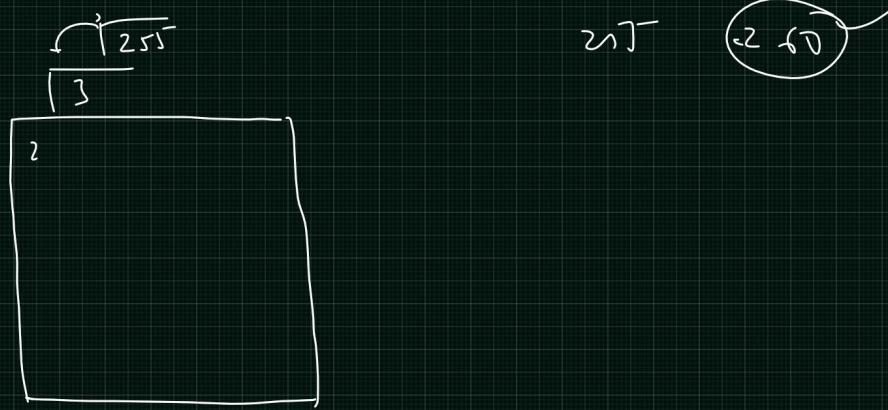
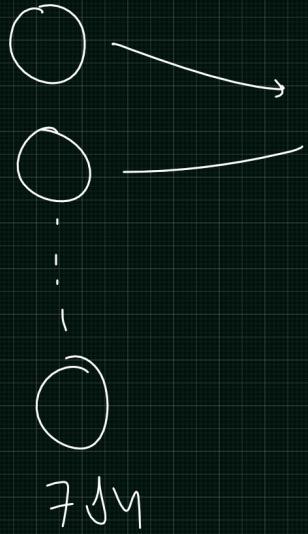
$$n_2 \rightarrow \circ$$

$$n_3 \rightarrow \circ$$

$$\left(\begin{array}{ccc} n_1 & n_2 & \dots \\ n_1 & n_2 & \dots \\ \vdots & \vdots & \ddots \end{array} \right) + \left[\begin{array}{c} b_1 \\ b_2 \\ b_3 \end{array} \right]_{3 \times 12}$$

$$\left[\begin{array}{c} \\ \\ \end{array} \right]_{2 \times 32} = \left(\begin{array}{cccc} b_1 & b_1 & \dots & b_1 \\ b_2 & b_2 & \dots & b_2 \end{array} \right)_{2 \times 32}$$

$$Z = \underbrace{Z_{2 \times 12}}_{= Z_{2 \times 12}}$$



$$\underline{\theta} = \left(\underbrace{\tilde{w}_{11}, \tilde{w}_{12}, \dots, \tilde{b}_1, \tilde{b}_2, \dots, \tilde{b}_c}_{\text{training parameters}} \right)$$