

## ASSIGNMENT - 5

AS-11

### CLASSICAL BITS

- The device computes by manipulation of these bits with the help of logic gates.
- A classical computer has a memory made up of bits where each bit holds either a one or zero.
- Classical bits are slow.
- Its circuit behaviour is based on classical physics.

### QUANTUM BITS

- The device computes by manipulating these bits with the help of quantum logic gates.
- Quantum bits are used in quantum computers.
- Quantum bits are faster.
- Its circuit behaviour is based on quantum mechanics.

AS-3) a) Let  $C_1\phi_1 + C_2\phi_2$  be the linear combination that is orthogonal to  $\phi$ , then since  $\phi$  is normalised.

$$\int \phi^* (C_1\phi_1 + C_2\phi_2) dx = C_1 + C_2 = 0 \quad \text{--- (1)}$$

$$\therefore \frac{C_1}{C_2} = -1$$

Separate values of  $C_1$  &  $C_2$  are obtained from the requirement that  $C_1\phi_1 + C_2\phi_2$  be normalised. Take  $C_1$  and  $C_2$  to be real.

$$\int (C_1\phi_1 + C_2\phi_2)^* (C_1\phi_1 + C_2\phi_2) dx = C_1^2 + C_2^2 + 2C_1C_2 = 1 \quad \text{--- (2)}$$

from eqn (1) & (2)

$$C_1 = \frac{d}{\sqrt{1-d^2}} \quad \text{--- (3)} \quad \therefore C_2 = \frac{-1}{\sqrt{1-d^2}} \quad \text{--- (4)}$$



$$(c_1\phi_1 - c_2\phi_2)/\sqrt{1-d^2}$$

This gives resulting expressions for  $c_1$  &  $c_2$  which are a valid solution.

This leads to the result that if  $f$  is normalised and orthogonal to  $g$  is so is  $\exp(is)f$ .

(b) Let  $(c_1\phi_1 + c_2\phi_2)$  be normalised & orthogonal  
Condition  $\rightarrow$

$$\int (c_1\phi_1 + c_2\phi_2)^* (c_1\phi_1 + c_2\phi_2) dx = (c_1 + c_2)(1+d) = 0$$

$$\therefore c_1 = -c_2$$

Normalising condition given (1)<sup>nd</sup> can be as before.  
from (2) & (5)

$$(c_1\phi_1 - c_2\phi_2)/\sqrt{2-d^2} \quad \text{--- (6)}$$

$\therefore$  (6) has the required properties



AS-2)  $\psi = \frac{1}{\sqrt{5}} |M_1\rangle - i\sqrt{7/15} |M_2\rangle + \frac{1}{\sqrt{3}} |M_3\rangle$

Normalised condition

$$\langle \psi | \psi \rangle = 1 \text{ or}$$

Sum of square of constants = 1

$$\rightarrow \left(\frac{1}{\sqrt{5}}\right)^2 + \left(-i\sqrt{7/15}\right)^2 + \left(\frac{1}{\sqrt{3}}\right)^2 = 1$$

$$\frac{1}{5} + \frac{7}{15} + \frac{1}{3} = 1$$

Hence the given state is normalised



Ans-4) The surface to volume ratio of material or substance made of nano-particle has a significant effect on the properties of the material. Material made-up of nano-particle have relation large surface area when compared to the same volume of material made up of bigger particles. It means that surface-volume ratio increases as radius of sphere decrease and vice-versa. Material made up of nano-particle have much greater surface area per unit volume ratio compared to material made of bigger particles.

Quantum confinement is change of electronic and optical properties when the material sample, is of sufficiently small size of typically 10 nano-meter or less. Band gap increases as size of nano-structure decreases. It is the spatial confinement of electron-hole excitation in one or more dimension within a material.

1D	confinement	:	Quantum well
2D	confinement	:	Quantum wire
3D	confinement	:	Quantum dot