

電腦視覺與應用

Computer Vision and Applications

Lecture02-2 Pinhole camera Supplementary Practice

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This is one example to help you to understand the following equation

homogenous **2D point** on image (unit: pixel)

General form: $\mathbf{x}_{\text{img}} = \mathbf{K}[\mathbf{R} \mid \mathbf{t}]\mathbf{X}_{\text{world}}$

3D point in Euclidean space
(says world coordinate)

Camera intrinsic
parameter

Camera transformation in this Euclidean space,
says extrinsic parameter (inverse to camera position and orientation)



Please download the material

- Download 3D ply file (Knight2.ply), and practice it by yourself
- In the enclosed zip, there is one photo called “Photo.jpg” and its corresponding camera parameter (in a virtual 3D environment)

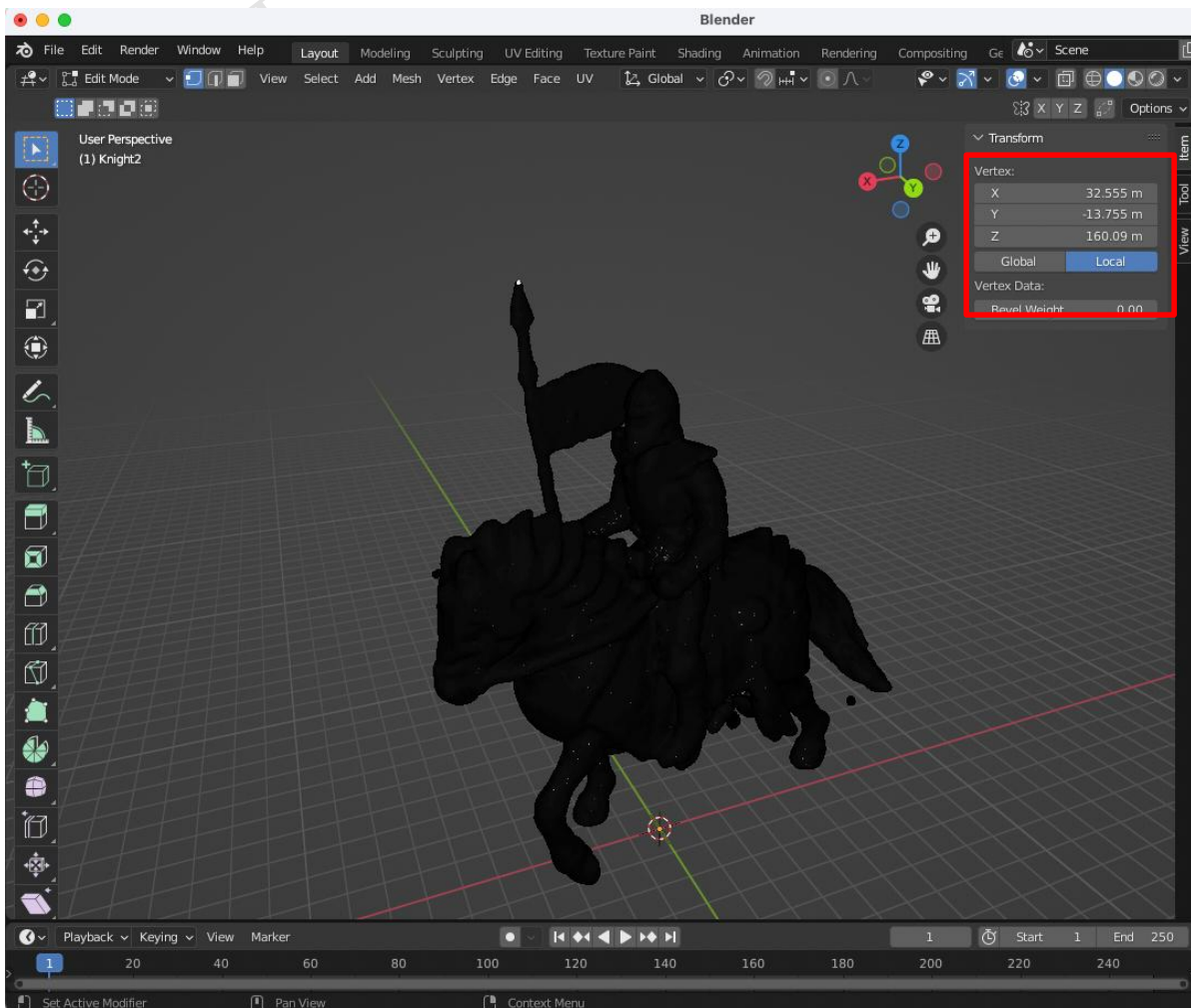
```

Intrinsic parameter
1008.303162 0.000000 561.500000
0.000000 1008.303223 428.000000
0.000000 0.000000 1.000000
Extrinsic parameter
-0.999688 -0.023195 -0.009252 -10.240249
0.007737 0.064585 -0.997882 82.185707
0.023743 -0.997643 -0.064385 225.871841
|
    
```





Try to retrieve the 3D coordinate of one vertex on the model.



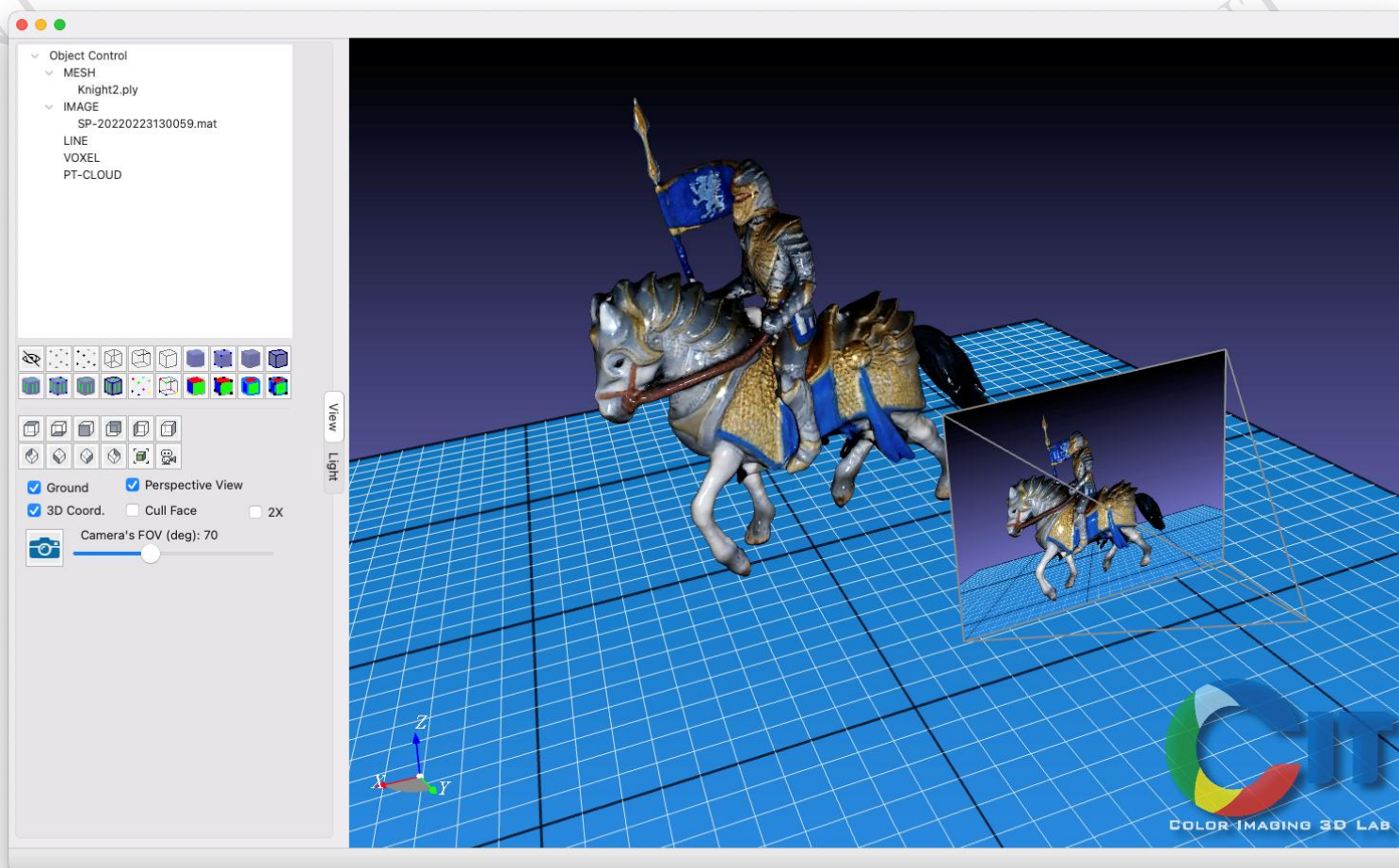
Read out the vector.

$[x, y, z] = [32.56, -13.76, 160.09]$

How to read the 3D coordinates of vertexes on a model
([video clip](#))



If you already know camera parameter (intrinsic and extrinsic parameters), try to verify projected 2D point on the image.





Open a calculator (matlab or scilab) to verify it.

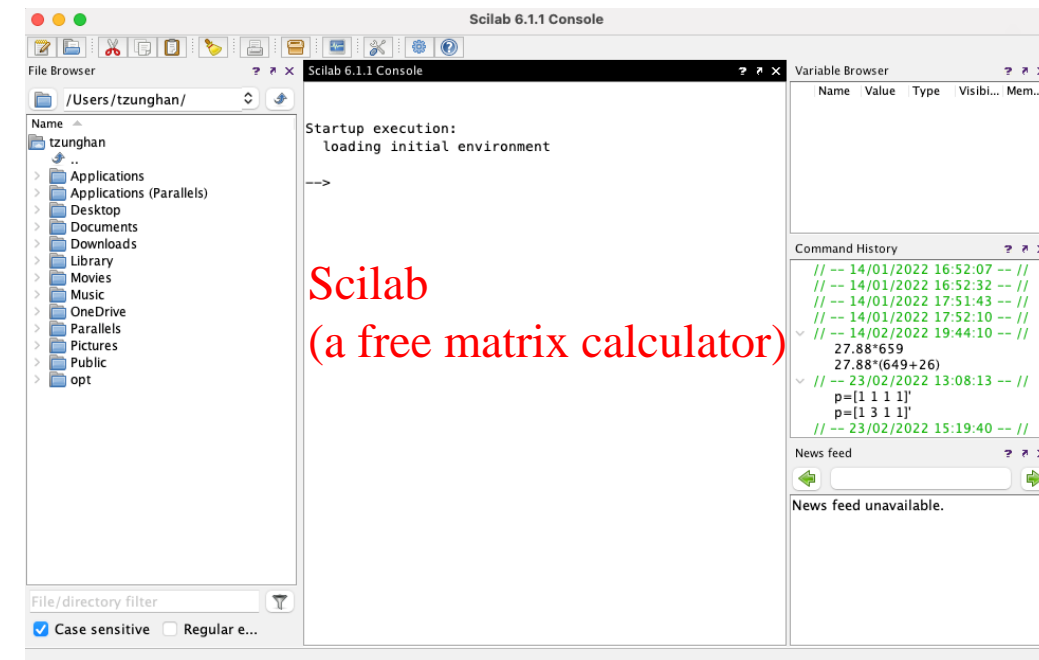
- Take scilab as an example. And assume

- 3D point $\mathbf{X}=[32.56, -13.76, 160.09 \ 1]'$ (a readout point from blender)

- Intrinsic parameter

$$\mathbf{K} = \begin{bmatrix} 1008.303162 & 0.000000 & 561.500000 \\ 0.000000 & 1008.303223 & 428.000000 \\ 0.000000 & 0.000000 & 1.000000 \end{bmatrix}$$

- Extrinsic parameter

$$\mathbf{RT} = \begin{bmatrix} -0.999688 & -0.023195 & -0.009252 & -10.240249 \\ 0.007737 & 0.064585 & -0.997882 & 82.185707 \\ 0.023743 & -0.997643 & -0.064385 & 225.871841 \end{bmatrix}$$


Scilab
(a free matrix calculator)



Calculating the projected 2D point by $\mathbf{x}_{\text{img}} = \mathbf{K}[\mathbf{R} \mid \mathbf{t}]\mathbf{X}_{\text{world}}$

```

Scilab 6.1.1 Console
Startup execution:
loading initial environment

--> X=[32.56, -13.76, 160.09 1]'
X =

    32.56
   -13.76
   160.09
        1.

--> K= [1008.303162 0.000000 561.500000
> 0.000000 1008.303223 428.000000
> 0.000000 0.000000 1.000000]
K =

    1008.3032    0.    561.5
         0.    1008.3032    428.
         0.         0.         1.

--> RT= [-0.999688 -0.023195 -0.009252 -10.240249
> 0.007737 0.064585 -0.997882 82.185707
> 0.023743 -0.997643 -0.064385 225.871841]
RT =

   -0.999688   -0.023195   -0.009252  -10.240249
    0.007737    0.064585   -0.997882    82.185707
    0.023743   -0.997643   -0.064385   225.87184

--> x = K*RT*X
x =

    84864.525
    19616.533
    230.06509
  
```

(homogenous 2D point)

$\mathbf{x} =$

84864.525
19616.533
230.06509

(normalize it)

--> $\mathbf{x} = \mathbf{x} ./ \mathbf{x}(3)$

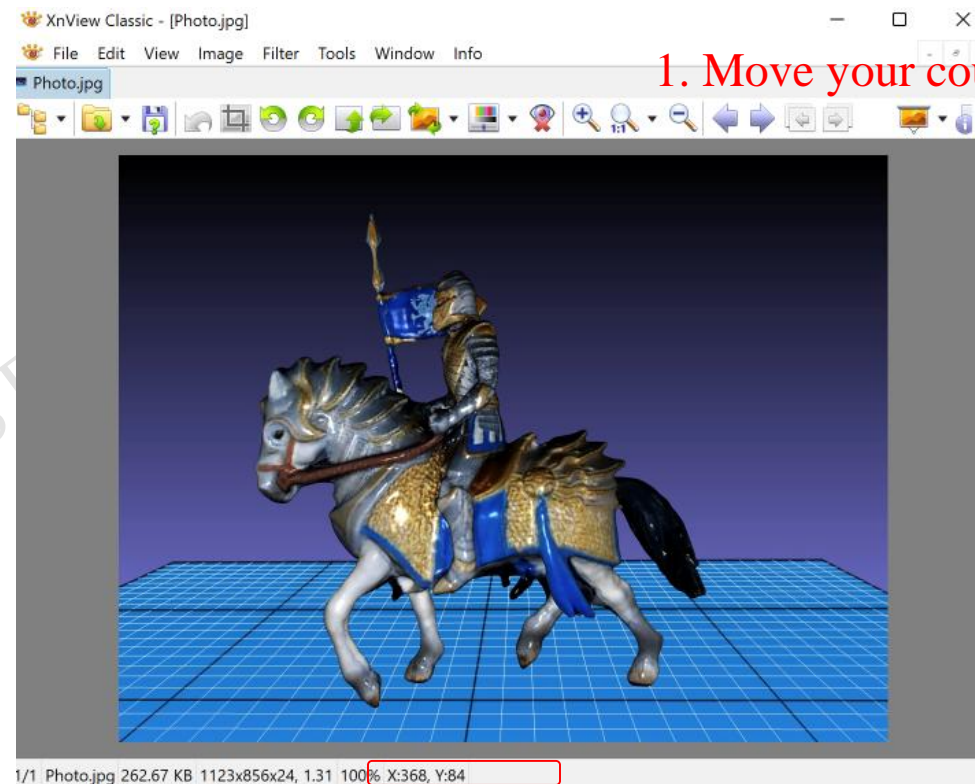
$\mathbf{x} =$

368.87181
85.265145
1.



Using image viewer to verify the correctness

- For example in XnView software, move your cursor to the position where you read out in blender.
- If you got a correct answer, try to verify for other 3D points.



1. Move your cursor to this position

2. Read the coordinate value and compare it with the output from your calculator



By the way...

```
--> X
```

```
X =
```

```
32.56
```

```
-13.76
```

```
160.09
```

```
1.
```

A 3D point which is defined in world coordinate

```
--> RT*X
```

```
ans =
```

```
-43.952080
```

```
-78.201995
```

```
230.06509
```

The same 3D point but it is defined in the camera coordinate



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