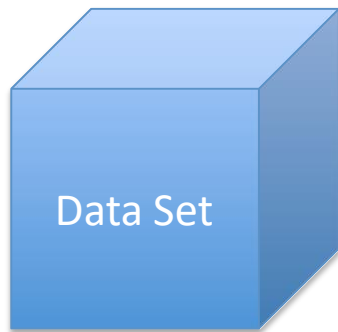


# Direct Volume Rendering

## Transfer Function Design

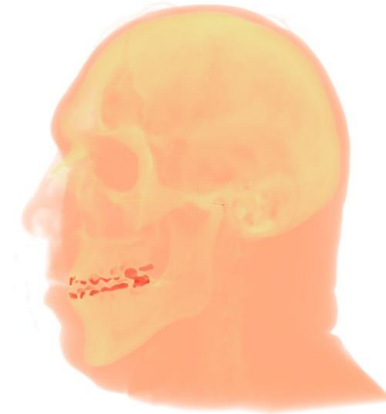
# Transfer Function

- Map a data sample to color and opacity



$$f_{color}(s) = (r, g, b)$$

$$f_{opacity}(s) = \alpha$$



- The sample could be
  - A single value (scalar)
  - Multiple values (scalar, gradient magnitude, etc)

# Transfer Function in Rendering Equation

$$I(D) = I_0 \times e^{-\int_0^D \tau(t) dt} + \int_0^D g(s) e^{-\int_s^D \tau(t) dt} ds$$

$$I_0 \prod_{i=1}^{i=n} (1 - \alpha_i) \quad \sum_{i=1}^{i=n} (g_i \times \prod_{j=i+1}^n (1 - \alpha_j))$$

Opacity
Color in (R,G,B)



# Transfer Function in Back-to-Front Compositing

The initial pixel color = Black

Back-to-Front compositing:  
use 'under' operator

$C = C1$  'under' background

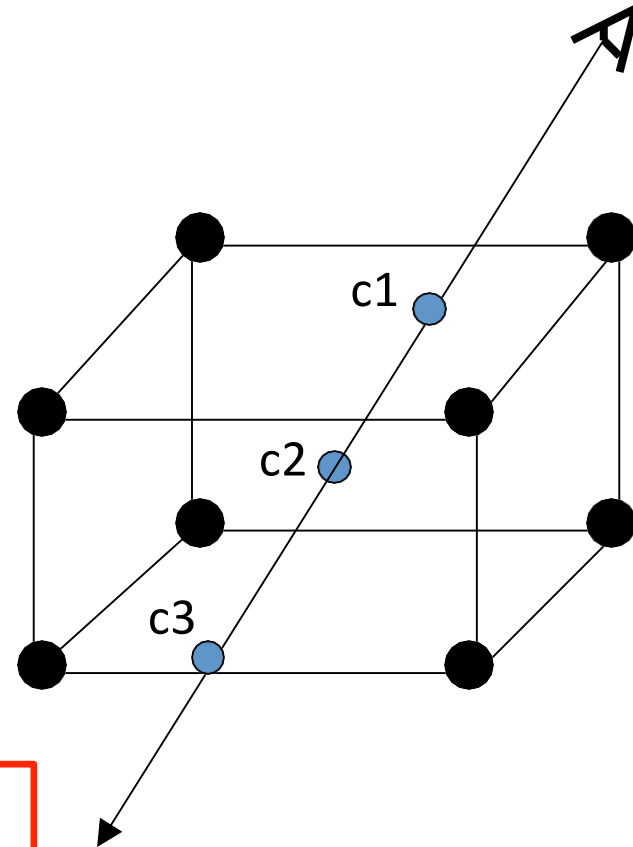
$C = C2$  'under'  $C$

$C = C3$  'under'  $C$

...

$$C_{out} = C_{in} * (1 - \alpha(x)) + C(x) * \alpha(x)$$

(this is the alpha blending formula)



# Transfer Function in Front-to-Back Compositing

Front-to-Back compositing:  
use 'over' operator

$C = \text{background 'over' } C1$

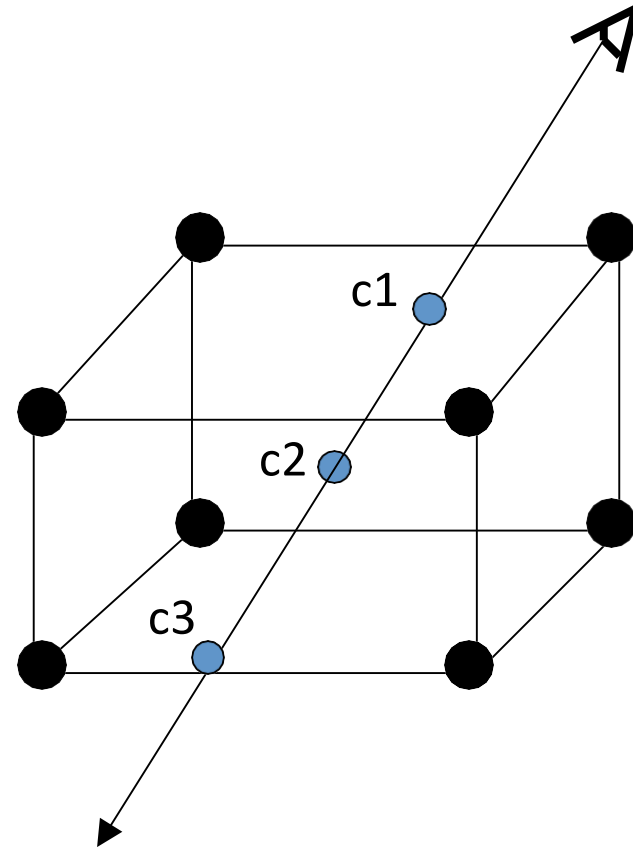
$C = C \text{ 'over' } C2$

$C = C \text{ 'over' } C3$

...

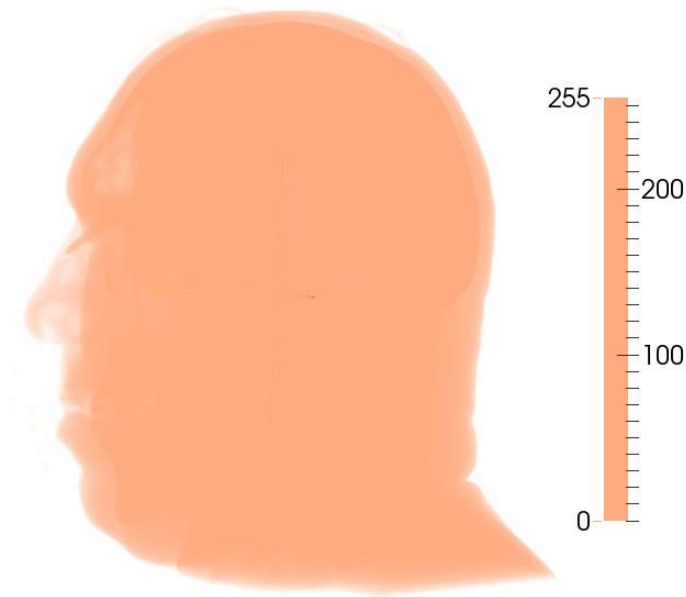
$$C_{\text{out}} = C_{\text{in}} + C(x) * (1 - \alpha_{\text{in}});$$

$$\alpha_{\text{out}} = \alpha_{\text{in}} + \alpha(x) * (1 - \alpha_{\text{in}})$$

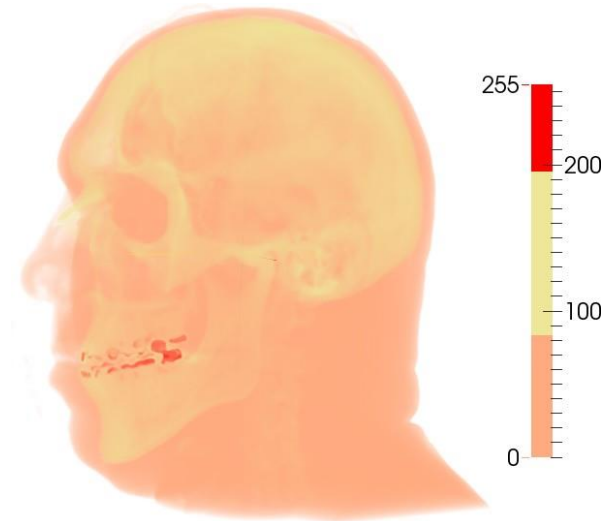


# Color in Transfer Function

- Color
  - Distinguish different materials



- All Materials uses same color
- See no features



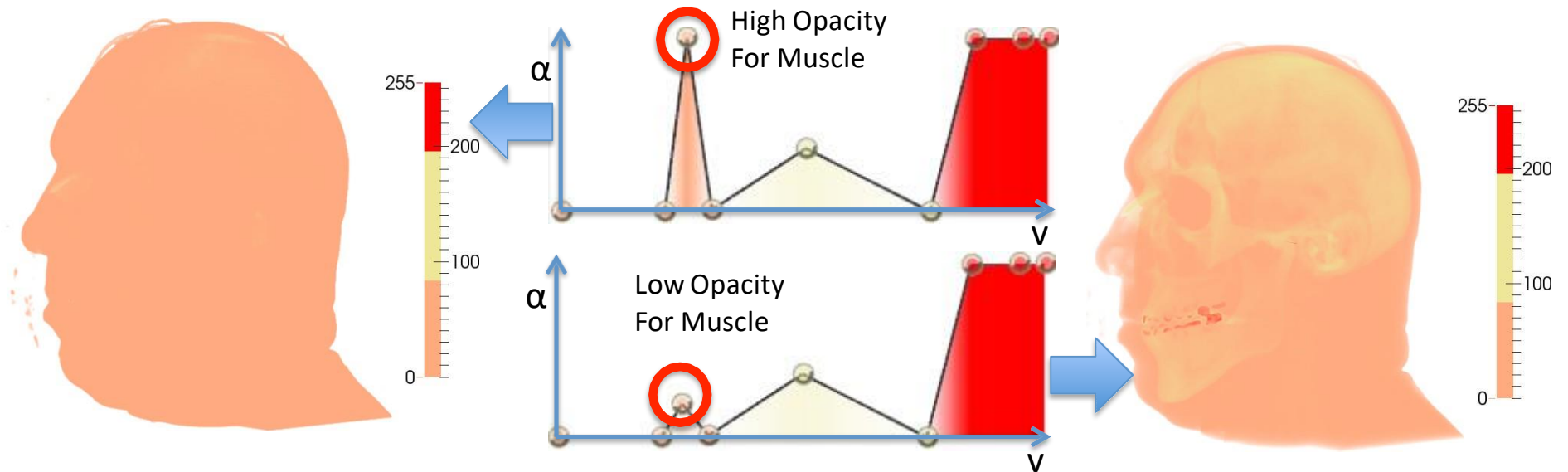
- Muscle: orange
- Bone: yellow
- Tooth: red



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# Opacity in Transfer Function

- Opacity
  - Opacity (transparency) of each sample
  - That multiple materials is shown in the rendered image provides more context



- Material inside the muscle is occlude
- See no features

- Make the muscle transparent
- See the bone and tooth



# Transfer Function Design

- Goal
  - Using transfer function to emphasize salient structures and de-emphasize other

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  - Using transfer function to emphasize salient structures and de-emphasize other
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  - Without knowing the data how to design a good transfer function?
  - A small difference in the transfer function could produce very different images
  - Some features are not easy to show without a lot of tweaking

# Transfer Function Design

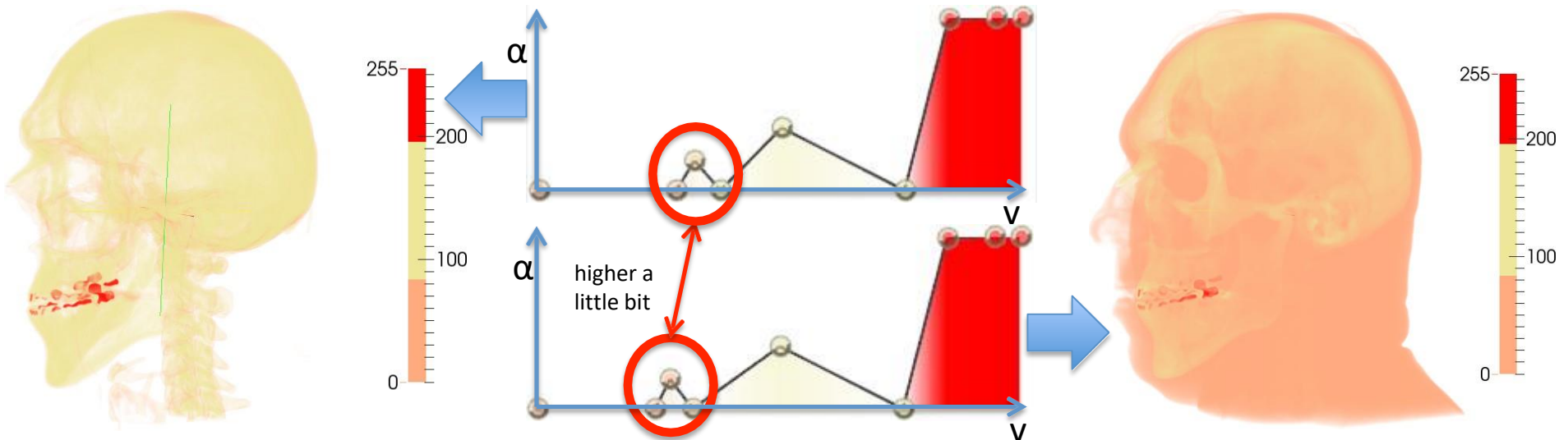
- Goal
  - Using transfer function to emphasize salient structures and de-emphasize other
- Challenges
  - Without knowing the data how to design a good transfer function?
  - A small difference in the transfer function could produce very different images
  - Some features are not easy to show without a lot of tweaking

Need algorithms and strategies to assist users to find the desired transfer function in a huge transfer function search space

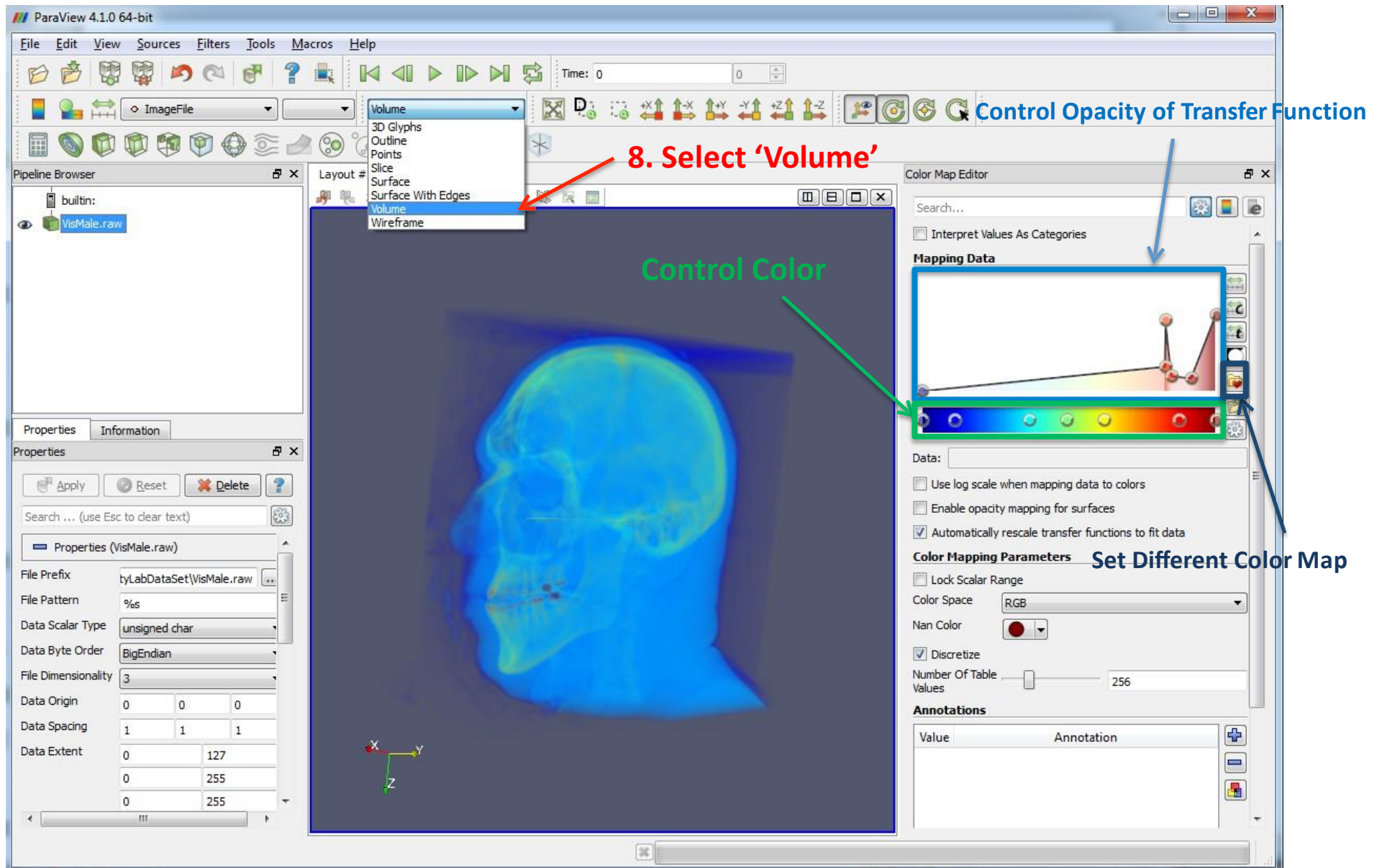
# Trial and Error

- Manually control the color and opacity of each scalar value using graphical user interface (GUI)
  - Very tedious work and inefficient
  - Small transfer function change can produce very different images

It could be difficult to get a good image without enough prior knowledge

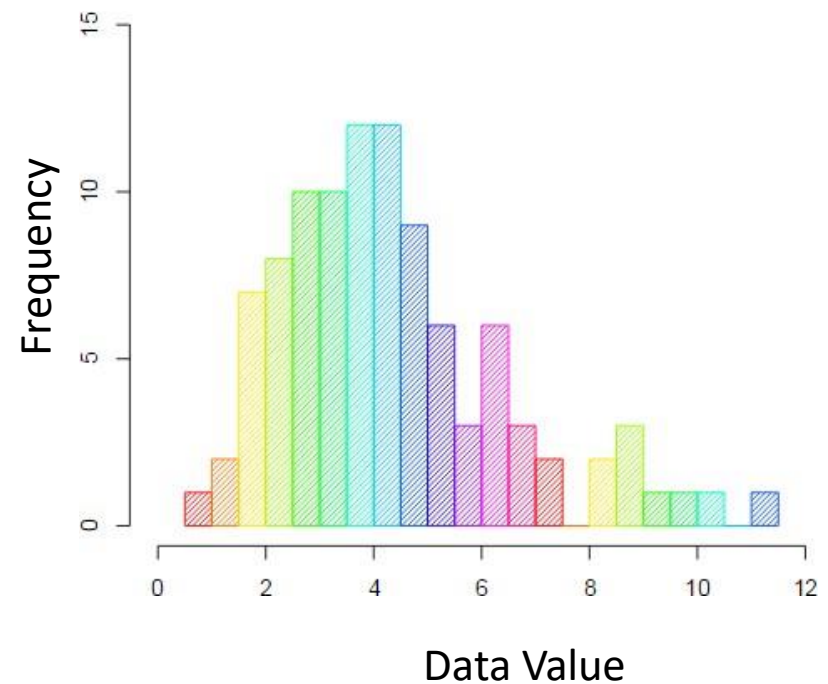


# Paraview



# Histogram Assisted Transfer Function Design

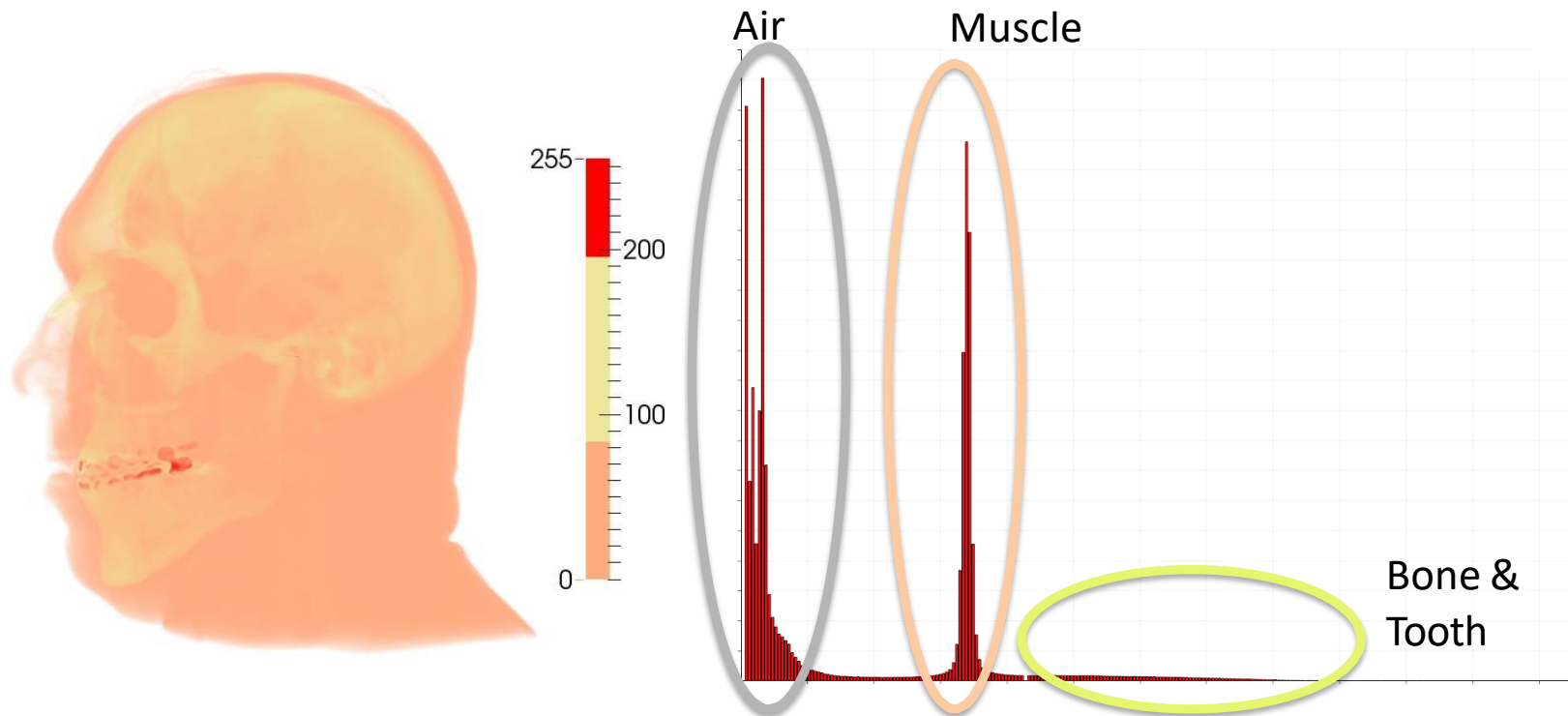
- Histogram
  - Divide the data range into finite intervals(bins)
  - Frequency of a bin is the number of samples whose values are in the interval





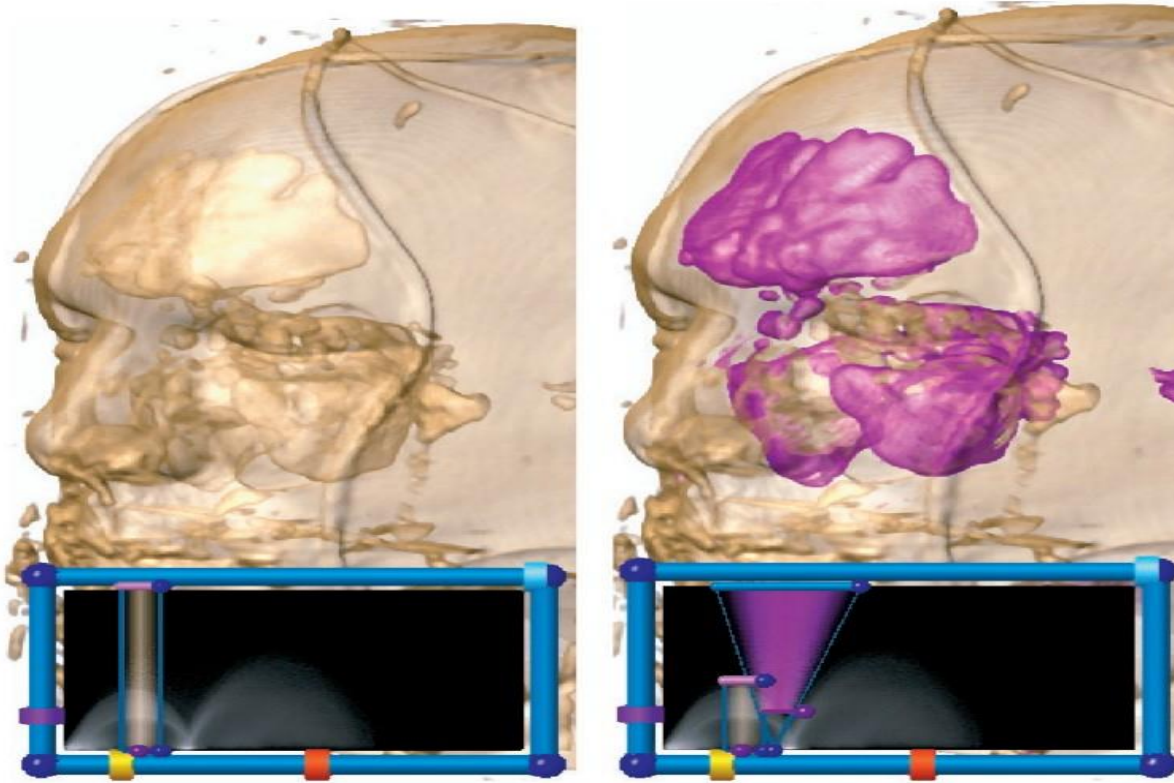
# Histogram Assisted Transfer Function Design

- Different features in the data set sometimes have values in different scalar ranges
- If this is the case, value clusters can be seen from the histogram
- Different value clusters can be assigned with different colors and opacities



# Multi-Dimensional Transfer Functions

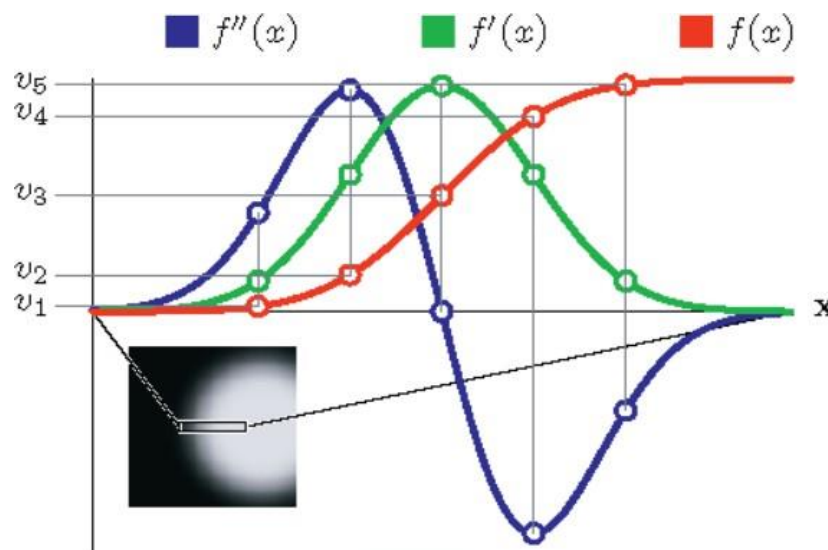
- Certain features cannot be captured by 1D histograms
  - boundary between two materials
    - Ex: emphasize the boundary between sinuses and tissue



**\*Interactive Volume Rendering Using Multi-Dimensional Transfer Functions and Direct Manipulation Widgets.**  
Joe Kniss. Gordon Kindlmann. Charles Hansen. 2001

# Multi-Dimensional Transfer Functions

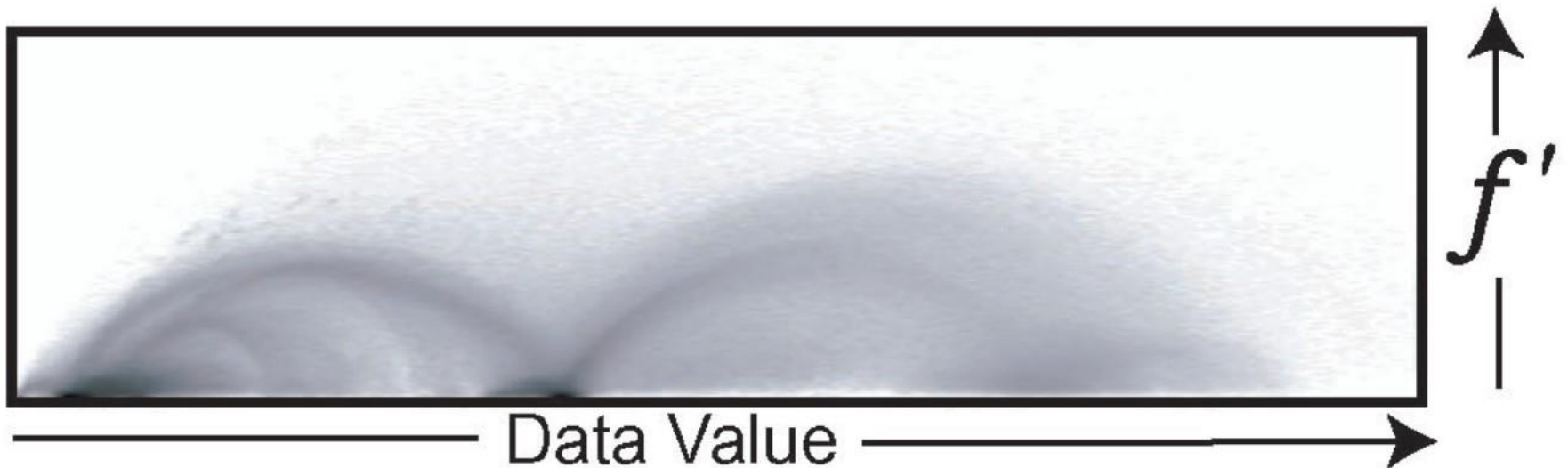
- How to detect/capture the boundaries
  - Values: step function
  - Gradients: local maximum
  - 2<sup>nd</sup> derivatives: zero crossing
- 1<sup>st</sup> derivative of the raw data at a point



\*Interactive Volume Rendering Using Multi-Dimensional Transfer Functions and Direct Manipulation Widgets.  
Joe Kniss. Gordon Kindlmann. Charles Hansen. 2001

# Multi-Dimension Transfer Function Design

- 2D Histogram
  - X-axis – data value
  - Y-axis – gradient
  - Color intensity – frequency of the histogram (darker means more here)



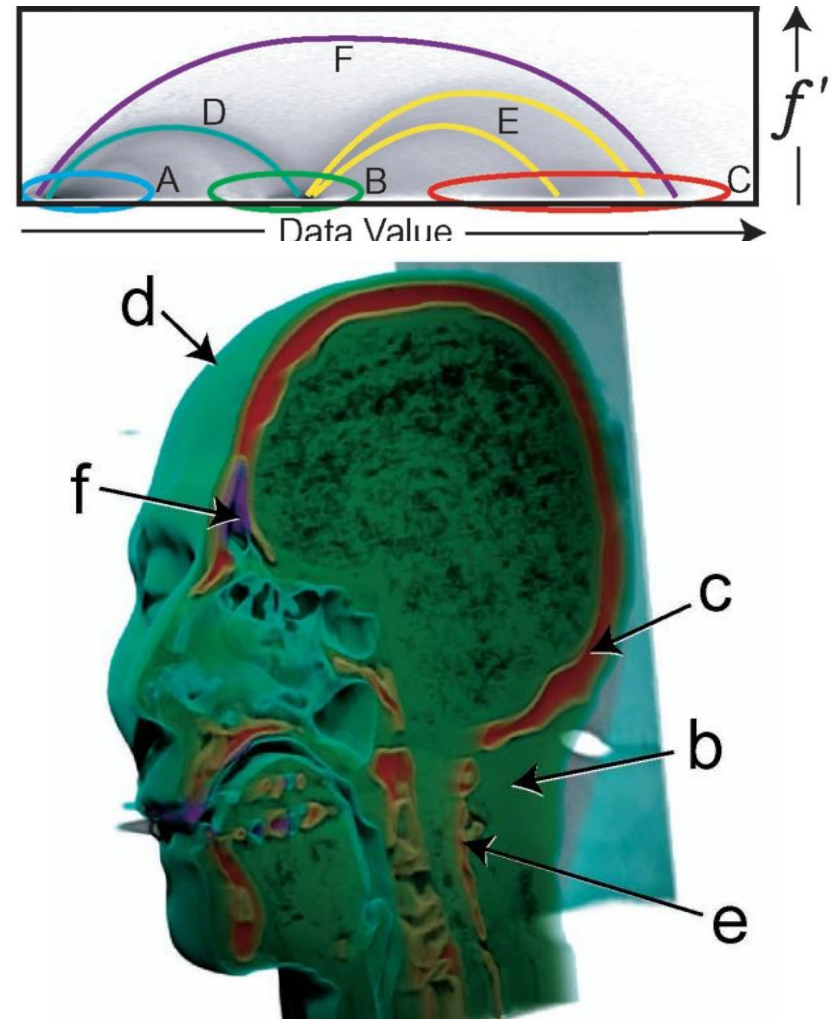
\*Interactive Volume Rendering Using Multi-Dimensional Transfer Functions and Direct Manipulation Widgets.  
Joe Kniss. Gordon Kindlmann. Charles Hansen. 2001



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# Multi-Dimensional Transfer Functions

- 1D histogram can capture homogeneous region only
  - A : air
  - B : tissue
  - C : bone
- 2D histogram can capture
  - D : air and tissue boundary
  - E : tissue and bone boundary
  - F : air and bone boundary



# References

- Marc Levoy, Display of Surface from Volume Data, IEEE Computer Graphics and Applications, Vol. 8, No. 3, May, 1988, pp. 29-37
- G. Kindlemann and J.W. Durkin, Semi-automatic Generation of Transfer Functions for Direct Volume Rendering, Proc. of IEEE Symposium on Volume Visualization, pp. 79-86, 1998
- J. Kinss, G. Kindlemann, C. Hansen, Multidimensional Transfer Function for Interactive Volume Rendering, IEEE Transactions on Visualization and Computer Graphics, Vol. 8, No. 3, pp. 270-285, 2002