

Topics covered:

- Viable Prefixes
- Valid Items

Viable Prefixes:

Consider the CFG:

$E \rightarrow E + T \mid T$

$T \rightarrow T * F \mid F$

$F \rightarrow \text{id}$

Let $w = \text{id} * \text{id}$ (input string)

Here is the trace of the SLR parsing algorithm:

STACK	INPUT	ACTION
\$	id * id \$	shift
\$ id	* id \$	reduce
\$ F	* id \$	reduce
\$ T	* id \$	shift
\$T *	id \$	shift
\$T * id	\$	reduce
\$T * F	\$	reduce
\$ T	\$	reduce
\$ E	\$	ACCEPT

We observe that at any point of time, the stack contents must be a prefix of a right sentential form. However, not all prefixes of a right sentential form can appear on the stack.

For example, consider the rightmost derivation:

Rightmost derivation of $id *$ id	Set of prefixes of a right sentential form	Viable Prefixes
$E \rightarrow T$	ϵ, T	T
$\rightarrow T * F$	$\epsilon, T, T *, T * F$	$T, T *, T * F$
$\rightarrow T * id$	$\epsilon, T, T *, T * id$	$T, T *, T * id$
$\rightarrow F * id$	$\epsilon, F, F *, F * id$	F
$\rightarrow id * id$	$\epsilon, id, id *, id * id$	id

Here, ' $id *$ ' is a prefix of a right sentential form. But it can never appear on the stack! This is because we will always reduce by $F \rightarrow id$ before shifting ' $*$ '

Definition (viable prefix): The prefixes of right sentential forms that can appear on the stack of a shift-reduce parser are called viable prefixes. Its a building block for recognizing handles.

By definition, a viable prefix is a prefix of a right sentential form that does not continue past the right end of the rightmost handle of that sentential form. It's a viable prefix because it is a prefix of the handle.

Example:

Let: $S \rightarrow X1 X2 X3 X4$

$A \rightarrow X1 X2$

Let $w = X1 X2 X3$

SLR parse trace:

STACK	INPUT
\$	$X1 X2 X3 \$$
$\$ X1$	$X2 X3 \$$
$\$ X1 X2$	$X3 \$$
$\$ A$	$X3 \$$
$\$ A X3$	$\$$
.	
.	

As we see, $X1 X2 X3$ will never appear on the stack. So, it is not a viable prefix.

Importance of Viable Prefixes:

The entire SLR parsing algorithm is based on the idea that the LR(0) automaton can recognize viable prefixes and reduce them appropriately.

Recognizing Viable Prefixes Idea: To recognize viable prefixes, we must

- Recognize a sequence of partial rhs's of productions, where
- Each sequence can eventually reduce to part of the missing suffix of its predecessor.

Valid Items:

Consider the item:

$A \rightarrow \beta 1 \cdot \beta 2$

Let $S \rightarrow \alpha A \beta$

$\rightarrow \alpha \beta 1 \beta 2 B$ (rightmost derivation, sentential form) .

Since the dot is between $\beta 1$ and $\beta 2$, $\alpha \beta 1$ will be on top of the stack.

So, $\alpha \beta 1$ is a viable prefix.

We say that $A \rightarrow \beta 1 \cdot \beta 2$ is a **valid item** for the viable prefix $\alpha \beta 1$.

Every viable prefix is associated with a valid item. In general, an item will be valid for many viable prefixes.